

Chapter 3

QUEUES

Objective

- To introduce:
 - Queues concept
 - Queues operations
 - Application using queues

CONTENT

- 3.1 Introduction
- 3.2 Queues using Array-Based Implementation
- 3.3 Queues Application: Queue Simulation

3.1 Introduction

- Queue is linear list in which data can only be inserted at one end, called the **rear**, and deleted from the other end, called the **front**.
- First-In-First-Out (FIFO) concept.

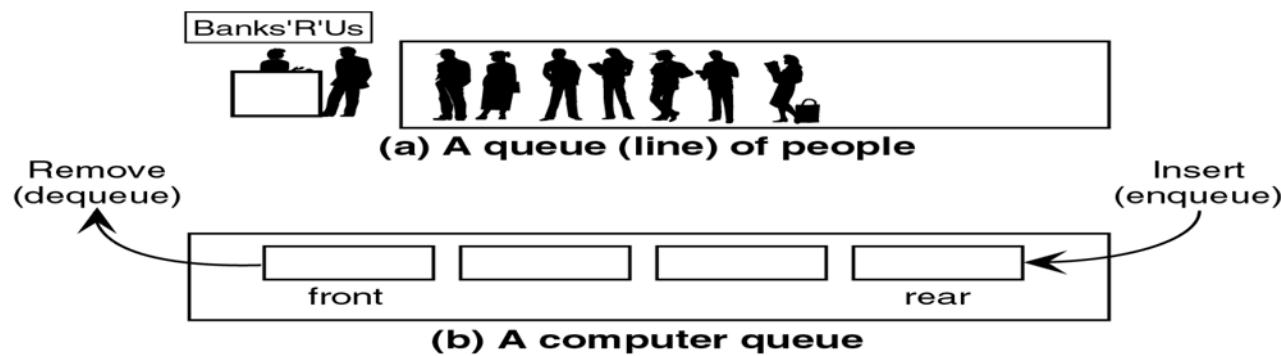


Figure 1: The queue concept

3.1 Introduction

- Two simple queue applications:
 - ✓ **Queue Simulation** – modeling activity used to generate statistics about the performance of queues.
 - ✓ **Categorizing Data** – rearrange data without destroying their basic sequence (multiple queues).

3.1 Introduction

■ Basic operations:

- I) Enqueue— insert a given element at the back of the queue.

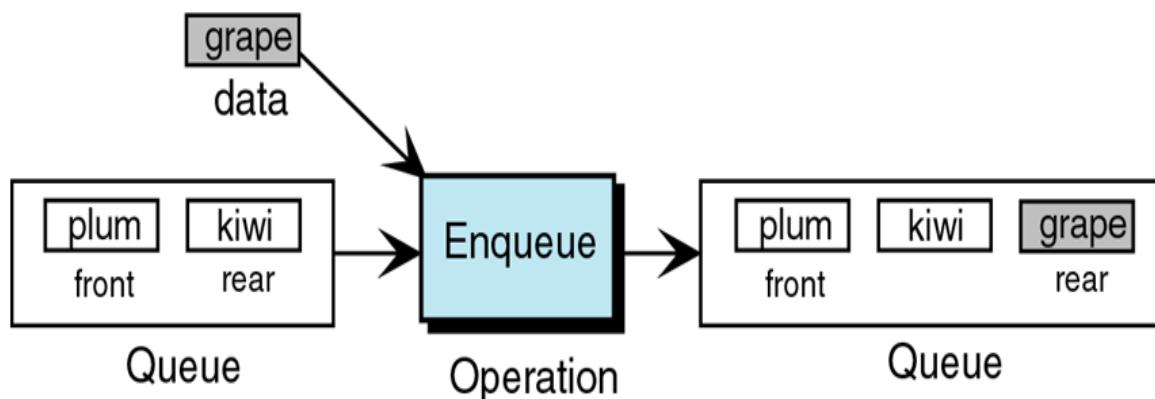


Figure 2: Add

3.1 Introduction

- 2) Dequeue – if the queue is not empty, delete and return the element that is at the front of the queue.

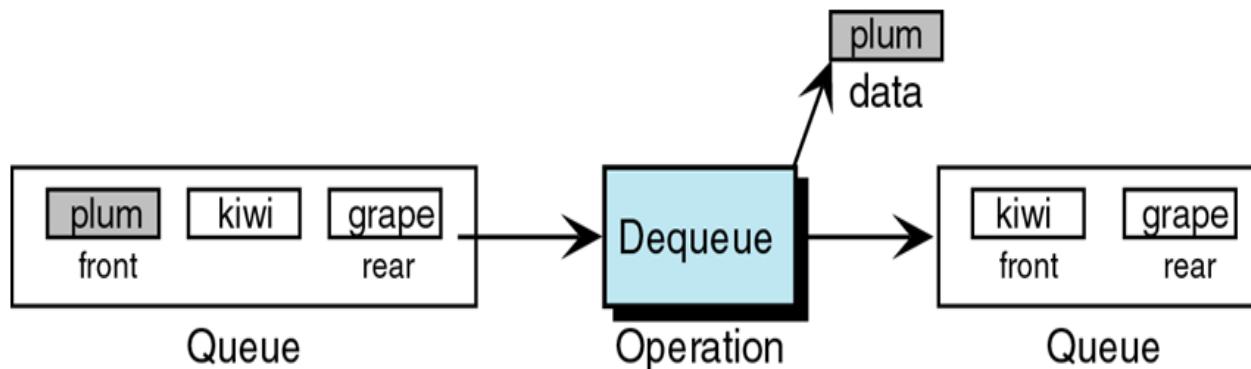


Figure 3: Remove

3.1 Introduction

- 3) Queue_front – if the queue is not empty, return the element that is at the front of the queue.

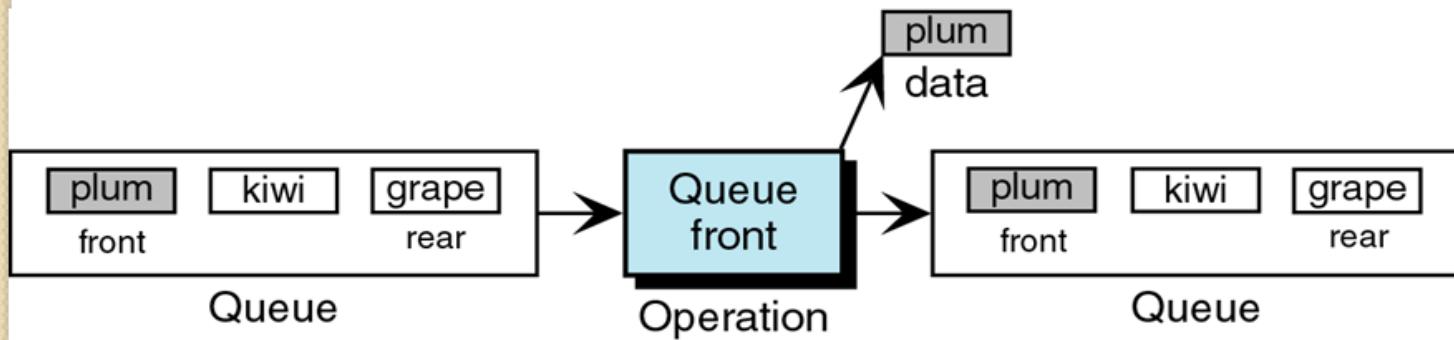


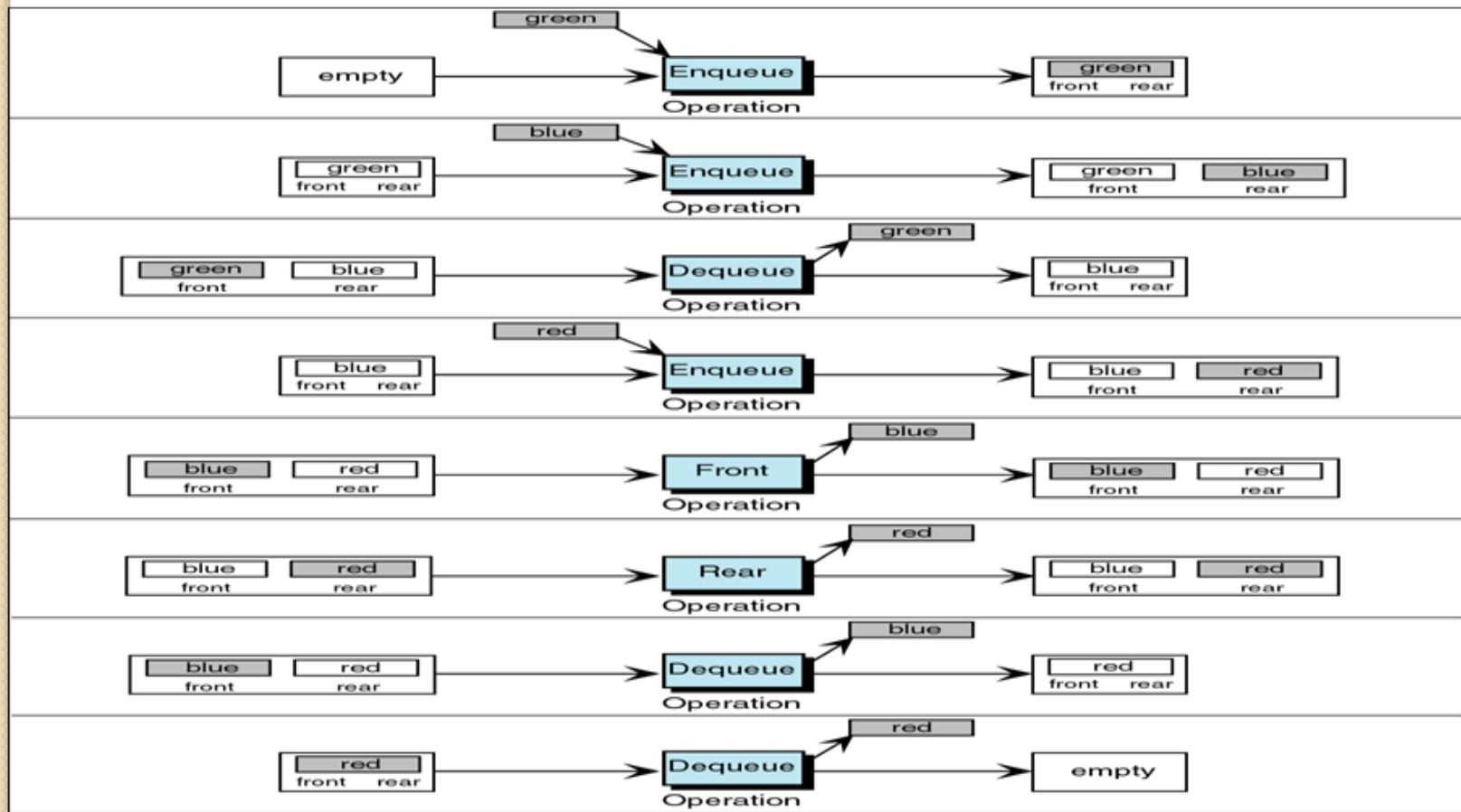
Figure 4: First

- 4) Size – return the number of elements in the queue.

- Example:

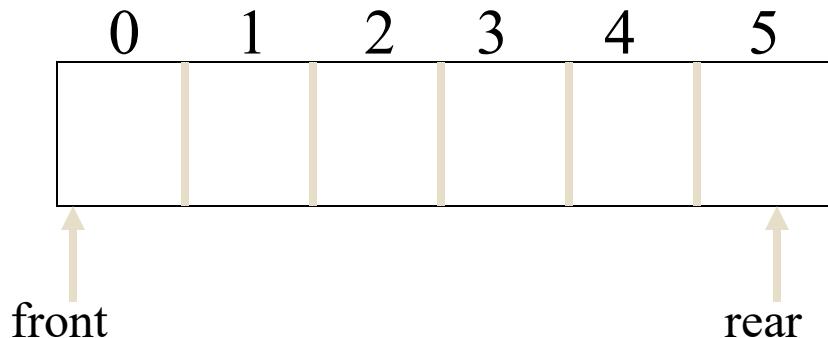
Given queue Q with list of operations as below. Illustrate the queue operations step by step:

Q.enqueue(green), Q. enqueue(blue), x=Q.dequeue(), Q.enqueue (red),
 frontItem = Q.Front(), lastItem = Q.Rear(), x=Q.dequeue(), y=Q.dequeue().



QUEUE USING ARRAY-BASED IMPLEMENTATION

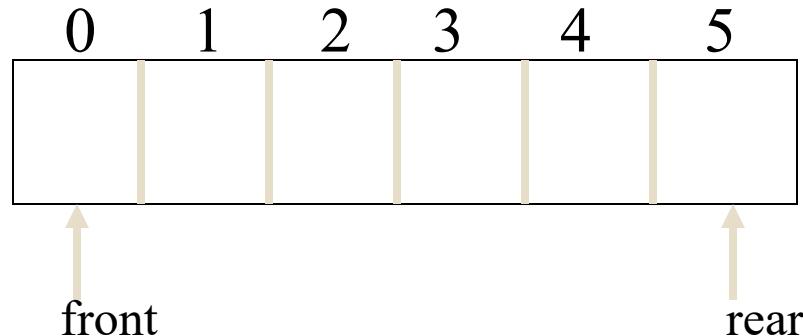
- Array Implementation
 - Different compared to Stack because of two variables: front and rear.
 - Let Q store characters, defined as arrays of 6 elements numbered 0 to 5 as follows with front and rear index.



QUEUE USING ARRAY-BASED IMPLEMENTATION

i. Start operation: construct a queue

```
Queue a;  
front = 0, rear = 5;
```

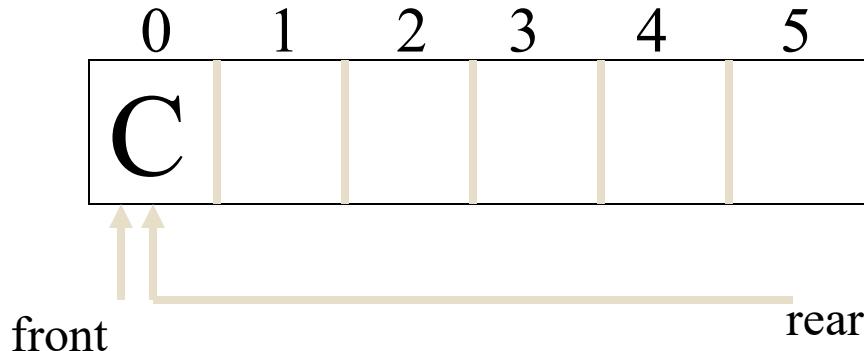


QUEUE USING ARRAY-BASED IMPLEMENTATION

2. Input character 'C', 'S', 'C', '3', '2', '0', '2':

```
a.enqueue('C');
```

```
rear = (rear + 1) % a.length;  
a[rear] = newInput;
```

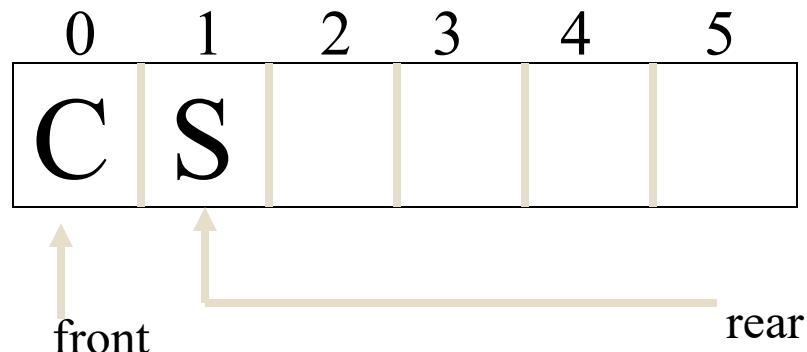


QUEUE USING ARRAY-BASED IMPLEMENTATION

3. Next input:

a.enqueue('S');

rear = (rear + 1) % a.length;
a[rear] = newInput;



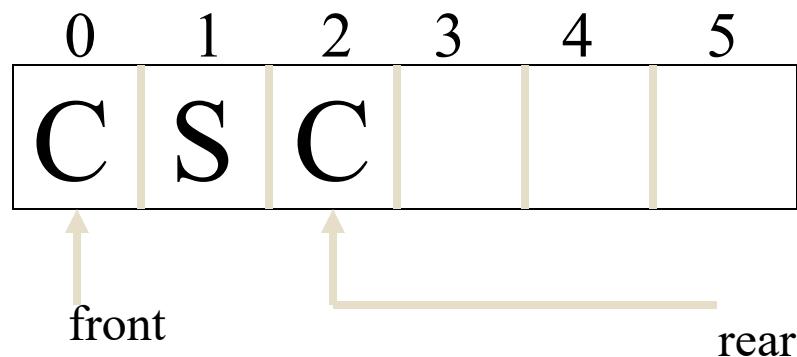
QUEUE USING ARRAY-BASED IMPLEMENTATION

4. Next input:

a.enqueue('C');

$\text{rear} = (\text{rear} + 1) \% \text{a.length};$

$\text{a}[\text{rear}] = \text{newInput};$

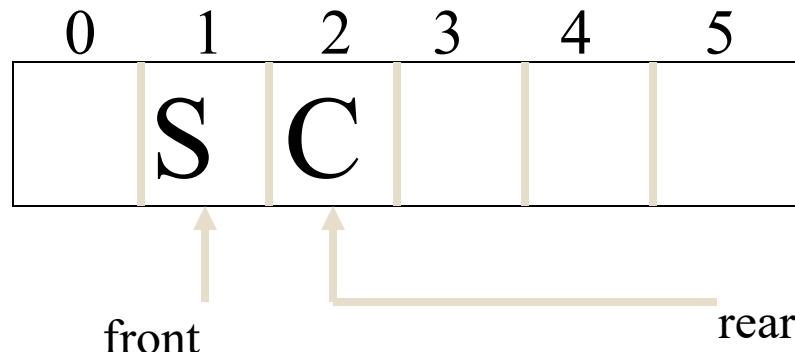


QUEUE USING ARRAY-BASED IMPLEMENTATION

5. Remove operation: remove the front item

a.dequeue ()

```
ch = a[front];  
a[front] = null;  
front = (front + 1) % a.length;
```

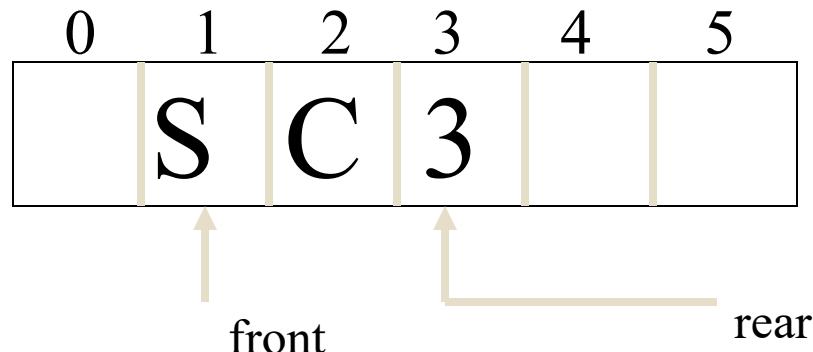


QUEUE USING ARRAY-BASED IMPLEMENTATION

6. Next input:

```
a.enqueue('3');
```

```
rear = (rear + 1) % a.length;  
a[rear] = newInput;
```

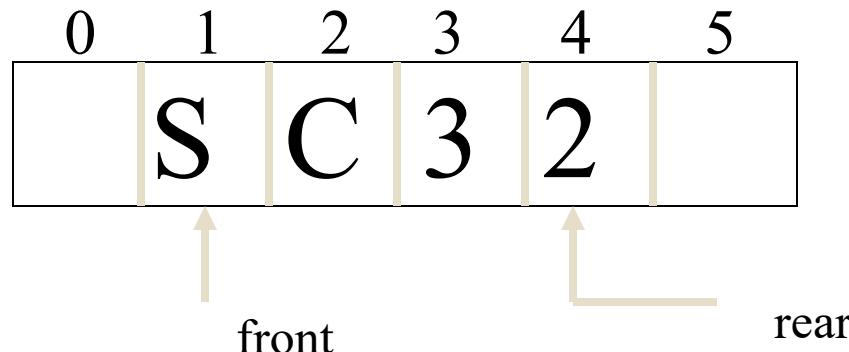


QUEUE USING ARRAY-BASED IMPLEMENTATION

7. Next input:

```
a.enqueue('2');
```

```
rear = (rear + 1) % a.length;  
a[rear] = newInput;
```

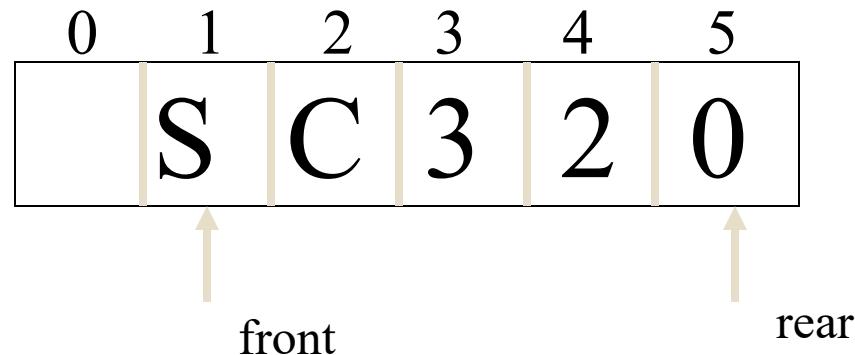


QUEUE USING ARRAY-BASED IMPLEMENTATION

8. Next input:

```
a.enqueue('0');
```

```
rear = (rear + 1) % a.length;  
a[rear] = newInput;
```

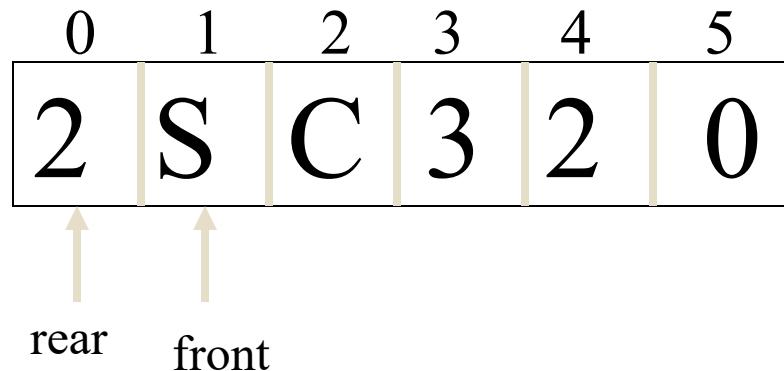


QUEUE USING ARRAY-BASED IMPLEMENTATION

9. Next input:

```
a.enqueue('2');
```

```
rear = (rear + 1) % a.length;  
a[rear] = newInput;
```

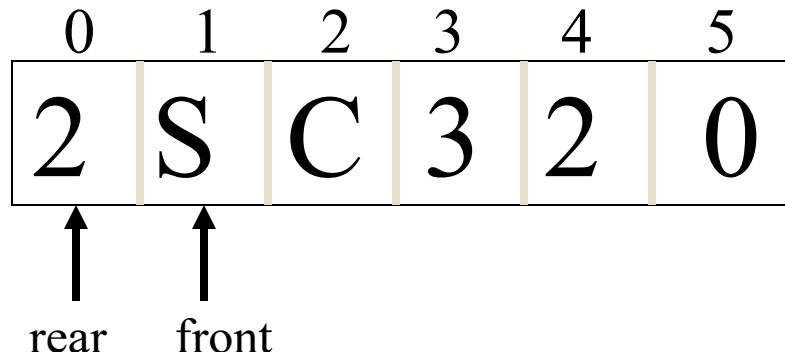


QUEUE USING ARRAY-BASED IMPLEMENTATION

10. The queue is already full. Before you can insert anymore character, check the queue first:

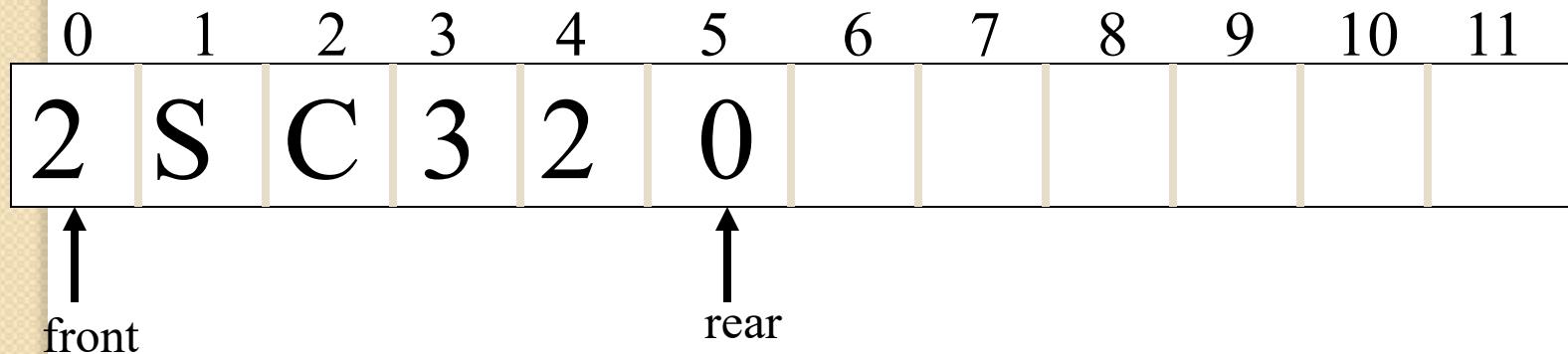
```
public boolean isFull() {  
    return (size == a.length);  
}
```

Cannot just only test whether `front == ((rear + 1) % a.length)` since it is true both when queue is full and when queue is empty.



11. You can increase the size:

```
if (isFull()) {  
    Object[] oldQ = a;  
  
    // Create new array of double size  
    a = new Object[2 * oldQ.length];  
  
    // Copy old array contents into new array  
    for (int i = 0; i < oldQ.length; i++) {  
        a[i] = oldQ[front];  
        front = (front + 1) % oldQ.length;  
    }  
    front = 0;  
    rear = oldQ.length - 1;  
}
```



QUEUE USING ARRAY-BASED IMPLEMENTATION

Queue Program: A Queue Interface

```
1 /* The <code>Queue</code> interface specifies the
2  * basic operations
3  * of a first-in-first-out (FIFO) containers. */
4
5 public interface Queue {
6
7 /* Adds the specified element to the back of this
8  * queue. */
9
10 public void enqueue(Object object);
11
```

```
12 /*Returns the element at the front of this queue.  
13 *  
14 * @throws IllegalStateException if this queue is  
15 * empty */  
16  
17 public Object getFront();  
18  
19 /* Removes and returns the element at the front  
20 * of  
21 * this queue.  
22 *  
23 * @throws IllegalStateException if this queue is  
24 * empty */  
25  
26 public Object dequeue();  
27 /* Returns the number of elements in this queue.  
28 * /  
29  
30 public int size();  
31 }
```

QUEUE USING ARRAY-BASED IMPLEMENTATION

- Queue Program: A Queue Interface

```
1 /* The <code>Queue</code> interface specifies the
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10 public void enqueue(Object object);
11
```

```
12 /*Returns the element at the front of this queue.  
13 *  
14 * @throws IllegalStateException if this queue is  
15 * empty */  
16  
17 public Object getFront();  
18  
19 /* Removes and returns the element at the front of  
20 * this queue.  
21 *  
22 * @throws IllegalStateException if this queue is  
23 * empty */  
24  
25 public Object dequeue();  
26  
27 /* Returns the number of elements in this queue. */  
28  
29 public int size();  
30 }
```

QUEUE USING ARRAY-BASED IMPLEMENTATION

The ArrayQueue class

```
public class ArrayQueue implements Queue {  
    private Object[] objQ;  
    private int front;  
    private int rear;  
    private int size;  
  
    public ArrayQueue(int capacity) {  
        objQ = new Object[capacity];  
        front = 0;  
        rear = capacity - 1;  
        size = 0;  
    }
```

```
public void enqueue(Object object) {  
    ensureCapacity();  
    rear = (rear + 1) % objQ.length;  
    objQ[rear] = object;  
    size++;  
}  
  
public Object dequeue() {  
    Object frontObj;  
  
    if (isEmpty()) throw new  
        IllegalStateException("queue is  
empty");  
  
    frontObj = objQ[front];  
    front = (front + 1) % objQ.length;  
    size--;  
  
    return frontObj;  
}
```

```
public boolean isFull() {  
    return size == objQ.length;  
}  
  
private void ensureCapacity() {  
    if (isFull()) {  
        Object[] oldQ = objQ;  
  
        objQ = new Object[2 * oldQ.length];  
  
        for (int i = 0; i < oldQ.length; i++) {  
            objQ[i] = oldQ[front];  
            front = (front + 1) % oldQ.length;  
        }  
        front = 0;  
        rear = oldQ.length - 1;  
    }  
}
```

```
public boolean isEmpty() {  
    return size == 0;  
}  
  
public Object getFront() {  
    Object frontObj;  
  
    if (isEmpty()) throw new  
        IllegalStateException("queue is empty");  
  
    frontObj = objQ[front];  
  
    return frontObj;  
}  
  
public int size() {  
    return size;  
}
```

The implementation class:

```
public class TestArrayQueue {  
    public static void main (String[] args) {  
        ArrayQueue queue = new ArrayQueue(4);  
  
        queue.enqueue("CARROTS");  
        queue.enqueue("ORANGES");  
        queue.enqueue("RAISINS");  
        queue.enqueue("PICKLES");  
        System.out.println("queue.size(): " + queue.size() +  
                           "\tqueue.getFront(): " + queue.getFront());  
        System.out.println("queue.dequeue(): " +  
                           queue.dequeue());  
        System.out.println("queue.dequeue(): " +  
                           queue.dequeue());  
        System.out.println("queue.dequeue(): " +  
                           queue.dequeue());
```



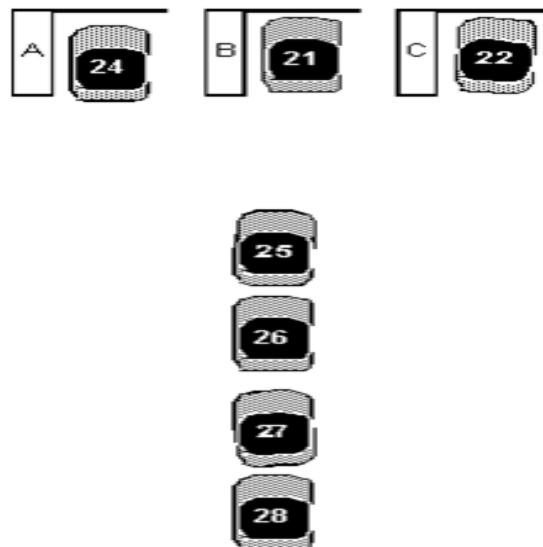
```
queue.size(): 4    queue.getFront(): CARROTS
queue.dequeue(): CARROTS
queue.dequeue(): ORANGES
queue.dequeue(): RAISINS
queue.size(): 1    queue.getFront(): PICKLES
queue.size(): 4    queue.getFront(): PICKLES
queue.dequeue(): PICKLES
queue.dequeue(): WALNUTS
queue.dequeue(): OYSTERS
queue.dequeue(): BANANAS
Exception in thread "main"
java.lang.IllegalStateException: queue is empty
    at ArrayQueue.dequeue(ArrayQueue.java:##)
    at TestArrayQueue.main(TestArrayQueue.java:##)
```

3.3 QUEUE APPLICATION: Queue Simulations

- Anything involving FIFO
 - Lines of people at checkout counters
 - Vehicles at traffic lights
 - Planes waiting to land and take off at airports
 - Assembly lines at a factory
 - Email processing
 - Some emails can have higher priority than others – use a **priority queue?**
- Usually need to model arrivals into queue using probability distributions.

3.3 QUEUE SIMULATION (John R. Hubbard)

- Consider the real-world example of cars arriving at a station of toll booths. The clients are the cars and the servers are the toll booths (or their operators).
- The client/server system is pictured as below with three toll booths, labeled A, B and C. The cars are numbered. Cars 24, 21 and 22 are being served, while cars 25-28 are waiting in the queue.



3.3 QUEUE APPLICATION: QUEUE SIMULATION

- The objects are:
 - ✓ Clients (cars)
 - ✓ Servers (toll booths)
 - ✓ A queue
- The events are:
 - ✓ A client arrives at the queue
 - ✓ A server begins serving a client
 - ✓ A server finishes serving a client

3.3 QUEUE APPLICATION: QUEUE SIMULATION

- Algorithm – Client/Server Simulation
 - 1. Repeat steps 2 and 6 for times $t = 0, 1, \dots$
 - 2. If $t =$ time for next arrival, do steps 3-5.
 - 3. Create a new **client**.
 - 4. Add the **client** to the queue.
 - 5. Set **time** for next arrival.
 - 6. Repeat steps 7 and 8 for each server.
 - 7. If $t =$ time for the **server** to finish serving, have it stop.
 - 8. If **server** is idle and the queue is not empty, do steps 9-10.
 - 9. Remove **client** from the queue.
 - 10. Tell **server** to start serving **client**.

3.3 QUEUE APPLICATION: QUEUE SIMULATION

- Client/Server Simulation

```
1 for (int t=0; ;t++) { //step 1
2   if (t==nextArrivalTime) { //step 2
3     Client client = clients[i++] = new SimClient(i,t); //step 3
4     queue.add(client); //step 4
5     nextArrivalTime = t + randomArrival.nextInt(); //step 5
6   }
7   for (int j=0;j<numServers; j++) { //step 6
8     Server server = servers[j];
9     if (t==server.getStopTime()) server.stopServing(t); //step 7
10    if (server.isIdle() && !queue.isEmpty()) { //step 8
11      Client client = (SimClient)queue.remove(); //step 9
12      server.startServing(client,t); //step 10
13    }
14  }
15 }
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

- Server Interface

```
1 public interface Server {  
2     public int getMeanServiceTime();  
3     public int getStopTime();  
4     public boolean isIdle();  
5     public void startServing(Client client, int t);  
6     public void stopServing(int t);  
7 }
```

- Client Interface

```
1 public interface Client {  
2     public void setStartTime(int t);  
3     public void setStopTime(int t);  
4 }
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

- Server and Client objects

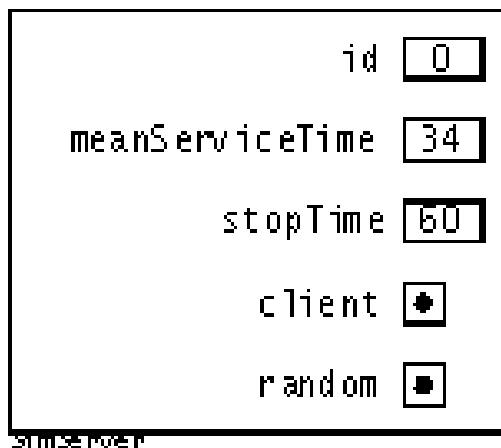


Figure 6.8 A `SimServer` object

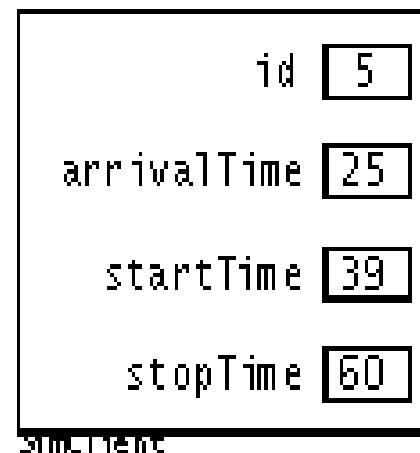


Figure 6.9 A `SimClient` object

3.3 QUEUE APPLICATION: QUEUE SIMULATION

- A Server class

```
public class SimServer implements Server {  
    private Client client;  
    private int id, meanServiceTime, stopTime=-1;  
    private java.util.Random random;  
  
    public SimServer(int id, int meanServiceTime) {  
        this.id = id;  
        this.meanServiceTime = meanServiceTime;  
        this.random = new ExponentialRandom(meanServiceTime);  
    }  
  
    public int getMeanServiceTime() {  
        return meanServiceTime;  
    }  
  
    public int getStopTime() {  
        return stopTime;  
    }
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

```
public boolean isIdle() {  
    return client==null;  }  
  
public void startServing(Client client, int t) {  
    this.client = client;  
    this.client.setStartTime(t);  
    this.stopTime = t + random.nextInt();  
    System.out.println(this + " started serving " + client  
        + " at time " + t + " and will finish at time " + stopTime);  }  
  
public void stopServing(int t) {  
    client.setStopTime(t);  
    System.out.println(this+ " stopped serving " + client  
        + " at time " + t);  
    client = null;  
}  
  
public String toString() {  
    String s="ABCDEFGHIJKLMNPQRSTUVWXYZ";  
    return "Server " + s.charAt(id);  }  
}
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

- Exponential Distribution

```
public class ExponentialRandom extends java.util.Random {  
    private double mean;  
  
    public ExponentialRandom(double mean) {  
        super(System.currentTimeMillis());  
        this.mean = mean;  
    }  
  
    public double nextDouble() {  
        return -mean*Math.log(1.0-super.nextDouble());  
    }  
  
    public int nextInt() {  
        return (int)Math.ceil(nextDouble());  
    }  
}
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

■ A Client Class

```
public class SimClient implements Client {  
    int id, arrivalTime=-1, startTime=-1, stopTime=-1;  
    public SimClient(int id, int t) {  
        this.id = id;  
        arrivalTime = t;  
        System.out.println(this + " arrived at time " + t);    }  
  
    public int getStartTime() {  
        return startTime;    }  
  
    public int getStopTime() {  
        return stopTime;    }  
  
    public void setStartTime(int t) {  
        startTime = t;    }  
  
    public void setStopTime(int t) {  
        stopTime = t;    }  
  
    public String toString() {  
        return "Client " + id;    }  
}
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

- A Simulation class

```
public class Simulation {  
    static int numServers;  
    static int numClients;  
    static int meanServiceTime;  
    static int meanInterarrivalTime;  
    static Server[] servers;  
    static Client[] clients;  
    static Queue queue = new LinkedQueue();  
    static java.util.Random randomArrival;  
    static java.util.Random randomService;  
  
    public static void main(String[] args) {  
        init(args);  
        // See Listing 6.3 on page 173 (John R. Hubbard)  
    }  
}
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

```
static void init(String[] args) {  
    if (args.length<4) {  
        System.out.println("Usage: java Simulation <numServers> "  
        + "<numClients> <meanServiceTime> <meanInterarrivalTime>");  
        System.out.println(" e.g.: java Simulation 3 100 12 4");  
        System.exit(0);  
    }  
    numServers = Integer.parseInt(args[0]);  
    numClients = Integer.parseInt(args[1]);  
    meanServiceTime = Integer.parseInt(args[2]);  
    meanInterarrivalTime = Integer.parseInt(args[3]);  
    servers = new Server[numServers];  
    clients = new Client[numClients];  
    randomService = new ExponentialRandom(meanServiceTime);  
    randomArrival = new ExponentialRandom(meanInterarrivalTime);  
    queue = new LinkedQueue();
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

```
for (int j=0; j<numServers; j++)  
    servers[j] = new SimServer(j,randomService.nextInt());  
  
System.out.println("      Number of servers = " + numServers);  
System.out.println("      Number of clients = " + numClients);  
System.out.println("      Mean service time = " + meanServiceTime);  
System.out.println("Mean interarrival time = "  
+ meanInterarrivalTime);  
  
for (int j=0; j<numServers; j++)  
    System.out.println("Mean service time for " + servers[j]  
    + " = "+ servers[j].getMeanServiceTime());  
}
```

3.3 QUEUE APPLICATION: QUEUE SIMULATION

- Simulation objects

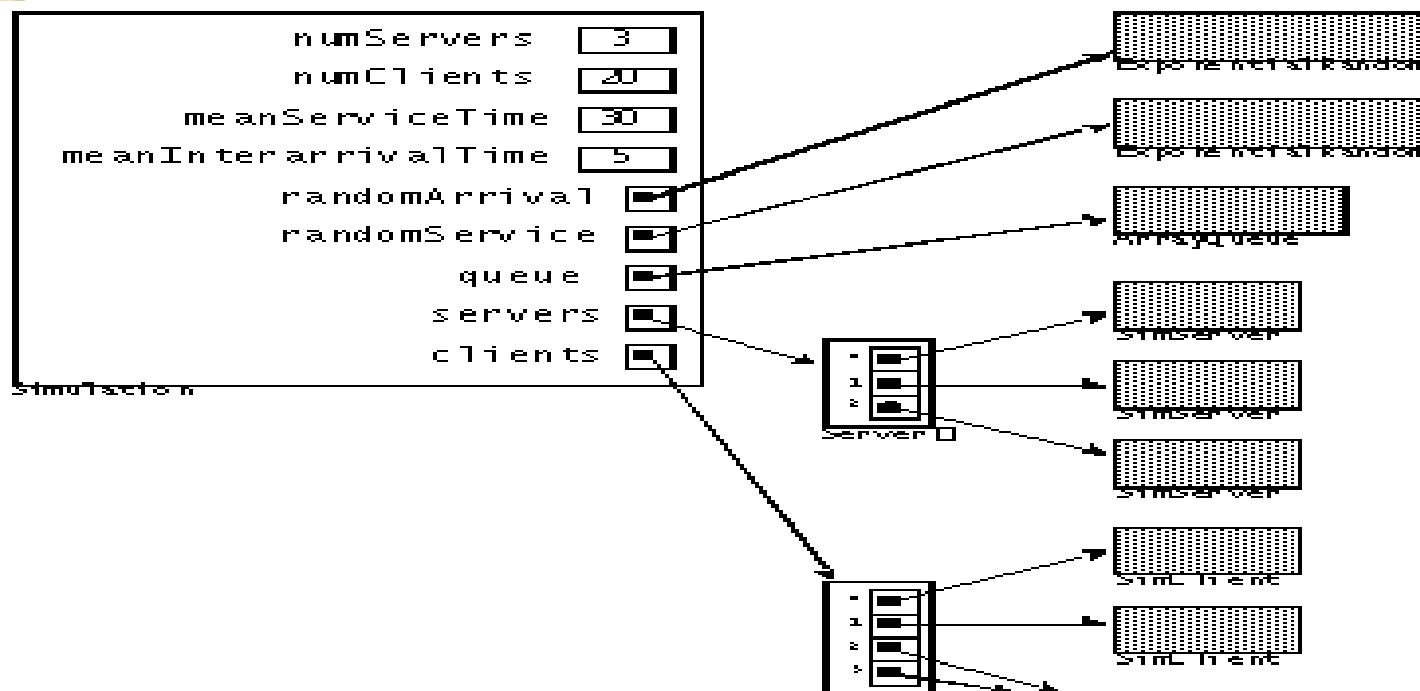
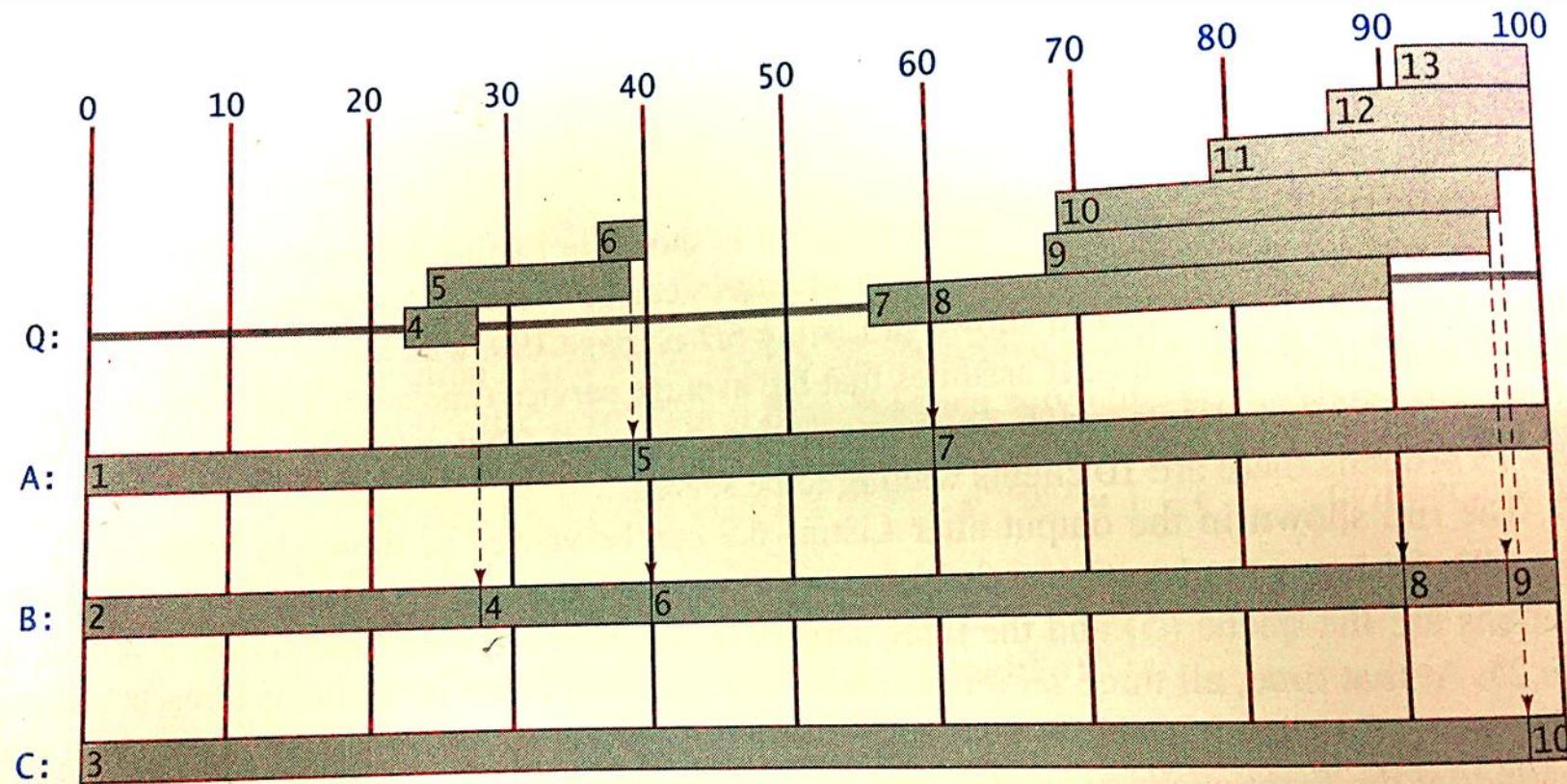


Figure 6.10 Simulation objects

3.3 QUEUE APPLICATION: QUEUE SIMULATION

- Arrivals and Departures



3.3 QUEUE APPLICATION: QUEUE SIMULATION

- Output

Number of servers = 3

Number of clients = 20

Mean service time = 30

Mean interarrival time = 5

Mean service time for Server A = 34

Mean service time for Server B = 19

Mean service time for Server C = 78

Client I arrived at time 0

The queue has 1 clients

The queue has 0 clients

3.3 QUEUE APPLICATION: QUEUE SIMULATION

Server A started serving Client 1 at time 0 and will finish at time 39

Client 2 arrived at time 6

The queue has 1 clients

The queue has 0 clients

Server B started serving Client 2 at time 6 and will finish at time 28

Client 3 arrived at time 10

The queue has 1 clients

The queue has 0 clients

Server C started serving Client 3 at time 10 and will finish at time 98

...

...

...