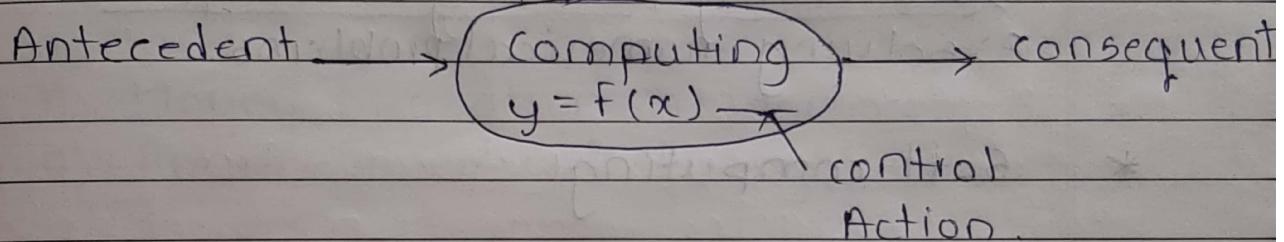


# chap 1. Fundamentals of soft computing

## \* soft computing

- concept of computation
- It is the use of Approximate calculations to provide Approximate but usable solutions to complex computational problems



$f$  = mapping function (maps input to O/P)  
or also called Algorithm.

## \* characteristics of computing

- 1) Should provide precise solution.
- 2) control action should unambiguous & accurate
- 3) Suitable for model problem, which is easy to model mathematically.
- 4) Should be Algorithm/ function available.

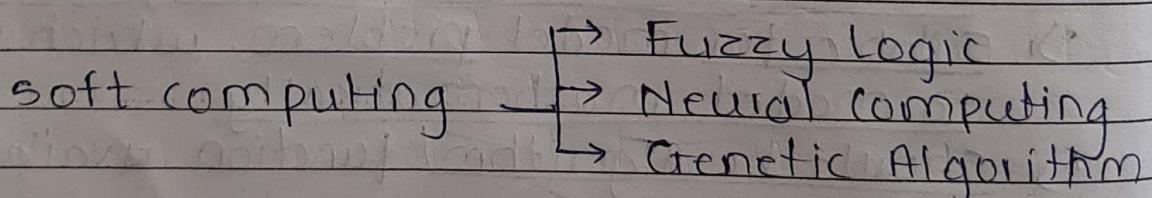
## \* Hard computing

- Introduced by Lotfizadeh.
- computing is hard if:-
  - a) Precise result is guaranteed,
  - b) control action is unambiguous,
  - c) control actions are defined by either in the form of some mathe. model or algo.
- Ex:-
  - 1) Searching , sorting techniques.
  - 2) Solving numerical problems.

## \* soft computing

- Introduced by Lotfizadeh.
- Soft computing is defined as:-

A collection of methodologies that aim to exploit the tolerance for imprecision & uncertainty to achieve tractability, robustness & low solution cost.



## \* characteristics of SC.

- 1) Does not require mathematical model.
- 2) May not yield the precise solution.
- 3) Algorithms are adaptive means it can adjust to the change of any dynamical situation.
- 4) Use some biological inspired methodology

Ex:-

- a) Handwritten Character Recognition (ANN)
- b) Money Allocation Problem
- c) Robot Movement (Fuzzy logic)

## \* Difference between HC & SC

HC	SC.
1) Requires precisely stated analytical model & it is computationally expensive	It is tolerance to imprecision, partial truth & approximation.
2) Based on Binary logic • crisp system, numerical analysis.	It is based on fuzzy logic, the neural net, evolutionary computation
3) Characteristics of precision & categoricity.	char. of approximation & dispositionality
4) It is deterministic	It is probabilistic.
5) Requires exact input data	can deal with ambiguous & noisy data.
6) Strictly sequential	can be carried out by parallel computing

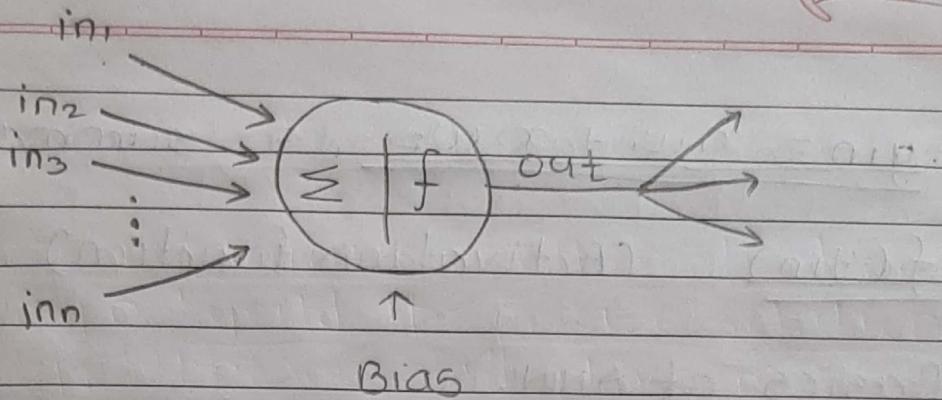
## \* (check Human Nervous System) slide = 18-21

### \* Neural Network.

- NN are computational models that mimic the complex function of the human brain.
- It consists of interconnected nodes or neurons that process & learn from data, enabling tasks such as pattern recognition & decision making in machine learning.
- Applications:-
  - a) As powerful problem solvers :- character recognition, object detection

### \* Artificial NN

- 1) ANN is a machine learning approach inspired by the way in which the brain performs a particular learning task.
- 2) ANN possesses a large no. of processing elements called nodes/neurons which operate in parallel.
- 3) Neurons are connected with each others by connection link.
- 4) Each link is associated with weights which contain information about input signal.
- 5) Each neuron has its own function of the inputs that neuron receives (Activation function) or has its own state.

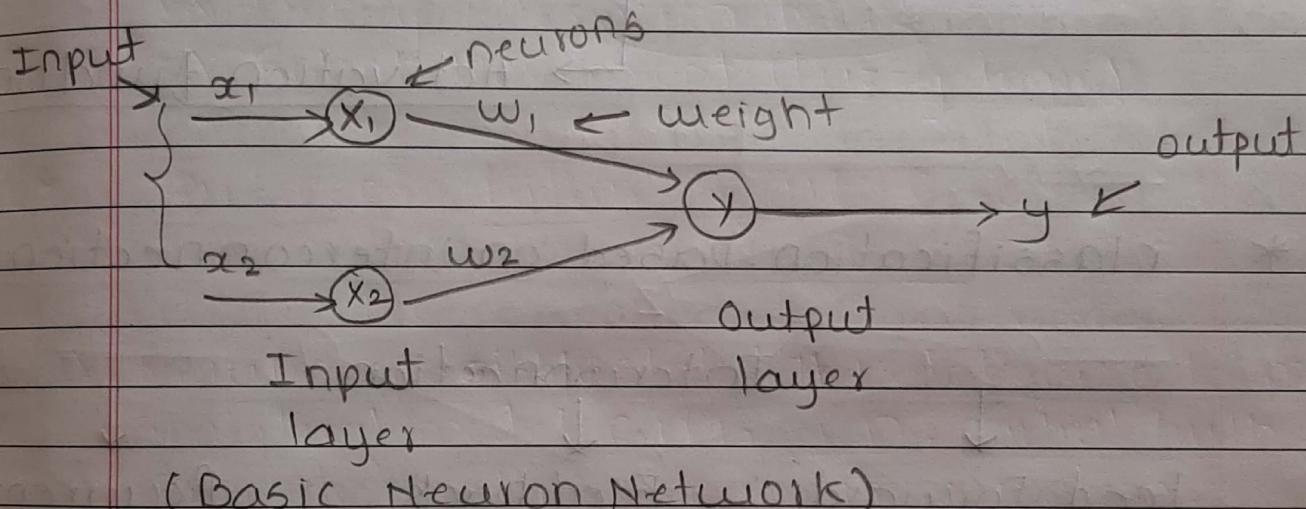


$\rightarrow$  Ex: human being

(c) Application:-

spam classification, Face Recognition, pattern recognition through a learning process.

(ANN - only one problem at a time)



(Basic Neuron Network)

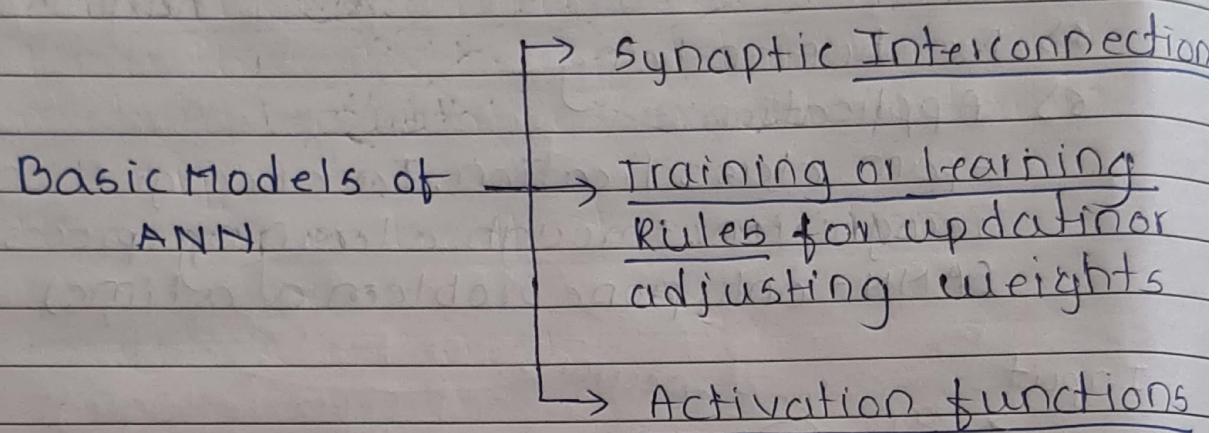
- Here links have weights which are random weights initially.
- Each neuron perform some summation & apply Activation function on summation.  
(summation = (product of input & weight's sum)  
i.e sum of product of IIP & weights)

\* slide (28-29) charac & App' of NN.

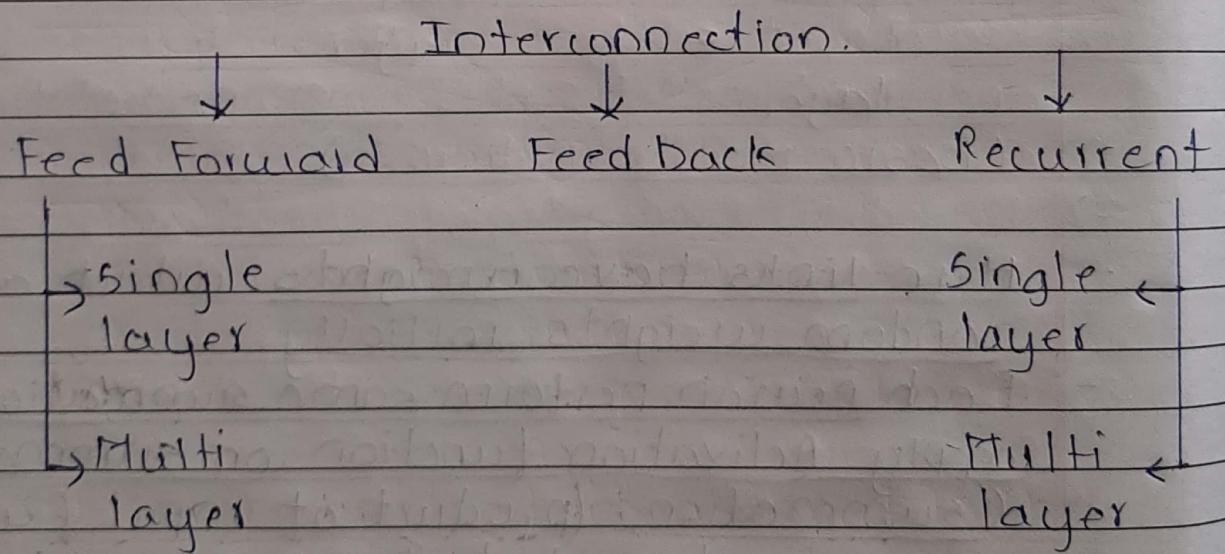
$$y_{in} = \underline{x_1 w_1 + x_2 w_2} = \text{summation}$$

$$y = f(y_{in}) \quad (\text{Activation function})$$

### \* Basics of ANN.

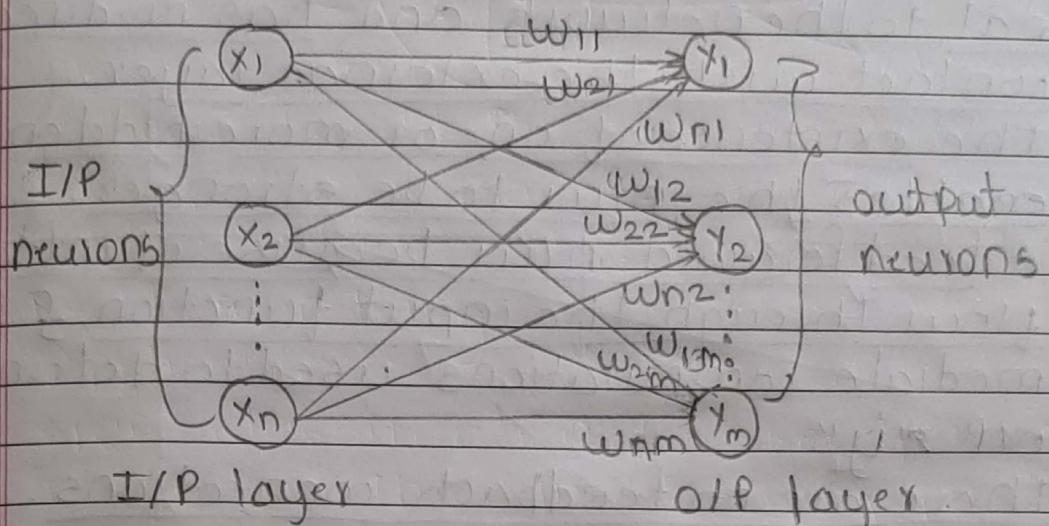


### \* Classification based on interconnection.



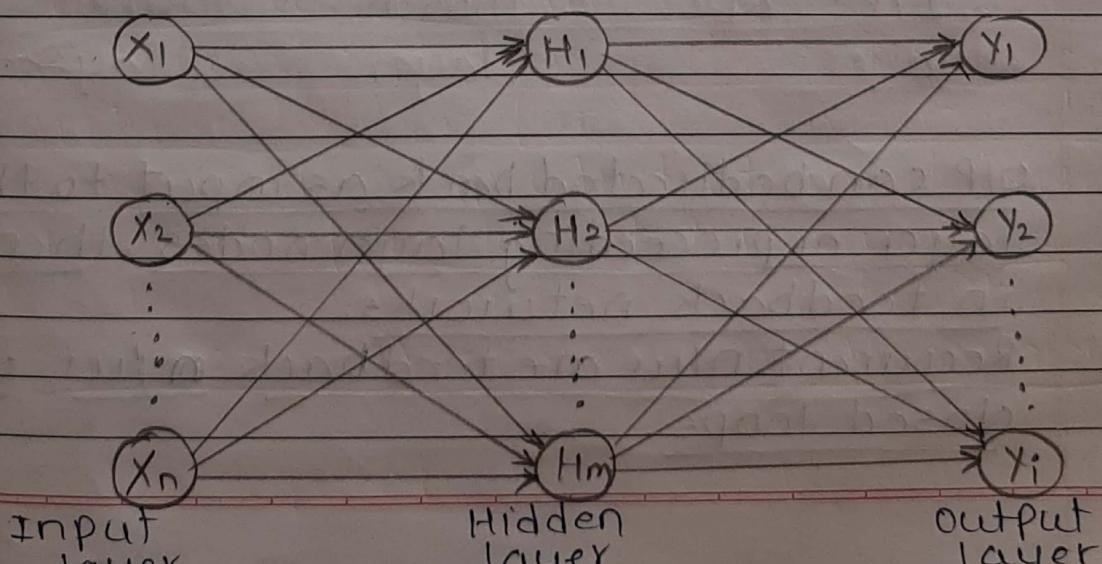
## A) Connections

### 1) Single Layer Feed Forward.



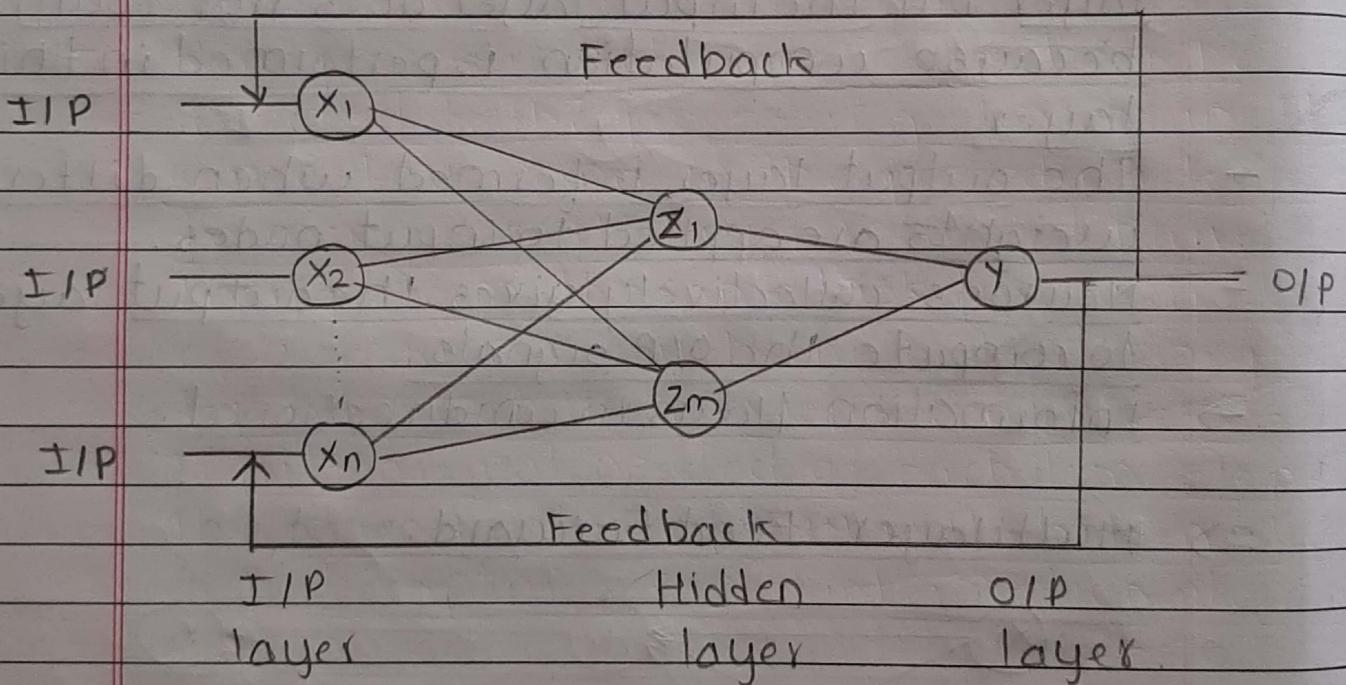
- Only two layers, input layer and output layer but the input layer does not count. because computation is performed in this layer.
- The output layer is formed when different weights are applied to input nodes.
- Neurons collectively gives the output layer to compute the O/P signals.
- Information flows in unidirectional.

### 2) Multilayer Feed Forward.



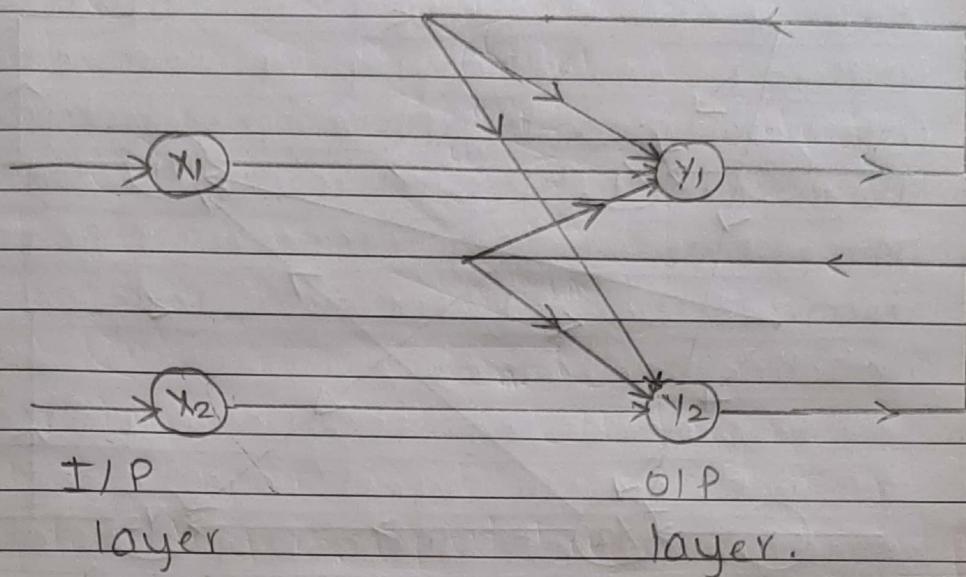
- this layer has a hidden layer that is internal to the network and has no direct contact with the external layer.
- the existence of one or more hidden layer enables the nnu to be stronger.
- A feed forward nnu because of information flow through the input function, & intermediate computations used to determine OIP  $\pi(y)$
- there are no feedback connections.

### 3) Feedback Network



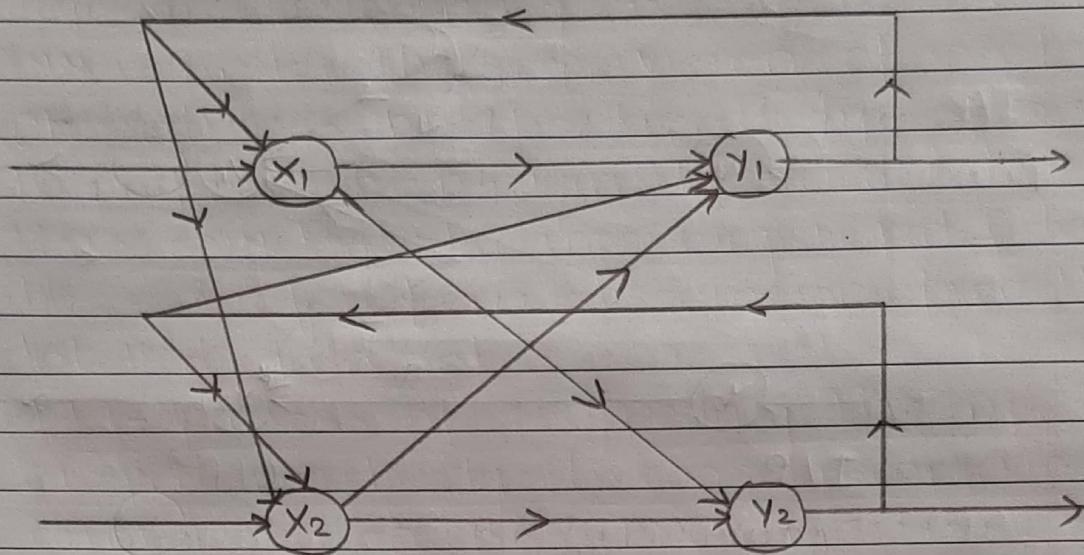
- OIP can be directed back as input to the same layer or preceding layer nodes, then it results in feedback networks.
- Recurrent nnu are feedback nnu with closed loops.

## 4) Recurrent Network (single layer)



- Feedback netw with closed loop are called Recurrent N/W
- Here the processing element's o/p can be directed back to itself or to another processing element or both.
- A recurrent neural n/w is a class of ANN where connection bet<sup>n</sup> nodes form a directed graph along a sequence.
- Allows it to exhibit dynamic temporal behaviour for a time sequence.

## 5) Multilayer Recurrent Network.



- Here processing element output can be directed to the processing element in the same layer and in the preceding layer forming a multilayer recurrent net.
- They perform the same task for every element of a sequence, with the output being dependent on the previous computations.
- Inputs are not needed at each time step
- The main feature of RNN is its hidden state, which captures some information about a sequence.

## \*> Learning Rules.

- The main property of an ANN is its capability to learn
- Learning or training is a process by means of which a neural network adapts itself to a stimulus by making proper parameter adjustments, resulting in desired response.

### \* Types:-

#### 1) Parameter Learning:-

- It updates the connecting weights in a neural net.

Ex Gradient decent, Back Propagation algorithm.

#### 2) Structure learning:-

- It focuses on change in nnu structure (includes the no. of processing elements (neurons) as well as their connection types)

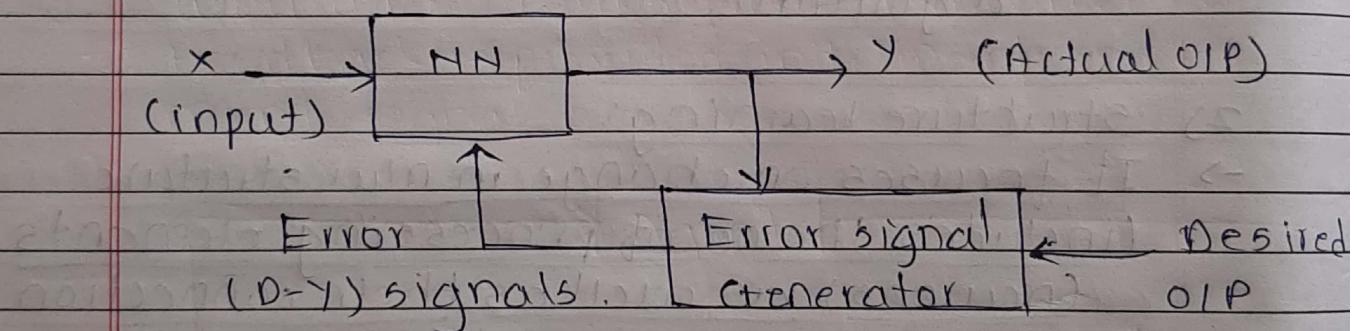
### \* Training (Parameter Learning)

The process of modifying the weights in the connections bet" nnu layers with objective of achieving the expected output is called training a network.

## \* Types (supervised, unsupervised, Reinforcement)

### 1) supervised learning

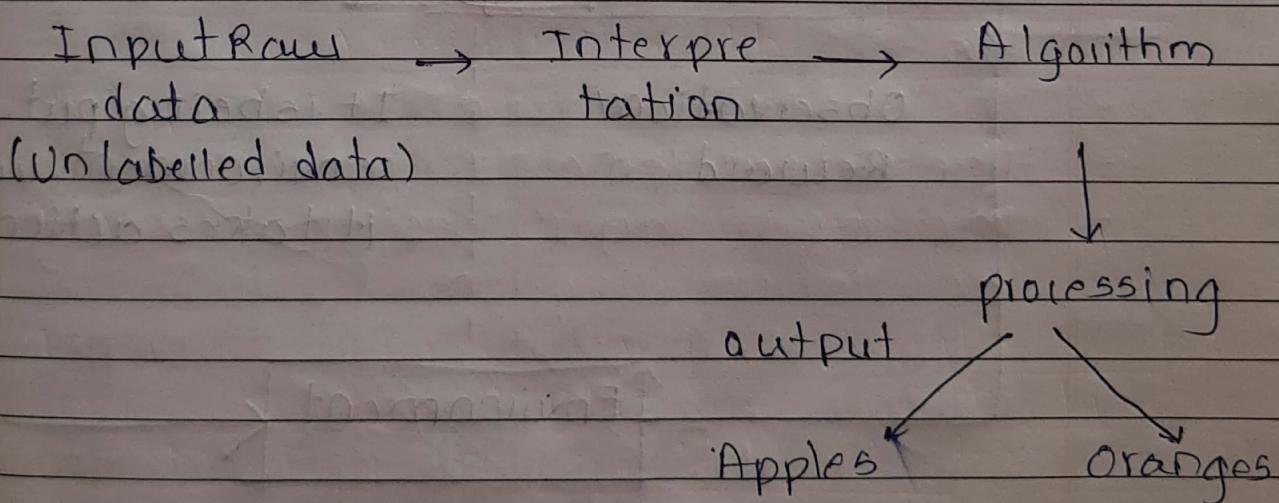
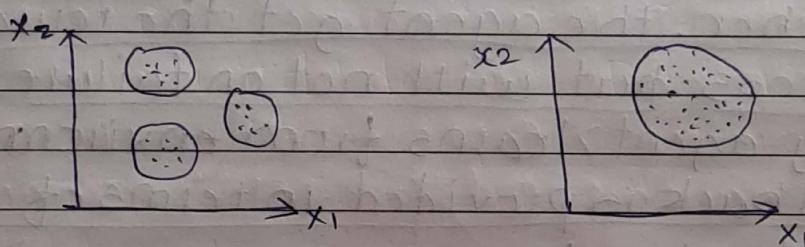
- ANN is under the supervision of an educator who utilizes his/her knowledge of system to prepare the NW with labeled data sets.
- Thus ANN learn by receiving input & target the set of a few observations from the labelled data set.
- It is process of comparing the input & output with objective and computing the error between the OIP & objective.
- It is used to solve classification and regression problems
- Training pair = [input vector, target vector]



### 2) Unsupervised Learning

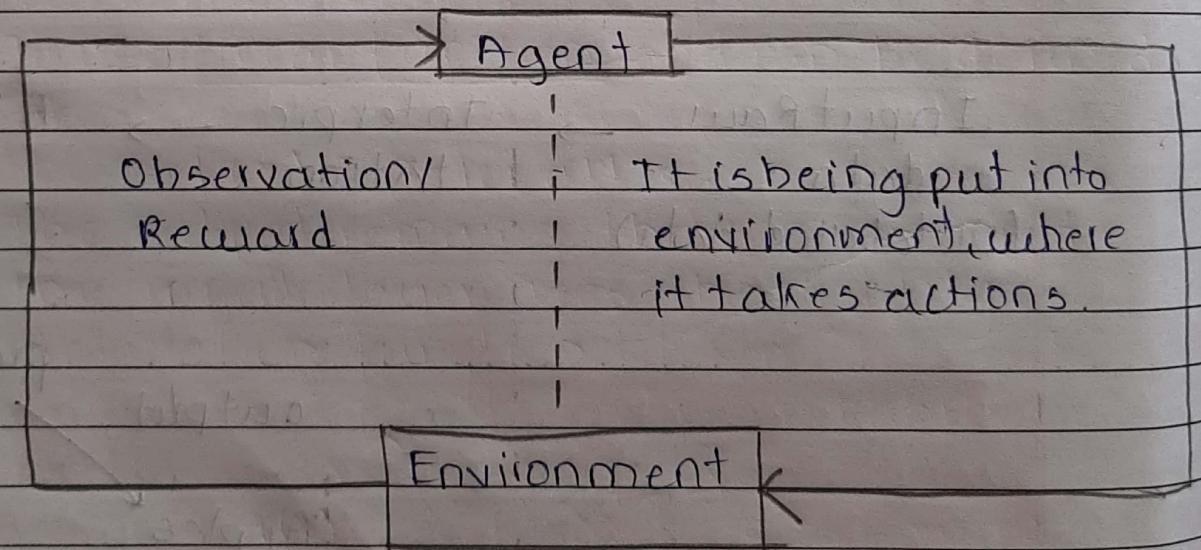
- This algorithm is completely opposite to supervised learning. In short there is no complete and clean labelled dataset in unsupervised learning.
- Unsupervised learning is self-organized learning. NW must discover patterns, regularities, features for input data over the output.

- Its main aim to explore the underlying patterns and predicts the output.
- We basically provide the machine with the data and ask it to look for hidden features and cluster the data in a way that make sense.
- Example:-
  - a) kmeans clustering
  - b) Neural Network
- All similar input patterns are grouped together as clusters (clustering). If a matching input pattern is not found a new cluster is formed.



### 3) Reinforcement Learning

- It is neither based on supervised or unsupervised learning.
- Moreover, here the algorithms learn to react to an environment on their own.
- It is rapidly growing and moreover producing a variety of learning algorithm
- these algorithms are useful in the field of Robotics, Gaming, etc.
- In R&E learning problem an agent tries to manipulate the environment.
- the agent travels from one state to another, the agent get the reward on success but will not on failure. In this way agent learns from environment.
- Feedback is provided in terms of reinforcement signals.



## Criteria

### Supervised

### Unsupervised Reinforcement

## \* Comparison table

### 1) Definition

Learns by using Trained using works on interacting with labelled data. unlabelled data. without any guidance the environment.

### 2) Type of data

Labelled data

Unlabelled data

### 3) Type of problem.

Regression and classification.

Association & clustering.

### 4) Algorithm

1) Linear Regression  
2) Non Linear  
3) SVM, KNN

1) Q-Learning  
2) SARSA.  
3) Neural NW

### 5) Aim

calculate outcomes

Discover patterns.

### 6) Application

Risk evaluation. Forecast sales.

Self driving cars, Gaming, Anomaly Detection.

### 7) Supervision

Extra supervision

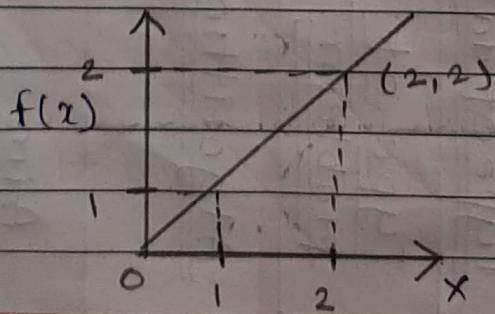
No supervision.

## \* Activation function

- The Activation function determines whether or not to stimulate a neuron by generating a weighted sum and then adding bias to it.
- In order to add non-linearity to a neuron's output, the activation function was created.
- It is used to determine the NN's OIP such as yes or no.
- The obtained values are mapped between  ~~$\pm \frac{1}{2}$ ,  $\pm \frac{1}{4}$~~  0 and 1 or -1 and 1, etc.  
(In short:- A.F. decides neuron should be activated or not)  
if value  $> 0$  (threshold) = Active  
value  $< 0$  (threshold) = Inactive

### 1) Identity function :-

- It is a linear function and can be defined as -
- $f(x) = x$  for all  $x$ .
- The output remains the same as input.
- the input layer uses the identity activation function.

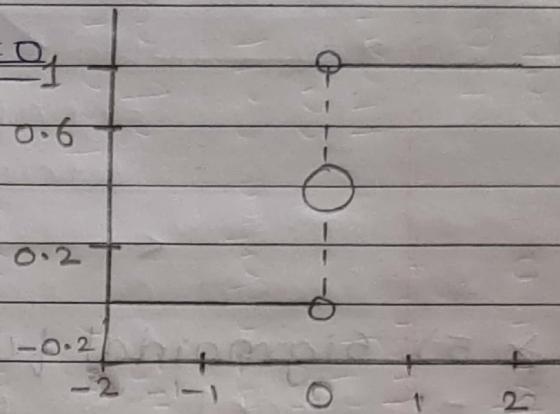


## 2) Binary step function.

- Binary step function depends on a threshold value that decides whether a neuron should be activated or not.
- If neuron is deactivated means its output is not passed onto the next hidden layer.

Binary step:- here  $\theta = 0$ ,

$$f(x) = \begin{cases} 0 & \text{for } x < 0 \\ 1 & \text{for } x \geq 0 \end{cases}$$

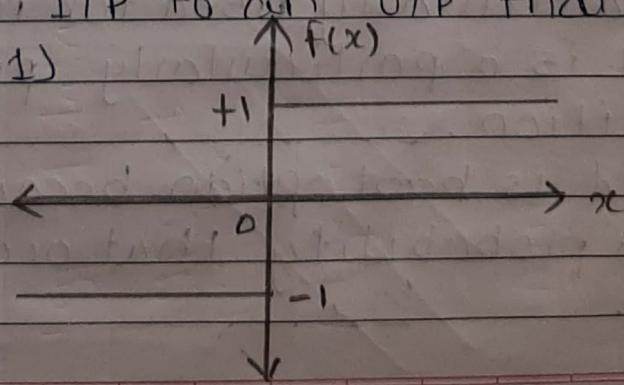


- But it cannot provide multivalue outputs

## 3) Bipolar step function:-

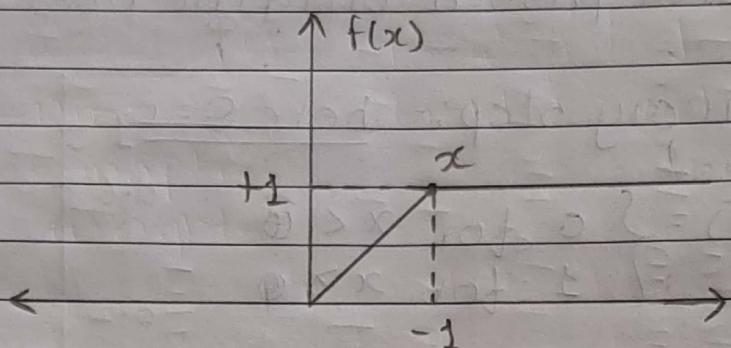
$$f(x) = \begin{cases} 1 & \text{if } x \geq 0 \\ -1 & \text{if } x < 0 \end{cases}$$

- $\theta$  (threshold value)
- This function is also used in single layer nets to convert the net, I/P to an O/P that is bipolar (-1 or 1)



#### 4) The Ramp function:-

$$f(x) = \begin{cases} 1 & \text{if } x > 1 \\ x & \text{if } 0 \leq x \leq 1 \\ 0 & \text{if } x < 0 \end{cases}$$

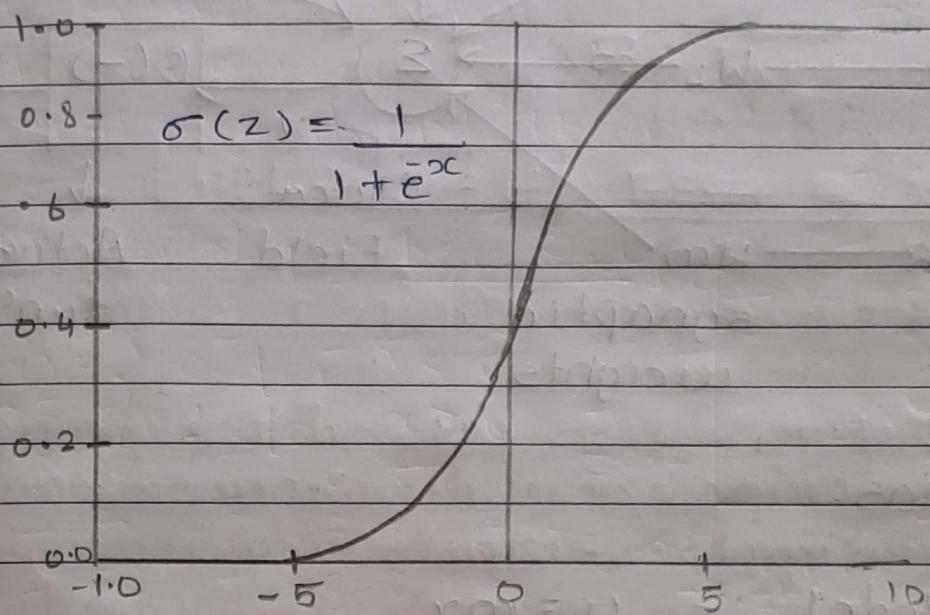


#### \* 5) Sigmoidal function:-

- Widely used in back-propagation nets because of the relationship between the value of the functions at a point & the value of the derivative at that point which reduces the computational burden during training.
  
- The sigmoid function curve has a s-shaped appearance. We employ the sigmoid function primarily because it occurs between (0 & 1).
- It is particularly used for models whose output is a particularly probabilistic prediction.
- Sigmoid is best option because anything has a probability that occurs betw 0 to 1

$$f(x) = \frac{1}{1+e^{-x}}$$

$x$  = summation term



#### \* Types

- 1) Binary sigmoid.
- 2) Bipolar sigmoid.

#### \* The neuron:-

- It is basic information processing unit of a NN
- Acti fun' ( $\Theta$ ) for limiting the amplitude of O/P (of the neuron).

$$y = \Theta(u+b)$$

- Adder funn :- computes weighted sum of I/P

$$u = \sum_{j=1}^m w_j x_j$$

By changing algo to  $y = mx + c$ , model can find a line which fits the given data.

Here constant "c" is a bias.

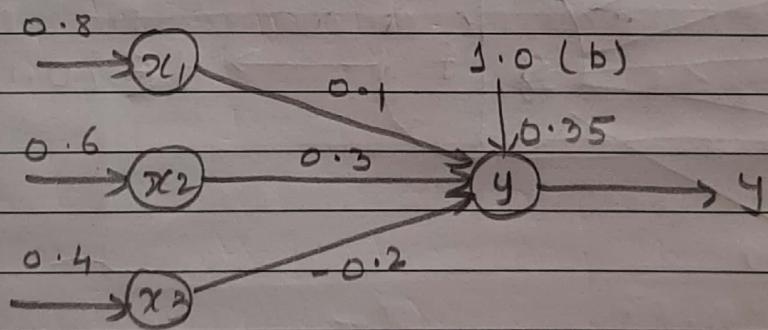
- Bias is a constant which helps the model in a way that it can fit best for the given data.
- In short, it gives freedom to perform best.

#### \* Types

- 1) Positive bias: - increase the net I/P
- 2) Negative bias: - decrease the net I/P  
(check slide:- 63-65)

#### \* Imp (Diff :- Brain & ANN)

#### \* Example of sigmoid function.



$$\sigma = y = f(y_{in}) = \frac{1}{1+e^{-y_{in}}} \quad \text{or} \quad y = f(x) = \frac{1}{1+e^{-x}}$$

$$z = y_{in} = b + \sum_{i=1}^n x_i w_i$$

$$= b + x_1 w_1 + x_2 w_2 + x_3 w_3$$

$$= \cancel{b} + 0.08 + 0.18 - 0.08 + 0.35$$

$$y_{in} = 0.53$$

$$y_i = \frac{1}{1 + e^{-x_i}}$$

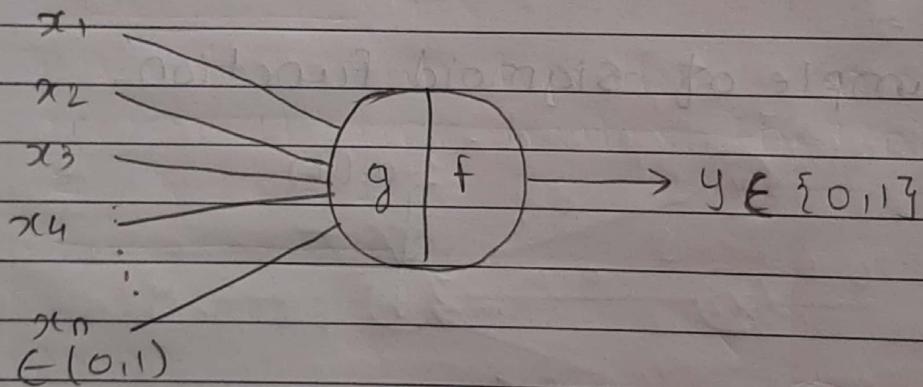
$$x_i = 0.53$$

$$= \frac{1}{1 + e^{-(0.53)}}$$

$$\underline{y = 0.6697} \quad | \quad y = 0.6294$$

### \* McCulloch-Pitts Neuron Model.

- McCulloch-Pitts proposed highly simplified computational Model of neuron (1943)
- g aggregates: inputs
- f: takes a decision based on aggregation.



- The inputs can be excitatory or inhibitory
- $y=0$  if any  $x_i$  is inhibitory.

$$g(x_1, x_2, \dots, x_n) = \boxed{g(x) = \sum_{i=1}^n x_i}$$

$$y = f(g(x)) = 1$$

$$z = f(g(x)) - 1 = 0$$

If  $g(x) \geq 0$  (Fires)

If  $g(x) < 0$  (Does not fire)

## 1) AND Gate.

0	1	O/P
0	0	0 $0 * 0 = 0$
0	1	0 $0 * 1 = 0$
1	0	0 $1 * 0 = 0$
1	1	1 $1 + 1 = \underline{2} \Rightarrow$

→ Here  $\theta = 2$  (take value 1st i.e. minimum) from O/P here it is 1, then the sum is 2  
Hence  $\theta = 2$

## 2) OR Gate.

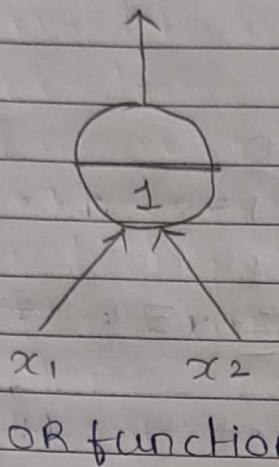
O/P	O/P
0	0 $0 + 0 = 0$
0	1 $0 + 1 = 1 \Rightarrow$ mini O/P (1st)
1	0 $1 + 0 = 1$
1	1 $1 + 1 = 2$

$$\theta = 1$$

3) NOR function:-  $\theta = 0$ 4) NOT function:-  $\theta = 0$

1) OR

$$\Rightarrow y \in \{0, 1\}$$



$$x_1 + x_2 = \sum_{i=1}^2 x_i \geq 1$$

$$(1, 1)$$

$$x_1 + x_2 = 0 = 1$$

$$(1, 0)$$

$$(0, 1)$$

$$(0, 0)$$

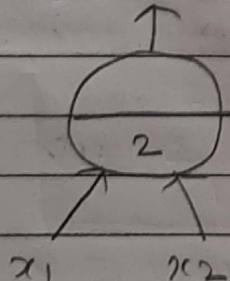
$$x_1$$

$$x_2$$

- Single MP neuron splits the IIP points (4 points for 2 binary inputs) into two halves.
- All inputs which produce an output 0 will be on one side (below the line) i.e  $\sum_{i=1}^2 x_i \leq 0 = 0$
- All inputs which produces an OIP 1 will lie on the line or above the line i.e  $\sum_{i=1}^2 x_i \geq 0 = 1$

2) AND

$$y \in \{0, 1\}$$



$$x_1 + x_2 = \sum_{i=1}^2 x_i \geq 2$$

$$(1, 0)$$

$$(0, 1)$$

$$(1, 1)$$

$$x_2$$

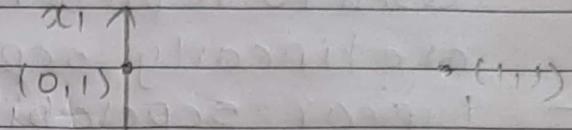
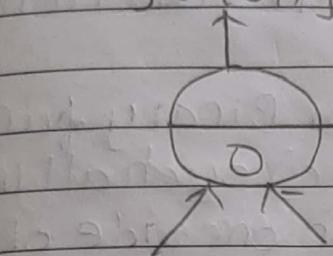
$$(0, 1)$$

$$(0, 0)$$

$$x_1$$

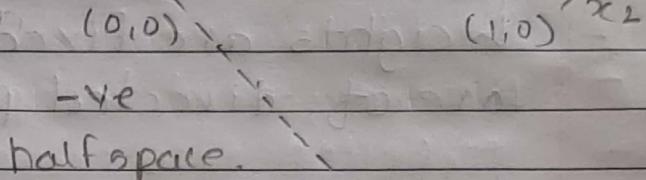
3) Tautology

$$y \in \{0, 1\}$$



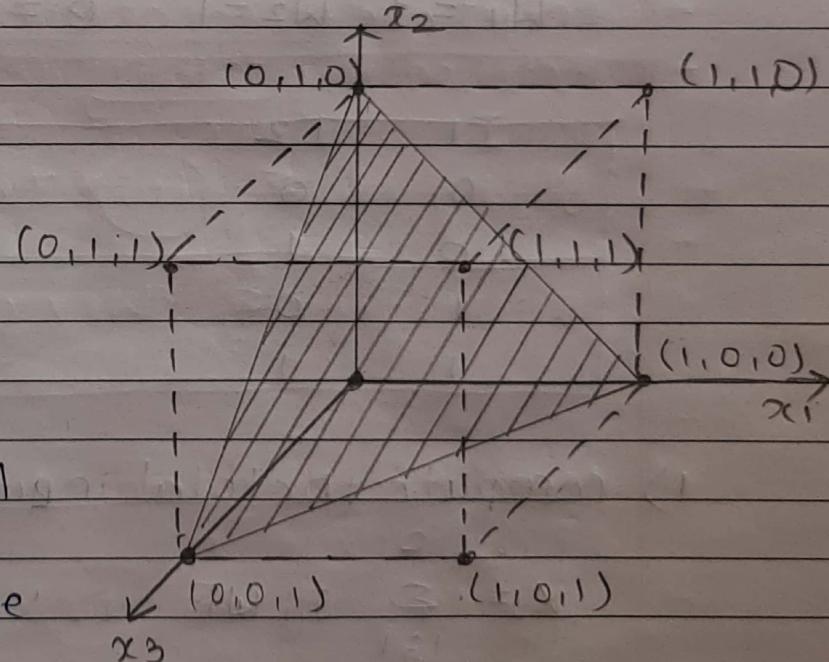
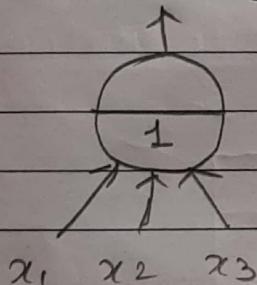
+ve halfspace

$$x_1 + x_2 = \sum_{i=1}^2 x_i \geq 0$$



\* For 2 points (Neurons)

$$y \in \{0, 1\}$$



OR function

only (0, 0, 0) will not produce 1  
hence it will be hidden

$$x_1 + x_2 + x_3 = 0 = 1$$

- A single McCulloch Pitts Neuron can be used to represent boolean functions which are linearly separable.
- Linear separability (For Binary functions)
  - There exist a line(plane) such all inputs which produce a "1" lie on one side of plane & all input produces "0" lie on other side of plane.
- Weights are fixed of neurons which are of directed path.

(Check slide : 70 to 74) Bird's example.

### \* Example

$$w_1 = 1 \quad w_2 = 1 \quad \theta = 0$$

I <sub>1</sub>	I <sub>2</sub>
0	0
0	1
1	0
1	1

1) compute the total input weighted

$$x = \sum_{i=1}^2 I_i w_i$$

$$\begin{aligned} x &= I_1 w_1 + I_2 w_2 + \cancel{\theta} \\ &= I_1 + I_2 \\ &= 1 + 1 \\ x &= 2 \end{aligned}$$

2) calculate the OIP using logistic sigmoid activation function.

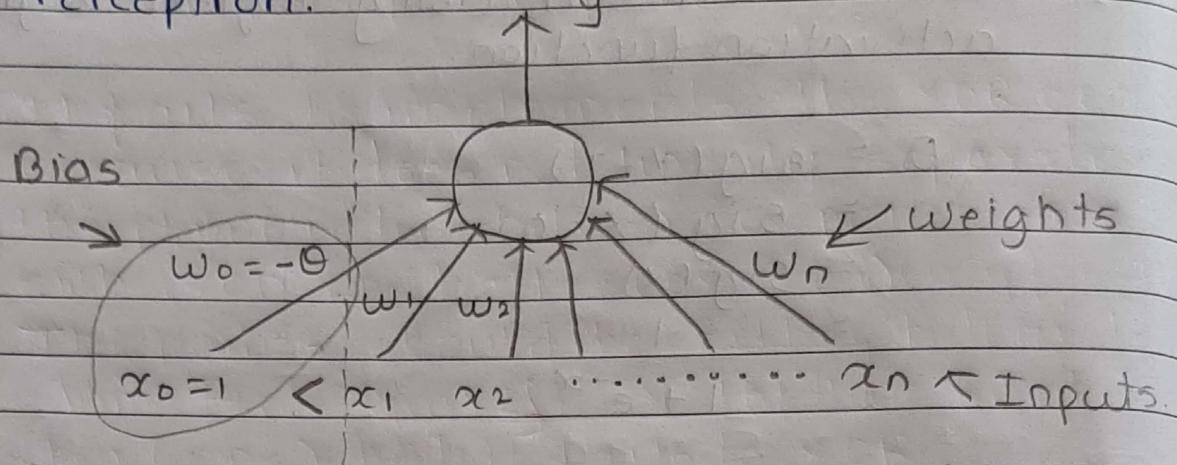
$$\begin{aligned}O &= \text{sig}(x - T) \\&= \text{sig}(x - 0) \\&= \text{sig}(x) \\&= \frac{1}{1 + e^{-x}}\end{aligned}$$

let  $T_1 = 0, T_2 = 0, x = 0$

$$\begin{aligned}O &= \text{sig}(x - T) \\&= \frac{1}{1 + e^{-(0)}} \\&= \frac{1}{1 + 1} \\&= \frac{1}{2}\end{aligned}$$

$$O = 0.5$$

## \* Perception.



- A more general computational model than McCulloch Pitts neuron.
- (Imp) Introduction of numerical weights for inputs and mechanism for learning weights.
- Includes learning algorithm includes theta and weights.
- Input are no longer limited to boolean values.
- Refined by Minsky

$$\boxed{\begin{aligned} y &= 1 \quad \text{if } \sum_{i=1}^n w_i x_i \geq 0 \\ y &= 0 \quad \text{if } \sum_{i=1}^n w_i x_i < 0 \end{aligned}}$$

## \* More Accepted convention.

$$\boxed{y = 1 \quad \text{if } \sum_{i=0}^n w_i x_i \geq 0} \quad \text{(fires if condition true)}$$

where  $x_0 = 1$ ,  $\theta = w_0 = -\theta$

~~Imp~~ Note:  $w_0$  is also called as Bias as it represents the prior.

\* Example

$$(w_0 = \text{bias}) = -\Theta$$

$x_1$	$x_2$	OR	$w_0 + \sum_{i=1}^2 w_i x_i \leq 0$
0	0	0	$w_0 + \sum_{i=1}^2 w_i x_i < 0$
0	1	1	$w_0 + w_1 > 0$
1	0	1	$w_0 + w_2 > 0$
1	1	1	$w_0 + w_1 + w_2 > 0$

$$w_0 + w_1 \cdot 0 + w_2 \cdot 0 = w_0 < 0$$

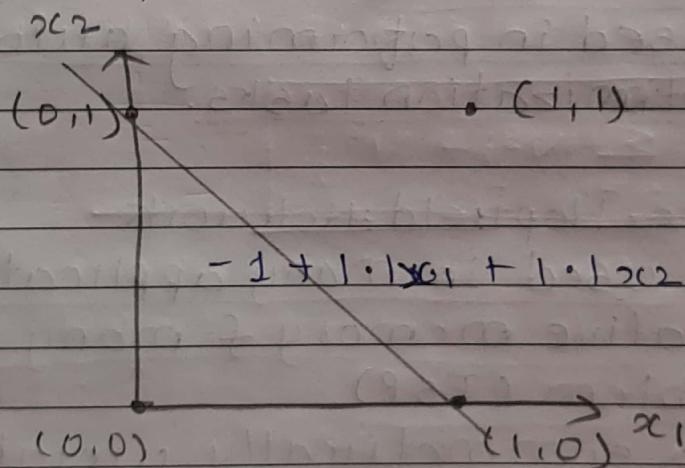
$$w_0 + w_1 \cdot 0 + w_2 \cdot 1 = w_2 > -w_0$$

$$w_0 + w_1 \cdot 1 + w_2 \cdot 0 = w_1 > -w_0$$

$$w_0 + w_1 \cdot 1 + w_2 \cdot 1 = w_1 + w_2 > -w_0$$

→ One of possible solution.

$$w_0 = -1, w_1 = 1 \cdot 1, w_2 = 1 \cdot 1$$



**IMP**

## \* Limitation of Perception model

- It fails to implements the XOR or XNOR because it does not linearly separate the plain (in two halves) i.e. points are either on one half & (ex of i).
- The points should be either below the line (for zero) & on the line or above for (one) but it fails to XOR.

## \* Hopfield Neural Network.

- Invented by Dr. John J. Hopfield.
- Consist of one layer of 'n' fully connected recurrent neurons
- It is used in performing auto-association and optimization tasks.

## \* Discrete Hopfield Network

- Can be used in many application of associative memory & many optimization of problem (TSP)
- It is a symmetrically weighted NW i.e. the value of (suppose)  $w_{12}$  is 2 then value of  $w_{21}$  is also 2
- Stores pattern in the form of weight, forms the O/P in which external pattern is provided
- Restores incomplete pattern.

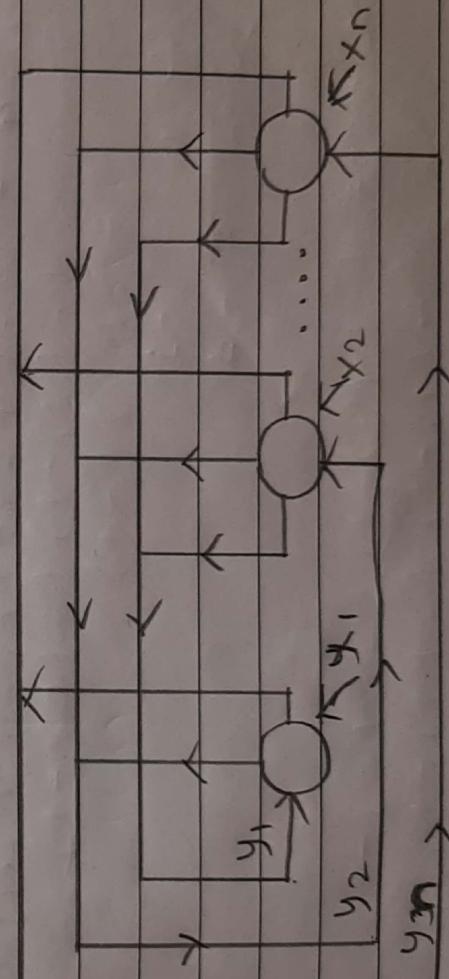
- Discrete Hopfield NN where each unit is connected to every other unit.
- It behaves in a discrete manner (fixed values) i.e. it gives finite distinct OIP generally of 2 types:
  - 1) Dinary (0,1)
  - 2) Bipolar (-1,1)

The NN has symmetrical weights with no-self-connections.

$$W_{ij} = W_{ji} \quad [W_{ii} = 0]$$

#### \* Structure & Architecture

- Each neuron has an incoming & non-inverting OIP
- Being fully connected, the OIP of each neuron is connected to all other neurons but not the self.



$x_1, x_2, \dots, x_n \rightarrow$  IIP to the given neurons  
 $y_1, y_2, \dots, y_n \rightarrow$  OIP obtained from a given neurons  
 $w_{ij} \rightarrow$  weight associated with connection between neurons.

\* Training Algorithm (Finding the weight matrix)

1) Binary pattern.

$$w_{ij} = \sum_{p=1}^P [2s_i(p) - 1][2s_j(p) - 1] \quad (w_{ij} \text{ for all } i \neq j)$$

$$\boxed{w_{ij} = \sum_{s=1}^n [2y^s_i - 1][2y^s_j - 1]} = w_{ji}$$

2) Bipolar pattern.

$$w_{jj} = \sum_{p=1}^P [s_i(p)s_j(p)] \quad (\text{where } w_{ij}=0 \text{ for all } i=j)$$

Imp  $\Rightarrow v_{i_{in}} \begin{cases} 1 & \text{if } v_i > 0 \\ v_i & \text{if } v_i = 0 \\ 0 & \text{if } v_i < 0 \end{cases}$

$$\boxed{w_{ij} = \sum_{s=1}^n v^s_i * v^s_j}$$