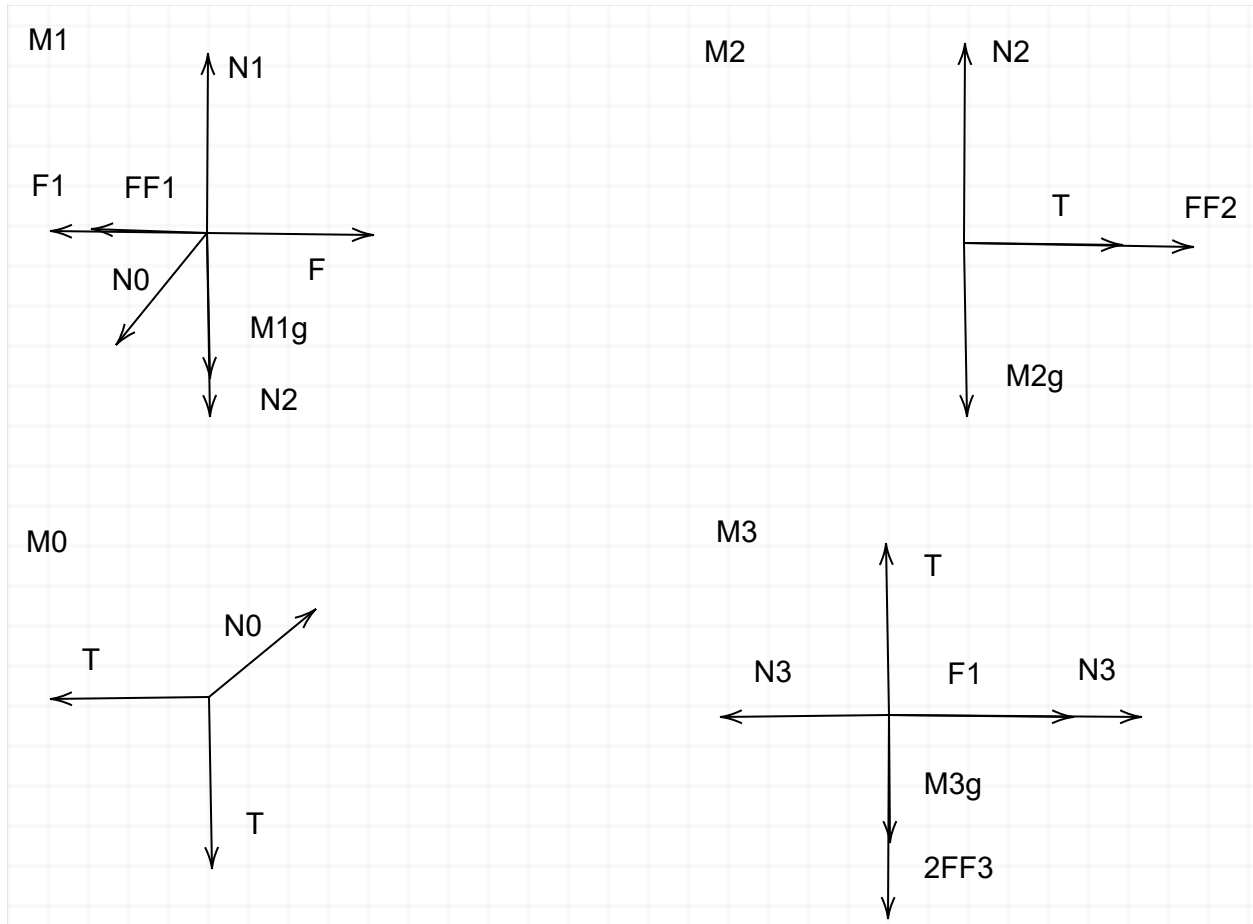


## Project02



I have assumed  $F$  is positive

We have the following equations:

$$M_1 \text{ in } x \text{ direction: } F - N_{0x} - F_{F1} - F_1 = M_1 a_1$$

$$M_1 \text{ in } y \text{ direction: } N_1 - M_1 g - N_2 - N_{0y} = 0 \text{ (doesn't move in } y \text{ direction)}$$

$$M_2 \text{ in } x \text{ direction: } F_{F2} + T = M_2 a_2$$

$$M_2 \text{ in } y \text{ direction: } N_2 - M_2 g = 0$$

$$M_3 \text{ in } x \text{ direction: } N_3 + F_1 - N_3 = M_3 a_{3x} \implies F_1 = M_3 a_{3x}$$

$$M_3 \text{ in } y \text{ direction: } T - M_3 g - 2F_{F3} = M_3 a_{3y}$$

$$M_0 \text{ in } x \text{ direction: } N_{0x} - T = M_0 g = 0 \implies N_{0x} = T$$

And the following constraints

$$\text{The length of the rope is constant} \implies a_1 - a_2 - a_{3y} = 0 \implies a_1 = a_2 + a_{3y}$$

$$M_3 \text{ cannot escape the hole} \implies a_1 = a_{3x}$$

$$x_1 - x_2 = a_2 t^2 / 2 \text{ (if } M_2 \text{ goes to the right and stops at } x_1) \implies a_2 = 2(x_1 - x_2) / t^2$$

$$y_1 - y_3 = a_{3y}t^2/2 \text{ (if } M_3 \text{ stops at the bottom)} \implies a_{3y} = 2(y_1 - y_3)/t^2$$

We have equal number of unknowns and equations and by solving we get:

$$t = \sqrt{\frac{2(x_1 - x_2)(\mu_1 M_2 - M_2) - 2(x_1 - x_2 + y_1 - y_3)(M_3 + M_1)}{\mu_1 \mu_2 M_2 g - F - \mu_2 M_2 g + \mu_1 M_1 g + \mu_1 M_2 g}} \implies$$

We can insert  $t$  and find  $a_1, a_2, a_{3x}, a_{3y}$ . after that we can find the coordinates at a given time  $t_0$  by inserting  $t$  in the following equations

$$X_{1n} = x_1 + a_1 t_0^2/2, \quad Y_{1n} = y_1$$

$$X_{2n} = x_2 + a_2 t_0^2/2 + a_1 t_0^2/2, \quad Y_{2n} = y_2$$

$$X_{3n} = X_{1n}, \quad Y_{3n} = y_3 + a_{3y} t_0^2/2$$

**Code workflow:**

We get the parameters  $M_1, M_2, M_3, F, \mu_1, \mu_2, \mu_2, x_1, x_2, x_3, y_1, y_2, y_3, t_0$  and find  $t$ , based on that we find  $a_1, a_2, a_{3x}, a_{3y}$  and then find the coordinates at time  $t_0$  using the equations above