

Life Expectancy Prediction

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Abstract

We have implemented a Linear Regression model to predict the life expectancy of the human population with our best model having an adjusted R-squared value of 0.8239, RMSE of 3.71, and MAE of 2.85, from the processed dataset having ~1650 observations of ~20 variables related to life expectancy and health factors for 193 countries provided by the Global Health Observatory (GHO) data repository under the World Health Organization (WHO). Several model building techniques including Forward Selection, Backward Elimination, and Stepwise Regression were used to obtain the candidate models, which were then evaluated with K-Fold Cross Validation to yield the model with the lowest RMSE value. Our best model passes the normality assumption and has no issues with the multicollinearity of the variables.

Introduction

Life expectancy is an estimate of the expected average number of years of life (or a person's age at death) for individuals who were born into a particular population. It is one of the most used summary indicators for the overall health of a population. Its levels and trends direct health policies, and researchers try to identify the determining risk factors to assess and forecast future developments.

The goal of this project is to build a Linear Regression model that can predict the life expectancy of the human population based on several factors such as the amount of alcohol consumption, average Body Mass Index (BMI), immunization of various vaccines among 1-year-olds such as Hepatitis B, Polio, and Diphtheria vaccines, and more, and also derive insights into what factors are significant in determining a higher or lower life expectancy of the human population.

Materials and Methods

Software and Packages Used

We have used R with the RStudio Integrated Development Environment for our analysis and for building the Linear Regression models. We have also used the R packages `corrplot`, `car`, `olsrr`, and `caret` to aid in our analysis and model building.

Dataset

The data related to life expectancy and health factors for 193 countries is taken from the Global Health Observatory (GHO) data repository under the World Health Organization (WHO). Its corresponding economic data was collected from the United Nations website for a period of 16 years (2000-2015).

The dataset is available at <https://www.kaggle.com/datasets/kumarajarshi/life-expectancy-who>.

Life Expectancy Data.csv contains the following fields:

- **Country** - Country Observed.
- **Year** - Year Observed.
- **Status** - Developed or Developing status.
- **Life.expectancy** - Life Expectancy in age.
- **Adult.Mortality** - Adult Mortality Rates on both sexes (probability of dying between 15-60 years/1000 population).
- **infant.deaths** - Number of Infant Deaths per 1000 population.
- **Alcohol** - Alcohol recorded per capita (15+) consumption (in litres of pure alcohol).
- **percentage.expenditure** - Expenditure on health as a percentage of Gross Domestic Product per capita (%).
- **Hepatitis.B** - Hepatitis B (HepB) immunization coverage among 1-year-olds (%).
- **Measles** - Number of reported Measles cases per 1000 population.
- **BMI** - Average Body Mass Index of entire population.
- **under.five.deaths** - Number of under-five deaths per 1000 population.
- **Polio** - Polio (Pol3) immunization coverage among 1-year-olds (%).
- **Total.expenditure** - General government expenditure on health as a percentage of total government expenditure (%).
- **Diphtheria** - Diphtheria tetanus toxoid and pertussis (DTP3) immunization coverage among 1-year-olds (%).
- **HIV.AIDS** - Deaths per 1000 live births due to HIV/AIDS (0-4 years).
- **GDP** - Gross Domestic Product per capita (in USD).
- **Population** - Population of the country.
- **thinness..1.19.years** - Prevalence of thinness among children and adolescents for Age 10 to 19 (%).
- **thinness.5.9.years** - Prevalence of thinness among children for Age 5 to 9 (%).
- **Income.composition.of.resources** - Human Development Index in terms of income composition of resources (index ranging from 0 to 1).
- **Schooling** - Number of years of Schooling (years).

In total, there are 2938 observations of 22 variables with 20 of them being numerical and 2 categorical (**Country** and **Status**).

We are using **Life.expectancy** to predict the life expectancy of the human population with the given independent variables in the dataset.

For data cleaning, we have dropped any observation that does not contain any value in any of its columns. This shrinks our dataset to 1649 observations.

We have plotted a boxplot and a histogram for all the numerical variables in the dataset. For categorical variables, we have plotted a barplot indicating the counts of each category of the variable. This can be viewed in Appendix A of the report.

Feature Selection

We have removed some of the variables for building the model due to the reasons mentioned below:

Country - Contains too many levels with no additional information to predict **Life.expectancy**.

Year - Contains time series data with no additional information to predict **Life.expectancy**.

We have also mutated **Hepatitis.B**, **Polio**, and **Diphtheria** for building the model since the range between their minimum values and their 1st Quartiles are too wide. We have mutated their values into 2 categorical values: '<90% Covered' and '>=90% Covered'.

This leaves us with 1649 observations of 20 variables with 16 of them being numerical and 4 categorical (**Status**, **Hepatitis.B**, **Polio**, and **Diphtheria**).

```
summary(life)
```

```
##      Status      Life.expectancy Adult.Mortality infant.deaths
## Length:1649      Min.   :44.0      Min.   : 1.0      Min.   : 0.00
## Class :character  1st Qu.:64.4      1st Qu.: 77.0      1st Qu.: 1.00
## Mode  :character  Median :71.7      Median :148.0      Median : 3.00
##                      Mean   :69.3      Mean   :168.2      Mean   : 32.55
##                      3rd Qu.:75.0      3rd Qu.:227.0      3rd Qu.: 22.00
##                      Max.   :89.0      Max.   :723.0      Max.   :1600.00
##      Alcohol      percentage.expenditure Hepatitis.B      Measles
## Min.   : 0.010      Min.   : 0.00      Length:1649      Min.   : 0
## 1st Qu.: 0.810      1st Qu.: 37.44      Class :character  1st Qu.: 0
## Median : 3.790      Median : 145.10      Mode  :character  Median : 15
## Mean   : 4.533      Mean   : 698.97                      Mean   : 2224
## 3rd Qu.: 7.340      3rd Qu.: 509.39                      3rd Qu.: 373
## Max.   :17.870      Max.   :18961.35                     Max.   :131441
##      BMI      under.five.deaths      Polio      Total.expenditure
## Min.   : 2.00      Min.   : 0.00      Length:1649      Min.   : 0.740
## 1st Qu.:19.50      1st Qu.: 1.00      Class :character  1st Qu.: 4.410
## Median :43.70      Median : 4.00      Mode  :character  Median : 5.840
## Mean   :38.13      Mean   : 44.22                      Mean   : 5.956
## 3rd Qu.:55.80      3rd Qu.: 29.00                      3rd Qu.: 7.470
## Max.   :77.10      Max.   :2100.00                     Max.   :14.390
##      Diphtheria      HIV.AIDS      GDP      Population
## Length:1649      Min.   : 0.100      Min.   : 1.68      Min.   :3.400e+01
## Class :character  1st Qu.: 0.100      1st Qu.: 462.15      1st Qu.:1.919e+05
## Mode  :character  Median : 0.100      Median : 1592.57      Median :1.420e+06
##                      Mean   : 1.984      Mean   : 5566.03      Mean   :1.465e+07
##                      3rd Qu.: 0.700      3rd Qu.: 4718.51      3rd Qu.:7.659e+06
##                      Max.   :50.600      Max.   :119172.74      Max.   :1.294e+09
## thinness..1.19.years thinness.5.9.years Income.composition.of.resources
## Min.   : 0.100      Min.   : 0.100      Min.   :0.0000
## 1st Qu.: 1.600      1st Qu.: 1.700      1st Qu.:0.5090
## Median : 3.000      Median : 3.200      Median :0.6730
## Mean   : 4.851      Mean   : 4.908      Mean   :0.6316
## 3rd Qu.: 7.100      3rd Qu.: 7.100      3rd Qu.:0.7510
## Max.   :27.200      Max.   :28.200      Max.   :0.9360
##      Schooling
## Min.   : 4.20
## 1st Qu.:10.30
## Median :12.30
## Mean   :12.12
## 3rd Qu.:14.00
## Max.   :20.70
```

Correlations

We would want to look at the correlation matrix to see which variables are correlated with the target variable, and also to check if any independent variable is also correlated with another independent variable. Correlated independent variables in a model can negatively impact its performance, and so if any such pair of independent correlated variables is found, we would keep only one of them in the model.

Since the number of variables is moderately large, we have plotted the correlation plot of the dataset rather than printing the correlation matrix by itself. The colors and their shades easily guide us to show which 2 variables are correlated.



There are a few takeaways from this correlation plot:

- Life expectancy has a strong positive correlation with Income.composition.of.resources and Schooling.
- Life expectancy has a negative correlation with Adult.Mortality, which makes sense since if the mortality rate of adult is high, then obviously the life expectancy will be low.
- Life expectancy has a very weak correlation with Measles and Population.
- There is a very strong correlation between infant.deaths and under.five.deaths, percentage.expenditure and GDP, and thinness..1.19.years and thinness.5.9.years, indicating multicollinearity between them. Therefore, we have removed under.five.deaths, percentage.expenditure, and thinness.5.9.years for building the model.

Model Building

We now build a Linear Regression Model using all the remaining variables to predict the life expectancy of the human population. We will set the level of α to be 0.05 throughout the analysis.

```
lmod_all = lm(Life.expectancy ~ ., data = life)
summary(lmod_all)
```

```
##
## Call:
## lm(formula = Life.expectancy ~ ., data = life)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -17.0274  -2.1069   0.0579   2.3922  11.5489
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    5.506e+01  8.102e-01  67.965 < 2e-16 ***
## StatusDeveloping -9.930e-01  3.464e-01  -2.867  0.0042 **
## Adult.Mortality -1.785e-02  9.663e-04 -18.477 < 2e-16 ***
## infant.deaths   -3.057e-03  1.260e-03  -2.425  0.0154 *
## Alcohol         -1.539e-01  3.381e-02  -4.552 5.72e-06 ***
## Hepatitis.B>=90% Covered -6.990e-01  3.174e-01  -2.202  0.0278 *
## Measles         1.668e-05  1.078e-05   1.547  0.1220
## BMI             3.591e-02  6.103e-03   5.884 4.85e-09 ***
## Polio>=90% Covered  5.337e-01  4.437e-01   1.203  0.2293
## Total.expenditure  7.441e-02  4.170e-02   1.784  0.0745 .
## Diphtheria>=90% Covered  9.665e-01  4.888e-01   1.977  0.0482 *
## HIV.AIDS        -4.278e-01  1.850e-02 -23.124 < 2e-16 ***
## GDP             6.096e-05  9.637e-06   6.326 3.24e-10 ***
## Population      2.558e-09  1.766e-09   1.449  0.1476
## thinness..1.19.years -4.799e-02  2.791e-02  -1.720  0.0857 .
## Income.composition.of.resources 1.041e+01  8.503e-01  12.244 < 2e-16 ***
## Schooling       8.790e-01  6.158e-02  14.274 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.688 on 1632 degrees of freedom
## Multiple R-squared:  0.826, Adjusted R-squared:  0.8243
## F-statistic: 484.1 on 16 and 1632 DF, p-value: < 2.2e-16
```

There are a few takeaways from this full model:

- The p-value of the model is $2.2e-16 < 0.05$, indicating that it is significant.
- The adjusted R-squared value of the model is 0.8243, indicating that about 82.43% of the variability observed in the target variable can be explained by the independent variables in the model, which is quite a good result and can possibly be improved even further with model selection.
- `Adult.Mortality`, `Alcohol`, `BMI`, `HIV.AIDS`, `GDP`, `Income.composition.of.resources` and `Schooling` are the most significant variables with p-value < 0.05 .
- From the model we can interpret that `Income.composition.of.resources` has a strong positive effect on life expectancy.
- From the model we can interpret that `StatusDeveloping`, `Adult.Mortality`, `infant.deaths`, `Alcohol`, `HIV.AIDS`, and `thinness..1.19.years` may have a negative effect on life expectancy.
- A peculiar result we can interpret from the model is that `Hepatitis.B>=90% Covered` may also have a negative effect on life expectancy.

We now generate models by using different techniques like Forward Selection Method, Backward Elimination Method and Stepwise Regression Method.

Forward Selection Method

The Forward Selection method involves building a model starting with no variables in the model, testing the addition of each variable using a chosen model fit criterion (in our case the p-to-enter value), adding the variable (if any) whose inclusion gives the most statistically significant improvement of the fit, and repeating this process until none improves the model to a statistically significant extent.

For building the model using Forward Selection method, we have used the default p-to-enter value of 0.3.

```
ols_step_forward_p(lmod_all)
```

```
##
##                               Selection Summary
## -----
##      Variable                R-Square    Adj.    C(p)      AIC      RMSE
## Step      Entered              R-Square    R-Square              RMSE
## -----
##      1      Schooling          0.5294      0.5292      2767.6453      10612.7157      6.0362
##      2      HIV.AIDS          0.7304      0.7301      885.2760      9696.3271      4.5704
##      3      Adult.Mortality    0.7871      0.7867      355.5223      9308.9473      4.0627
##      4      Income.composition.of.resources 0.8092      0.8087      150.4656      9130.3986      3.8474
##      5      BMI                0.8144      0.8138      103.6254      9086.7666      3.7957
##      6      GDP                0.8197      0.8190      55.8305      9040.9050      3.7422
##      7      Diphtheria         0.8214      0.8206      42.0679      9027.4602      3.7258
##      8      Alcohol            0.8226      0.8217      32.8339      9018.3638      3.7144
##      9      thinness..1.19.years 0.8235      0.8225      26.3197      9011.9039      3.7061
##     10      Status            0.8244      0.8233      19.8462      9005.4410      3.6977
##     11      Hepatitis.B        0.8248      0.8236      17.7935      9003.3780      3.6943
##     12      Total.expenditure  0.8251      0.8239      16.7491      9002.3193      3.6920
##     13      infant.deaths      0.8254      0.8240      16.6117      9002.1684      3.6907
##     14      Measles            0.8256      0.8241      16.5671      9002.1083      3.6895
##     15      Population         0.8258      0.8242      16.4465      9001.9689      3.6882
##     16      Polio             0.8260      0.8243      17.0000      9002.5080      3.6877
## -----
```

The Forward Selection method included all the variables in the model.

Backward Elimination Method

The Backward Elimination method involves building a model starting with all candidate variables, testing the deletion of each variable using a chosen model fit criterion (in our case the p-to-remove value), deleting the variable (if any) whose loss gives the most statistically insignificant deterioration of the model fit, and repeating this process until no further variables can be deleted without a statistically significant loss of fit.

For building the model using Backward Elimination method, we have used the default p-to-remove value of 0.3.

```
ols_step_backward_p(lmod_all)
```

```
## [1] "No variables have been removed from the model."
```

The Backward Elimination method did not eliminate any variables from the model.

Stepwise Regression Method

The Stepwise Regression method is a combination of the above two methods, starting with no variables in the model and testing at each step for variables to be included or excluded.

For building the model using Stepwise Regression method, we have used the default p-to-enter value of 0.1 and the default p-to-remove value of 0.3.

```
ols_step_both_p(lmod_all)
```

```
##
##                                     Stepwise Selection Summary
## -----
##                                     Added/
## Step          Variable             Removed    R-Square    Adj.      C(p)      AIC
## -----
##      1          Schooling          addition    0.529      0.529    2767.6450  10612.71
##      2          HIV.AIDS          addition    0.730      0.730    885.2760   9696.32
##      3      Adult.Mortality          addition    0.787      0.787    355.5220   9308.94
##      4  Income.composition.of.resources  addition    0.809      0.809    150.4660   9130.39
##      5              BMI          addition    0.814      0.814    103.6250   9086.76
##      6              GDP          addition    0.820      0.819     55.8310   9040.90
##      7          Diphtheria          addition    0.821      0.821     42.0680   9027.46
##      8          Alcohol          addition    0.823      0.822     32.8340   9018.36
##      9      thinness..1.19.years          addition    0.823      0.823     26.3200   9011.90
##     10              Status          addition    0.824      0.823     19.8460   9005.44
##     11          Hepatitis.B          addition    0.825      0.824     17.7930   9003.37
##     12      Total.expenditure          addition    0.825      0.824     16.7490   9002.31
## -----
```

A total of 12 variables were included in the model built using Stepwise Regression method.

In summary, the variables chosen by the methods are indicated in the following table (x denotes the variable was chosen by the method):

Model Selection Method	Status	Adult.Mortality	infant.deaths	Alcohol
Forward Selection	x	x	x	x
Backward Elimination	x	x	x	x
Stepwise Regression	x	x		x

Model Selection Method	Hepatitis.B	Measles	BMI	Polio	Total.expenditure
Forward Selection	x	x	x	x	x
Backward Elimination	x	x	x	x	x
Stepwise Regression	x		x		x

Model Selection Method	Diphtheria	HIV.AIDS	GDP	Population
Forward Selection	x	x	x	x
Backward Elimination	x	x	x	x
Stepwise Regression	x	x	x	

Model Selection Method	thinness..1.19.years	Income.composition.of.resources	Schooling
Forward Selection	x		x
Backward Elimination	x		x
Stepwise Regression	x		x

Both the Forward Selection method and Backward Elimination method have chosen the same set of variables.

K-Fold Cross Validation

We were left with 2 models - the full model and the model built using Stepwise Regression method - as our candidate models. To choose the better model as our final model, we ran K-Fold Cross Validation on each of the above models, and subsequently picked the model with the lowest RMSE value as our final model. We chose the value of K to be 5.

In K-Fold Cross-Validation, the original sample of the dataset is randomly partitioned into K equal sized subsamples. Of the K subsamples, a single subsample is retained as the validation data for testing the model, and the remaining K-1 subsamples are used as training data. The cross-validation process is then repeated K times, with each of the K subsamples used exactly once as the validation data. The K results are then averaged to produce a single estimation, which in our case is the mean RMSE value.

```
# Define training control
set.seed(13245)
train.control = trainControl(method = 'cv', number = 5)
```

Cross-Validation for the full model:

```
# Train the model
CV_all = train(
  Life.expectancy ~ .,
  data = life,
  method = 'lm',
  trControl = train.control
)
```



```
# Summarize the results
CV_all
```

```
## Linear Regression
##
## 1649 samples
## 16 predictor
##
## No pre-processing
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 1318, 1319, 1319, 1320, 1320
## Resampling results:
##
## RMSE      Rsquared   MAE
## 3.719367  0.8214392  2.853294
##
## Tuning parameter 'intercept' was held constant at a value of TRUE
```

Cross-Validation for model chosen by Stepwise Regression method:

```
# Train the model
CV_stepwise = train(
  Life.expectancy ~ Schooling + HIV.AIDS + Adult.Mortality + Income.composition.of.resources + BMI + GDP.per.capita
  data = life,
  method = 'lm',
  trControl = train.control
)
```

```
# Summarize the results
CV_stepwise
```

```
## Linear Regression
##
## 1649 samples
## 12 predictor
##
## No pre-processing
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 1319, 1320, 1318, 1320, 1319
## Resampling results:
##
## RMSE      Rsquared   MAE
## 3.718134  0.8211816  2.853578
##
## Tuning parameter 'intercept' was held constant at a value of TRUE
```

Results of 5-Fold Cross-Validation of the 2 models:

```
rbind(CV_all$results, CV_stepwise$results)
```

	intercept	RMSE	Rsquared	MAE	RMSESD	RsquaredSD	MAESD
## 1	TRUE	3.719367	0.8214392	2.853294	0.1466741	0.01735040	0.1035478
## 2	TRUE	3.718134	0.8211816	2.853578	0.2043897	0.01790453	0.1159896

Since the model chosen by Stepwise Regression method `lmod_stepwise` has a lower RMSE value, we have selected this model to be our final model.

Results

Out of the 2 candidate models, we have picked the model chosen by the Stepwise Regression model to be our final model.

```
lmod_final = lm(
  Life.expectancy ~ Schooling + HIV.AIDS + Adult.Mortality + Income.composition.of.resources + BMI + GDP
  data = life
)
summary(lmod_final)
```

```
##
## Call:
## lm(formula = Life.expectancy ~ Schooling + HIV.AIDS + Adult.Mortality +
##     Income.composition.of.resources + BMI + GDP + Diphtheria +
##     Alcohol + thinness..1.19.years + Status + Hepatitis.B + Total.expenditure,
##     data = life)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -16.9828  -2.1039   0.0534   2.3728  11.4923
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    5.505e+01  8.059e-01  68.312 < 2e-16 ***
## Schooling       8.931e-01  6.129e-02  14.572 < 2e-16 ***
## HIV.AIDS       -4.269e-01  1.846e-02 -23.131 < 2e-16 ***
## Adult.Mortality -1.781e-02  9.641e-04 -18.471 < 2e-16 ***
## Income.composition.of.resources 1.034e+01  8.471e-01  12.204 < 2e-16 ***
## BMI            3.577e-02  6.082e-03   5.881 4.94e-09 ***
## GDP            6.079e-05  9.646e-06   6.302 3.77e-10 ***
## Diphtheria>=90% Covered 1.452e+00  3.444e-01   4.215 2.64e-05 ***
## Alcohol        -1.607e-01  3.355e-02  -4.789 1.83e-06 ***
## thinness..1.19.years -6.820e-02  2.502e-02  -2.726 0.00648 **
## StatusDeveloping -9.968e-01  3.465e-01  -2.877 0.00407 **
## Hepatitis.B>=90% Covered -6.338e-01  3.140e-01  -2.018 0.04371 *
## Total.expenditure 7.257e-02  4.164e-02   1.743 0.08155 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.692 on 1636 degrees of freedom
## Multiple R-squared:  0.8251, Adjusted R-squared:  0.8239
## F-statistic: 643.3 on 12 and 1636 DF, p-value: < 2.2e-16
```

The final model contains 12 variables: Schooling, HIV.AIDS, Adult.Mortality, Income.composition.of.resources, BMI, GDP, Diphtheria, Alcohol, thinness..1.19.years, Status, Hepatitis.B, and Total.expenditure.

There are a few takeaways from this final model:

- The p-value of the model is $2.2e-16 < 0.05$, indicating that it is significant.
- The adjusted R-squared value of the model is 0.8239, indicating that about 82.39% of the variability observed in the target variable can be explained by the independent variables in the model.
- Pretty much all the variables in the model are the most significant variables with p-value < 0.05 .
- From the model we can interpret that `Income.composition.of.resources` has a strong positive effect on life expectancy.
- From the model we can interpret that `HIV.AIDS`, `Adult.Mortality`, `Alcohol`, `thinness..1.19.years`, and `StatusDeveloping`, may have a negative effect on life expectancy.
- `Hepatitis.B>=90% Covered` may also have a negative effect on life expectancy, the same observation we had seen previously on the full model.

Model Error Estimation

We have primarily used the R-squared, the adjusted R-squared, the root-mean-square error (RMSE), and the mean absolute error (MAE) as the metric for evaluating our models.

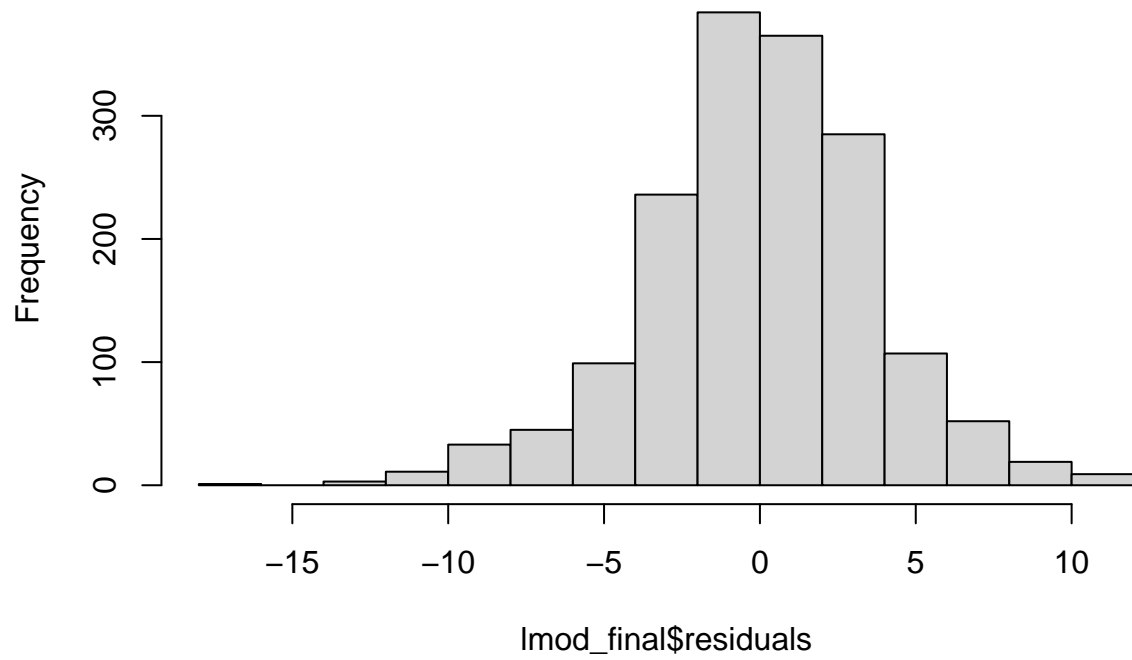
The estimates for the final model are derived from the results of 5-Fold Cross Validation, and are summarized in the following table:

Metric	Estimate
R-squared	0.8219568
RMSE	3.711009
MAE	2.846318

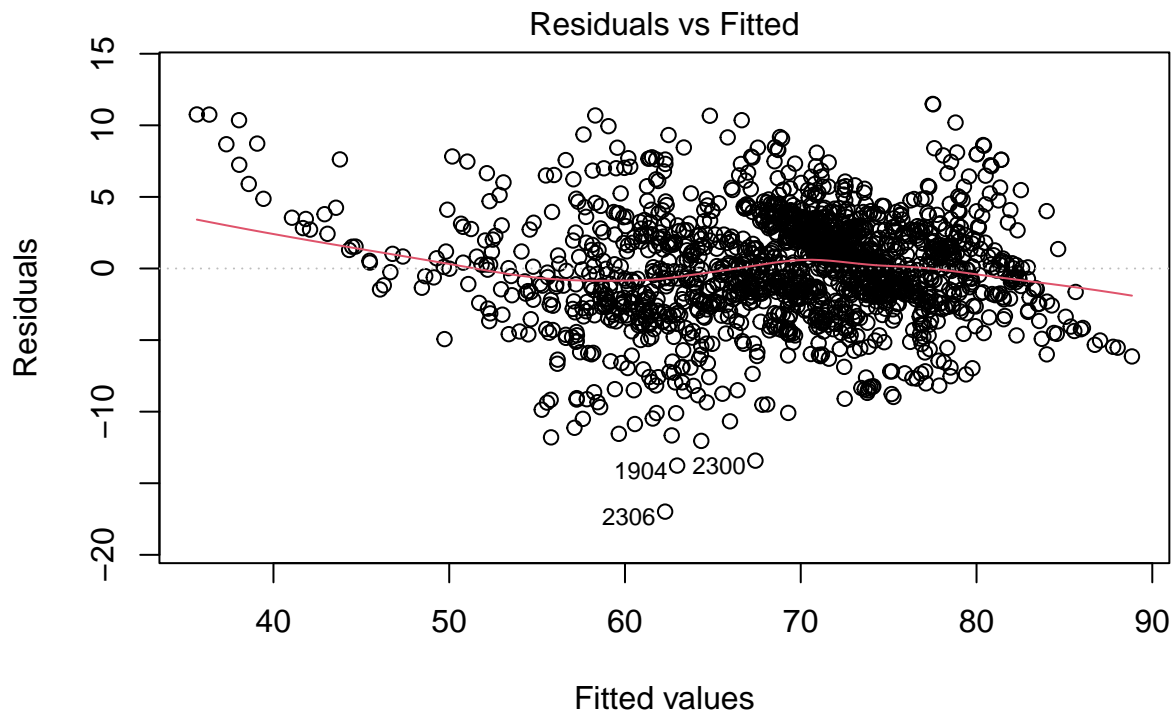
Model Adequacy Checking

Normality Testing:

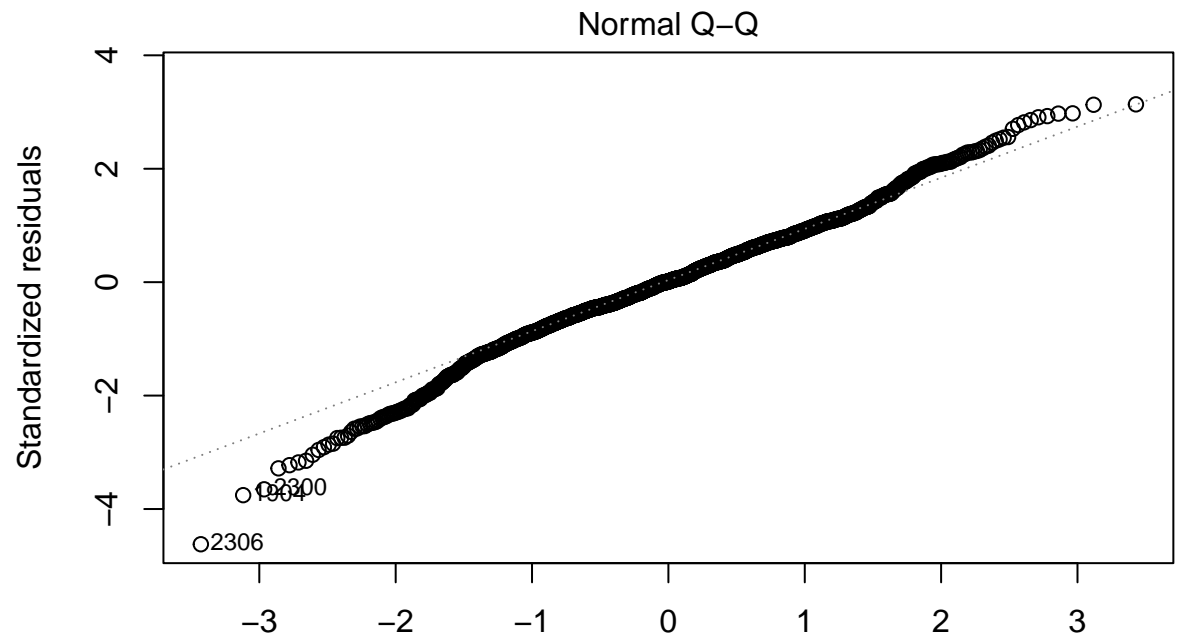
Histogram of lmod_final\$residuals



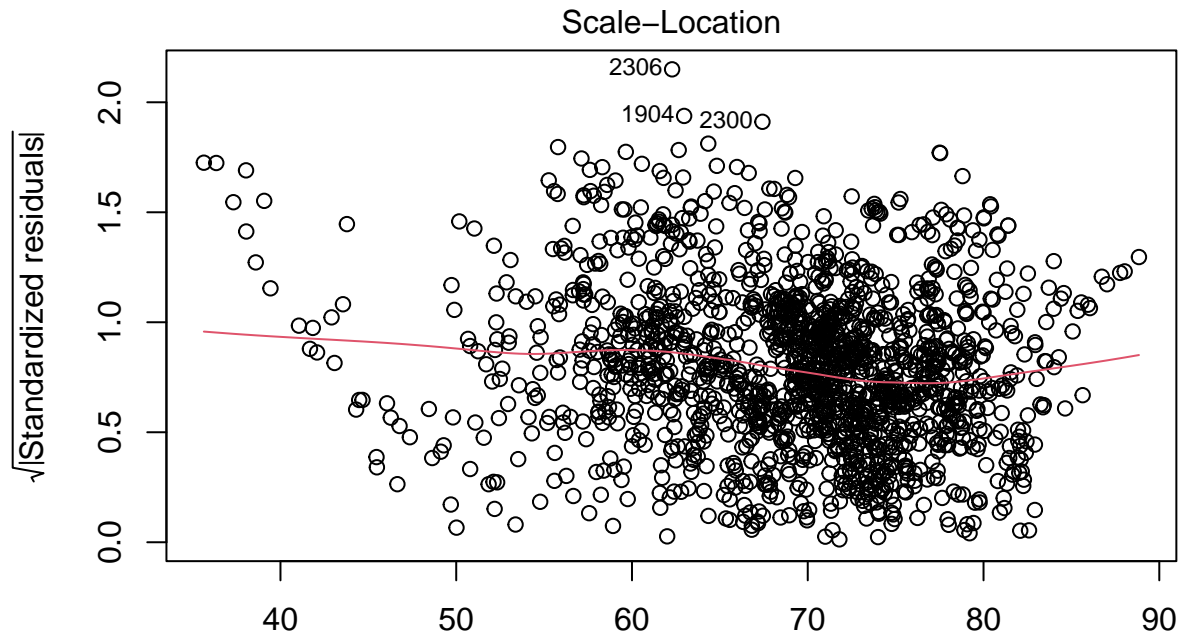
Most of the residuals seem to be distributed in the center, indicating that they are distributed normally.



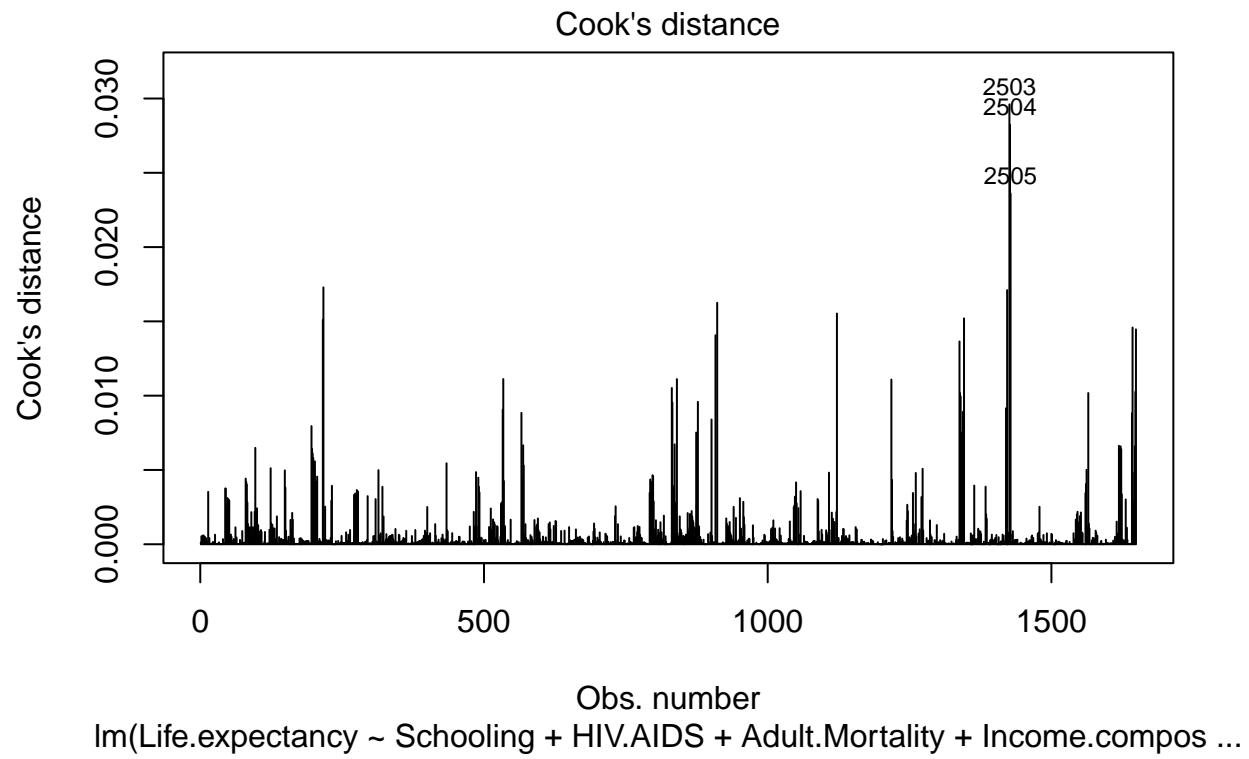
lm(Life.expectancy ~ Schooling + HIV.AIDS + Adult.Mortality + Income.compos ...

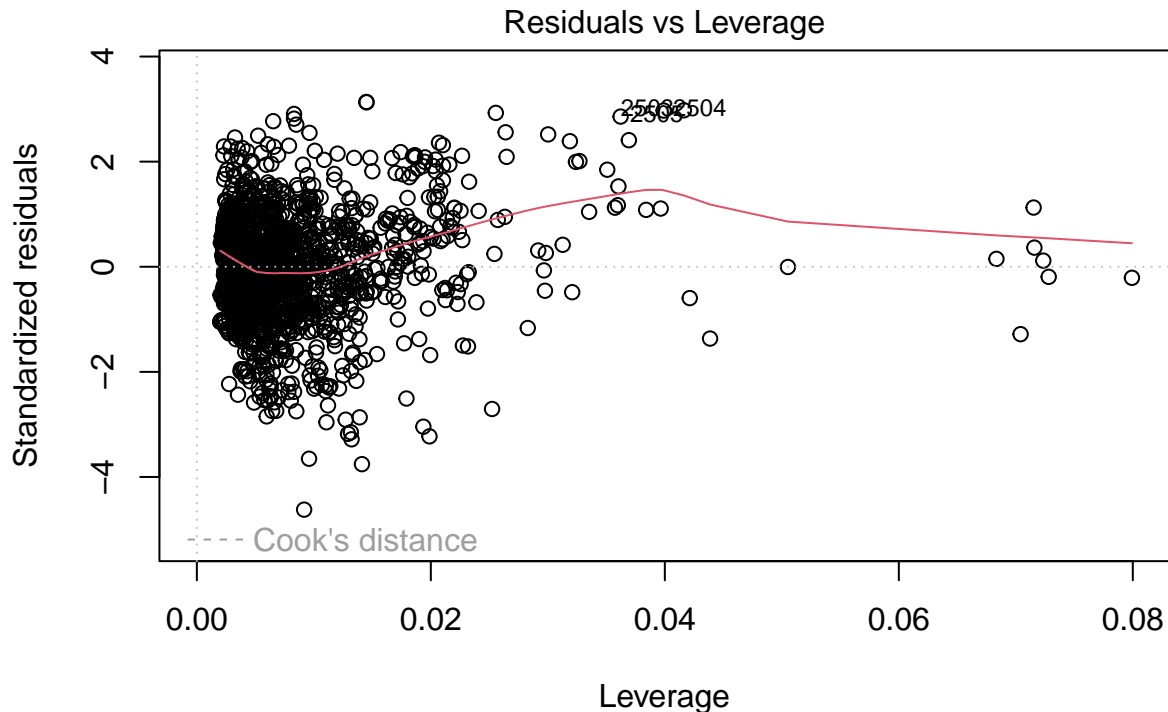


Im(Life.expectancy ~ Schooling + HIV.AIDS + Adult.Mortality + Income.compos ...



Fitted values
 $\text{lm}(\text{Life.expectancy} \sim \text{Schooling} + \text{HIV.AIDS} + \text{Adult.Mortality} + \text{Income.compos} \dots)$





$\text{lm}(\text{Life.expectancy} \sim \text{Schooling} + \text{HIV.AIDS} + \text{Adult.Mortality} + \text{Income.compos} \dots)$

There is no obvious observable pattern in the above plots, indicating that the model is appropriate.

Finally, we run a multicollinearity test to see if there is any multicollinearity between the variables in the model. We have used the Variance Inflation Factor (VIF) to determine the multicollinearity between the variables.

```
vif(lmod_final)
```

##	Schooling	HIV.AIDS
##	3.548828	1.498703
##	Adult.Mortality	Income.composition.of.resources
##	1.764485	2.908091
##	BMI	GDP
##	1.745170	1.481404
##	Diphtheria	Alcohol
##	3.511705	2.209220
##	thinness..1.19.years	Status
##	1.600520	1.818933
##	Hepatitis.B	Total.expenditure
##	2.981721	1.108283

A $\text{VIF} > 10$ implies serious problems with multicollinearity.

Since the VIF for all of the predictors is less than 10, there seems to be no issue with multicollinearity.

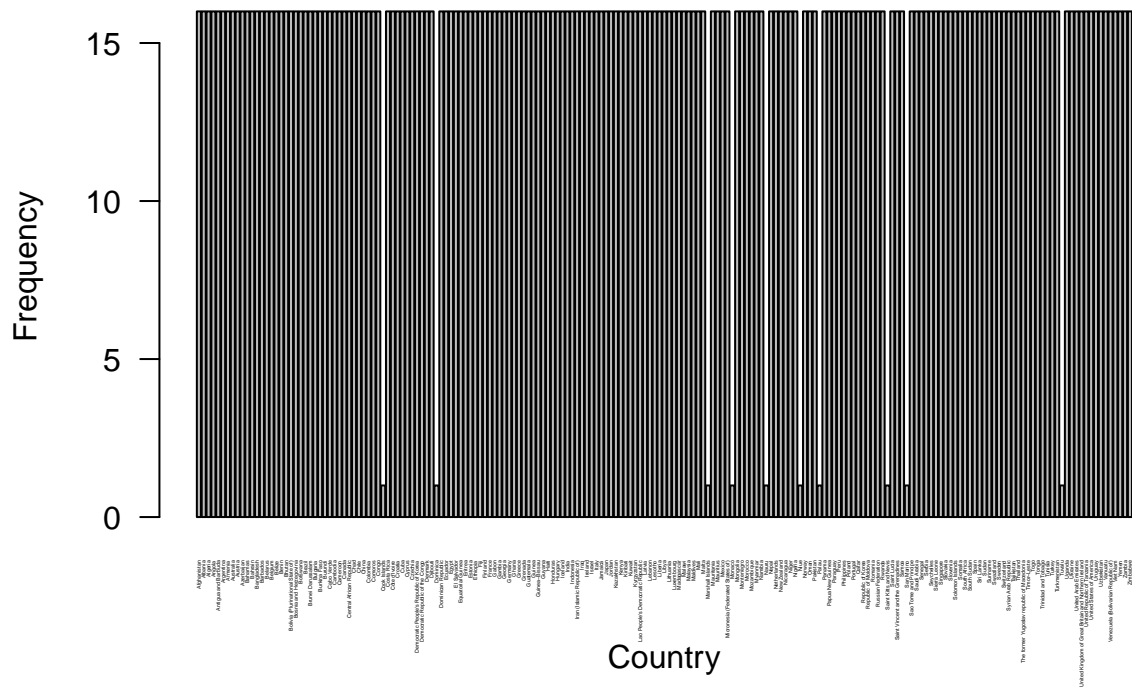
Discussion

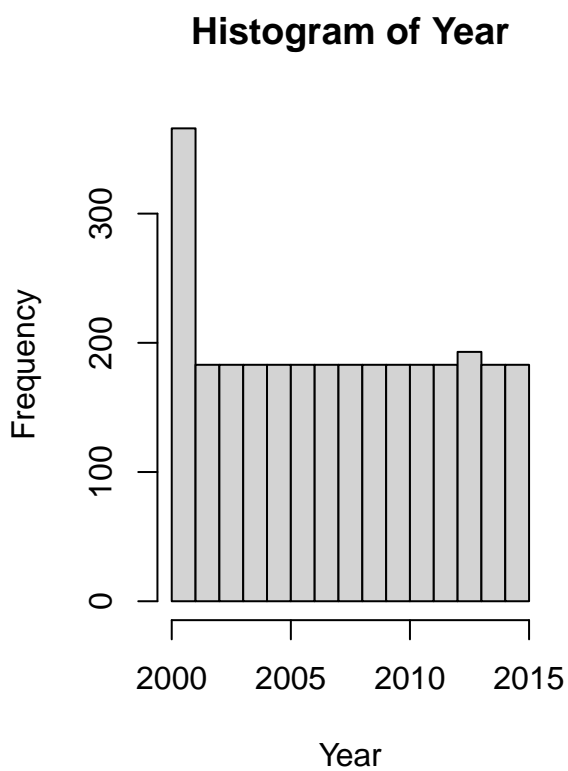
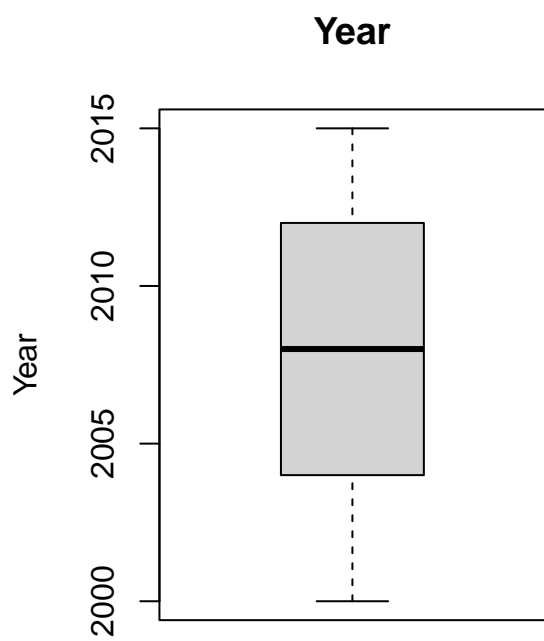
Literature Cited

[1] Luy M, Di Giulio P, Di Lego V, Lazarevič P, Sauerberg M. Life Expectancy: Frequently Used, but Hardly Understood. *Gerontology*. 2020;66(1):95-104. doi: 10.1159/000500955. Epub 2019 Aug 7. PMID: 31390630; PMCID: PMC7026938.

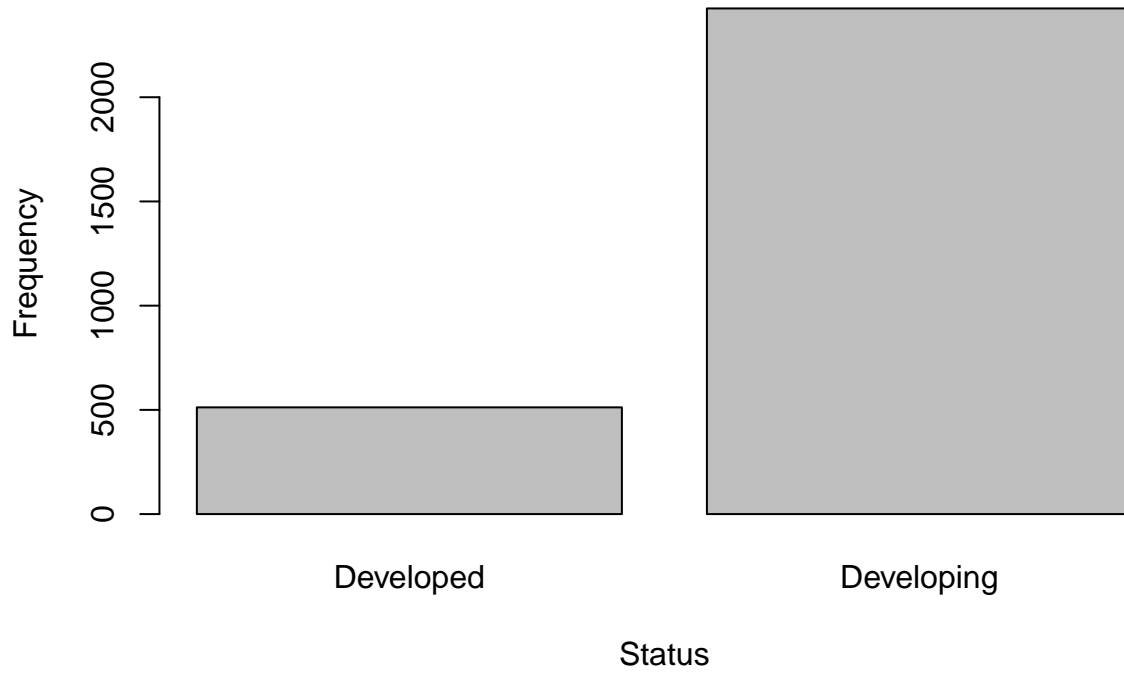
Appendix A - Variable Distribution Plots

Barplot of Country

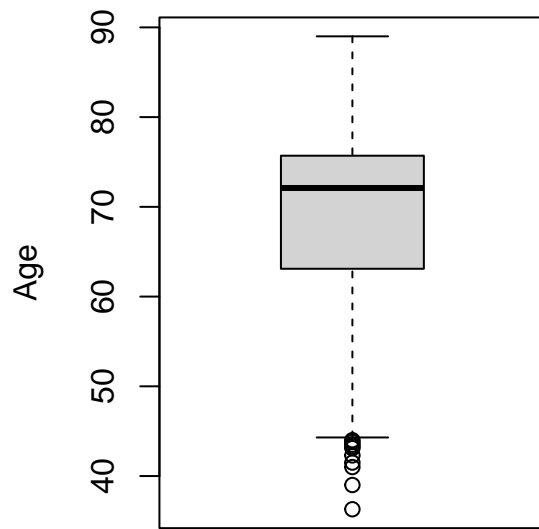




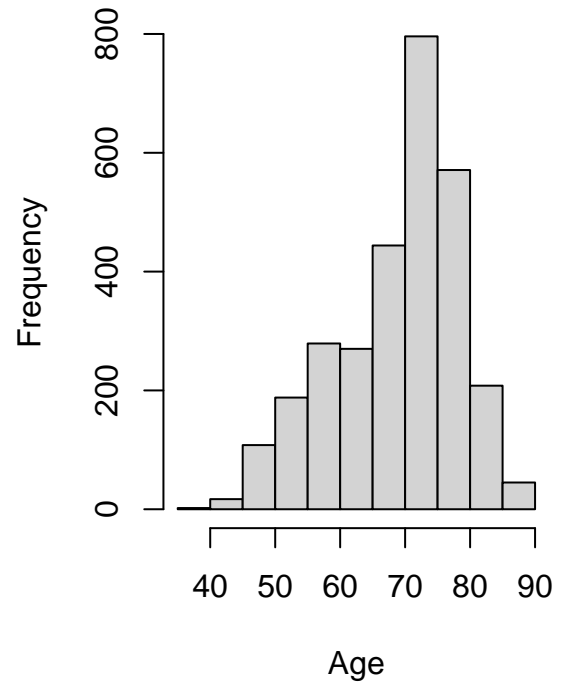
Barplot of Status



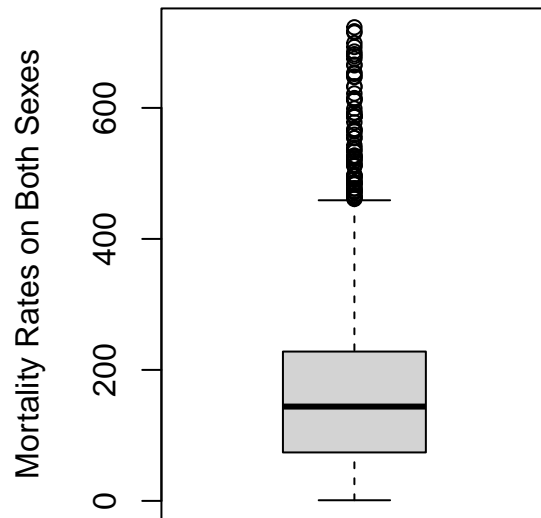
Life Expectancy



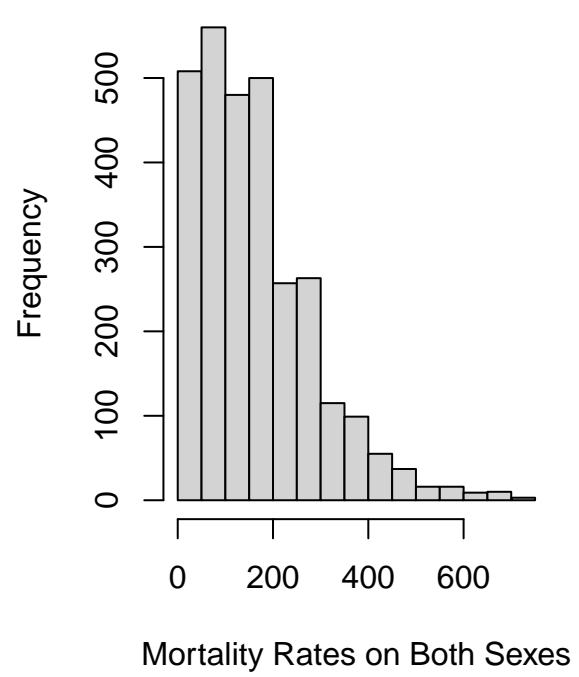
Histogram of Life Expectancy



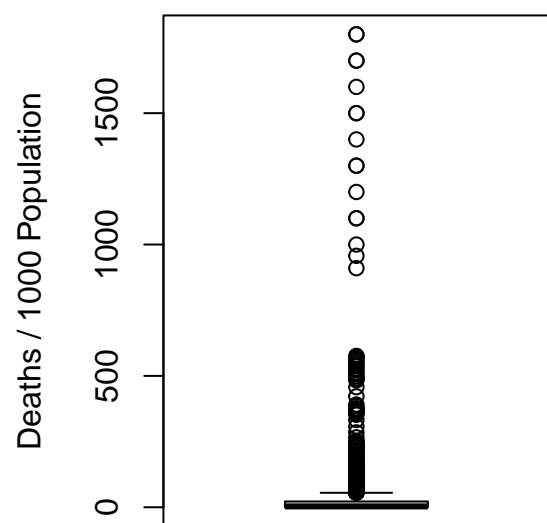
Adult Mortality Rate



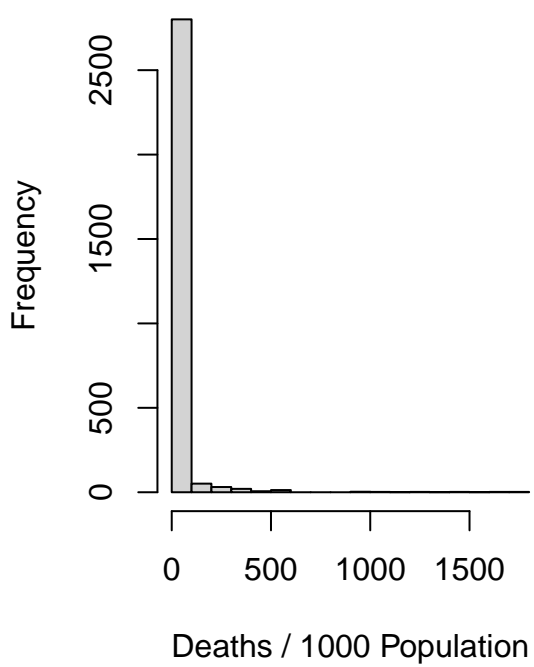
Histogram of Adult Mortality Rate



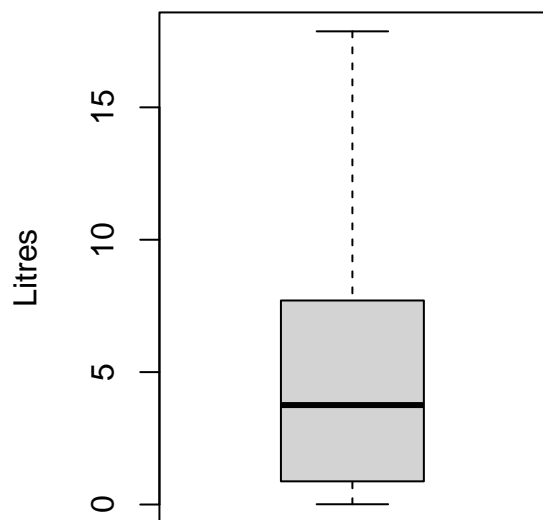
Infant Deaths



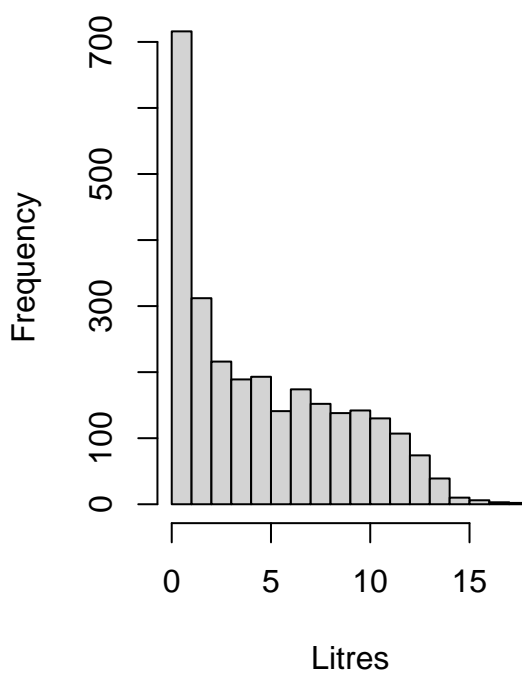
Histogram of Infant Deaths

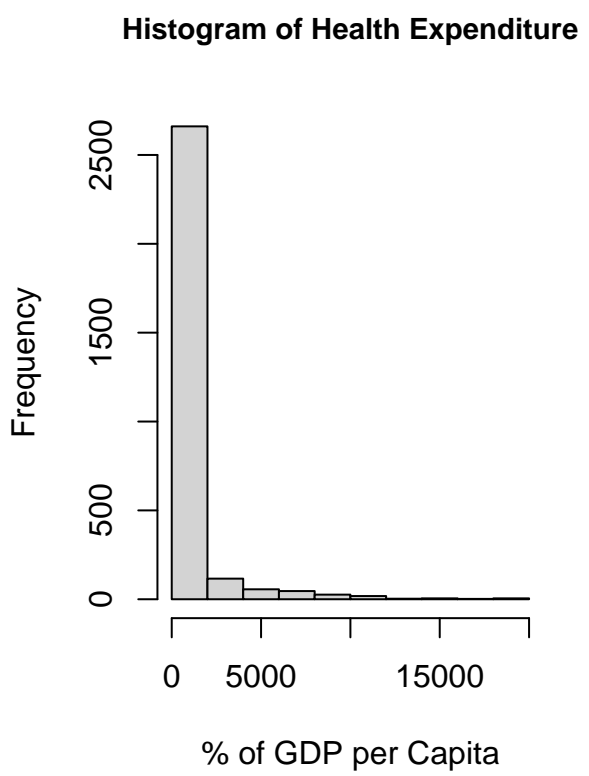
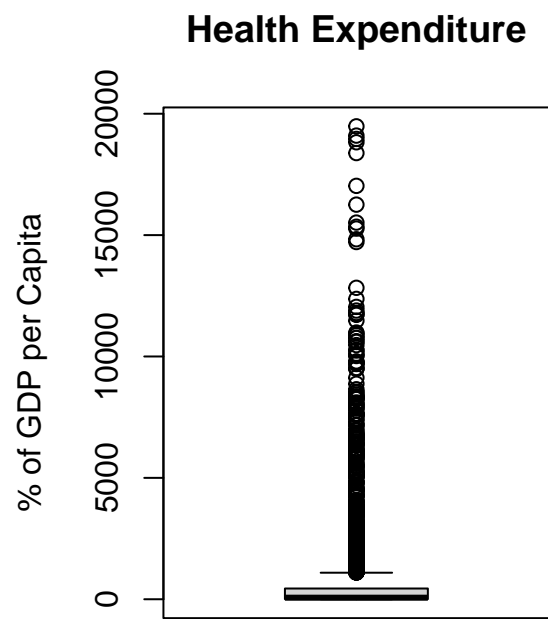


Alcohol Consumption

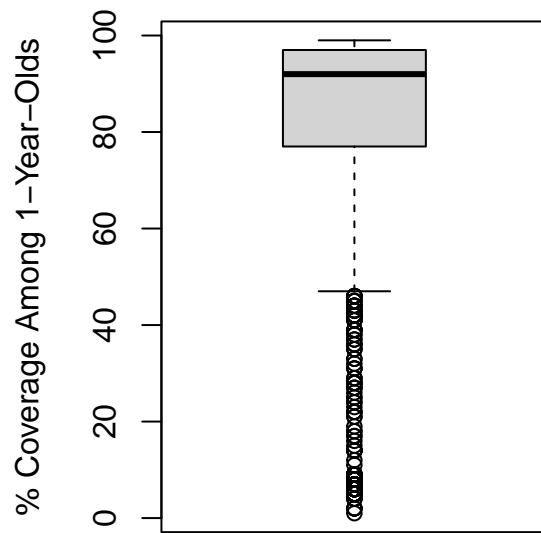


Histogram of Alcohol Consumption

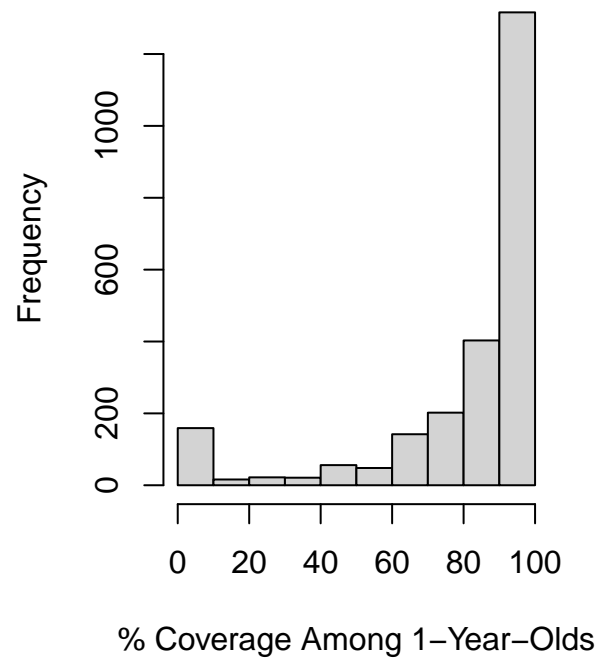




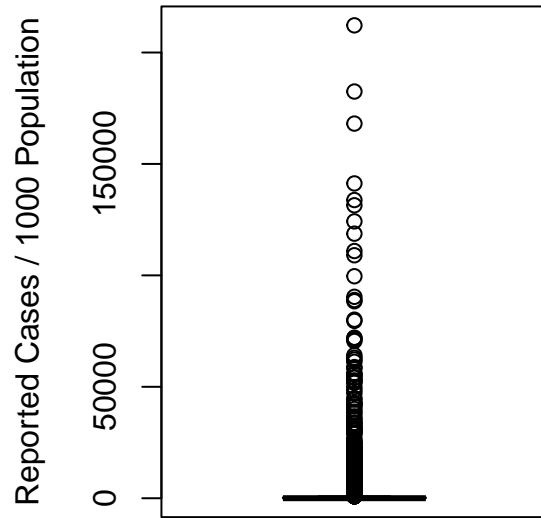
Hepatitis B (HepB) Immunization



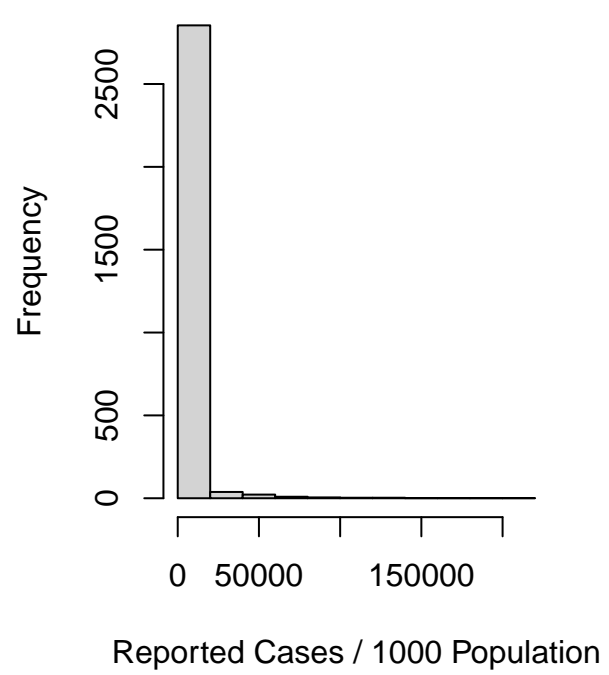
Histogram of HepB Immunization



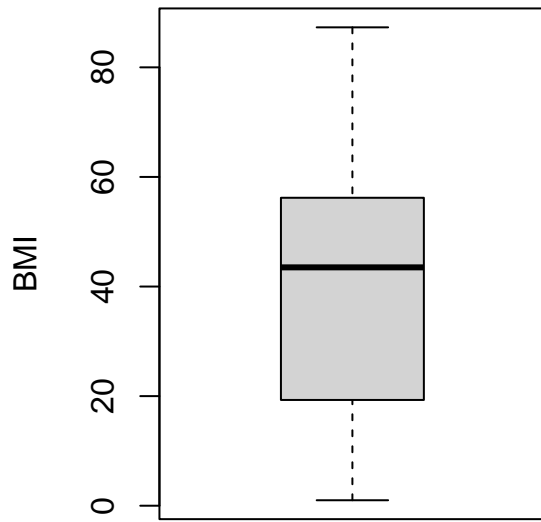
Measles



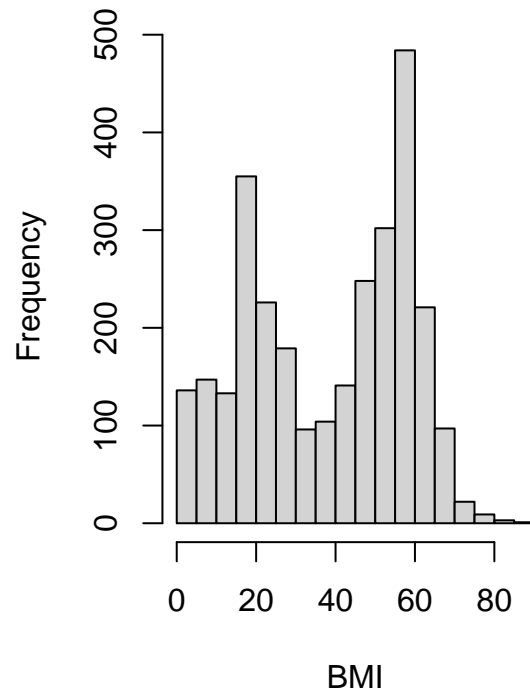
Histogram of Measles



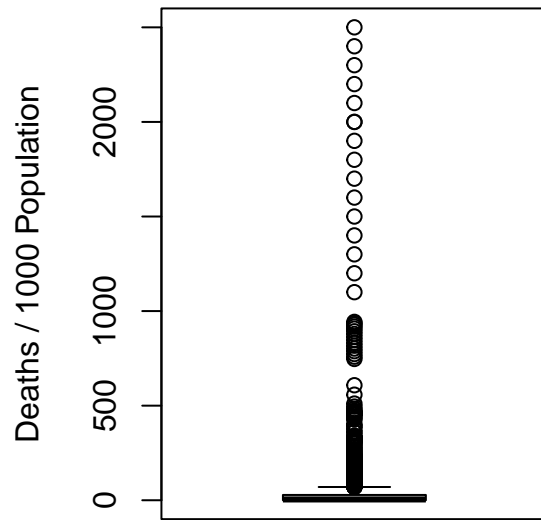
Average BMI



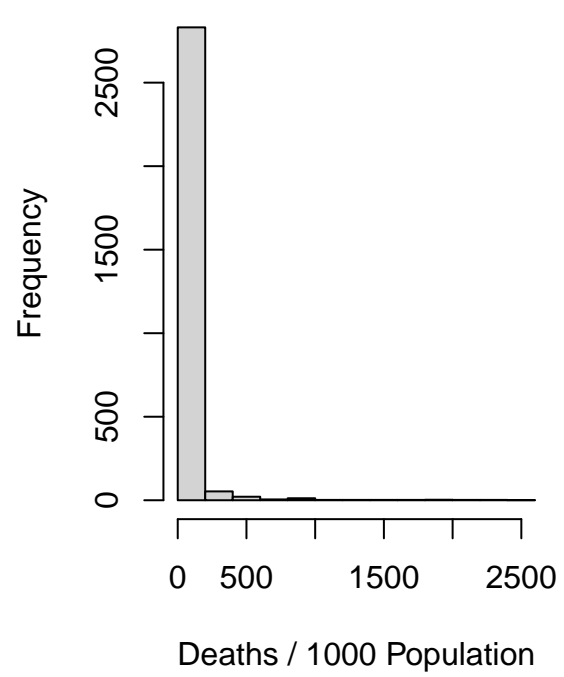
Histogram of Average BMI



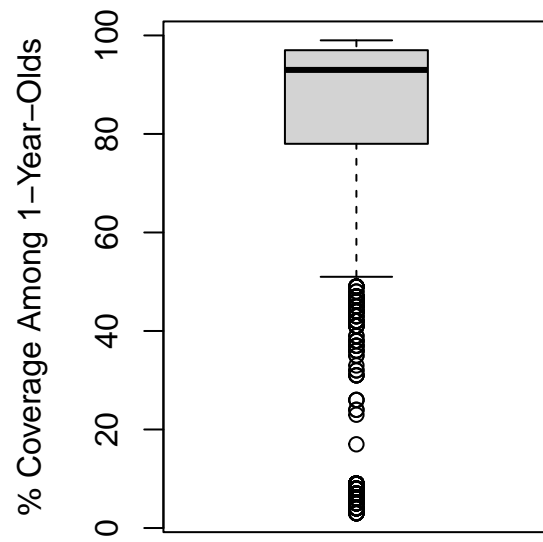
Under-Five Deaths



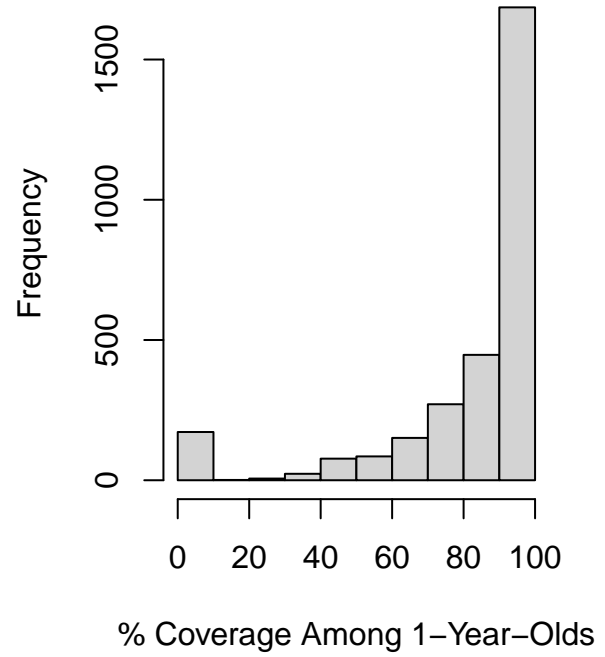
Histogram of Under-Five Deaths



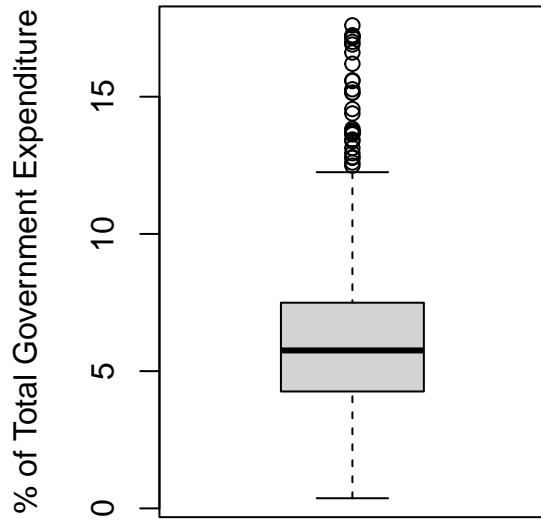
Polio (Pol3) Immunization



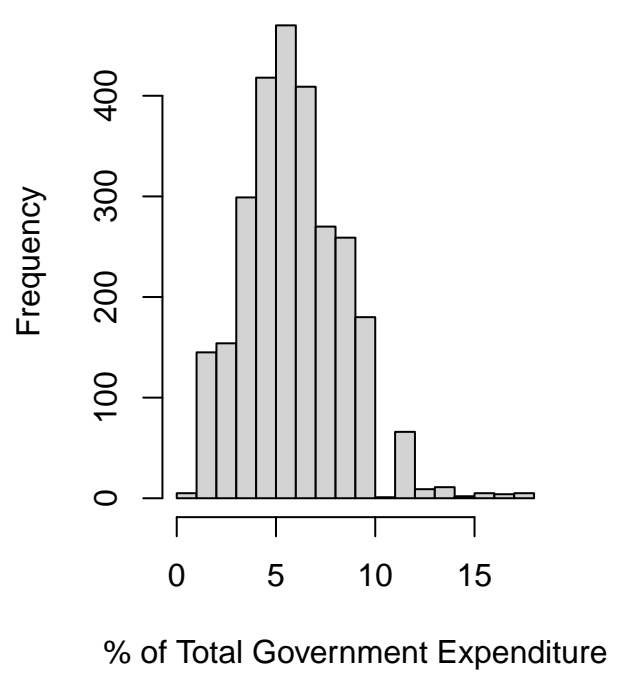
Histogram of Pol3 Immunization



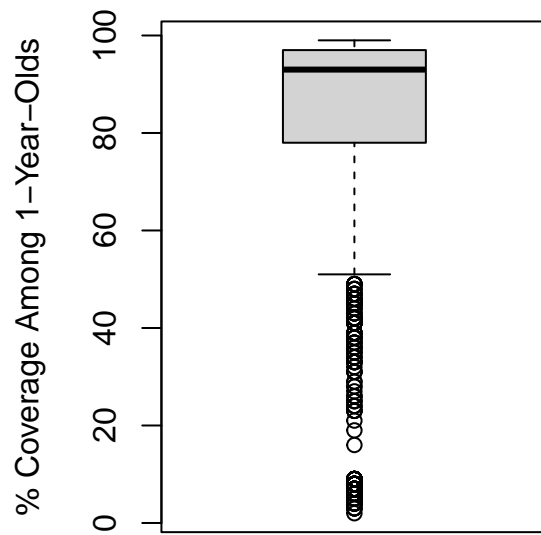
General Government Health Expenditure



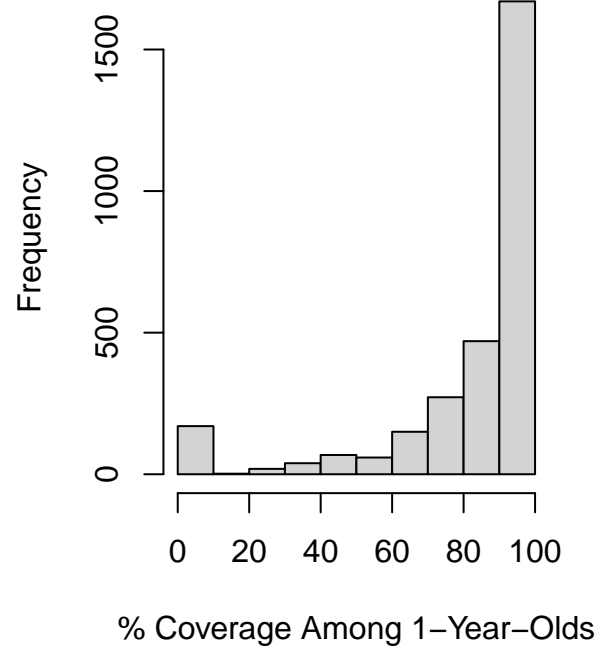
Histogram of General Government Health Expenditure



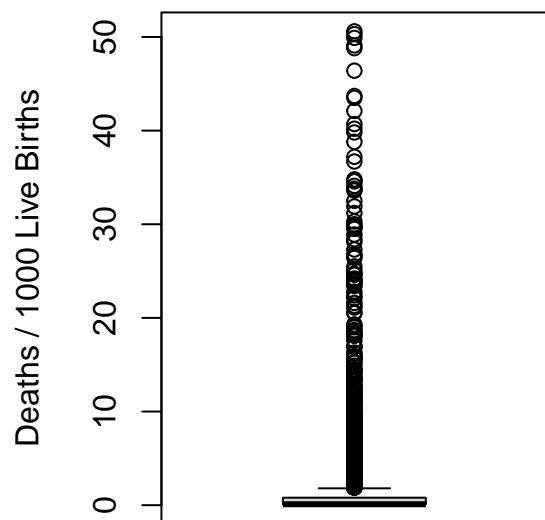
DTP3 Immunization



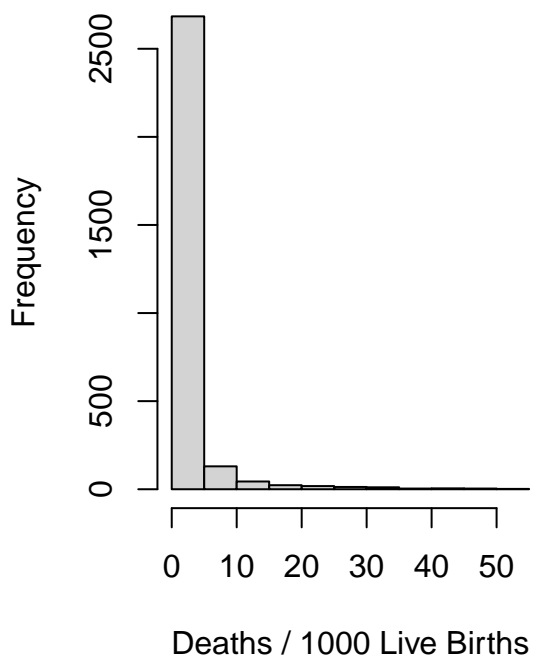
Histogram of DTP3 Immunization

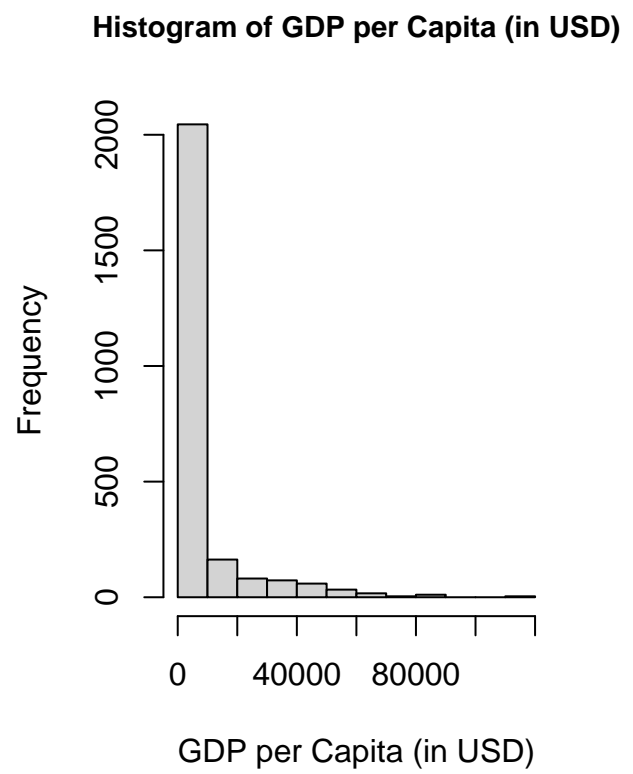
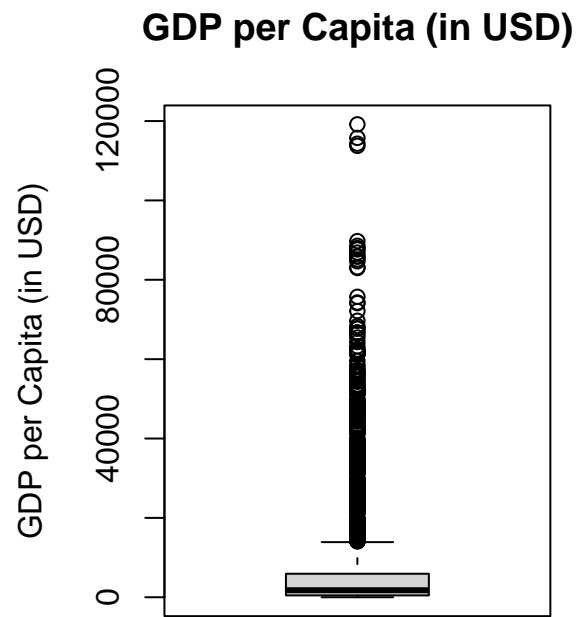


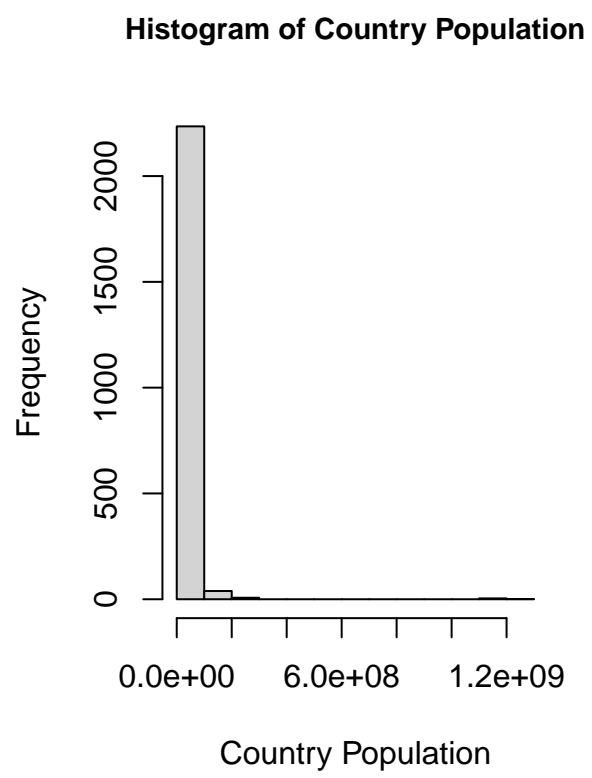
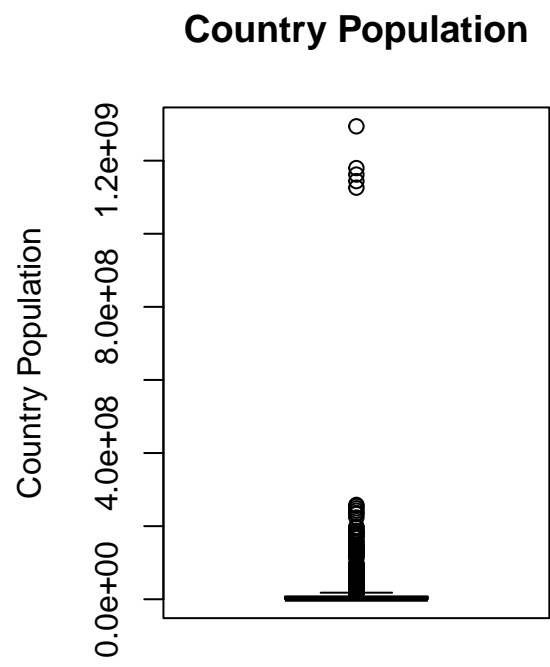
HIV/AIDS (0–4 Years)



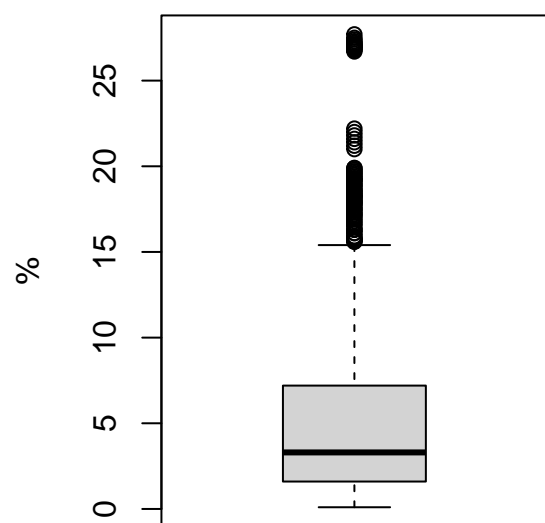
Histogram of HIV/AIDS (0–4 Years)



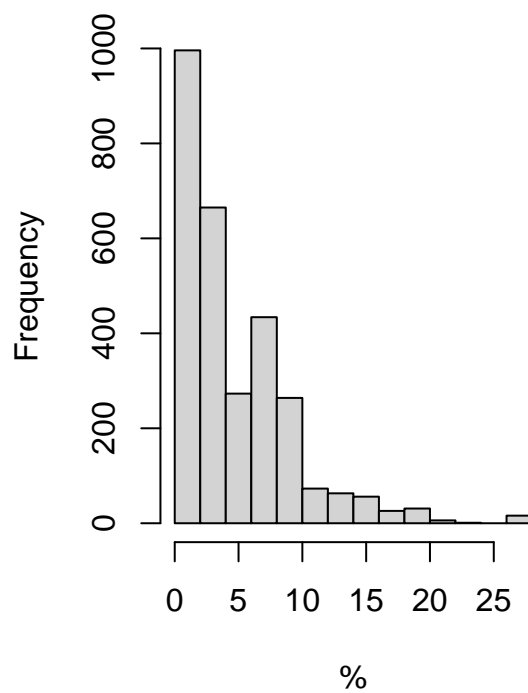




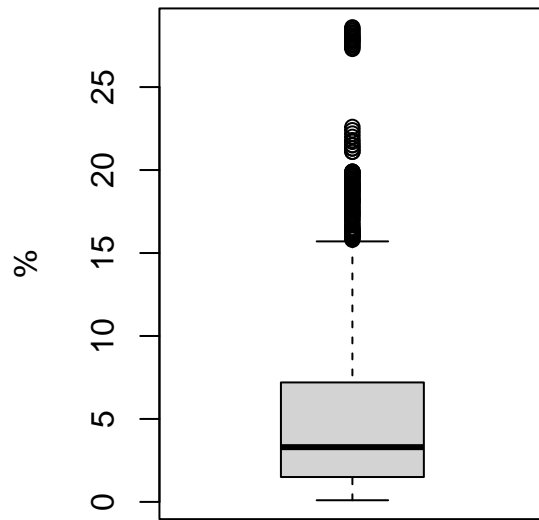
Prevalence of Thinness (10–19 Years)



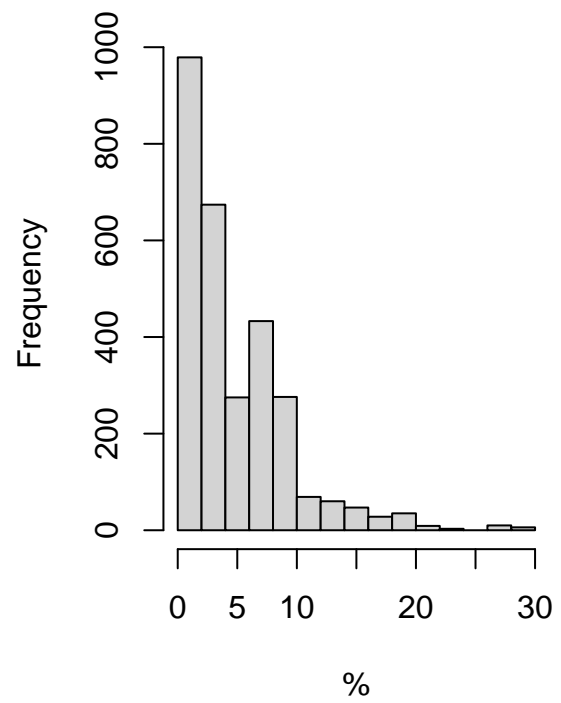
Histogram of Prevalence of Thinness (10–19 Years)

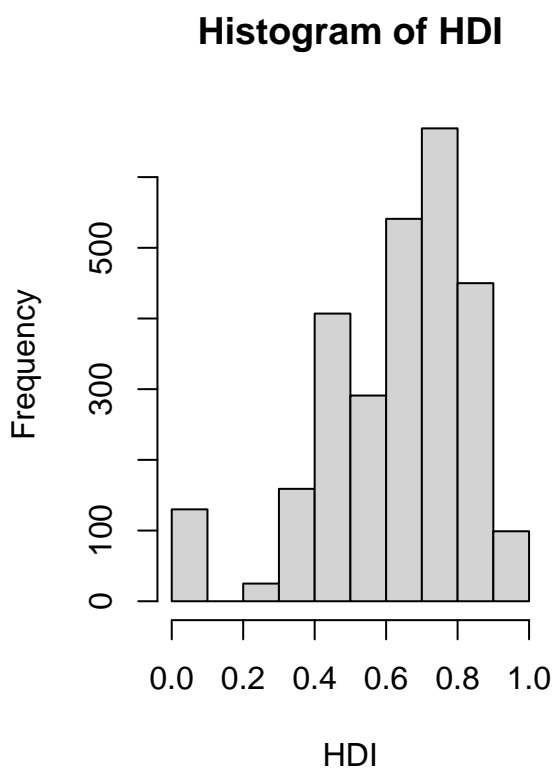
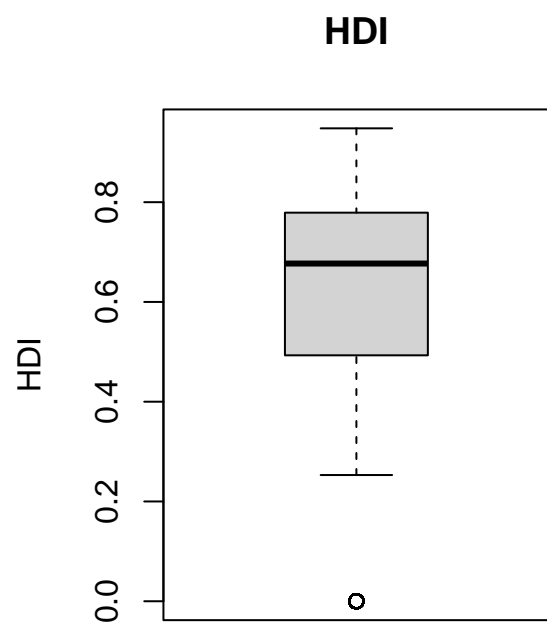


Prevalence of Thinness (5–9 Years)

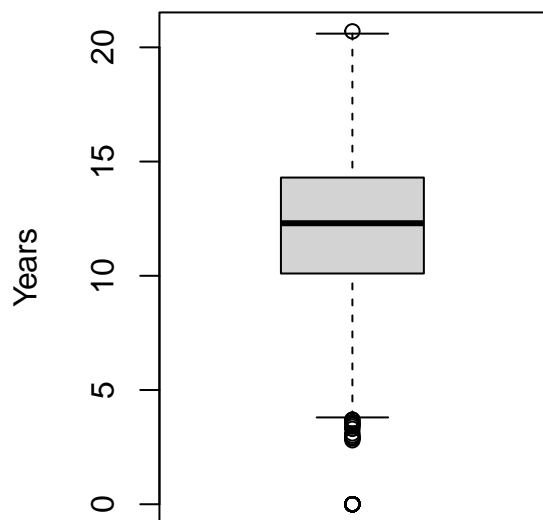


Histogram of Prevalence of Thinness (5–9 Years)





Schooling



Histogram of Schooling

