



Chapter 3

QUEUES

Objective

- To introduce:
 - Queues concept
 - Queues operations
 - Application using queues

CONTENT

- 3.1 Introduction
- 3.2 Queues using Array-Based Implementation
- 3.3 Queues Application: Queue Simulation

3.1 Introduction

- Queue is linear list in which data can only be inserted at one end, called the **rear**, and deleted from the other end, called the **front**.
- First-In-First-Out (FIFO) concept.

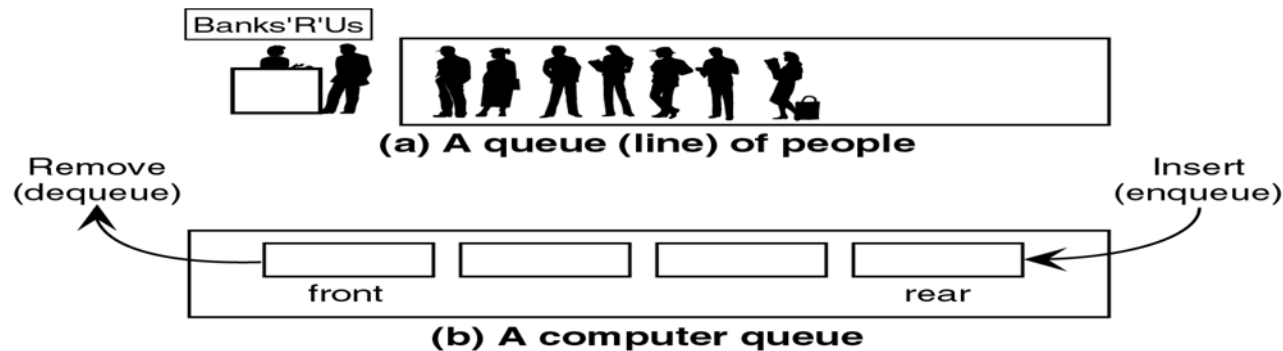


Figure 1: The queue concept

3.1 Introduction

- Two simple queue applications:
 - ✓ **Queue Simulation** – modeling activity used to generate statistics about the performance of queues.
 - ✓ **Categorizing Data** – rearrange data without destroying their basic sequence (multiple queues).

3.1 Introduction

■ Basic operations:

1) Enqueue— insert a given element at the back of the queue.

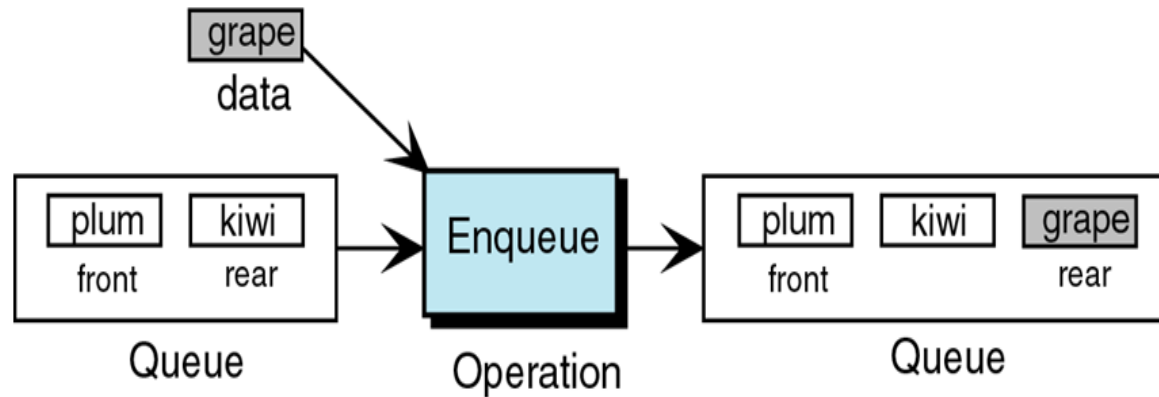


Figure 2: Add

3.1 Introduction

- 2) Dequeue – if the queue is not empty, delete and return the element that is at the front of the queue.

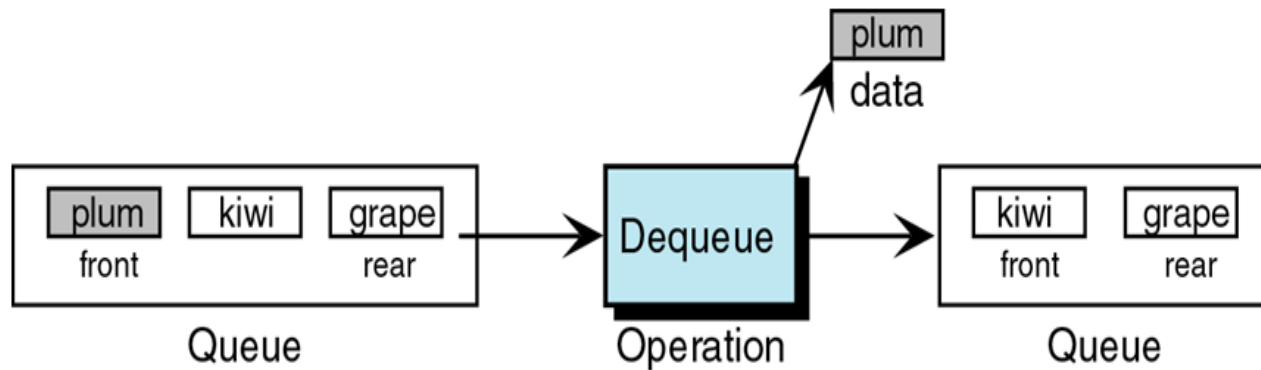


Figure 3: Remove

3.1 Introduction

- 3) Queue_front – if the queue is not empty, return the element that is at the front of the queue.

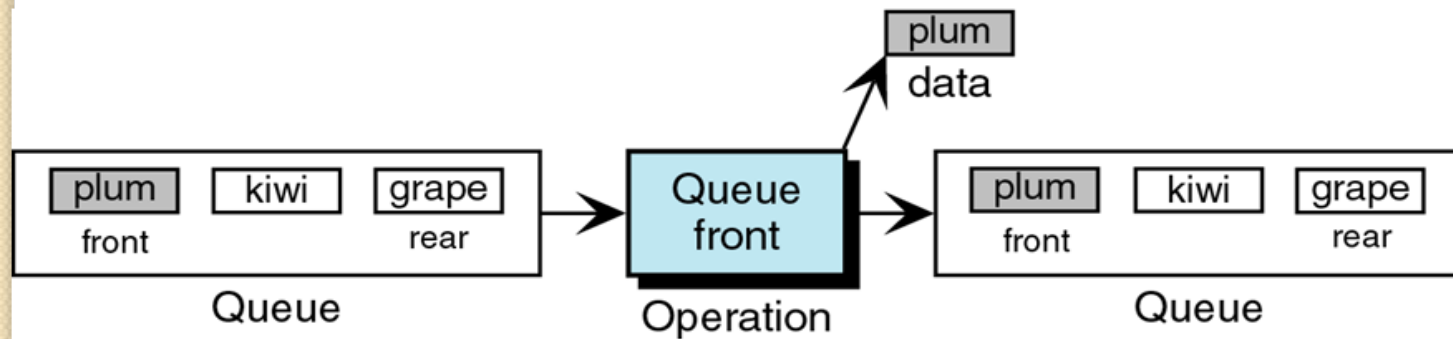


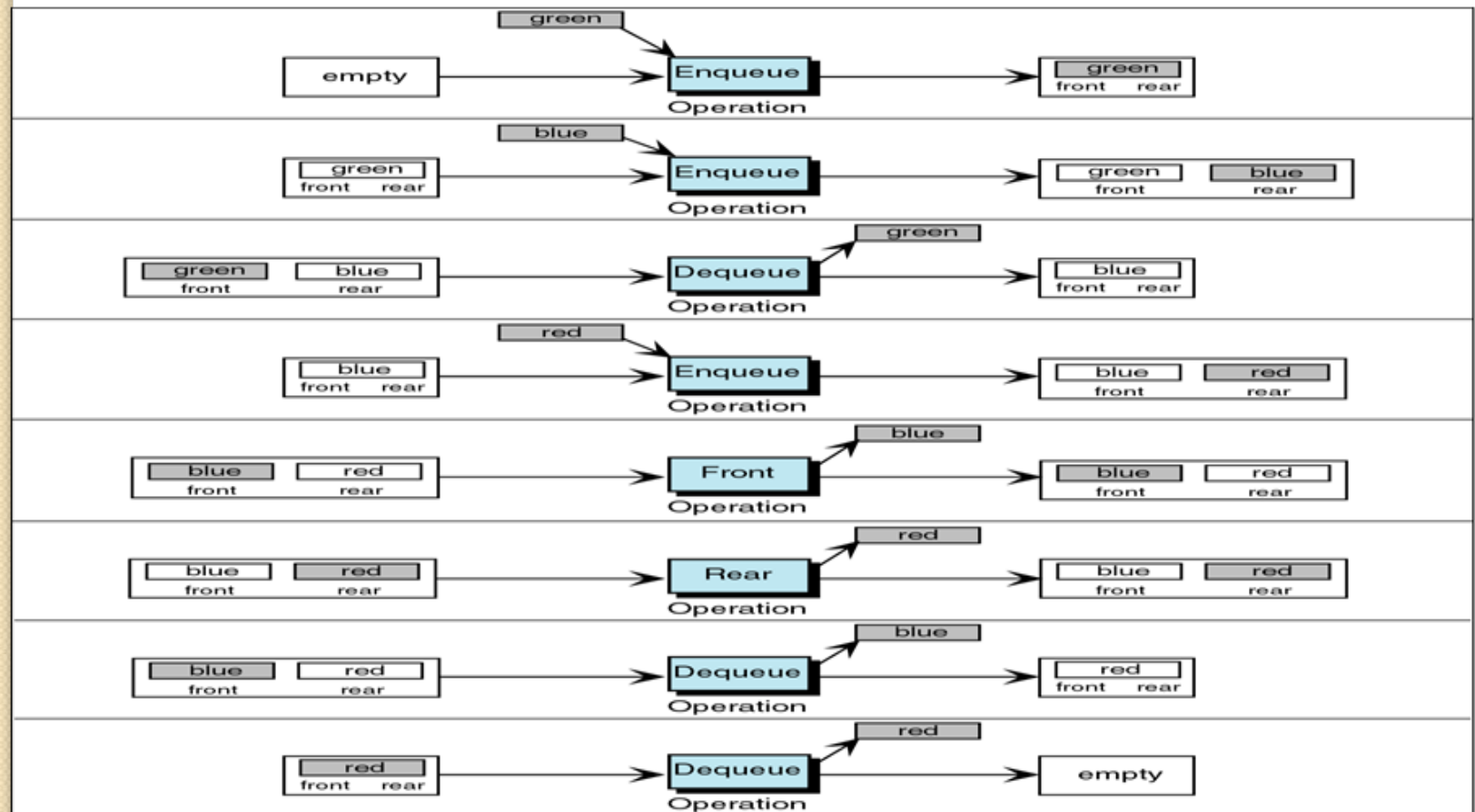
Figure 4: First

- 4) Size – return the number of elements in the queue.

Example:

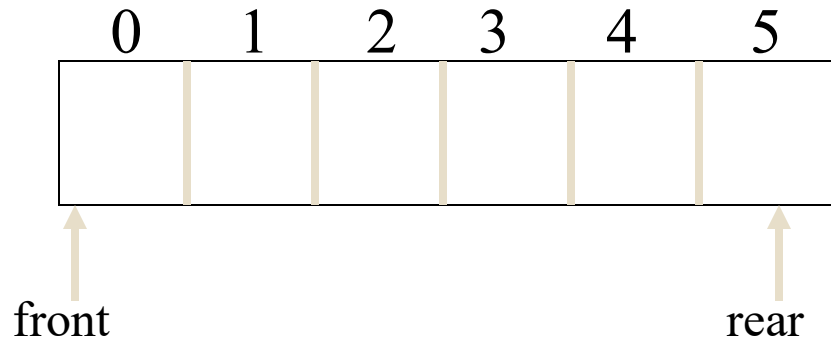
Given queue Q with list of operations as below. Illustrate the queue operations step by step:

Q.enqueue(green), Q.enqueue(blue), x=Q.dequeue(), Q.enqueue(red),
frontItem = Q.Front(), lastItem = Q.Rear(), x=Q.dequeue(), y=Q.dequeue().



QUEUE USING ARRAY-BASED IMPLEMENTATION

- Array Implementation
 - Different compared to Stack because of two variables: front and rear.
 - Let Q store characters, defined as arrays of 6 elements numbered 0 to 5 as follows with front and rear index.

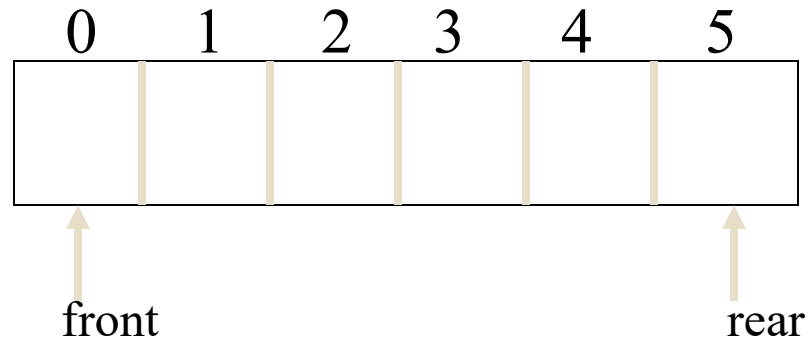


QUEUE USING ARRAY-BASED IMPLEMENTATION

1. Start operation: construct a queue

```
Queue a;
```

```
front = 0, rear = 5;
```

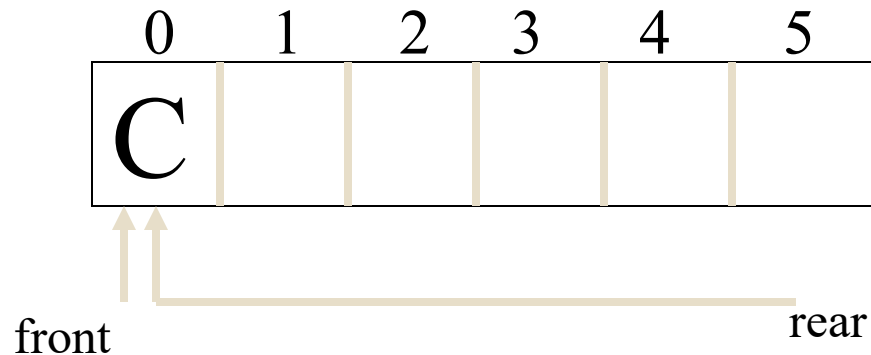


QUEUE USING ARRAY-BASED IMPLEMENTATION

2. Input character 'C', 'S', 'C', '3', '2', '0', '2':

```
a.enqueue('C');
```

```
rear = (rear + 1) % a.length;  
a[rear] = newInput;
```

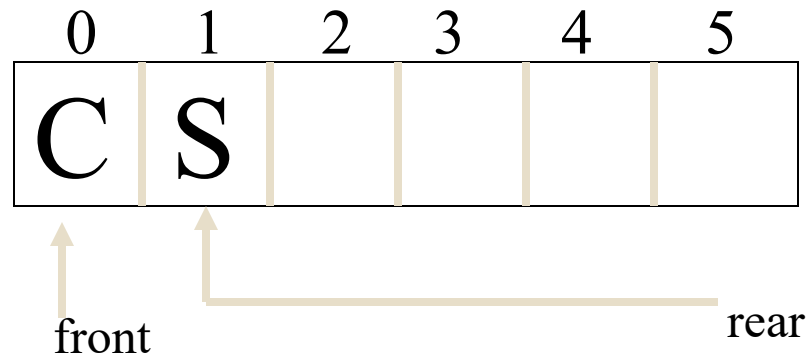


QUEUE USING ARRAY-BASED IMPLEMENTATION

3. Next input:

```
a.enqueue ( 'S' ) ;
```

```
rear = (rear + 1) % a.length;  
a[rear] = newInput;
```



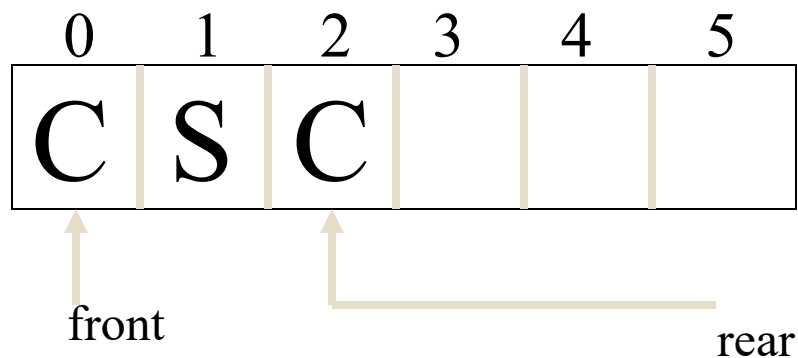
QUEUE USING ARRAY-BASED IMPLEMENTATION

4. Next input:

```
a.enqueue('C');
```

```
rear = (rear + 1) % a.length;
```

```
a[rear] = newInput;
```



QUEUE USING ARRAY-BASED IMPLEMENTATION

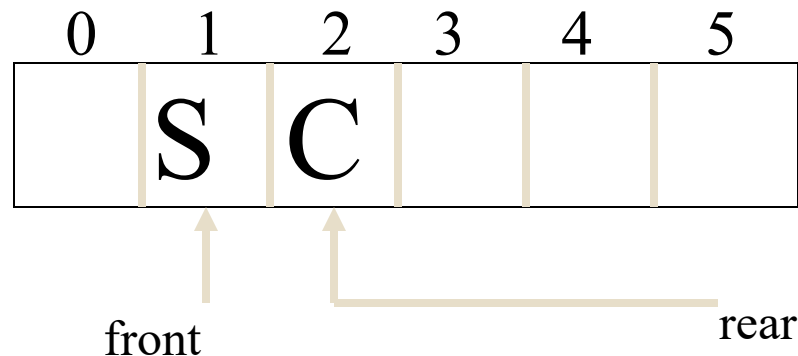
5. Remove operation: remove the front item

```
a.dequeue()
```

```
ch = a[front];
```

```
a[front] = null;
```

```
front = (front + 1) % a.length;
```

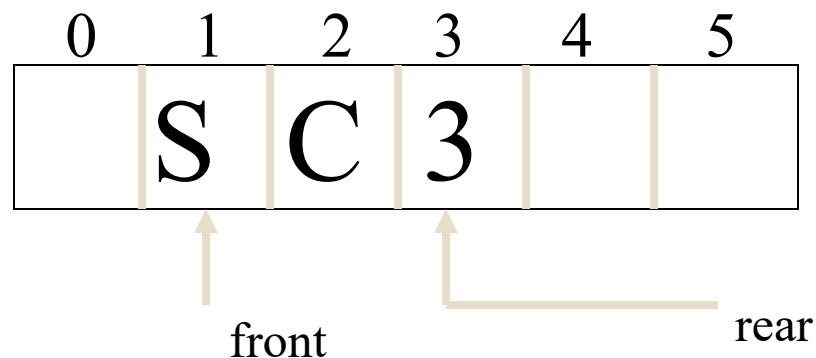


QUEUE USING ARRAY-BASED IMPLEMENTATION

6. Next input:

```
a.enqueue('3');
```

```
rear = (rear + 1) % a.length;  
a[rear] = newInput;
```

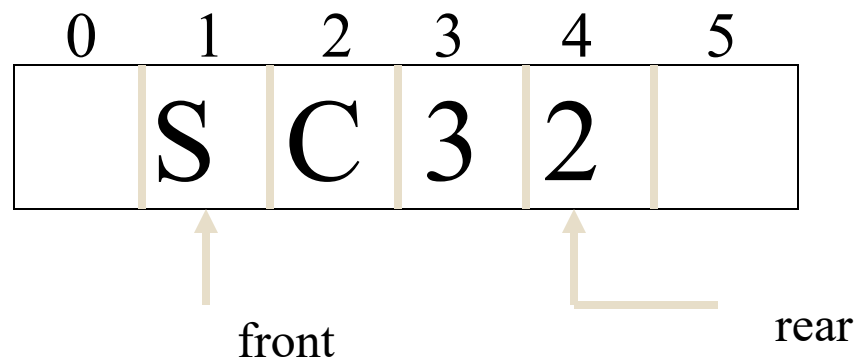


QUEUE USING ARRAY-BASED IMPLEMENTATION

7. Next input:

```
a.enqueue('2');
```

```
rear = (rear + 1) % a.length;  
a[rear] = newInput;
```

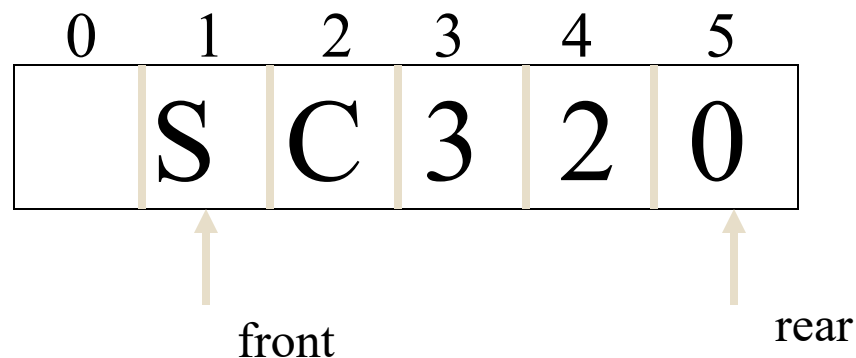


QUEUE USING ARRAY-BASED IMPLEMENTATION

8. Next input:

```
a.enqueue( '0' );
```

```
rear = (rear + 1) % a.length;  
a[rear] = newInput;
```

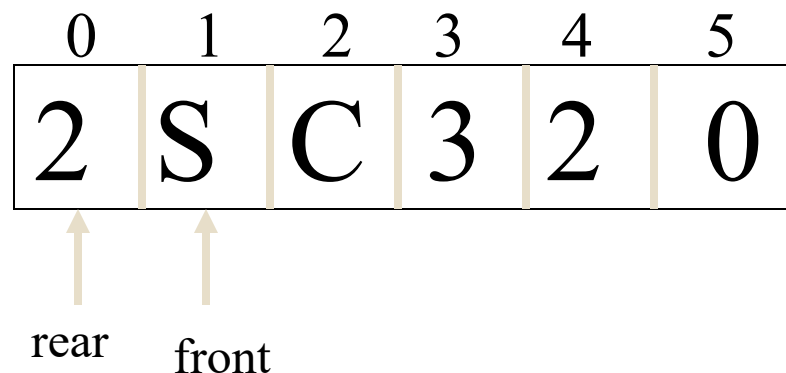


QUEUE USING ARRAY-BASED IMPLEMENTATION

9. Next input:

```
a.enqueue('2');
```

```
rear = (rear + 1) % a.length;  
a[rear] = newInput;
```

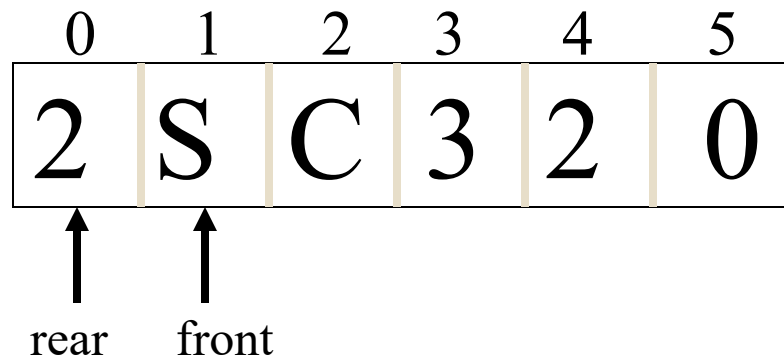


QUEUE USING ARRAY-BASED IMPLEMENTATION

10. The queue is already full. Before you can insert anymore character, check the queue first:

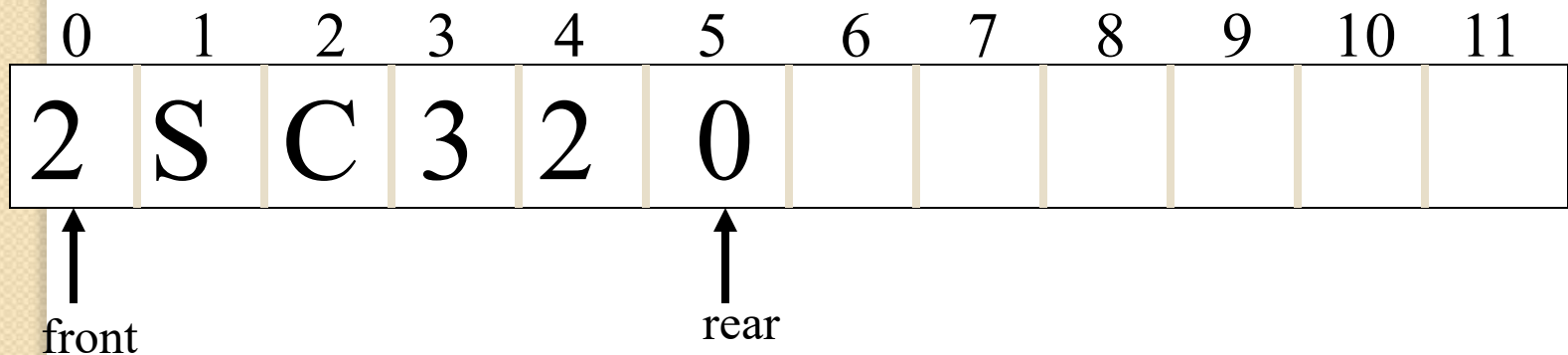
```
public boolean isFull() {  
    return (size == a.length);  
}
```

Cannot just only test whether $\text{front} == ((\text{rear} + 1) \% \text{a.length})$ since it is true both when queue is full and when queue is empty.



11. You can increase the size:

```
if (isFull()) {  
    Object[] oldQ = a;  
  
    // Create new array of double size  
    a = new Object[2 * oldQ.length];  
  
    // Copy old array contents into new array  
    for (int i = 0; i < oldQ.length; i++) {  
        a[i] = oldQ[front];  
        front = (front + 1) % oldQ.length;  
    }  
    front = 0;  
    rear = oldQ.length - 1;  
}
```



QUEUE USING ARRAY-BASED IMPLEMENTATION

Queue Program: A Queue Interface

```
1  /* The <code>Queue</code> interface specifies the
2   * basic operations
3   * of a first-in-first-out (FIFO) containers. */
4
5  public interface Queue {
6
7   /* Adds the specified element to the back of this
8    * queue. */
9
10 public void enqueue(Object object);
11
```

```
12 /*Returns the element at the front of this queue.
13  *
14 * @throws IllegalStateException if this queue is
15 * empty */
16
17 public Object getFront();
18
19 /* Removes and returns the element at the front
20  * of
21  * this queue.
22  * @throws IllegalStateException if this queue is
23  * empty */
24
25 public Object dequeue();
26
27 /* Returns the number of elements in this queue.
28  */
29 public int size();
30 }
```

QUEUE USING ARRAY-BASED IMPLEMENTATION

- Queue Program: A Queue Interface

```
1  /* The <code>Queue</code> interface specifies the
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3   * of a first-in-first-out (FIFO) containers. */
4
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9
10 public void enqueue(Object object);
11
```

```
12  /*Returns the element at the front of this queue.
13   *
14   * @throws IllegalStateException if this queue is
15   * empty */
16
17  public Object getFront();
18
19  /* Removes and returns the element at the front of
20   * this queue.
21   *
22   * @throws IllegalStateException if this queue is
23   * empty */
24
25  public Object dequeue();
26
27  /* Returns the number of elements in this queue. */
28
29  public int size();
30  }
```


QUEUE USING ARRAY-BASED IMPLEMENTATION

The ArrayQueue class

```
public class ArrayQueue implements Queue {  
    private Object[] objQ;  
    private int front;  
    private int rear;  
    private int size;  
  
    public ArrayQueue(int capacity) {  
        objQ = new Object[capacity];  
        front = 0;  
        rear = capacity - 1;  
        size = 0;  
    }  
}
```

```
public void enqueue(Object object) {  
    ensureCapacity();  
    rear = (rear + 1) % objQ.length;  
    objQ[rear] = object;  
    size++;  
}
```


```
public Object dequeue() {  
    Object frontObj;  
  
    if (isEmpty()) throw new  
        IllegalStateException("queue is  
        empty");  
  
    frontObj = objQ[front];  
    front = (front + 1) % objQ.length;  
    size--;  
  
    return frontObj;  
}
```

```
public boolean isFull() {
    return size == objQ.length;
}

private void ensureCapacity() {
    if (isFull()) {
        Object[] oldQ = objQ;

        objQ = new Object[2 * oldQ.length];

        for (int i = 0; i < oldQ.length; i++) {
            objQ[i] = oldQ[front];
            front = (front + 1) % oldQ.length;
        }
        front = 0;
        rear = oldQ.length - 1;
    }
}
```



```
public boolean isEmpty() {  
    return size == 0;  
}
```

```
public Object getFront() {  
    Object frontObj;  
  
    if (isEmpty()) throw new  
        IllegalStateException("queue is empty");  
  
    frontObj = objQ[front];  
  
    return frontObj;  
}
```

```
public int size() {  
    return size;  
}
```

The implementation class:

```
public class TestArrayQueue {  
    public static void main (String[] args) {  
        ArrayQueue queue = new ArrayQueue(4);  
  
        queue.enqueue("CARROTS");  
        queue.enqueue("ORANGES");  
        queue.enqueue("RAISINS");  
        queue.enqueue("PICKLES");  
        System.out.println("queue.size(): " + queue.size() +  
            "\tqueue.getFront(): " + queue.getFront());  
        System.out.println("queue.dequeue(): " +  
            queue.dequeue());  
        System.out.println("queue.dequeue(): " +  
            queue.dequeue());  
        System.out.println("queue.dequeue(): " +  
            queue.dequeue());  
    }  
}
```

```
System.out.println("queue.size(): " + queue.size() +  
    "\tqueue.getFront(): " + queue.getFront());  
queue.enqueue("WALNUTS");  
queue.enqueue("OYSTERS");  
queue.enqueue("BANANAS");  
System.out.println("queue.size(): " + queue.size() +  
    "\tqueue.getFront(): " + queue.getFront());  
System.out.println("queue.dequeue(): " +  
    queue.dequeue());  
System.out.println("queue.dequeue(): " +  
    queue.dequeue());  
System.out.println("queue.dequeue(): " +  
    queue.dequeue());  
System.out.println("queue.dequeue(): " +  
    queue.dequeue());  
System.out.println("queue.dequeue(): " +  
    queue.dequeue());
```

```
}
```

```
}
```

queue.size(): 4 queue.getFront(): CARROTS

queue.dequeue(): CARROTS

queue.dequeue(): ORANGES

queue.dequeue(): RAISINS

queue.size(): 1 queue.getFront(): PICKLES

queue.size(): 4 queue.getFront(): PICKLES

queue.dequeue(): PICKLES

queue.dequeue(): WALNUTS

queue.dequeue(): OYSTERS

queue.dequeue(): BANANAS

Exception in thread "main"

java.lang.IllegalStateException: queue is empty

at ArrayQueue.dequeue(ArrayQueue.java:##)

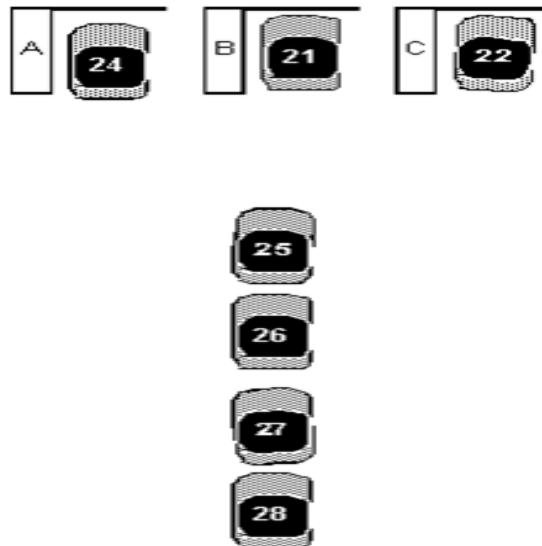
at TestArrayQueue.main(TestArrayQueue.java:##)

3.3 QUEUE APPLICATION: Queue Simulations

- Anything involving FIFO
 - Lines of people at checkout counters
 - Vehicles at traffic lights
 - Planes waiting to land and take off at airports
 - Assembly lines at a factory
 - Email processing
 - Some emails can have higher priority than others – use a **priority queue**?
- Usually need to model arrivals into queue using probability distributions.

3.3 QUEUE SIMULATION (John R. Hubbard)

- Consider the real-world example of cars arriving at a station of toll booths. The clients are the cars and the servers are the toll booths (or their operators).
- The client/server system is pictured as below with three toll booths, labeled A, B and C. The cars are numbered. Cars 24, 21 and 22 are being served, while cars 25-28 are waiting in the queue.



3.3 QUEUE APPLICATION: QUEUE SIMULATION

- The objects are:
 - ✓ Clients (cars)
 - ✓ Servers (toll booths)
 - ✓ A queue
- The events are:
 - ✓ A client arrives at the queue
 - ✓ A server begins serving a client
 - ✓ A server finishes serving a client

3.3 QUEUE APPLICATION: QUEUE SIMULATION

■ Algorithm – Client/Server Simulation

1. Repeat steps 2 and 6 for times $t = 0, 1, \dots$
2. If t = time for next arrival, do steps 3-5.
3. Create a new **client**.
4. Add the **client** to the queue.
5. Set **time** for next arrival.
6. Repeat steps 7 and 8 for each server.
7. If t = **time** for the **server** to finish serving, have it stop.
8. If **server** is idle and the queue is not empty, do steps 9-10.
9. Remove **client** from the queue.
10. Tell **server** to start serving **client**.

3.3 QUEUE APPLICATION: QUEUE SIMULATION

■ Client/Server Simulation

```
1 for (int t=0;;t++) { //step 1
2   if (t==nextArrivalTime) { //step 2
3     Client client = clients[i++] = new SimClient(i,t); //step 3
4     queue.add(client); //step 4
5     nextArrivalTime = t + randomArrival.nextInt(); //step 5
6   }
7   for (int j=0;j<numServers;j++) { //step 6
8     Server server = servers[j];
9     if (t==server.getStopTime()) server.stopServing(t); //step 7
10    if (server.isIdle() && !queue.isEmpty()) { //step 8
11      Client client = (SimClient)queue.remove(); //step 9
12      server.startServing(client,t); //step 10
13    }
14  }
15 }
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

■ Server Interface

```
1 public interface Server {  
2     public int getMeanServiceTime();  
3     public int getStopTime();  
4     public boolean isIdle();  
5     public void startServing(Client client, int t);  
6     public void stopServing(int t);  
7 }
```

■ Client Interface

```
1 public interface Client {  
2     public void setStartTime(int t);  
3     public void setStopTime(int t);  
4 }
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

- Server and Client objects

id	<input type="text" value="0"/>
meanServiceTime	<input type="text" value="34"/>
stopTime	<input type="text" value="60"/>
client	<input type="checkbox"/>
random	<input type="checkbox"/>

simServer

Figure 6.8 A **SimServer** object

id	<input type="text" value="5"/>
arrivalTime	<input type="text" value="25"/>
startTime	<input type="text" value="39"/>
stopTime	<input type="text" value="60"/>

simClient

Figure 6.9 A **SimClient** object

3.3 QUEUE APPLICATION: QUEUE SIMULATION

- A Server class

```
public class SimServer implements Server {
    private Client client;
    private int id, meanServiceTime, stopTime=-1;
    private java.util.Random random;

    public SimServer(int id, int meanServiceTime) {
        this.id = id;
        this.meanServiceTime = meanServiceTime;
        this.random = new ExponentialRandom(meanServiceTime);
    }

    public int getMeanServiceTime() {
        return meanServiceTime;
    }

    public int getStopTime() {
        return stopTime;
    }
}
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

```
public boolean isIdle() {
    return client==null; }

public void startServing(Client client, int t) {
    this.client = client;
    this.client.setStartTime(t);
    this.stopTime = t + random.nextInt();
    System.out.println(this + " started serving " + client
        + " at time " + t + " and will finish at time " + stopTime); }

public void stopServing(int t) {
    client.setStopTime(t);
    System.out.println(this+ " stopped serving " + client
        + " at time " + t);
    client = null;
}

public String toString() {
    String s="ABCDEFGHIJKLMNOPQRSTUVWXYZ";
    return "Server " + s.charAt(id); }
}
```


3.3 QUEUE APPLICATION: QUEUE SIMULATION

- Exponential Distribution

```
public class ExponentialRandom extends java.util.Random {  
    private double mean;  
  
    public ExponentialRandom(double mean) {  
        super(System.currentTimeMillis());  
        this.mean = mean;  
    }  
  
    public double nextDouble() {  
        return -mean*Math.log(1.0-super.nextDouble());  
    }  
  
    public int nextInt() {  
        return (int)Math.ceil(nextDouble());  
    }  
}
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

■ A Client Class

```
public class SimClient implements Client {
    int id, arrivalTime=-1, startTime=-1, stopTime=-1;
    public SimClient(int id, int t) {
        this.id = id;
        arrivalTime = t;
        System.out.println(this + " arrived at time " + t);
    }

    public int getStartTime() {
        return startTime;
    }

    public int getStopTime() {
        return stopTime;
    }

    public void setStartTime(int t) {
        startTime = t;
    }

    public void setStopTime(int t) {
        stopTime = t;
    }

    public String toString() {
        return "Client " + id;
    }
}
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

- A Simulation class

```
public class Simulation {
    static int numServers;
    static int numClients;
    static int meanServiceTime;
    static int meanInterarrivalTime;
    static Server[] servers;
    static Client[] clients;
    static Queue queue = new LinkedQueue();
    static java.util.Random randomArrival;
    static java.util.Random randomService;

    public static void main(String[] args) {
        init(args);
        // See Listing 6.3 on page 173 (John R. Hurbbard)
    }
}
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

```
static void init(String[] args) {
    if (args.length < 4) {
        System.out.println("Usage: java Simulation <numServers> "
            + "<numClients> <meanServiceTime> <meanInterarrivalTime>");
        System.out.println(" e.g.: java Simulation 3 100 12 4");
        System.exit(0);
    }
    numServers = Integer.parseInt(args[0]);
    numClients = Integer.parseInt(args[1]);
    meanServiceTime = Integer.parseInt(args[2]);
    meanInterarrivalTime = Integer.parseInt(args[3]);
    servers = new Server[numServers];
    clients = new Client[numClients];
    randomService = new ExponentialRandom(meanServiceTime);
    randomArrival = new ExponentialRandom(meanInterarrivalTime);
    queue = new LinkedQueue();
}
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

```
for (int j=0; j<numServers; j++)
    servers[j] = new SimServer(j,randomService.nextInt());
System.out.println("    Number of servers = " + numServers);
System.out.println("    Number of clients = " + numClients);
System.out.println("    Mean service time = " + meanServiceTime);
System.out.println("Mean interarrival time = "
+ meanInterarrivalTime);
for (int j=0; j<numServers; j++)
    System.out.println("Mean service time for " + servers[j]
        + " = "+ servers[j].getMeanServiceTime());
}}
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

- Simulation objects

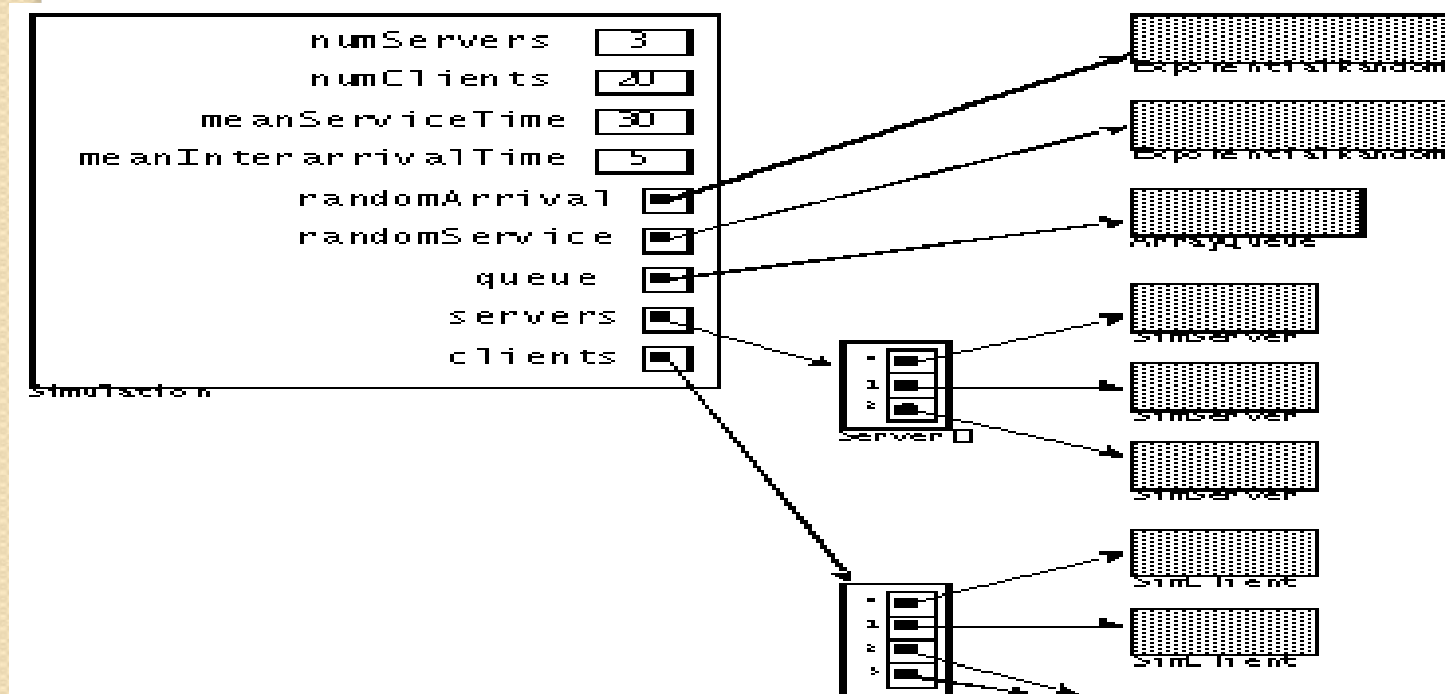
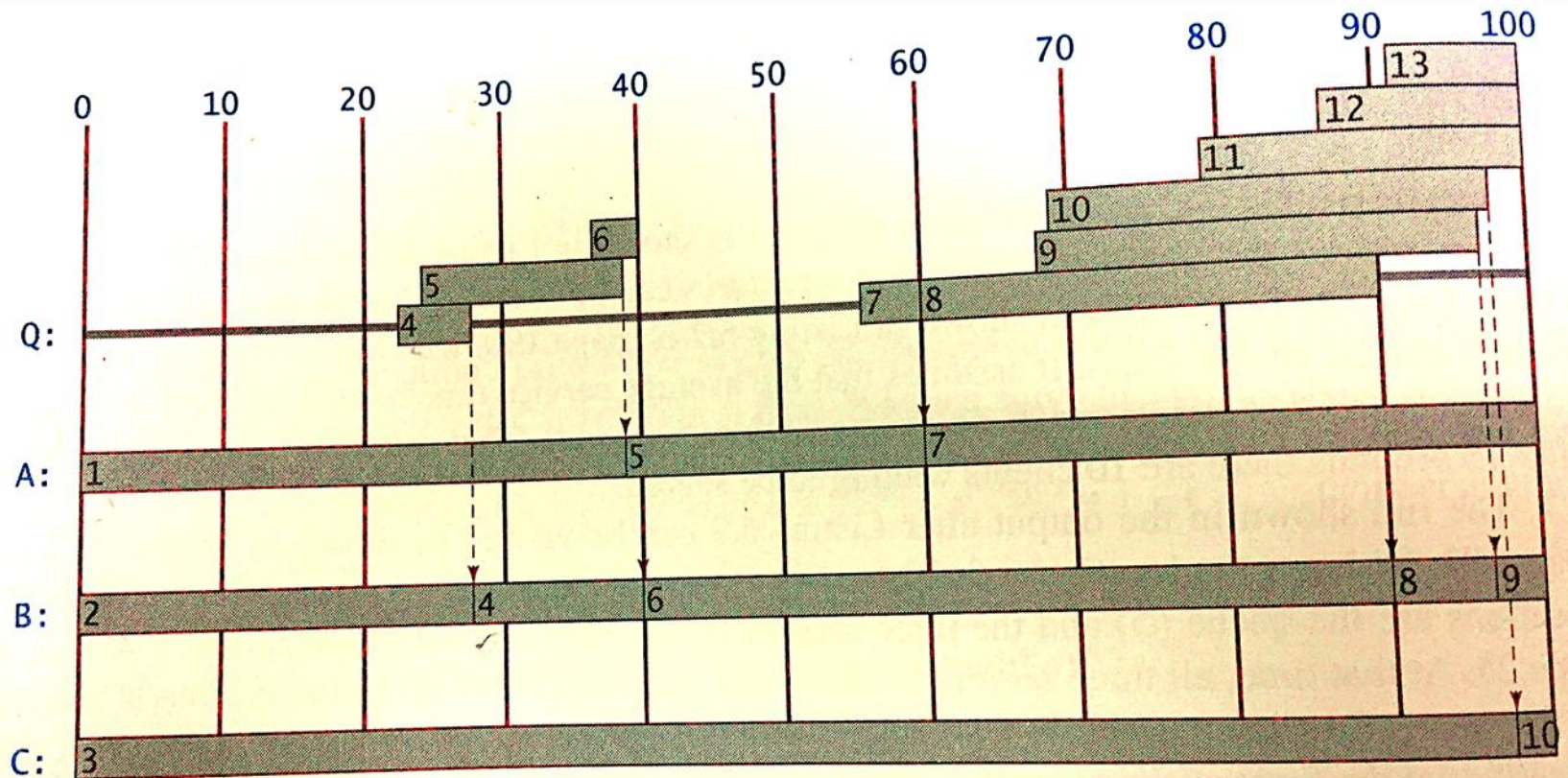


Figure 6.10 Simulation objects

3.3 QUEUE APPLICATION: QUEUE SIMULATION

- Arrivals and Departures



3.3 QUEUE APPLICATION: QUEUE SIMULATION

- Output

Number of servers = 3

Number of clients = 20

Mean service time = 30

Mean interarrival time = 5

Mean service time for Server A = 34

Mean service time for Server B = 19

Mean service time for Server C = 78

Client 1 arrived at time 0

The queue has 1 clients

The queue has 0 clients

3.3 QUEUE APPLICATION: QUEUE SIMULATION

Server A started serving Client 1 at time 0 and will finish at time 39

Client 2 arrived at time 6

The queue has 1 clients

The queue has 0 clients

Server B started serving Client 2 at time 6 and will finish at time 28

Client 3 arrived at time 10

The queue has 1 clients

The queue has 0 clients

Server C started serving Client 3 at time 10 and will finish at time 98

...

...

...