# Introduction to Vinyl

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July 9, 2014

Haskell records are nominally typed

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```
data R = R \{ x :: X \}
```

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```
data R = R { x :: X }
data R' = R' { x :: X } -- ^Error
```

# Structural Typing

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Sharing field names and accessors

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- Sharing field names and accessors
- Record types may be characterized structurally

How do we express the type of a function which adds a field to a record?

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$$\frac{x:\{foo:A;\vec{rs}\}}{f(x):\{foo:A,bar:B;\vec{rs}\}}$$

**data** (s :: Symbol) ::: (t :: \*) = Field

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data Rec ::  $[*] \rightarrow *$  where

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```

```
data Rec :: [*] \rightarrow * where RNil :: Rec '[]
```

```
data (s :: Symbol) ::: (t :: *) = Field

data Rec :: [*] → * where
    RNil :: Rec '[]
    (:&) :: !t → !(Rec rs) → Rec ((s ::: t) ': rs)
```

```
\label{eq:data} \begin{tabular}{ll} \textbf{data} & (s::Symbol) ::: (t::*) = Field \\ \\ \textbf{data} & Rec :: [*] \rightarrow * \textbf{where} \\ \\ & RNil :: Rec '[] \\ & (:\&) :: !t \rightarrow !(Rec \ rs) \rightarrow Rec \ ((s:::t) \ ': rs) \\ \\ \textbf{class} & s \in (rs::[*]) \\ \\ \end{tabular}
```

```
data (s :: Symbol) ::: (t :: *) = Field
data Rec :: [*] \rightarrow * where
  RNil :: Rec '[]
  (:\&) :: !t \rightarrow !(Rec rs) \rightarrow Rec ((s ::: t) ': rs)
class s \in (rs :: [*])
class ss \subseteq (rs :: [*]) where
  cast :: Rec rs → Rec ss
```

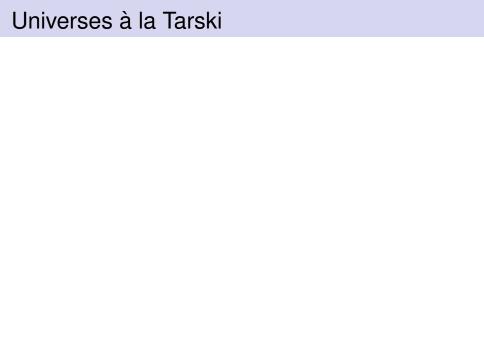
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data (s :: Symbol) ::: (t :: *) = Field
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(=:) : s ::: t \rightarrow t \rightarrow Rec '[s ::: t]
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(\oplus): Rec ss \rightarrow Rec ts \rightarrow Rec (ss ++ ts)
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data Rec :: [*] \rightarrow * where
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class s \in (rs :: [*])
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(=:) : s ::: t \rightarrow t \rightarrow Rec '[s ::: t]
(\oplus): Rec ss \rightarrow Rec ts \rightarrow Rec (ss ++ ts)
lens : s ::: t \in rs \Rightarrow s ::: t \rightarrow Lens' (Rec rs) t
```

```
f :: Rec ("foo" ::: A ': rs)

→ Rec ("bar" ::: B ': "foo" ::: A ': rs)
```



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- ▶ Function  $El_{\mathcal{U}}: \mathcal{U} \to \mathsf{Type}$ .

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$$\frac{\Gamma \vdash s : \mathcal{U}}{\Gamma \vdash El_{\mathcal{U}}(s) : \mathsf{Type}}$$

universe-empty.pdf

universe-embedded.pdf

universe-populated.pdf

universe-interpretation.pdf

# Records in Haskell

### Records in Haskell

data Rec :: ( $\mathcal{U} \to *$ )  $\to$  [  $\mathcal{U}$  ]  $\to *$  where

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```
data Rec :: (\mathcal{U} \to *) \to [\ \mathcal{U}\ ] \to * where
RNil :: Rec el_{\mathcal{U}} '[]
(:&) :: !(el_{\mathcal{U}} r) \to !(Rec el_{\mathcal{U}} rs) \to Rec el_{\mathcal{U}} (r ': rs)
```

 $\textbf{data} \; \mathsf{TyFun} :: * \to * \to *$ 

```
data TyFun :: * \rightarrow * \rightarrow *
type family (f :: TyFun k I \rightarrow *) $ (x :: k) :: I
```

```
data TyFun :: * \rightarrow * \rightarrow * type family (f :: TyFun k l \rightarrow *) $ (x :: k) :: l

data Rec :: (TyFun \mathcal{U} * \rightarrow *) \rightarrow [ \mathcal{U} ] \rightarrow * where
RNil :: Rec el_{\mathcal{U}} '[]
(:&) :: !(el_{\mathcal{U}} $ r) \rightarrow !(Rec el_{\mathcal{U}} rs) \rightarrow Rec el_{\mathcal{U}} (r ': rs)
```

data Id :: (TyFun k k)  $\rightarrow$  \* where type instance Id \$ x = x

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**type** HList rs = Rec ld rs

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type HList rs = Rec ld rs

ex :: HList  $[\mathbb{Z}, Bool, String]$ 

```
data Id :: (TyFun k k) \rightarrow * where type instance Id $ x = x
```

type HList rs = Rec ld rs

```
ex :: HList [\mathbb{Z}, Bool, String] ex = 34 :& True :& "vinyl" :& RNil
```

bob :: Rec  $EI_{\mathcal{A}}$  [Name, Email Work]

bob :: Rec El<sub>A</sub> [Name, Email Work] bob = Name =: "Robert<sub>→</sub>Harper" ⊕ Email Work =: "rwh@cs.cmu.edu"

```
bob :: Rec El_{\mathcal{A}} [Name, Email Work]
bob = Name =: "Robert_Harper"
\oplus Email Work =: "rwh@cs.cmu.edu"
```

```
validateName :: String \rightarrow Either Error String validateEmail :: String \rightarrow Either Error String validatePhone :: [\mathbb{N}] \rightarrow Either Error [\mathbb{N}]
```

```
bob :: Rec El_{\mathcal{A}} [Name, Email Work]
bob = Name =: "Robert_Harper"
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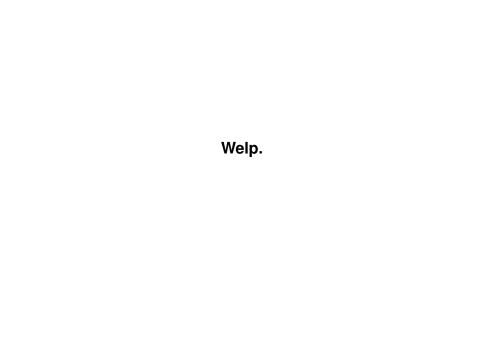
```
validateName :: String \rightarrow Either Error String validateEmail :: String \rightarrow Either Error String validatePhone :: [\mathbb{N}] \rightarrow Either Error [\mathbb{N}]
```

```
bob :: Rec El_A [Name, Email Work]
bob = Name =: "Robert_Harper"
\oplus Email Work =: "rwh@cs.cmu.edu"
```

```
validateName :: String \rightarrow Either Error String validateEmail :: String \rightarrow Either Error String validatePhone :: [\mathbb{N}] \rightarrow Either Error [\mathbb{N}]
```

validateContact
:: Rec El<sub>A</sub> [Name, Email Work]

→ **Either** Error (Rec El<sub>A</sub> [Name, Email Work])



```
data Rec :: (TyFun \mathcal{U} * \to *) \to [\mathcal{U}] \to * where RNil :: Rec el<sub>\mathcal{U}</sub> '[] (:&) :: !(el<sub>\mathcal{U}</sub> $ r) \to !(Rec el<sub>\mathcal{U}</sub> rs) \to Rec el<sub>\mathcal{U}</sub> (r ': rs)
```

```
data Rec :: (TyFun \mathcal{U} * \to *) \to (* \to *) \to [\mathcal{U}] \to * where RNil :: Rec el_{\mathcal{U}} f '[] (:&) :: !(f (el_{\mathcal{U}} \ \ r)) \to !(Rec \ el_{\mathcal{U}} \ \ f \ rs) \to Rec \ el_{\mathcal{U}} \ f \ (r \ \ ': rs)
```

```
data Rec :: (TyFun \mathcal{U} * \to *) \to (* \to *) \to [\mathcal{U}] \to * where RNil :: Rec el_{\mathcal{U}} f '[] (:&) :: !(f (el_{\mathcal{U}} $ r)) \to !(Rec el_{\mathcal{U}} f rs) \to Rec el_{\mathcal{U}} f (r ': rs)
```

(=:) : Applicative f  $\Rightarrow$  sing r  $\rightarrow$  el<sub> $\mathcal{U}$ </sub> \$ r  $\rightarrow$  Rec el<sub> $\mathcal{U}$ </sub> f '[r]

```
data Rec :: (TyFun \mathcal{U} * \to *) \to (* \to *) \to [\mathcal{U}] \to * where RNil :: Rec el<sub>\mathcal{U}</sub> f '[] (:&) :: !(f (el<sub>\mathcal{U}</sub> $ r)) \to !(Rec el<sub>\mathcal{U}</sub> f rs) \to Rec el<sub>\mathcal{U}</sub> f (r ': rs)
```

(=:) : Applicative f  $\Rightarrow$  sing r  $\rightarrow$  el<sub>\(\mathcal{U}\)</sub> \\$ r  $\rightarrow$  Rec el<sub>\(\mathcal{U}\)</sub> f '[r] k =: x = pure x : & RNiI

```
data Rec :: (TyFun \mathcal{U} * \to *) \to (* \to *) \to [\mathcal{U}] \to * where RNil :: Rec el_{\mathcal{U}} f '[] (:&) :: !(f (el_{\mathcal{U}} \$ r)) \to !(Rec el_{\mathcal{U}} f rs) \to Rec el_{\mathcal{U}} f (r ': rs) (=:) : Applicative f \Rightarrow sing r \to el_{\mathcal{U}} $ r \to Rec el_{\mathcal{U}} f '[r] k =: x = pure x :& RNil (\Leftarrow): sing r \to f (el_{\mathcal{U}} \$ r) \to Rec el_{\mathcal{U}} f '[r]
```

```
data Rec :: (TyFun \mathcal{U} * \to *) \to (* \to *) \to [\mathcal{U}] \to * where RNil :: Rec el_{\mathcal{U}} f '[] (:&) :: !(f (el_{\mathcal{U}} \$ r)) \to !(Rec \ el_{\mathcal{U}} \ f \ rs) \to Rec \ el_{\mathcal{U}} \ f (r ': rs) (=:) : Applicative f \Rightarrow sing r \to el_{\mathcal{U}} \$ r \to Rec \ el_{\mathcal{U}} \ f '[r] k =: x = pure x :& RNil (\Leftarrow): sing r \to f (el_{\mathcal{U}} \$ r) \to Rec \ el_{\mathcal{U}} \ f '[r] k \Leftarrow x = x :& RNil
```

 $\textbf{type} \; \mathsf{Rec}_{\mathcal{A}} = \mathsf{Rec} \; \mathsf{El}_{\mathcal{A}}$ 

**type**  $Rec_A = Rec El_A$ bob ::  $Rec_A$  Identity [Name, Email Work]

```
type Rec_{\mathcal{A}} = Rec \ El_{\mathcal{A}}
bob :: Rec_{\mathcal{A}} Identity [Name, Email Work]
bob = Name =: "Robert_Harper"
\oplus Email Work =: "rwh@cs.cmu.edu"
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```
type Rec_{\mathcal{A}} = Rec \ El_{\mathcal{A}}
bob :: Rec_{\mathcal{A}} Identity [Name, Email Work]
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```

**type** Validator  $a = a \rightarrow$  **Either** Error a

**type** Validator  $a = a \rightarrow \textbf{Either}$  Error a validateName ::  $Rec_{\mathcal{A}}$  Validator '[Name] validatePhone ::  $\forall \ell$ .  $Rec_{\mathcal{A}}$  Validator '[Phone  $\ell$ ] validateEmail ::  $\forall \ell$ .  $Rec_{\mathcal{A}}$  Validator '[Email  $\ell$ ]

```
type Validator a = a \rightarrow \textbf{Either} Error a validateName :: Rec_{\mathcal{A}} Validator '[Name] validatePhone :: \forall \ell. Rec_{\mathcal{A}} Validator '[Phone \ell] validateEmail :: \forall \ell. Rec_{\mathcal{A}} Validator '[Email \ell]
```

```
type TotalContact =
  [ Name, Email Home, Email Work
  , Phone Home, Phone Work ]
```

```
type Validator a = a \rightarrow \textbf{Either} Error a validateName :: Rec_{\mathcal{A}} Validator '[Name] validatePhone :: \forall \ell. Rec_{\mathcal{A}} Validator '[Phone \ell] validateEmail :: \forall \ell. Rec_{\mathcal{A}} Validator '[Email \ell]
```

```
type TotalContact =
  [ Name, Email Home, Email Work
  , Phone Home, Phone Work ]
```

validateContact ::  $Rec_A$  Validator TotalContact validateContact = validateName

- ⊕ validateEmail
- ⊕ validateEmail
- ⊕ validatePhone
- ⊕ validatePhone

**newtype** Lift o f g x = Lift  $\{ runLift :: f x 'o' g x \}$ 

```
newtype Lift o f g x = Lift { runLift :: f x 'o' g x }
```

**type** Validator = Lift  $(\rightarrow)$  Identity (**Either** Error)

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**type** Validator = Lift  $(\rightarrow)$  Identity (**Either** Error)

**newtype** Lift o f g x = Lift { runLift :: f x 'o' g x } **type** Validator = Lift ( $\rightarrow$ ) Identity (**Either** Error)

(\*) :: Rec $_{\mathcal{U}}$  (Lift ( $\rightarrow$ ) f g) rs  $\rightarrow$  Rec $_{\mathcal{U}}$  f rs  $\rightarrow$  Rec $_{\mathcal{U}}$  g rs rdist :: Applicative f  $\Rightarrow$  Rec $_{\mathcal{U}}$  f rs  $\rightarrow$  f (Rec $_{\mathcal{U}}$  Identity rs)

```
newtype Lift o f g x = Lift { runLift :: f x 'o' g x } type Validator = Lift (\rightarrow) Identity (Either Error) (\textcircled{*}) :: Rec_{\mathcal{U}} (Lift (\rightarrow) f g) rs \rightarrow Rec_{\mathcal{U}} f rs \rightarrow Rec_{\mathcal{U}} g rs rdist :: Applicative f \Rightarrow Rec_{\mathcal{U}} f rs \rightarrow f (Rec_{\mathcal{U}} Identity rs)
```

```
\begin{array}{l} \textbf{newtype} \ \mathsf{Lift} \ \mathsf{o} \ \mathsf{f} \ \mathsf{g} \ \mathsf{x} = \mathsf{Lift} \ \{ \ \mathsf{runLift} :: \mathsf{f} \ \mathsf{x} \ \mathsf{'o'} \ \mathsf{g} \ \mathsf{x} \ \} \\ \textbf{type} \ \mathsf{Validator} = \mathsf{Lift} \ (\to) \ \mathsf{Identity} \ (\textbf{Either} \ \mathsf{Error}) \\ (\textcircled{\textcircled{}}) \ :: \ \mathsf{Rec}_{\mathcal{U}} \ (\mathsf{Lift} \ (\to) \ \mathsf{f} \ \mathsf{g}) \ \mathsf{rs} \to \mathsf{Rec}_{\mathcal{U}} \ \mathsf{f} \ \mathsf{rs} \to \mathsf{Rec}_{\mathcal{U}} \ \mathsf{g} \ \mathsf{rs} \\ \mathsf{rdist} \ :: \ \mathsf{Applicative} \ \mathsf{f} \ \Rightarrow \ \mathsf{Rec}_{\mathcal{U}} \ \mathsf{f} \ \mathsf{rs} \to \mathsf{f} \ (\mathsf{Rec}_{\mathcal{U}} \ \mathsf{Identity} \ \mathsf{rs}) \end{array}
```

validateContact :: Rec<sub>A</sub> Validator TotalContact

```
\begin{tabular}{ll} \textbf{newtype} & \begin{tabular}{ll} \textbf{Lift} of g x = \begin{tabular}{ll} \textbf{Lift} of g x = \begin{tabular}{ll} \textbf{Lift} (\textbf{runLift} :: f x 'o' g x \\ \textbf{Lift} (\rightarrow) & \begin{tabular}{ll} \textbf{Lift} (\rightarrow
```

validateContact ::  $Rec_A$  Validator TotalContact

bobValid ::  $Rec_A$  (**Either** Error) [Name, Email Work]

```
\begin{tabular}{ll} \textbf{newtype} & Lift of g x = Lift \{ runLift :: f x 'o' g x \} \\ \textbf{type} & Validator = Lift ($\rightarrow$) Identity (\textbf{Either} Error) \\ (\textcircled{*}) :: Rec_{\mathcal{U}} (Lift ($\rightarrow$) f g) rs $\rightarrow$ Rec_{\mathcal{U}} f rs $\rightarrow$ Rec_{\mathcal{U}} g rs \\ rdist :: Applicative f $\Rightarrow$ Rec_{\mathcal{U}} f rs $\rightarrow$ f (Rec_{\mathcal{U}} Identity rs) \\ \end{tabular}
```

validateContact ::  $Rec_A$  Validator TotalContact

bobValid ::  $Rec_A$  (**Either** Error) [Name, Email Work] bobValid = cast validateContact \* bob

```
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```

validateContact :: Rec<sub>A</sub> Validator TotalContact

bobValid :: Rec<sub>A</sub> (**Either** Error) [Name, Email Work] bobValid = cast validateContact \* bob

validBob :: **Either** Error ( $Rec_A$  Identity [Name, Email Work])

```
\begin{tabular}{ll} \textbf{newtype} & \begin{tabular}{ll} \textbf{Lift} of g x = \begin{tabular}{ll} \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (runLift :: f x 'o' g x ) \\ \textbf{Lift} (r
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validateContact :: Rec<sub>A</sub> Validator TotalContact

bobValid ::  $Rec_A$  (**Either** Error) [Name, Email Work] bobValid = cast validateContact \* bob

validBob :: **Either** Error (Rec<sub>A</sub> Identity [Name, Email Work]) validBob = rdist bobValid

