

```
In [3]: import numpy as np
import matplotlib
import skimage
import IPython
import imagecodecs  #(New 2025)

import matplotlib.pyplot as plt
from IPython.display import HTML
from matplotlib import animation, rc

from skimage.color import rgb2gray
from skimage import data
from skimage.filters import gaussian
from skimage.segmentation import active_contour  # For active_contour function
from skimage.util import random_noise

 # For active_contour function
from skimage.segmentation import chan_vese, morphological_chan_vese, checker

 # For some image filtering
from skimage.morphology import white_tophat, black_tophat, disk

import skimage.io

from IPython.core.interactiveshell import InteractiveShell
InteractiveShell.ast_node_interactivity = "all"

 # PRINT VERSIONS
print("np.__version__", np.__version__)
print("matplotlib.__version__", matplotlib.__version__)
print("skimage.__version__", skimage.__version__)
print("IPython.__version__", IPython.__version__)
print("imagecodecs.__version__", imagecodecs.__version__)

np.__version__ 2.2.1
matplotlib.__version__ 3.10.0
skimage.__version__ 0.25.0
IPython.__version__ 8.31.0
imagecodecs.__version__ 2024.12.30
```

```
In [4]: def edge_map(img, sigma):
        blur = skimage.filters.gaussian(img, sigma)
        return skimage.filters.sobel(blur)

def edge_map2(img, sigma):
    blur = skimage.filters.gaussian(img, sigma)
    return skimage.filters.scharr(blur)

def subtract_background(image, radius=5, light_bg=False):
    str_el = disk(radius)
    if light_bg:
        return black_tophat(image, str_el)
    else:
        return white_tophat(image, str_el)
```

```

def define_initial_circle(R0,r0,c0,Nber_pts=400):
    # Define initial contour shape
    s = np.linspace(0, 2*np.pi, Nber_pts)
    Radius = R0
    r = r0 + Radius*np.sin(s)
    c = c0 + Radius*np.cos(s) #col
    init = np.array([r, c]).T
    return init

## Create slides for animation
def animate_cv(image, segs, interval=1000):
    fig, ax = plt.subplots(figsize=(8, 8))
    ax.imshow(image, cmap='gray');
    im = ax.imshow(segs[0], alpha=0.5, cmap='inferno');
    ax.axis('off')

    def init():
        im.set_data(segs[0])
        return [im]

    def animate(i):
        im.set_array(segs[i])
        return [im]

    anim = animation.FuncAnimation(fig, animate, init_func=init,
                                   frames=len(segs), interval=1000, blit=True)

    return anim

def animate_snake(image, segs, interval=500):
    fig, ax = plt.subplots(figsize=(6, 6))
    ax.imshow(image, cmap='gray');
    # im = ax.imshow(segs[0], alpha=0.5, cmap='inferno');
    #ax.plot(segs[0][:, 1], segs[0][:, 0], '--r', lw=3)
    ax.axis('off')
    line, = ax.plot([], [], '-r', lw=2)

    def init():
        line.set_data(segs[0][:, 1], segs[0][:, 0])
        return [line,]

    def animate(i):
        line.set_data(segs[i][:, 1], segs[i][:, 0])
        return [line,]

    anim = animation.FuncAnimation(fig, animate, init_func=init,
                                   frames=len(segs), interval=1000, blit=True)

    return anim

#####
def store_evolution_in(lst):

```

```

"""Returns a callback function to store the evolution of the level sets
the given list.
"""

def _store(x):
    lst.append(np.copy(x))

return _store

```

Read images

This part reads a series of images that you can then use in various tests.

Note that some images are provided with ground-truth masks of structures of interest:

1. OCT_tissue
2. CTabd (CT of the abdomen)
3. US nodule (Ultrasound image with a nodule)
4. images_blood_cells/000016.png [several images available]

```

In [51]: # import warnings
# warnings.filterwarnings( "ignore", module = "matplotlib\.*" )
# skimage.io.imshow(img_mask)

# Binary images - w/o ground truth
img_star = skimage.io.imread('./images_misc/smooth_star.png', as_gr
edge_star = edge_map(img_star, sigma=0)
img_star_noisy = skimage.io.imread('./images_misc/smooth_star_noisy.png',
edge_star_noisy = edge_map(img_star_noisy, sigma=0)
img_binshape = skimage.io.imread('./images_misc/binary_shape_2024.png',
edge_binshape = edge_map(img_binshape, sigma=0)
img_cardiacshape = skimage.io.imread('./images_misc/cardiac_mri_mask.png',
edge_cardiacshape = edge_map(img_cardiacshape, sigma=0)

# Microscopy images - w/o ground truth # line changed 2025
img_hela = skimage.io.imread('./images_misc/hela_big.png')

# OCT eye images - w/o ground truth
img_oct_eye = skimage.io.imread('./images_misc/OCT_normal.jpeg', as_gray =
img_oct_eye = np.squeeze(img_oct_eye)
img_oct_eye = img_oct_eye.astype('float64')
img_oct_eye = img_oct_eye/np.max(img_oct_eye)

edge_oct_eye = edge_map(img_oct_eye, sigma=2)

# CT abdo images - with ground truth
img_CTabd = skimage.io.imread('./images_misc/CT_kidney_im.png', as_gray
edge_CTabd = edge_map(img_CTabd, sigma=2)
gt_CTabd = skimage.io.imread('./images_misc/CT_kidney_mask.png', as_gra
edge_gt_CTabd = edge_map(gt_CTabd, sigma=2)

```

```
# Cell images - with ground truth
img_cell = skimage.io.imread('./images_blood_cells/0000152.png', as_gray =
edge_cell = edge_map(img_cell, sigma=2)
#skimage.io.imshow(img_cell)
gt_cell = skimage.io.imread('./masks_blood_cells/0000152.png', as_gray = True
edge_gt_cell = edge_map(gt_cell, sigma=2)

# Cell image - challenge multi
img_cell2 = skimage.io.imread('./images_misc/cell_00236.tif', as_gray =
edge_cell2 = edge_map(img_cell2, sigma=2)
gt_cell2 = skimage.io.imread('./images_misc/cell_00236_label.tiff', as_
edge_gt_cell2 = edge_map(gt_cell2, sigma=2)

# Hela Cell image - Cell tracking challenge
img_helat1 = skimage.io.imread('./images_misc/hela_t001.tif', as_gray =
edge_helat1 = edge_map(img_helat1, sigma=2)
gt_helat1 = skimage.io.imread('./images_misc/hela_mask001.tif', as_gray
edge_gt_helat1 = edge_map(gt_helat1, sigma=2)

# Fluo Cell image - Cell tracking challenge
img_fluo = skimage.io.imread('./images_misc/fluo000.tif', as_gray = True
edge_fluo = edge_map(img_fluo, sigma=2)
gt_fluo = skimage.io.imread('./images_misc/fluo000_seg.tif', as_gray =
edge_gt_fluo = edge_map(gt_fluo, sigma=2)

# OCT image of tissue - with ground truth
img_oct_tissue = skimage.io.imread('./OCT_myocardium/case272.tif', as_gray
edge_oct_tissue = edge_map(img_oct_tissue, sigma=2)
gt_oct_tissue = skimage.io.imread('./OCT_myocardium/case272_label.tiff', as
edge_gt_oct_tissue = edge_map(gt_oct_tissue, sigma=2)

# US image of a nodule - with ground truth
img_USnodule = skimage.io.imread('./thyroid_nodule/1074.png', as_gray = True
edge_USnodule = edge_map(img_USnodule, sigma=2)
gt_USnodule = skimage.io.imread('./thyroid_nodule/1074_mask.png', as_gray
edge_gt_USnodule = edge_map(gt_USnodule, sigma=2)

# PLOTS

fig, axes = plt.subplots(6,4, figsize=(8, 8))
ax = axes.ravel()

ax[0].imshow(img_cell, cmap=plt.cm.gray);
ax[1].imshow(edge_cell, cmap=plt.cm.gray);
ax[2].imshow(gt_cell, cmap=plt.cm.gray);
ax[3].imshow(edge_gt_cell, cmap=plt.cm.gray);

ax[4].imshow(img_CTabd, cmap=plt.cm.gray);
ax[5].imshow(edge_CTabd, cmap=plt.cm.gray);
ax[6].imshow(gt_CTabd, cmap=plt.cm.gray);
ax[7].imshow(edge_gt_CTabd, cmap=plt.cm.gray);

ax[8].imshow(img_fluo, cmap=plt.cm.gray);
ax[9].imshow(edge_fluo, cmap=plt.cm.gray);
ax[10].imshow(gt_fluo, cmap=plt.cm.gray);
```

```
ax[11].imshow(edge_gt_fluo, cmap=plt.cm.gray);

ax[12].imshow(img_oct_tissue, cmap=plt.cm.gray);
ax[13].imshow(edge_oct_tissue, cmap=plt.cm.gray);
ax[14].imshow(gt_oct_tissue, cmap=plt.cm.gray);
ax[15].imshow(edge_gt_oct_tissue, cmap=plt.cm.gray);

ax[16].imshow(img_cardiacshape, cmap=plt.cm.gray);
ax[17].imshow(edge_cardiacshape, cmap=plt.cm.gray);

ax[18].imshow(img_oct_eye, cmap=plt.cm.gray);
ax[19].imshow(edge_oct_eye, cmap=plt.cm.gray);

ax[20].imshow(img_star, cmap=plt.cm.gray);
ax[21].imshow(edge_star, cmap=plt.cm.gray);
ax[22].imshow(img_star_noisy, cmap=plt.cm.gray);
ax[23].imshow(edge_star_noisy, cmap=plt.cm.gray);

for i in range(0,24):
    ax[i].set_xticks([]), ax[i].set_yticks([]);
fig.tight_layout()
plt.show();
```

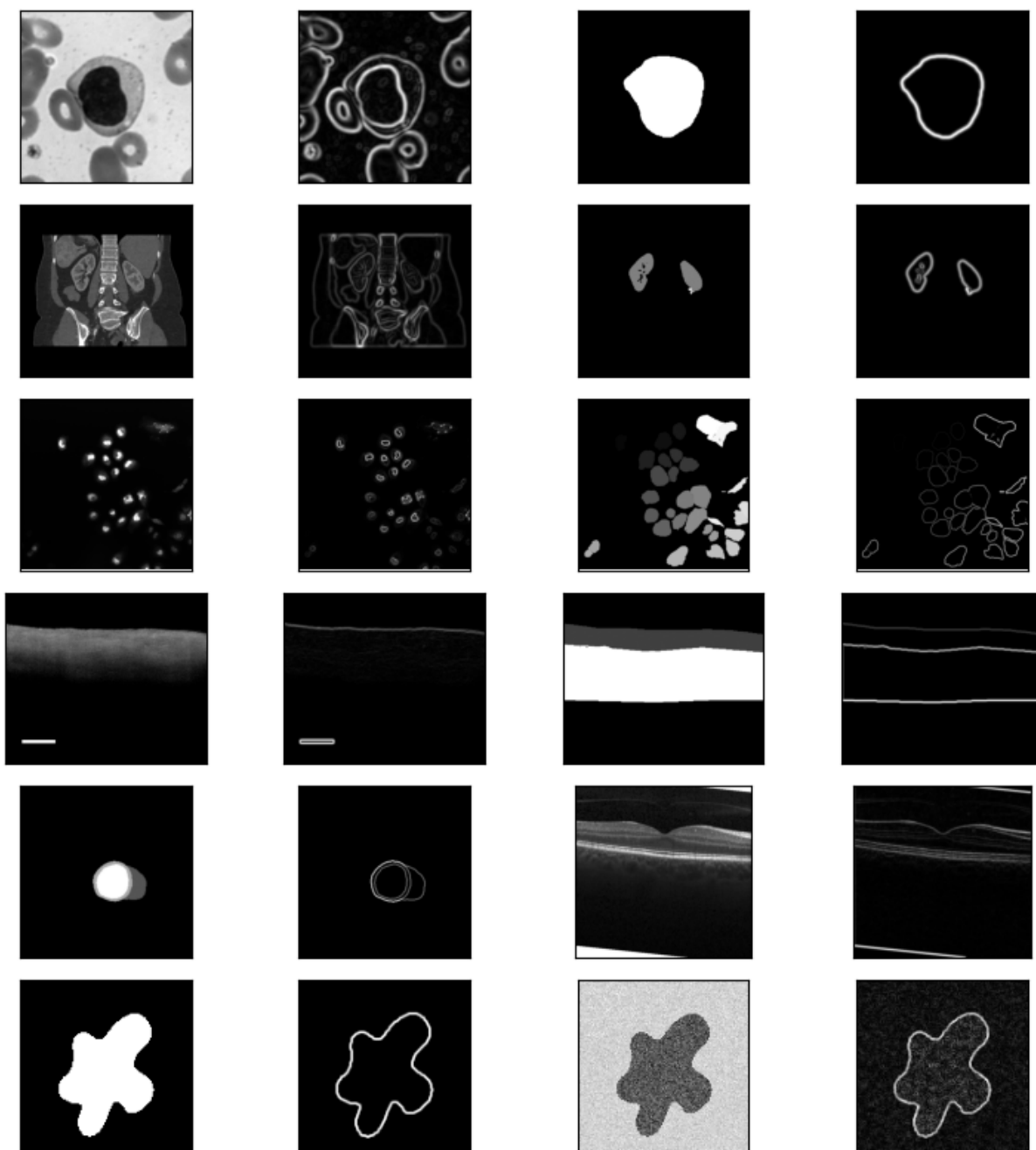


Image properties:

Range of values and data type matter ...

Some routines won't work if your image type is int8 or uint8... Here is how to check your image data type

And regularly check your image content in terms of:

- intensities range of values
- distributions of intensities via its histogram

```

In [6]: img_test = img_cell #img_star_noisy#img_oct_eye #img_CTabd #img_cell
Sigma_val = 2
edge_test = edge_map(img_test, sigma=Sigma_val)

## Print some basic image properties
print("Image size of img_test is: ", img_test.shape)
print("Data type of img_test is: ", img_test.dtype)
print("min - max value in image:" , np.min(img_test), np.max(img_test))

## Hot to plot a Histogram
hist_test, bins_test = np.histogram(img_test.flatten(), bins=256)
hist_edge_test, bins_edges_test = np.histogram(edge_test.flatten(), bins=256)

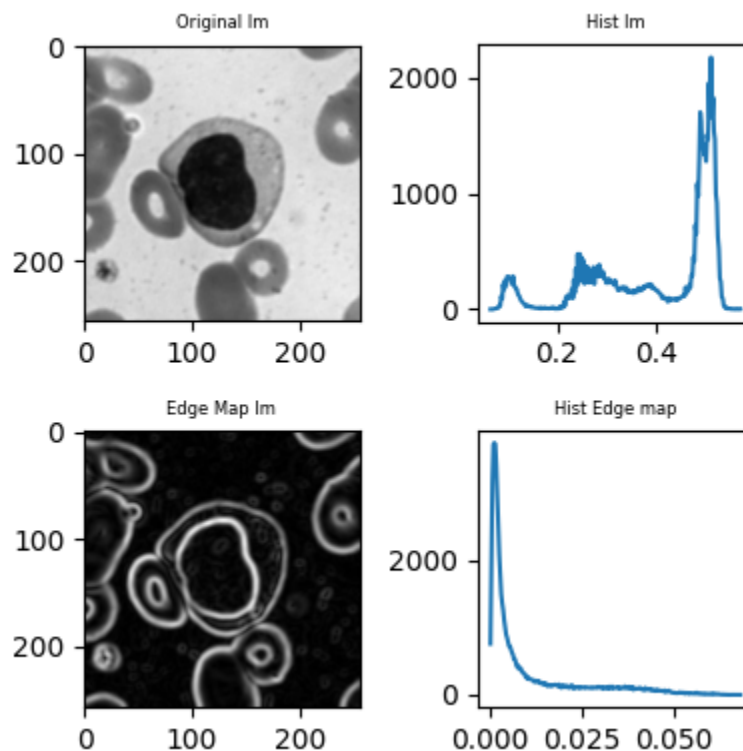
fig, axes = plt.subplots(2,2, figsize=(4, 4))
ax = axes.ravel()
ax[0].imshow(img_test, cmap=plt.cm.gray);
ax[0].set_title("Original Im", fontsize=6);
ax[1].plot(bins_test[0:-1], hist_test);
ax[1].set_title("Hist Im", fontsize=6);
ax[2].imshow(edge_test, cmap=plt.cm.gray);
ax[2].set_title("Edge Map Im", fontsize=6);
ax[3].plot(bins_edges_test[0:-1], hist_edge_test);
ax[3].set_title("Hist Edge map", fontsize=6);
fig.tight_layout()
plt.show();

```

Image size of img_test is: (256, 256)

Data type of img_test is: float64

min - max value in image: 0.06550980392156862 0.5724509803921568



Edge maps

Deformable models rely on edge maps. Most routines have their own strategy coded to compute the edge map.

- Edge maps usually involve smoothing of the image, to be robust to noise. Make sure you understand how this is controlled in the routine you use.
- Edge maps usually show pixels with high gradient magnitudes in white (high values)
- Most deformable model routines can be fed directly with an Edge Map rather than the original image as its input
- Some routine expect to be fed with an inverse edge map where high gradient locations have small values, to stop the contour via a velocity set to ~zero.

```
In [7]: img_to_test = img_oct_eye
print("Data type of img_test is: ", img_test.dtype)
print("min - max value in image:" , np.min(img_test), np.max(img_test))

Font_size = 9

# Classic Edge map with Gaussian smoothing controled by sigma
edge_test1 = edge_map(img_to_test, sigma=1)
edge_test2 = edge_map(img_to_test, sigma=2)
edge_test2_l = np.log2((edge_test2*100)+1)
edge_testl_2 = edge_map(np.log2((img_to_test+1)*100), sigma=2)

# Inversed Edge map
# Returns Edge map = 1.0 / np.sqrt(1.0 + alpha * gradnorm)
edge_inv_test = skimage.segmentation.inverse_gaussian_gradient(img_to_test,

fig, axes = plt.subplots(2,3, figsize=(6, 6))
ax = axes.ravel()

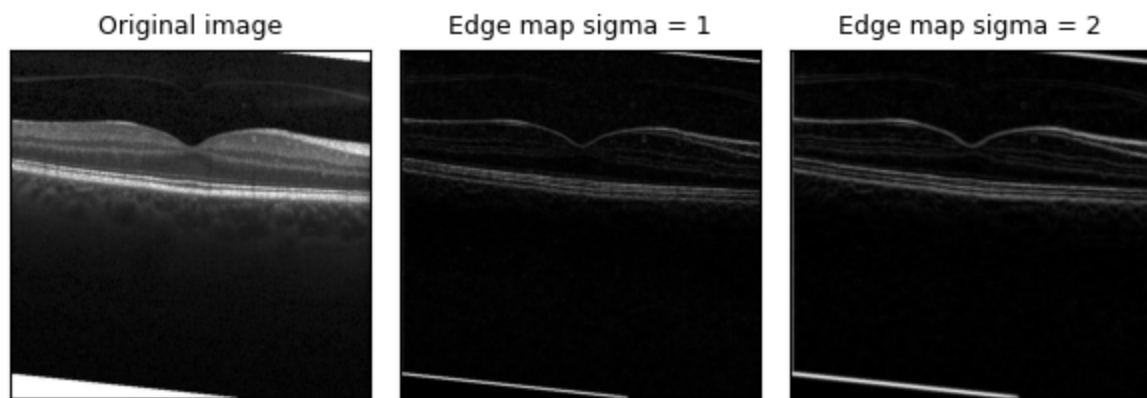
ax[0].imshow(img_to_test, cmap=plt.cm.gray);
ax[0].set_title("Original image", fontsize=Font_size);
ax[1].imshow(edge_test1, cmap=plt.cm.gray);
ax[1].set_title("Edge map sigma = 1", fontsize=Font_size);
ax[2].imshow(edge_test2, cmap=plt.cm.gray);
ax[2].set_title("Edge map sigma = 2", fontsize=Font_size);
ax[3].imshow(edge_inv_test, cmap=plt.cm.gray);
ax[3].set_title("Edge map inversed + sigma = 2", fontsize=Font_size);
ax[4].imshow(edge_test2_l, cmap=plt.cm.gray);
ax[4].set_title("Log(Edge map) + sigma = 2", fontsize=Font_size);
ax[5].imshow(edge_testl_2, cmap=plt.cm.gray);
ax[5].set_title("Edge map on Log+ sigma = 2", fontsize=Font_size);

for i in range(0,6):
    ax[i].set_xticks([]), ax[i].set_yticks([]);

fig.tight_layout()
plt.show();
```


Data type of img_test is: float64

min - max value in image: 0.06550980392156862 0.5724509803921568



Edge map inverted + sigma = 2 Log(Edge map) + sigma = 2 Edge map on Log+ sigma = 2

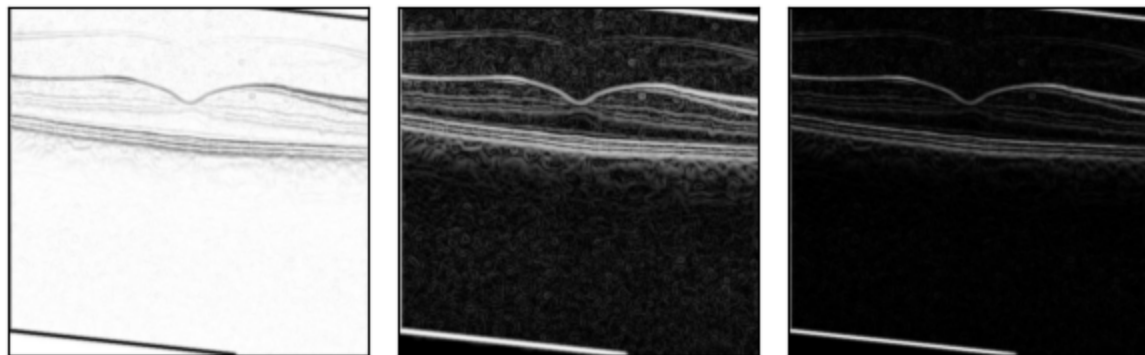


Image transforms

Let you test some image transformations based on morphological operators and histogram manipulation. When transforming image contrast, it is always interesting to look at the differences between the original image and the transformed version.

```
In [8]: img_ori_to_test = img_fluo #img_CTabd #img_oct_eye #img_CTabd
img_to_test = img_ori_to_test
epsilon = 0.000001 #to prevent log on 0
img_eps = np.full_like(img_to_test, epsilon)
PRE_ENHANCE = 1
OPTION_ENHANCE = 4 # can be 0 (nothing) OR 1,2,3,4 for different enchanceme
Font_size = 9

# Run all OPTION_ENHANCE for display here
gamma_corrected = skimage.exposure.adjust_gamma(img_to_test, 0.8)
logarithmic_corrected = skimage.exposure.adjust_log(img_to_test, gain=1, inv
img_open = skimage.morphology.diameter_opening(img_to_test, 40,
img_adapteq = skimage.exposure.equalize_adapthist(img_to_test, cli

# PRE ENHANCEMENT OPTIONS:
if PRE_ENHANCE==1:
```

```

if OPTION_ENHANCE==1:
    # Gamma
    img_to_test = gamma_corrected
elif OPTION_ENHANCE==2:
    # Logarithmic (0 = gain*log(1 + I)) or if Inv (0 = gain*(2**I - 1))
    img_to_test = logarithmic_corrected
elif OPTION_ENHANCE==3:
    # Morpho Opening
    img_to_test = img_open
elif OPTION_ENHANCE==4:
    # Contrast Limited Adaptive Histogram Equalization (CLAHE).
    img_to_test = img_adapteq

# Enhance details either dark around light background of vice versa with the
Radius_val = 15
img_test1 = subtract_background(img_to_test, radius=Radius_val, light_bg=False)
img_test2 = subtract_background(img_to_test, radius=Radius_val, light_bg=True)

# SHOW OUTPUTS
fig, axes = plt.subplots(2,5, figsize=(10, 4), constrained_layout=True)
ax = axes.ravel()
Shrink_factor_colormap = 0.5
ax[0].imshow(img_ori_to_test, cmap=plt.cm.gray);
ax[0].set_title("Ori", fontsize=6);

ax[1].imshow(img_open, cmap=plt.cm.gray);
ax[1].set_title("Opening", fontsize=Font_size);
ax[2].imshow(gamma_corrected, cmap=plt.cm.gray);
ax[2].set_title("Gamma correction", fontsize=Font_size);
ax[3].imshow(logarithmic_corrected, cmap=plt.cm.gray);
ax[3].set_title("Log correction", fontsize=Font_size);
ax[4].imshow(img_adapteq, cmap=plt.cm.gray);
ax[4].set_title("Adapt Hist Eq", fontsize=Font_size);

ax[5].imshow(img_test1, cmap=plt.cm.gray);
ax[5].set_title("Tophat Dark bkg", fontsize=Font_size);
ax[6].imshow(img_test2, cmap=plt.cm.gray);
ax[6].set_title("Tophat Light bkg", fontsize=Font_size);

tmp_show = ax[7].imshow(img_to_test-img_test2, cmap=plt.cm.gray);
ax[7].set_title("Diff: (Ori-Light bkg)", fontsize=Font_size);
plt.colorbar(tmp_show, ax=ax[7], shrink=Shrink_factor_colormap, location='right')

tmp_show = ax[8].imshow(abs(img_to_test-img_test2), cmap=plt.cm.gray);
ax[8].set_title("Diff: abs(Ori-Light bkg)", fontsize=Font_size);
plt.colorbar(tmp_show, ax=ax[8], shrink=Shrink_factor_colormap, location='right')

tmp_show = ax[9].imshow(np.log2(abs(img_to_test-img_test2+img_eps)), cmap=plt.cm.gray);
ax[9].set_title("Diff: log(abs(Ori-Light bkg))", fontsize=Font_size);
plt.colorbar(tmp_show, ax=ax[9], shrink=Shrink_factor_colormap, location='right')

for i in range(0,10):
    ax[i].set_xticks([]), ax[i].set_yticks([]);

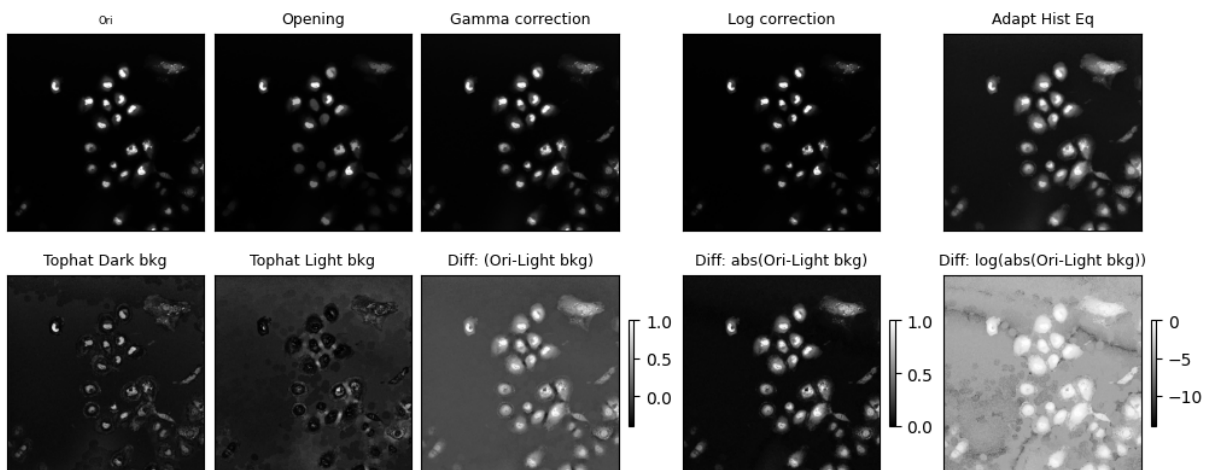
#fig.tight_layout() # not compatible with option constrained_layout=True in
plt.show();

```

```

/var/folders/81/3v_d9rcn7wd1szht19l1v89c0000gn/T/ipykernel_48152/293332637
7.py:64: RuntimeWarning: divide by zero encountered in log2
  tmp_show = ax[9].imshow(np.log2(abs(img_to_test-img_test2+img_eps)), cmap=
plt.cm.gray);

```



Seg #1:

Snake on a binary shape + noise effects

This part of the practical work uses the routine **active_contour** from skimage.

Default **parameter values** are:

- $\alpha=0.01$ (Snake length shape parameter. Higher values makes snake contract faster.)
- $\beta=0.1$ (Snake smoothness shape parameter. Higher values makes snake smoother.)
- $\gamma=0.01$ (Explicit time stepping parameter - Equivalent to the viscosity of the environment)
- $\text{max_px_move}=1.0$

There are two **other parameters** that define the final image information used to define external forces used to define regions: $\text{img} = w_{\text{line}} \times \text{img} + w_{\text{edge}} \times \text{edge}$:

- $w_{\text{line_val}} = 0$ (default) | $=1$ if want to input `edge` map directly. Use negative values to attract toward dark
- $w_{\text{edge_val}} = 1$ (default) | $=0$ if do not want to use internal edge map. Use negative values to repel snake from edges

TODO:

Provide answers in text boxes

Q1.1. Run the code for `img_to_seg=img_cardiacshape` using `img_ori` and all

parameter values as provided, except for changing the R0 value. Comment on behavior for:

- R0=10:
- R0=20:
- R0=30:
- R0=50:

Q1.2. For R0=30 test the segmentation without smoothing and then with Niter_smooth = 1 and 2. Comment on the segmentation quality for:

- no smoothing:
- Niter_smooth = 1:
- Niter_smooth = 2:

Q1.3. Now run the segmentation on the **noisy version** of the image. 2 types of noise are simulated: (1) Additive Gaussian noise, (2) Speckle (multiplicative) noise.

Q1.3.1 Check **appearance** of the 2 noisy images. Why is there no noise in the background in the speckle case?

Answer:

Q1.3.2 Using **R0=50**, run the segmentation on the noisy images **without** and with **smoothing** (Niter_smooth= 1). Comment on segmentation quality or issues for the 4 observations:

- Speckle noise + no smoothing:
- Speckle noise + smoothing:
- Gaussian noise + no smoothing:
- Gaussian noise + smoothing:

```
In [ ]: # 1ST image
img_ori      = img_cardiacshape; r0 = 175; c0=175; R0 = 10
img_noisy     = random_noise(img_ori, mode='gaussian', mean = 0.1, clip =
img_noisy     = random_noise(img_ori, mode='speckle', mean = 0.1, clip = T

# Choose image to segment
img_to_seg    = img_ori
img_to_seg_raw = img_to_seg # to plot later on

alpha_val     = 0.01 ; beta_val = 0.1 ; gamma_val = 0.01;
convergence_val = 1e-4; Niter_snake = 1800;

# Initialise contour
init = define_initial_circle(R0, r0, c0)
```

```

# Pre-smooth the image
Niter_smooth      = 1 # set to 0 for no smoothing
img_to_seg        = gaussian(img_to_seg, Niter_smooth, preserve_range=False)

# Run active contour
snake1 = active_contour(img_to_seg,
                        init, max_num_iter=1, convergence=convergence_val,
                        alpha=alpha_val, beta=beta_val, gamma=gamma_val)
snake10 = active_contour(img_to_seg,
                        init, max_num_iter=10, convergence=convergence_val,
                        alpha=alpha_val, beta=beta_val, gamma=gamma_val)
snake_max = active_contour(img_to_seg,
                        init, max_num_iter=Niter_snake, convergence=convergence_val,
                        alpha=alpha_val, beta=beta_val, gamma=gamma_val)

# Display results
fig, axes = plt.subplots(1,2, figsize=(8, 4), constrained_layout=True)
ax        = axes.ravel()
Font_size = 9
ax[0].imshow(img_to_seg_raw, cmap=plt.cm.gray);
ax[0].set_xticks([]), ax[0].set_yticks([]);
ax[0].set_title("Image to segment", fontsize=Font_size);

ax[1].imshow(img_to_seg, cmap=plt.cm.gray);
ax[1].plot(init[:, 1], init[:, 0], '--y', lw=1);
ax[1].plot(snake10[:, 1], snake1[:, 0], '-b', lw=1);
ax[1].plot(snake10[:, 1], snake10[:, 0], '-g', lw=1);
ax[1].plot(snake_max[:, 1], snake_max[:, 0], '-r', lw=2);
ax[1].set_xticks([]), ax[1].set_yticks([]);
ax[1].axis([0, img_to_seg.shape[1], img_to_seg.shape[0], 0]);
ax[1].set_title("Smoothed image + Seg", fontsize=Font_size);

plt.show();

```

Seg #2:

Snake on Cell image

We are using here **img_to_seg = img_cell** for which you have a ground truth mask **gt_cell** of the target segmentation for the bright right cell.

TODO

Q2.1 Segment large right cell: Run with code as provided and check quality of the segmentation versus the ground-truth. Did it work?

Answer:

Q2.2 Now aiming to segment the internal dark part of the cell: change only values for

Niter_smooth and R0 and propose a solution that works.

Answer: managed to obtain a correct segmentation with Niter_smooth = XX and R0 = XX

Q2.3 Segment small left cell: Run with the proposed initialisation and check correct segmentation of the whole left cell. Now change ONLY some initial contour parameter(s) **[r0 = 153; c0=66; R0 = 25]** to obtain a perfect segmentation of the internal bright center of the cell.

Answer: managed to obtain a correct segmentation with [r0 = XX; c0=XX; R0 = XX]

```
In [ ]: # Input image and parameter values
img_to_seg = img_cell;
img_gt      = gt_cell;

# Large right cell - ground truth provided
r0 = 128; c0=128; R0 = 53
# Small left cell - no ground truth
#r0 = 153; c0=66; R0 = 25

alpha_val = 0.01 ; beta_val = 0.1 ; gamma_val = 0.01;
convergence_val = 1e-4; Niter_snake = 1200;

# Pre smooth the image
Niter_smooth = 1
img_to_seg = gaussian(img_to_seg, Niter_smooth, preserve_range=False)

# Initialise contour
init = define_initial_circle(R0,r0,c0)

# Run active contour
snake30 = active_contour(img_to_seg,
                        init, max_num_iter=30, convergence=convergence_val,
                        alpha=alpha_val, beta=beta_val, gamma=gamma_val)
snake = active_contour(img_to_seg,
                      init, max_num_iter=Niter_snake, convergence=convergence_val,
                      alpha=alpha_val, beta=beta_val, gamma=gamma_val)

# Display results
fig, axes = plt.subplots(1,2, figsize=(8, 4),constrained_layout=True)
ax        = axes.ravel()
Font_size = 9

ax[0].imshow(img_to_seg, cmap=plt.cm.gray)
ax[0].plot(init[:, 1], init[:, 0], '--y', lw=1)
ax[0].plot(snake30[:, 1], snake30[:, 0], '-b', lw=1.5)
ax[0].plot(snake[:, 1], snake[:, 0], '-r', lw=2)
ax[0].set_xticks([]), ax[0].set_yticks([])
ax[0].axis([0, img_to_seg.shape[1], img_to_seg.shape[0], 0])
```

```

ax[1].imshow(img_gt, cmap=plt.cm.gray)
ax[1].plot(init[:, 1], init[:, 0], '--y', lw=1)
ax[1].plot(snake30[:, 1], snake30[:, 0], '-b', lw=1.5)
ax[1].plot(snake[:, 1], snake[:, 0], '-r', lw=2)
ax[1].set_xticks([]), ax[1].set_yticks([])
ax[1].axis([0, img_to_seg.shape[1], img_to_seg.shape[0], 0])

plt.show();

```

Seg # 3

A tool to visualise the deformations of the snake over iterations

TO DO:

Run the code with provided parameter values.

Q3.1 Checking the video, would you confirm that the snake has converged and is stable?

Answer:

Q3.2 Change R_0 to $R_0 = 52$. Has convergence time been shorter or longer? Did you expect such observation (yes/no)?

Answer: convergence time shorter/longer. It was (not?) expected since XX...

```

In [ ]: img_to_seg      = img_cell
        img_to_seg_ori = img_to_seg

# Init to segment cell
r0 = 128; c0=128; R0 = 53
alpha_val = 0.01 ; beta_val = 0.1 ; gamma_val = 0.01;
convergence_val = 1e-4; Niter_snake = 800;

# Pre filter the image
img_adapteq = skimage.exposure.equalize_adapthist(img_to_seg, clip_limit=0.0)
# Pre smooth the image
Niter_smooth = 1
img_to_seg = gaussian(img_to_seg, Niter_smooth, preserve_range=False)

# Initialise contour
init = define_initial_circle(R0,r0,c0)

# Run active contour while saving intermediate contours to see deformations
segs = []

```

```

print('start')
for i in range(1, Niter_snake, 20):
    print(i, " ", end='')
    segs.append(active_contour(img_to_seg, init, max_num_iter=i, convergence
                              alpha=alpha_val, beta=beta_val, gamma=gamma_val))

print('stop')
np.save('ANIM_contours.npy', np.array(segs))

# display animation
segs = np.load('ANIM_contours.npy')
anim = animate_snake(img_to_seg, segs);
HTML(anim.to_html5_video())

```

Seg # 4

Snake with Gradient Vector Flow (GVF)

This implementation of the GVF is performed by computing the edge map, diffusing the gradient over the whole image and directly input the GVF_edge_map to be used as external forces by setting $w_{line}=1$ and $w_{edge}=0$ in the active_contour function.

TODO:

Q4.1.1 Report the visual differences in the GVF_map between $\mu=5$ and $\mu=15$.

Answer:

Q4.1.2 What is the μ parameter controlling?

Answer: The μ parameter controls for XX.

Q4.2 Why does $\mu=15$ enable to obtain a correct segmentation?

Answer:

Q4.3 Report what happens when segmenting with the classic Edge_map rather than the GVF_map.

Answer:

```

In [ ]: import gvf_elsa2
        from gvf_elsa2 import gradient_field, gradient_vector_flow

# Image to seg
img_to_seg = img_star

```



```

r0 = 64; c0=64; R0 = 50

alpha_val = 0.01 ; beta_val = 0.1; gamma_val = 0.01;
convergence_val = 1e-4; Niter_snake = 200;

# Initialise contour
init = define_initial_circle(R0,r0,c0,Nber_pts=400)

# Compute edge map and gvf
img_to_seg = img_to_seg.astype(np.float32) / np.max(img_to_seg)
Edge_map = edge_map(img_to_seg,sigma=1)

fx, fy = gradient_field(img_to_seg)
gx, gy = gradient_vector_flow(fx, fy, mu=5)
GVF_map = np.sqrt(gx**2 + gy**2)

# Run active contour while saving intermediate contours to see deformations
Map_to_seg = Edge_map

# Run active contour while saving intermediate contours to see deformations
segs = []
print('start')
for i in range(1,Niter_snake,10):
    print(i, " ", end='')
    segs.append(active_contour(Map_to_seg, init, max_num_iter=i, convergence
                              alpha=alpha_val, beta=beta_val, gamma=gamma_val,
                              w_line=1,w_edge=0))

print('stop')
np.save('ANIM_contours.npy', np.array(segs))

# display animation
segs = np.load('ANIM_contours.npy')
anim = animate_snake(Map_to_seg, segs);
HTML(anim.to_html5_video())

```

Seg # 5:

The active contour with fixed end points

You will now run the active_contour with the option to maintain some points from the initial contour fixed. You are working with the **img_oct_eye** which shows different layers of the retina. The **active_contour** routine is called to used directly the **Edge_map** as input.

TO DO:

Q5.1 Rank the 4 options for the Edge_map options from top to worst to segment the two layers wrt to segmentation quality and robustness to layer selection.

Answer: Ranked Edge_map options from best to worst:

1. edge_test1
2. edge_test2
3. edge_test2_l
4. edge_testl_2

```
In [ ]: img_to_seg = img_oct_eye

# init for 1st layer
r_left = 103; r_right=138; c_left=0; c_right = 510
# init for 2nd layer
#r_left = 158; r_right=204; c_left=0; c_right = 510

alpha_val = 0.01 ; beta_val = 0.1; gamma_val = 0.01;
convergence_val = 1e-4; Niter_snake = 500;
w_line_val=1; w_edge_val=0;

# Computation of edge maps
edge_test1      = edge_map(img_to_seg, sigma=1)
edge_test2      = edge_map(img_to_seg, sigma=2)
edge_test2_l    = np.log2((edge_test2*100)+1)
edge_testl_2    = edge_map(np.log2((img_to_seg+1)*100), sigma=2)

# Selection of edge_map to use
Edge_map        = edge_test1

# Initialise contour
Nber_pts_contour = 200
r                = np.linspace(r_left, r_right, Nber_pts_contour)
c                = np.linspace(c_left, c_right, Nber_pts_contour)
init             = np.array([r, c]).T

snake = active_contour(Edge_map,
                       init, boundary_condition='fixed-fixed', max_num_iter=N
                       alpha=alpha_val, beta=beta_val, gamma=gamma_val,
                       w_line=w_line_val, w_edge=w_edge_val)

# FIGURE

fig, ax = plt.subplots(figsize=(9, 5));
ax.imshow(Edge_map[0:300,:], cmap=plt.cm.gray);
ax.plot(init[:, 1], init[:, 0], '--y', lw=2);
ax.plot(snake[:, 1], snake[:, 0], '-r', lw=3);
ax.set_xticks([]), ax.set_yticks([]);
ax.set(xlim=(0, 500));
plt.show();
```

Seg # 6

BONUS - Optional

Your turn on proposing a motivated pipeline using the snake capabilities from the `active_contour` function

TODO:

Choose a new image in the pool provided and propose a segmentation pipeline using the `active_contour` approach. Options on points to work on include:

- Pre-filter the image as you wish
- Manually or automatically position the initial contour
- Provide one segmentation result or merge several solutions in a probability map
- Detect issues in contour shape during deformations and propose an early stop criteria.

Q6 Provide code + visual illustrations of results

Answer

Seg #7

Test on the Geometric Level-Set formulation using the Chan-Vese model.

Skimage provides two implementations of the Chan-Vese approach:

[1] `chan_vese`: |implementation or original paper
and

[2] `morphological_chan_vese`: faster implementation but less precise. "Active contours without edges implemented with morphological operators. It is required that the inside of the object looks different on average than the outside (i.e., the inner area of the object should be darker or lighter than the outer area on average)."

The contours of objects are now encoded in a level set function **Φ** .

The **initialisation** tested here is with a "checkerboard" pattern for 2 classes (object and background).

For the **`chan_vese`** original implementation, the **hyper-parameters** include:

- $\mu = 0.25$ (default) | edge regularisation terms. Similar to 'edge length' weight parameter. Higher μ values will produce 'smoother' contours.
- $dt = 0.5$ (default) | delta time step for each optimisation step.
- $\lambda_1=1, \lambda_2=1$ (default) | weights in the cost metric to balance inside and

outside homogeneity terms.

- `tol=1e-3` (default) | Tolerance to test if the contours are "stable" and stop early.

The output contains: `cv[0]=Seg` and `cv[1]=Phi`

For the **morphological_chan_vese** implementation, the only **hyper-parameter** is the number of smoothing iterations (1 to 4 recommended).

TO DO:

Using **Chan-Vese** original implementation:

Q7.1 Run the code on **img_hela** with 200 iterations using **raw image** and the same image after **histogram equalisation**. What are differences observed in the Segmentation results and in the numerical values of the Phi level set function?

Answer:

Differences in the segmentation results: The segmented region is approximately the same, but the histogram equalisation makes the region selected smoother and more accurate (the segmentation without filtering shows some regions outside the main area).
Differences in the Phi values: The functions values without histogram equalisation appear with aliasing. The same figure with the pre filtering shows a much smoother function, without aliasing

Q7.2 Run the code on **img_hela** with **2** iterations using raw image. Why does the Segmentation image show the structures to segment but with "gray" values while this is a binary image?

Answer: This happens because of the initialization parameter `checkboard`. Then, the function ϕ follows a checkboard pattern, varying from positive to negative. This creates the optical illusion of appearing gray, but in fact, it is a grid of black and white squares.

Q7.3 Run the code on **img_hela** with 200 iterations using raw image but changing the `tol_val = 10-5`. Comment on major differences observed compared to `tol_val = 10-3` and propose an explanation:

Answer: The biggest difference is on the contours of the segmented region. With a lower `tol_val`, the contours are smoother and with less abrupt changes.

Q7.4 Run the code on **img_cell** with 200 iterations using raw image. Comment on the issue observed with this method if you compare to the segmentation targeted given in **gt_cell**:

Answer: The method creates holes in the segmentation that should not have appeared.

It also segments other cells that partially appear in the image. Moreover, it seems like the method segments the background instead of the cell (the cell appears black).

Using **morphological_chan_vese** implementation:

Q7.5 Run the code on **img_cell** with 100 iterations using raw image. Compare using `Init_method_cv_morpho= "checkerboard" or "disk". :`

Answer:

General benefits from this implementation of Chan-Vese: This method correctly tries to segment the cell from the background (instead of the other way around).

Common issue seen on both segmentation results: Other objects are segmented with the cell. In this implementation, holes keep appearing inside the segmented area.

Issue seen when using Morpho CV + disk: With the disk initialization, the cell in the middle of the image seems to have been correctly segmented (without holes), but it is black, which suggests the function is segmenting the background. Moreover, there seems to be small particles that were mistakenly segmented with the cell. Finally, the segmentation of the cell joins with the segmentation of another cell in the bottom of the image.

Using one of the **chan_vese** implementation:

Q7.6 Segment the image: **img_fluo** and report the setup that lead to the best result. Include a display of the prefiltered-image and the segmentation results in the notebook. You can use any filtering you want :

Answer:

Parameters used: $\text{tol_val} = 10^{-5}$, 200 iterations, morphological implementation

Initialisation used: checkerboard

Pre-processing used: Gaussian filtering ($\sigma = 5$) followed by histogram equalization

Bonus points

Q7.7 Evaluate the quality of the segmentation of **img_fluo** Display together your segmentation results and the ground-truth provided. Propose a measure to compare these segmentations. Provide code and display results in a new cell below :

Answer: Add here any comment you would like to add

```
In [85]: img_raw      = img_fluo # img_hela[0] changed 2025 for some environments - img
img_to_seg = img_raw

# PARAMETERS
```

```

mu_val=0.5 ; lambda1_val=1; lambda2_val=1;
tol_val=1e-5; dt_val=0.5

smoothing_val = 1
PRE_FILTER     = 1

Num_iter_cv_ori      = 200
Num_iter_cv_morpho   = 200

CHAN_VESE_ORI = 0
Init_method_cv_ori      = "checkerboard" # "checkerboard" or "disk" or "small di
Init_method_cv_morpho   = "checkerboard" # "disk" # or "disk" or "small di

# Pre-filter (TO TURN ON IF ASKED)
if PRE_FILTER:
    img_gauss = skimage.filters.gaussian(img_raw, sigma=5)
    img_adapteq = skimage.exposure.equalize_adapthist(img_gauss, clip_limit=
    img_to_seg = img_adapteq

# Select image to segment and print information
print("min - max value in image:" , np.min(img_to_seg), np.max(img_to_seg))
print("size of image:" , img_to_seg.shape)

# run segmentation
if CHAN_VESE_ORI == 1:
    # STANDARD implementation from original paper
    init_ls = checkerboard_level_set(img_to_seg.shape, 45)

    cv = chan_vese(img_to_seg, mu=mu_val, lambda1=lambda1_val, lambda2=lambd
                    tol=tol_val, dt=dt_val,
                    max_num_iter=Num_iter_cv_ori, init_level_set=Init_method_
                    extended_output=True)

    # Show results
    Nber_plots = 4
    fig, axes = plt.subplots(2,2,figsize=(7, 7))
    ax = axes.ravel()
    ax[0].imshow(img_to_seg, cmap=plt.cm.gray)
    ax[0].set_title("Image to segment", fontsize=12);
    ax[1].imshow(1-cv[0], cmap=plt.cm.gray)
    title = f'C-V with - {len(cv[2])} iterations'
    ax[1].set_title(title, fontsize=12)
    ax[2].imshow(1-cv[0][0:64,0:64], cmap=plt.cm.gray)
    ax[2].set_title("Zoom on segmentation result", fontsize=12);
    tmp_show = ax[3].imshow(cv[1][0:64,0:64], cmap=plt.cm.jet)
    ax[3].set_title("Zoom on final Phi", fontsize=12);
    plt.colorbar(tmp_show,ax=ax[3], shrink=0.75, location='right')

    print("min - max value in Seg (cv[0]):" , np.min(cv[0]), np.max(cv[0]))

else:
    # FASTER implementation implemented with morphological operators BUT LES
    cv = morphological_chan_vese(img_to_seg, num_iter=Num_iter_cv_morpho

```

```

smoothing=smoothing_val, init_level_se

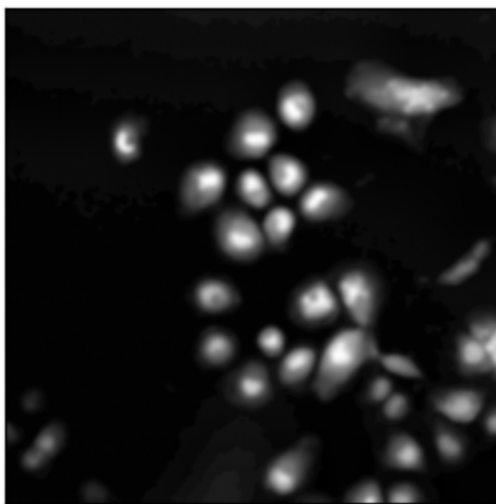
# Show results
Nber_plots = 2
fig, ax = plt.subplots(1,2,figsize=(7, 7))
ax[0].imshow(img_to_seg, cmap=plt.cm.gray)
ax[1].imshow(1-cv, cmap=plt.cm.gray)
title = f'C-V_morph with - {Num_iter_cv_morpho} iterations'
ax[1].set_title(title, fontsize=12)

for i in range(0,Nber_plots):
    ax[i].set_xticks([]), ax[i].set_yticks([]);

plt.show();

```

min - max value in image: 0.0 1.0
size of image: (1024, 1024)

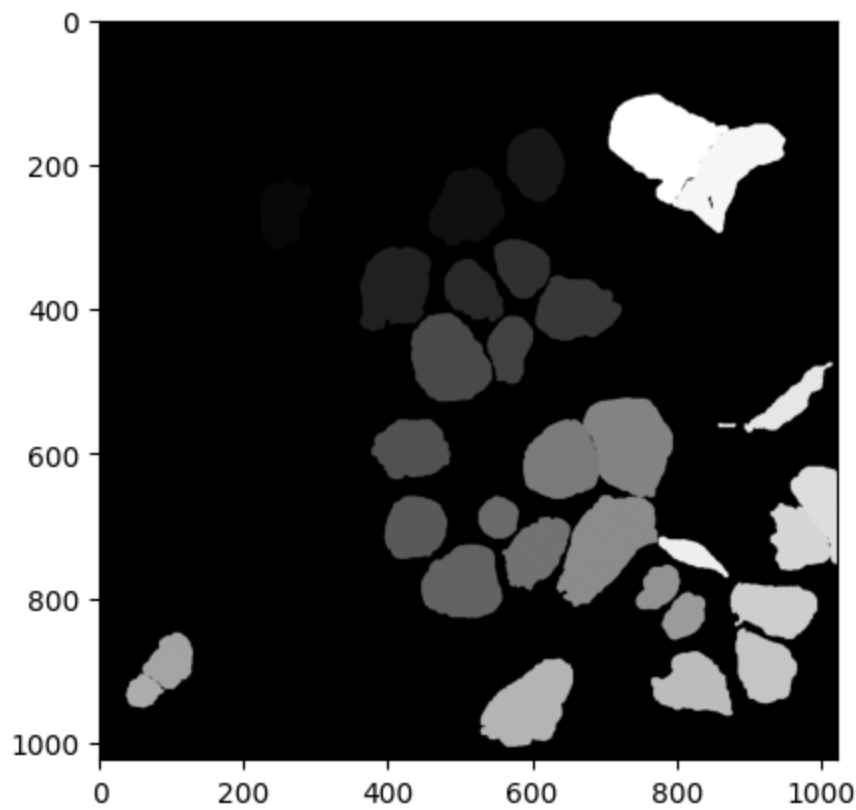


C-V_morph with - 200 iterations



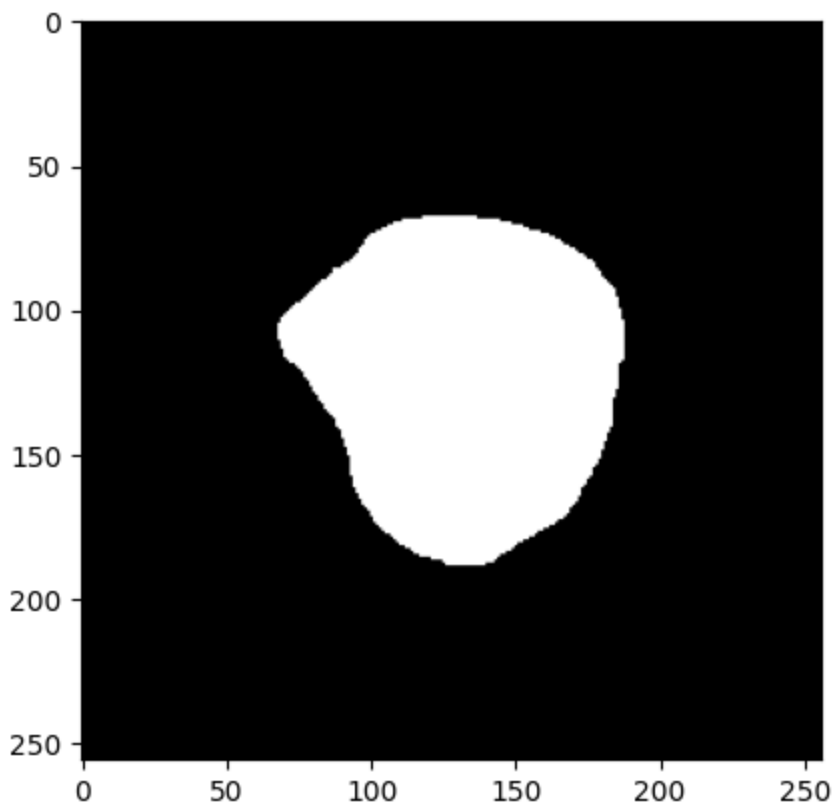
In [59]: `plt.imshow(gt_fluo, cmap="gray")`

Out[59]: `<matplotlib.image.AxesImage at 0x12d0c0cd0>`



```
In [30]: plt.imshow(gt_cell, cmap="gray")
```

```
Out[30]: <matplotlib.image.AxesImage at 0x11e26bd90>
```



Seg # 8

Geometric active contours with balloon force

Controlling level-set deformable model with speed values acting on the contour.

You are provided with a tool to track the deformation patterns of the active contour over iterations.

The geometric active contour routine is **morphological_geodesic_active_contour** which deforms a level set function with local speed values. It has the following **hyper-parameters** :

- **Thresh_cont_val** = 'auto'=> np.percentile(image, 40) (default if 'auto') | pixels < Thresh_cont_val are considered borders. The evolution of the contour will stop on these pixels. (It is used in the code to cancel the balloon speed using: Threshold_mask_balloon = image > threshold / np.abs(Balloon_weight))
- **Balloon_weight** = 1 (default) | weight of the balloon force. Can be negative to inflate/deflate
- **Smooth_cont_iter** = 1 (default) | Number of times a smoothing operator is applied per iteration

TO DO:

Q8.1: Segment the **img_cell** with the provided configuration to **inflate** the initial contour using Conf #1. What is the issue when compared to the targeted ground-truth (GT) segmentation ?

Answer: The method segmented only the center of the cell, instead of the whole cell.

Q8.2: Segment the **img_cell** with the provided configuration to **inflate** the initial contour using Conf #2.

- What is the issue when compared to the targeted ground-truth (GT) segmentation ?

Answer: It also segments another cell with the one begin analysed. This extra segmentations shows a hole as well.

- What benefit(s) do you observe when using this "implicit" formulation of a deformable model versus a snake-like "explicit" model using the same initialisation set-up and a balloon force: ?

Answer: One main advantage is that the implicit (level-set) formulation naturally

allows the contour to split or merge during deformation without extra work. An explicit (snake-like) model would need special handling whenever its topology changes.

Q8.3: Now Segment the **img_CTabd** with the provided configuration Conf #3 to **deflate** the initial contour (Adjust balloon parameter accordingly). Comment with your own words the quality and properties of the obtained segmentation:

Answer: The kidneys are correctly segmented, but the function segments other parts of the image, like the spine. It also wrongly adds some particles to the segmentation result.

Bonus points

Q8.4a: Check by yourself and explain why you think pre-processing using `skimage.morphology.diameter_closing` help the segmentation on **img_CTabd** ?

Answer:

Q8.4b: Provide a different set up (with printed code and results) with different initialisation and/or pre-processing set-up that leads to a correct segmentation of the 2 kidneys (as in the ground truth).

Answer:

```
In [91]: # img_cell:
# img_raw      = img_cell ;
# gt_seg       = gt_cell

# img_CTabd:
img_raw      = img_CTabd ;
gt_seg       = gt_CTabd

# Select img to segment
img_to_seg = img_raw;

# Conf #1: Disk parameters to initialise shape for INFLATION on img_cell
# r0 = 130;  c0 = 125 ; R0 = 30  # inflate
# Conf #2: Disk parameters to initialise shape for INFLATION on img on img_c
# r0 = 130;  c0 = 125 ; R0 = 45  # inflate
# Conf #3: Disk parameters to initialise shape for DEFLATION on img
r0 = 130;  c0 = 145 ; R0 = 85  # deflate TO KEEP ON CTabd

# Hyper-parameter for Balloon velocity:
Balloon_weight = -1 ; # +1 or -1 to Inflate or deflate

# Additional Hyper-parameters for geodesic deformable model:
Threshold_contour_level = 20;
```

```
Smooth_cont_iter      = 1 ; # Number of times a smoothing operator is appl
Niter_snake           = 600

# Hyper-parameter for preparing the input data:
INV_EDGE_MAP = 1; # needed when using the Balloon force

# Pre-processing the image with closing
img_to_seg = skimage.morphology.diameter_closing(img_to_seg, 40, connectivit

# Inverse edge image: Compute the magnitude of the gradients in the image an
# then inverts the result in the range [0, 1]
if INV_EDGE_MAP:
    img_to_seg = skimage.segmentation.inverse_gaussian_gradient(
        img_to_seg, alpha=50, sigma=2)

# Print information
print("min - max value in image to seg:" , np.min(img_to_seg), np.max(img_to
print("size of image to seg:" , img_to_seg.shape)

# Set and print threshold used in morphological_geodesic_active_contour
# Areas of the inverse edge map with value < Threshold will be considered bo
Threshold_contour = np.percentile(img_to_seg, Threshold_contour_level);
Thresh_cont_val   = Threshold_contour ; # 'auto' ; # pixels < Thresh_cont_va
print("threshold used in morphological_geodesic", Thresh_cont_val)

# initialise call back
evolution = []
callback = store_evolution_in(evolution)

# Initialise contour as a disk
init_ls   = skimage.segmentation.disk_level_set(img_to_seg.shape, center=[r0,

# Run geodesic active contour
ls        = morphological_geodesic_active_contour(
    img_to_seg, Niter_snake, init_ls,
    smoothing=Smooth_cont_iter, balloon=Balloon_weight,
    threshold=Thresh_cont_val,
    iter_callback=callback);

# Figure with plots of level-set evolution
fig, axes = plt.subplots(2, 2, figsize=(8, 8));
ax = axes.flatten();

ax[0].imshow(img_raw, cmap="gray");
ax[0].set_axis_off();
contour = ax[0].contour(evolution[0], [0.5], colors='y');
#contour.collections[0].set_label("Contours"); #removed 2025
ax[0].contour(ls, [0.5], colors='r');
ax[0].set_title("Img ori + contours", fontsize=12);

ax[1].imshow(img_to_seg, cmap="gray");
ax[1].set_axis_off();
contour = ax[1].contour(evolution[0], [0.5], colors='y');
#contour.collections[0].set_label("Contours"); #removed 2025
#contour.set_label("Contours"); # option to update 2025
```

```
#ax[0].contour(ls, [0.5], colors='r');#removed 2025
ax[1].contour(ls, [0.5], colors='r');
ax[1].set_title("Img to seg + contours", fontsize=12);
#ax[1].contour(ls, [0.5], colors='r');#removed 2025

ax[2].imshow(img_to_seg, cmap="gray");
ax[2].set_axis_off();
contour = ax[2].contour(evolution[0], [0.5], colors='y');
#contour.collections[0].set_label("Contours"); # removed 2025
title = f'Morphological GAC Curve evolution';
ax[2].set_title(title, fontsize=12);
for i in range(1, Niter_snake-1, 5):
    contour = ax[2].contour(evolution[i], [0.5], linewidths=0.5, colors='r')

ax[3].imshow(gt_seg, cmap="gray");
ax[3].set_axis_off();
ax[3].contour(ls, [0.5], colors='r');
ax[3].set_title("GT segmentation mask", fontsize=12);

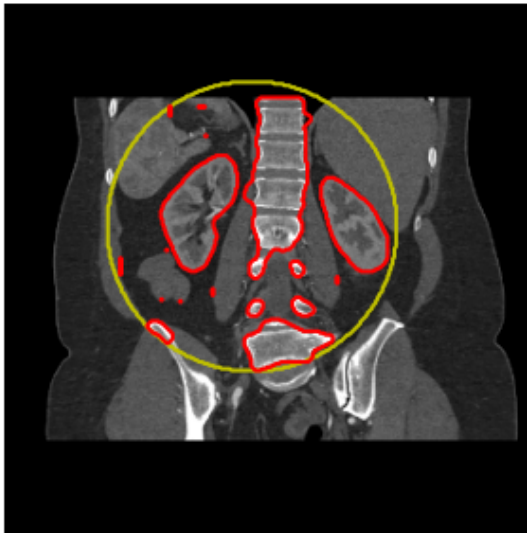
plt.show();
```

min - max value in image to seg: 0.3062454376394709 1.0

size of image to seg: (311, 311)

threshold used in morphological_geodesic 0.7199191982831742

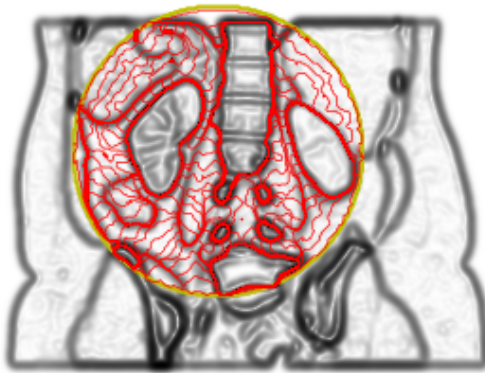
Img ori + contours



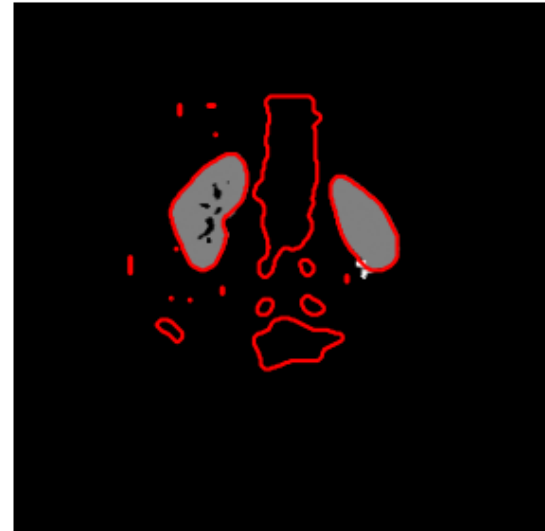
Img to seg + contours



Morphological GAC Curve evolution



GT segmentation mask



In []: