



IIT JEE - 2021

Home Assignment - 2 | Functions | Mathematics

- Let $f(x) = 4 \cos \sqrt{x^2 - \frac{\pi^2}{9}}$. Then, the range of $f(x)$ is:
 (A) $[-1, 1]$ (B) $[-4, 4]$ (C) $[0, 1]$ (D) None of these
- Let $f(x) = |x - 2| + |x - 3| + |x - 4|$ and $g(x) = f(x + 1)$. Then:
 (A) $g(x)$ is an even function (B) $g(x)$ is an odd function
 (C) $g(x)$ is neither even nor odd (D) $g(x)$ is periodic
- The range of the function $f(x) = \frac{5}{3 - x^2}$ is:
 (A) $(-\infty, 0) \cup \left[\frac{5}{3}, \infty\right)$ (B) $(-\infty, 0) \cup \left(\frac{5}{3}, \infty\right)$
 (C) $(-\infty, 0] \cup \left[\frac{5}{3}, \infty\right)$ (D) None of these
- The range of $f(x) = \sqrt{|x| - x}$ is:
 (A) $(0, \infty)$ (B) $[0, \infty)$ (C) $(-\infty, 0)$ (D) $(-\infty, 0]$
- If $f(x) = \log \frac{1+x}{1-x}$ and $g(x) = \frac{3x+x^3}{1+3x^2}$ then $(f \circ g)(x)$ is equal to:
 (A) $f(x)$ (B) $2f(x)$ (C) $3f(x)$ (D) $4f(x)$
- If $f(x) = \frac{x-1}{x+1}$, then $f(2x)$ is:
 (A) $\frac{f(x)+1}{f(x)+3}$ (B) $\frac{3f(x)+1}{f(x)+3}$ (C) $\frac{f(x)+3}{f(x)+1}$ (D) $\frac{f(x)+3}{3f(x)+1}$
- Let $f(x) = x$ and $g(x) = |x|$ for all $x \in \mathbb{R}$. Then the function $\phi(x)$ satisfying $[\phi(x) - f(x)]^2 + [\phi(x) - g(x)]^2 = 0$ is:
 (A) $\phi(x) = x, x \in [0, \infty)$ (B) $\phi(x) = x, x \in \mathbb{R}$
 (C) $\phi(x) = -x, x \in (-\infty, 0]$ (D) $\phi(x) = x + |x|, x \in \mathbb{R}$

8. If $f(x) = \frac{1}{2}[3^x + 3^{-x}]$, $g(x) = \frac{1}{2}[3^x - 3^{-x}]$, then $f(x)g(y) + f(y)g(x)$ is equal to:
(A) $f(x+y)$ **(B)** $g(x+y)$ **(C)** $2f(x)$ **(D)** $2g(x)$
9. The domain of $f(x) = \frac{1}{|\sin x| + \sin x}$ is:
(A) \mathbb{R} **(B)** $\bigcup_{n \in \mathbb{Z}} ((2n+1)\pi, (2n+2)\pi)$
(C) $\bigcup_{n \in \mathbb{Z}} (2n\pi, (2n+1)\pi)$ **(D)** ϕ
10. The domain of $\sin \log \left[\frac{\sqrt{4-x^2}}{1-x} \right]$ is:
(A) $(-1, 1)$ **(B)** $(-2, 1)$ **(C)** $(-2, -1)$ **(D)** $(1, 2)$