

Q2

d We can solve a linear system of equations $Ax = b$ using LU decomposition along with forward substitution (to solve for y) and backward substitution (to solve for x)

Step 1: Using the 'myLU' function, to compute the LU factorization of matrix A , we get 2 matrices which are L and U where L : Lower triangular, U : Upper triangular such that $A = LU$

$$[L, U] = \text{myLU}(A);$$

Step 2: Next we can utilise the 'fwdSubst' function to solve for y in $Ly = b$. [$Ux = b$. Substitute Ux as ' y ' [$Ux = y$]]

$$y = \text{fwdSubst}(L, b);$$

where L : Lower Triangular matrix
 b : right-hand side vector

Step 3: Now that we have y , we can solve for x in equation $Ux = y$ using backward substitution

We can use the 'backSubst' function to solve for x by performing backward substitution

$$x = \text{backSubst}(U, y)$$

where U : Upper triangular matrix

y : Solution vector obtained from forward substitution.

Step 4 After performing the above steps (Step 1-3) the variable ' x ' will contain the solution to the linear system $Ax = b$.