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You will implement BFS and DFS on a directed graph. First, you will write class `Graph`. In addition, you will implement some member functions that solve specific problems on a directed graph.

**Step 1.** Write `graph.h` and `graph.cpp` files where you will declare and define class `Graph`.

Class `Graph` will have a default constructor that will read input from the standard input (keyboard) using *cin*. The input will be given in this format:

```
N M
1 3
4 5
0 2
3 5
2 3
```

Where `N` is an integer, the total number of vertices (nodes) in a graph and `M` is an integer, the total number of edges in the graph.

Here are the data members of class `Graph`:

```
vector< vector<int> > Adj; //adjacency lists of the graph
vector< int > distance; //for BFS
vector<int> parents; //for BFS and DFS
vector<char> colors; //for DFS
vector<TimeStamp> stamps; //for DFS
int size; //total vertices
```

Your program will read input integer `N` and will resize `Adj` to size `N`. Then your program will read `M`, and will run *for* loop to read in `M` pairs (`u`, `v`) and will push `v` into `Adj[u]`. The default constructor also needs to resize the rest of vectors to size `N`. **This is important:** after the default constructor has been called, all vectors of the class must have size `N`.

You are given another class ***TimeStamp***, with the following declaration in ***timestamp.h*** file:

```
class TimeStamp{
public:
    TimeStamp(): d(0), f(0){};
    int d; //discovery time
    int f; //finish time
}
```

**Step 2.** Implement BFS and DFS and other member functions for class Graph.

Member function	Description	Test files
<code>void printGraph();</code>	This function prints the adjacency lists in this format u: v1 v2 v3 where u is the vertex whose Adjacency list is printed, and vertices v1, v2 and v3 are the vertices in the Adjacency list of u. There is a colon after u and then space after the colon, and space after each vertex in Adj[u], and then <b>endl</b>	t00
<code>void printNeighbors(int u);</code>	This function takes an integer <i>u</i> as a parameter, <i>u</i> is a vertex in the graph. The function prints neighbors of <i>u</i> (i.e. vertices <i>v</i> such that there is an edge from <i>u</i> to <i>v</i> in the graph) in the format: <vertex><space>...<vertex><space><endl>	t01
<code>bool isNeighbor(int u, int v);</code>	This function takes two vertices as parameters, <i>u</i> and <i>v</i> , and returns <i>true</i> if there is an edge from <i>u</i> to <i>v</i> in the graph.	t02
<code>void bfs(int s)</code>	This function implements BFS algorithm. The parameter <i>s</i> is the source, from which BFS starts running. It initializes <i>distance</i> array to INT_MAX (defined in <limits>, so you need to include <limits>) It initializes <i>parents[i]</i> to i. It uses <queue> of the standard library (include it). To use queue, just do: queue<int> aq; //aq is the name of the queue Uses pseudocode from lecture notes. bfs will print out a node as it pops the node from the queue. cout << node << " "; After queue is empty, then print out <b>endl</b>	t03
<code>void dfs()</code> <code>void dfsVisit(int u, int &amp;atime)</code>	This function implements DFS algorithm. dfs() initializes arrays <i>colors</i> , <i>parents</i> , <i>stamps</i> , and contains the main <i>for</i> loop, from which <i>dfsVisit</i> is called on each node whose color is White. Parameter <i>u</i> of <i>dfsVisit</i> is the current node, and parameter <i>atime</i> is the current time stamp used. DFS will print out a node inside dfsVisit before processing Adj[u]: cout << u << " "; After the main <i>for</i> loop, print out <b>endl</b>	t04
<code>void printPath(int v)</code>  <i>You may have a helper function in addition</i>	This function must be called after bfs is called, so that parents array has been calculated by the time printPath is called.	t05

	Parameter <i>v</i> is the node from which we start backtracking the path from the source <i>s</i> to <i>v</i> . Path is printed in the format: <node><space>...<node><space><endl>	
void printLevels(int s)	This function uses code of bfs, but modifies it slightly by using queue< pair<int, int> > where <i>first</i> in pair is a node, and <i>second</i> is the distance from the source to this node. Include <utility> to use C++ pair. When enqueueing a node into the queue, make a pair: pair<int, int>(node, dist) and push it into the queue. Nodes at the same levels will be in consecutive order inside the queue. You will need to maintain a variable, current level being printed, and when the next popped node from the queue has a different distance than the current level, then reset this variable to the new level, print out <b>endl</b> after the last level and only then print the node on the new line.	t06
bool isCycle() bool isCycleVisit(int u, int & atime)	This function uses code of <i>dfs</i> and <i>dfs_visit</i> , but it will modify this code. Whenever a node <i>v</i> in Adj[ <i>u</i> ] is found such that <i>v</i> is Grey, this means that <i>v</i> is an ancestor of <i>u</i> in the DFS-tree, and that there exists the path from <i>v</i> to <i>u</i> , and edge ( <i>u</i> , <i>v</i> ) concludes the cycle consisting of this path and edge ( <i>u</i> , <i>v</i> ). At this point (Grey vertex has been discovered), return <i>true</i> . Stop traversal after <i>true</i> has been returned. If the main <i>for</i> loop has been finished, and every time <i>isCycleVisit</i> has been called, it returned <i>false</i> , then return <i>false</i> . This function does not print anything, just returns <i>Boolean</i> .	t07-t10
Test t11 tests all the functions above		t11

**Submission:** Submit graph.h and graph.cpp on turnin to Assignment11.

**Grading:** If your program does not compile, you will receive 0 (no partial credit). Otherwise, grading will be done according to the table below:

Function	Tests	Points for these tests
printGraph	t00	0
printNeighbors	t01	0
isNeighbor	t02	0
Bfs	t03	10
Dfs	t04	10
printPath	t05	10
printLevels	t06	25
isCycle	t07-t10	25
All	t11	20