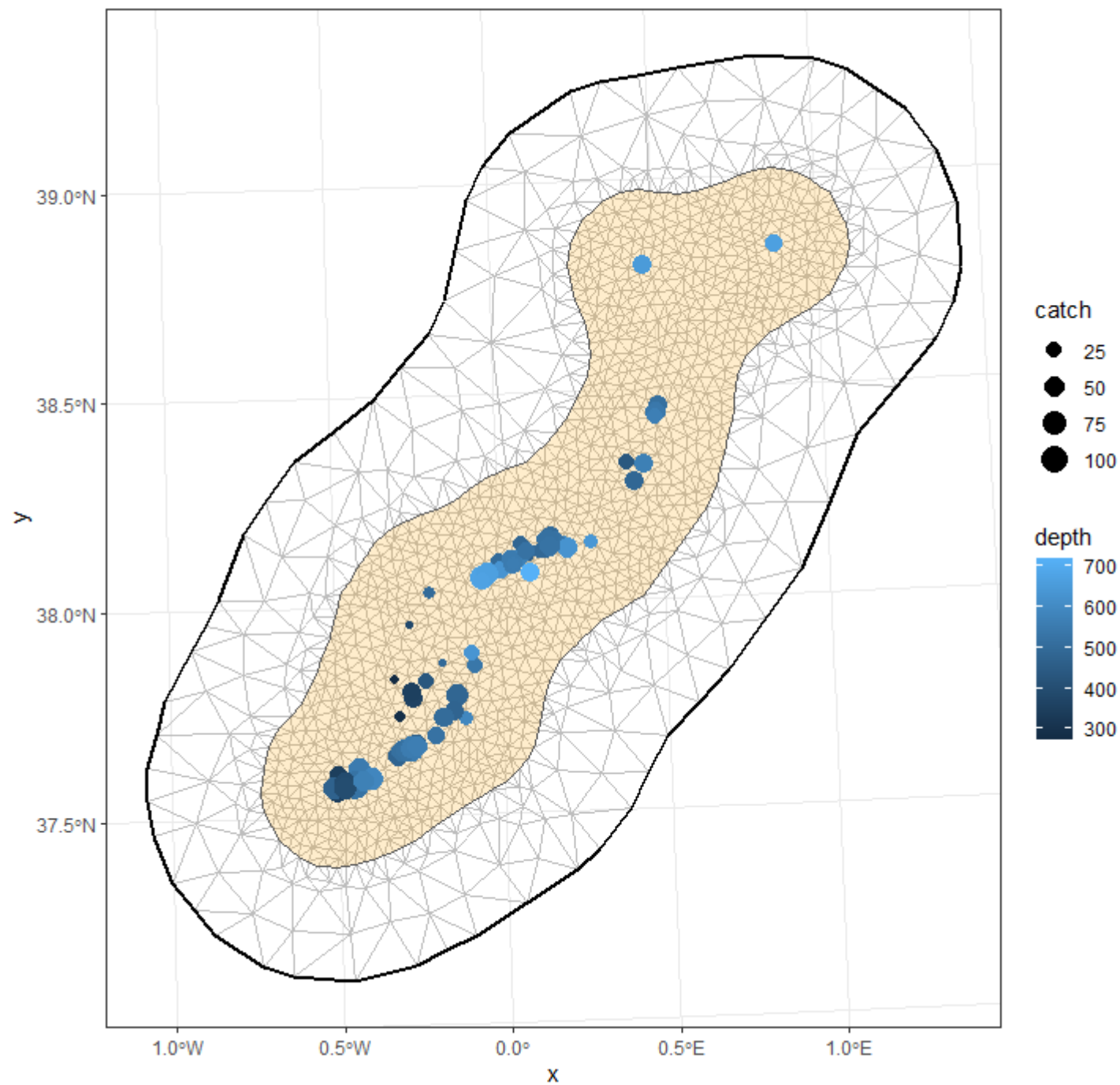


Hands on!

A gentle introduction to inlabru



Preferential
sampling

```
graph LR; A[Preferential sampling] --> B[Counts  
Poisson]; A --> C[Points  
Log-Gaussian Cox Process];
```

A diagram illustrating the concept of Preferential sampling. A central green box labeled "Preferential sampling" branches into two purple boxes. The top purple box is labeled "Counts" and "Poisson". The bottom purple box is labeled "Points" and "Log-Gaussian Cox Process".

Counts

Poisson

Points

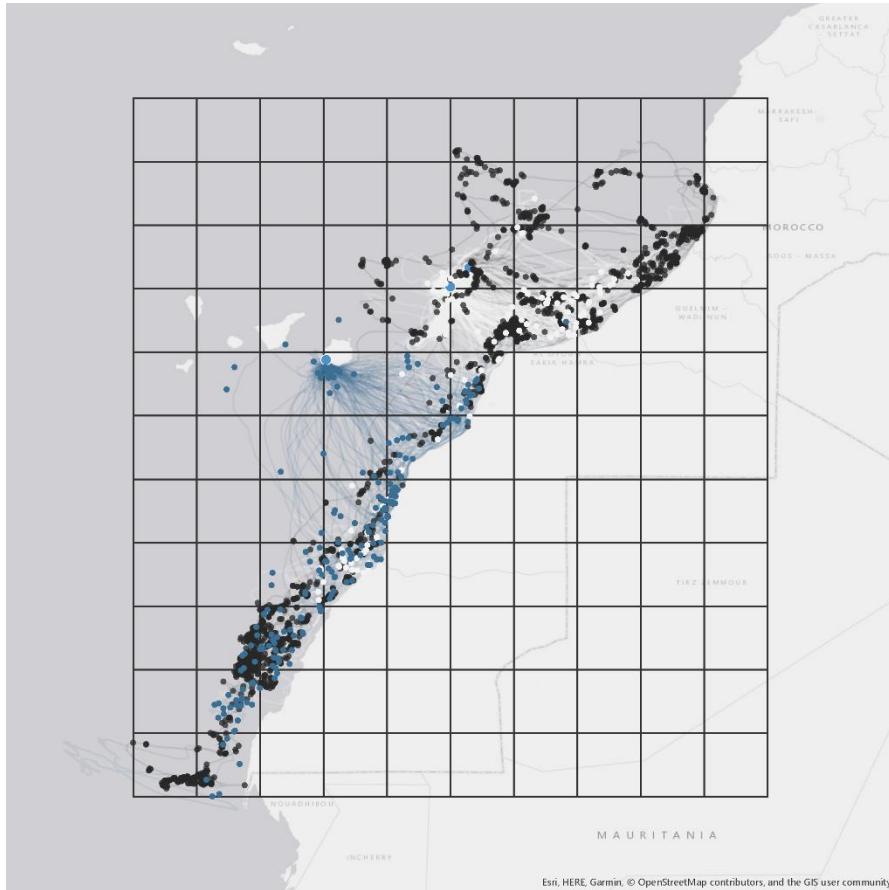
Log-Gaussian Cox
Process

Points: Log-gaussian Cox Process

$$N(A) \sim \int_A \lambda(s) d(s)$$
$$\log(\lambda(s)) = Z(s)$$

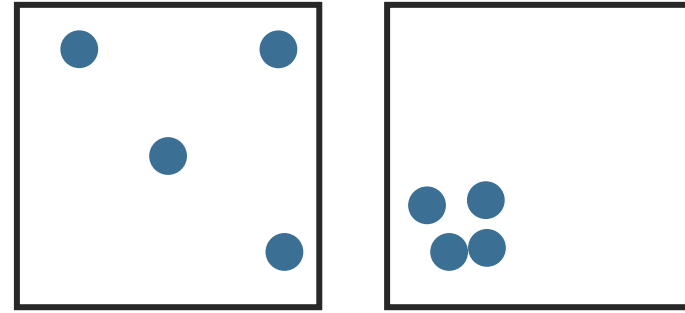
$$Z(s) = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + W(s)$$

Points: Log-gaussian Cox Process



Traditional SDM approach: grid

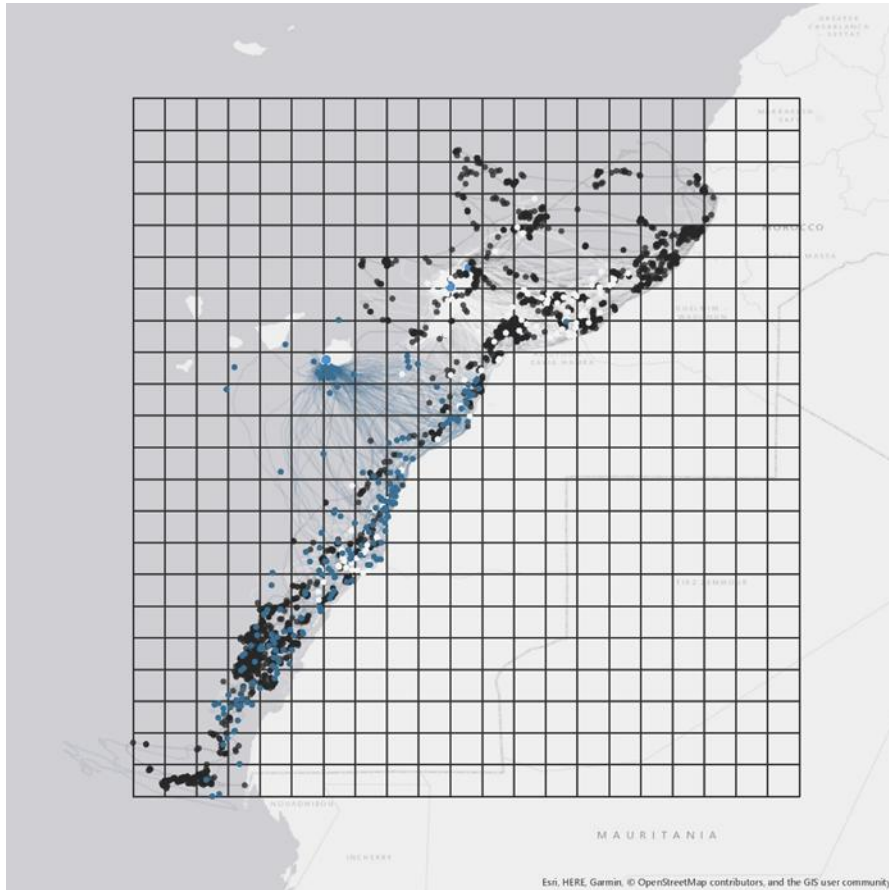
- Loss of information



- Scale dependent

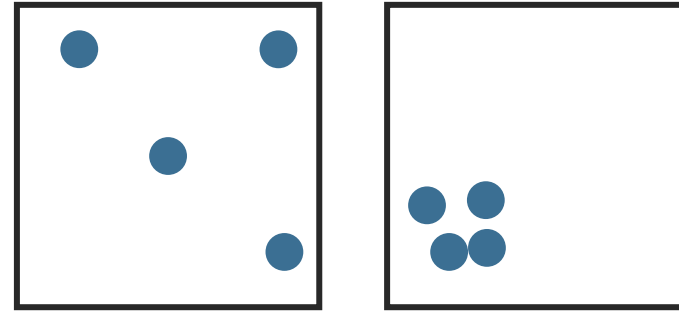
- Spatial autocorrelation ignored

Points: Log-gaussian Cox Process



Traditional SDM approach: grid

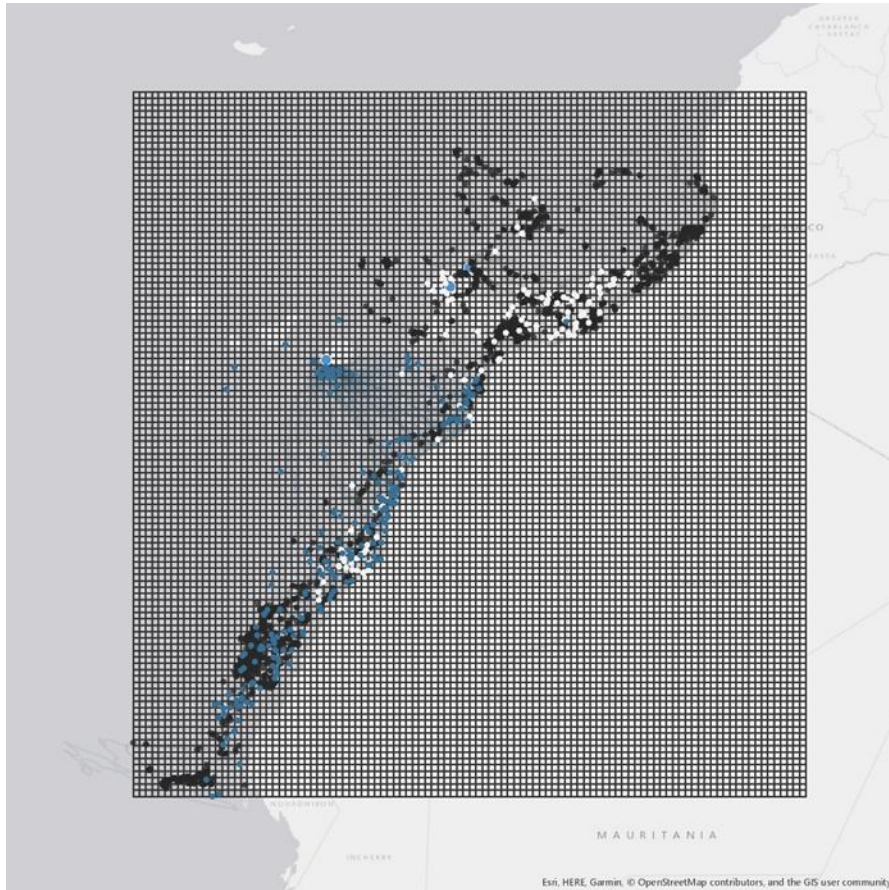
- Loss of information



- Scale dependent

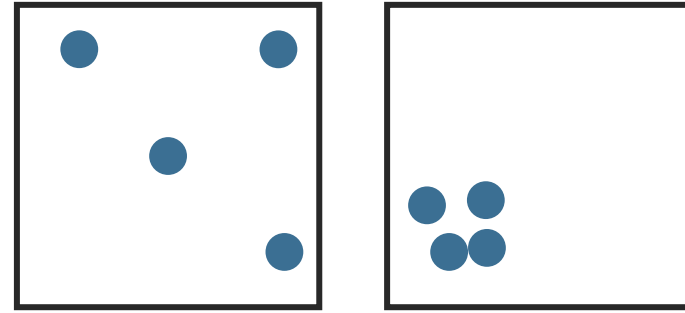
- Spatial autocorrelation ignored

Points: Log-gaussian Cox Process



Traditional SDM approach: grid

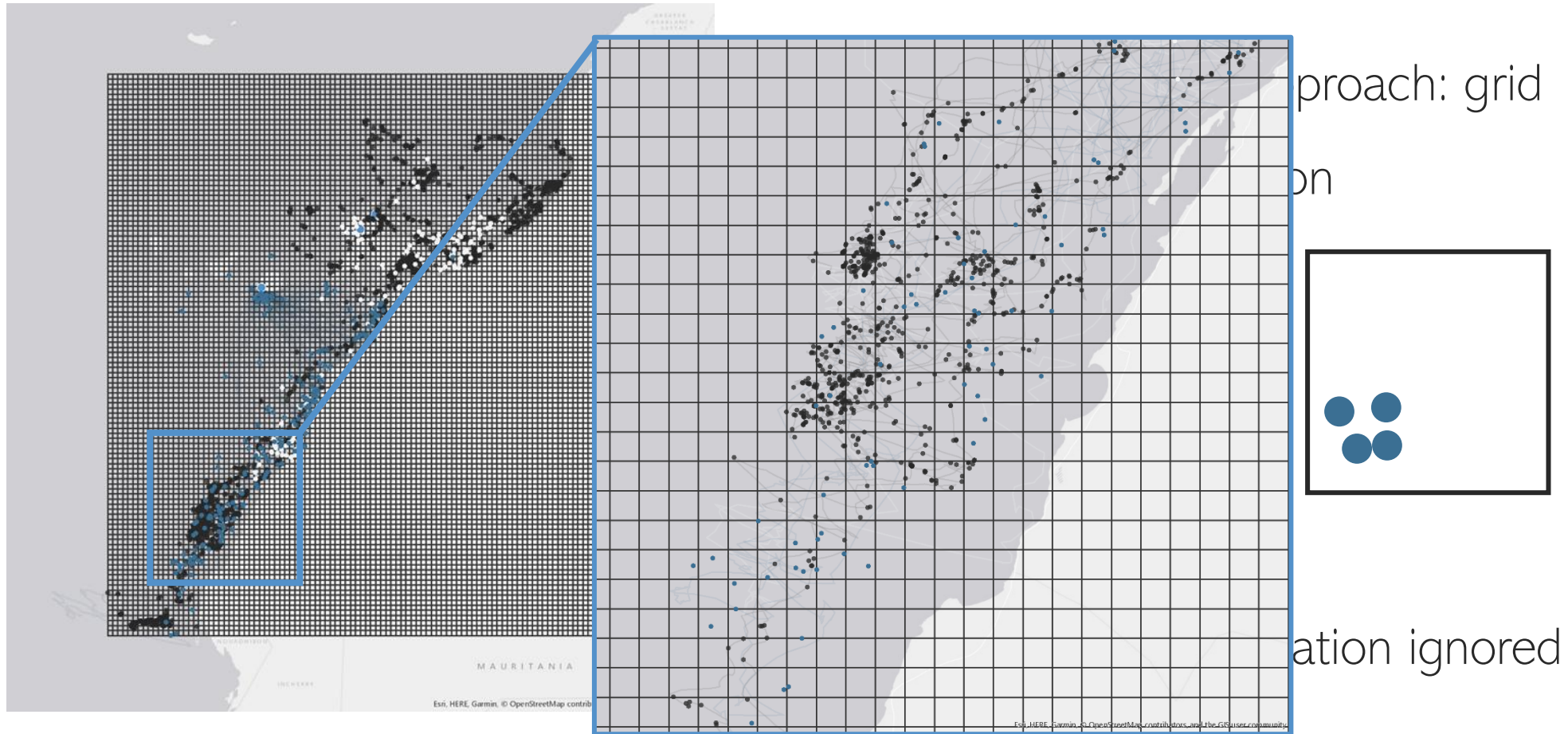
- Loss of information



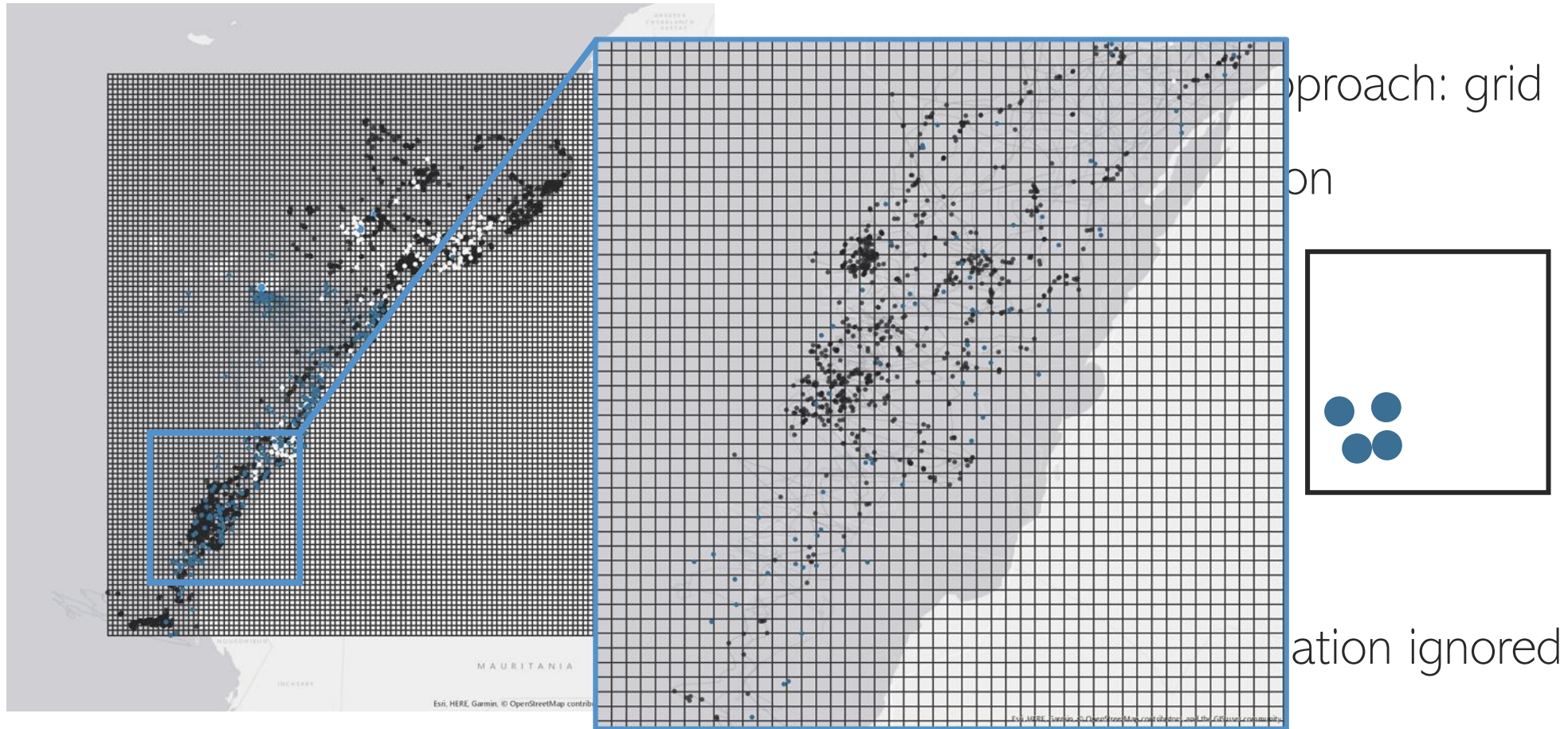
- Scale dependent

- Spatial autocorrelation ignored

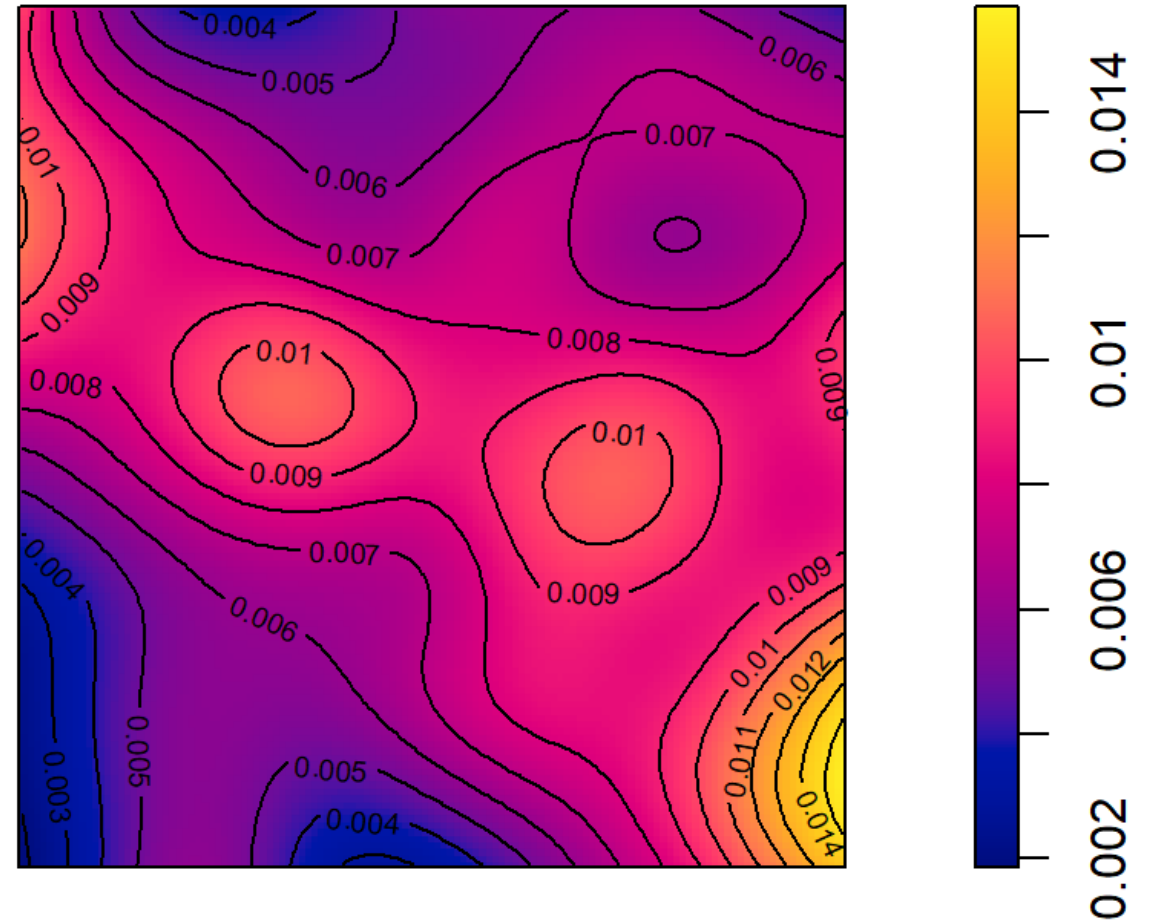
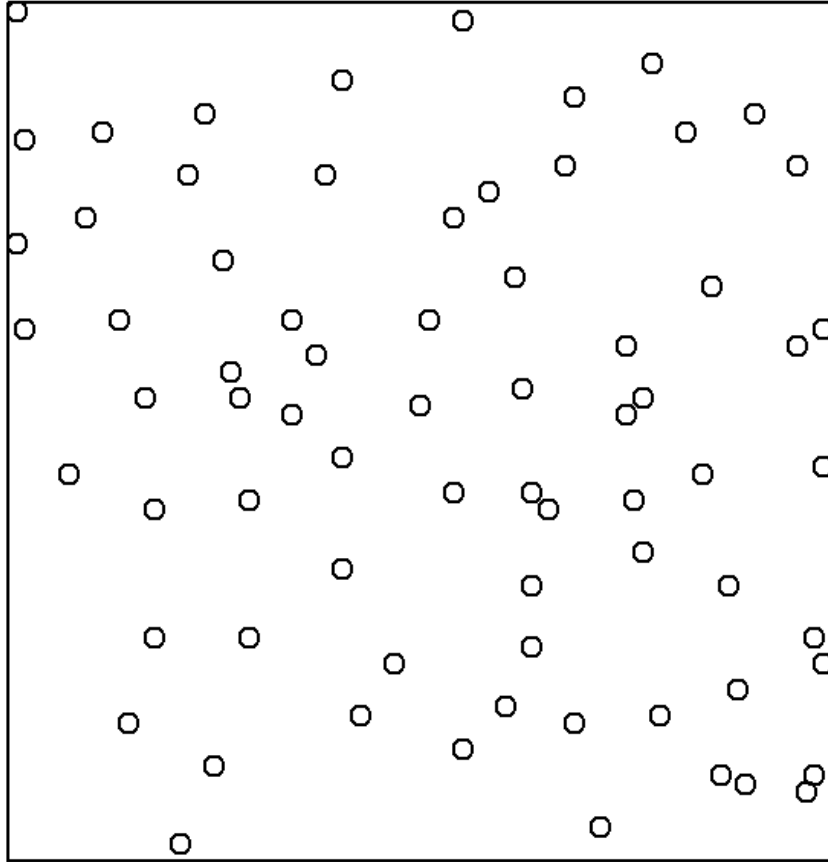
Points: Log-gaussian Cox Process



Points: Log-gaussian Cox Process



Points: Log-gaussian Cox Process



Points: Log-gaussian Cox Process

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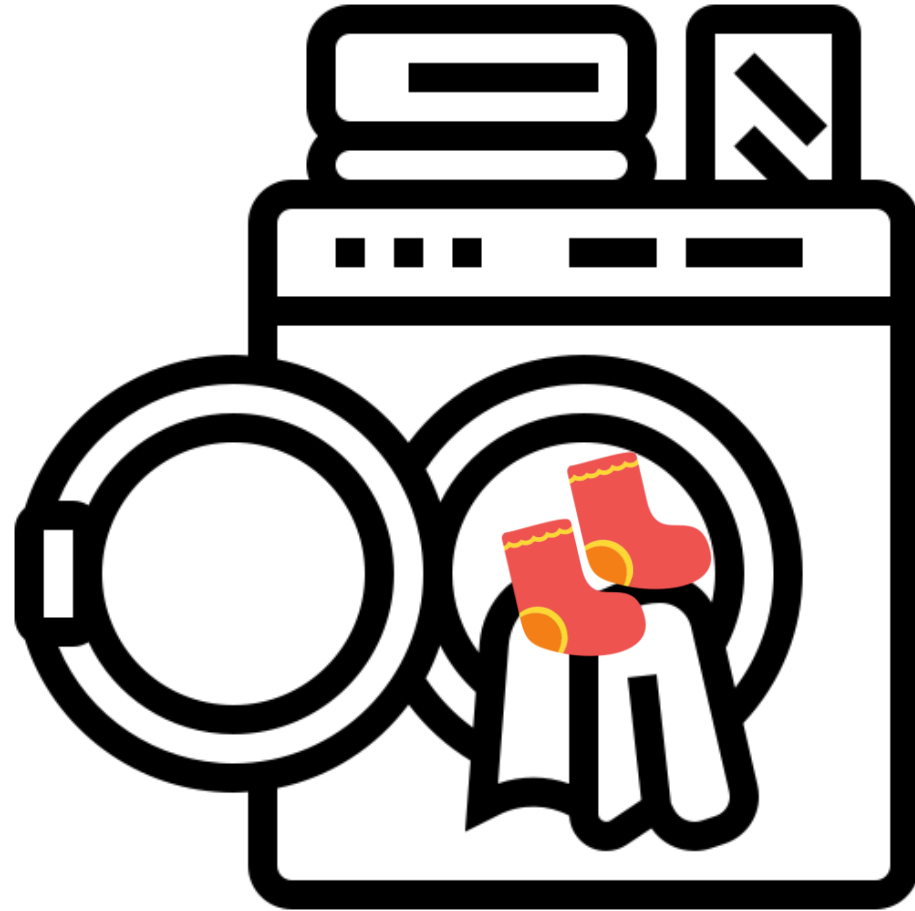
Points: Log-gaussian Cox Process

- Go to R script 1.1_basic_example.R...



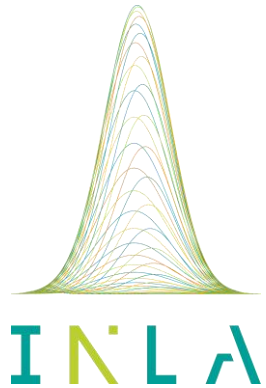
... and don't panic

INLA and inlabru: do I need to understand it?



Inlabru

Prof. Finn Lindgren
University of Edinburgh



Finn Lindgren

a Virginia Morera Pujol, R-inla discussion group

Hi,

personally, when I'm not specifically speaking about the implementation details, I would simply write the continuous formulation of the model, i.e.

$\log \lambda(s) = \eta(s),$
 $\{y_i\} \sim \text{Poisson process with intensity } \lambda(s) \text{ on } s \in \Omega$

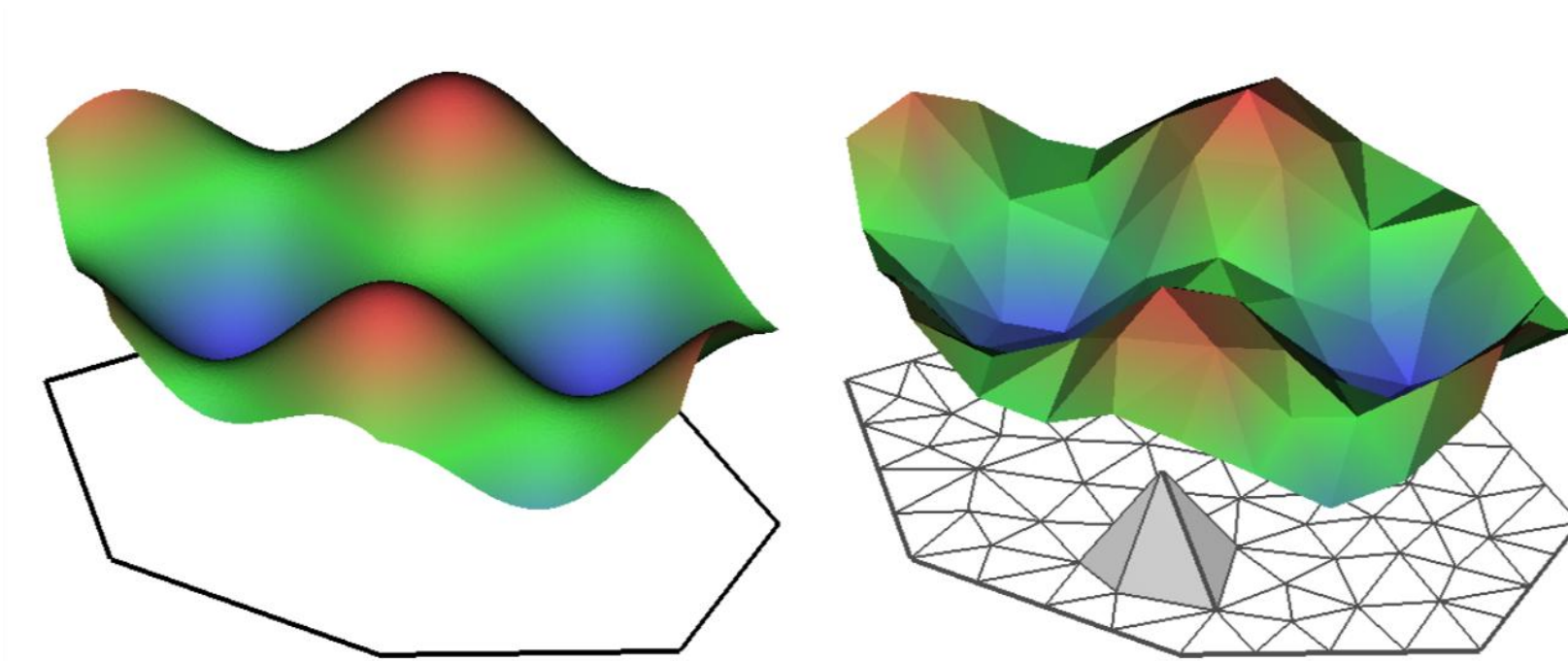
where $\eta(s)$ is the linear predictor evaluated at some location s , and mention that the integral $\int \lambda(s) ds$ in the likelihood is (with default settings) implemented using a trapezoidal integration scheme based on the triangulation mesh used to define the spde model. But if I really needed to write the approximation explicitly, I'd write that

$\int_{\Omega} \lambda(s) ds \approx \sum_{j=1}^J w_j \exp(\eta(s_j)),$
where $\{(s_j, w_j), j=1, \dots, J\}$ is the aforementioned triangular trapezoidal integration scheme.

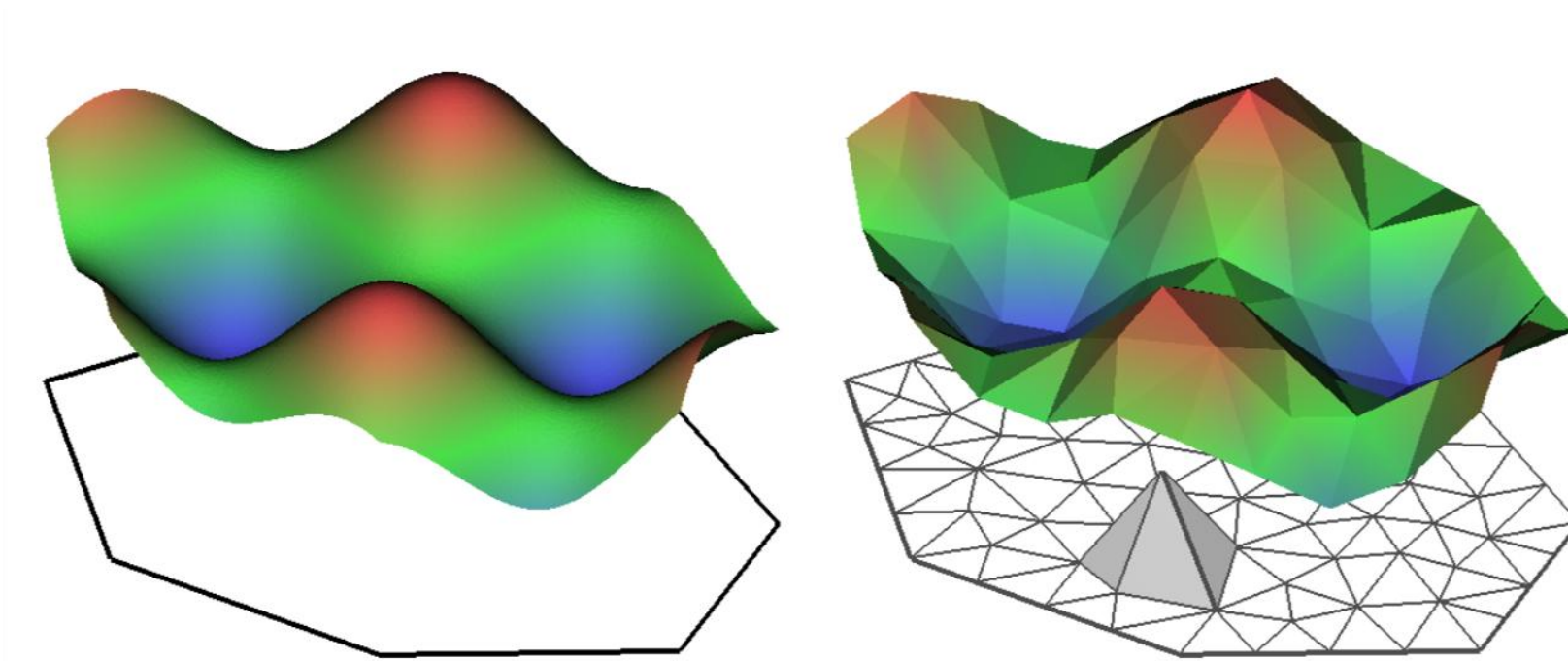
This is a basic numerical integration scheme for a sufficiently smooth function.



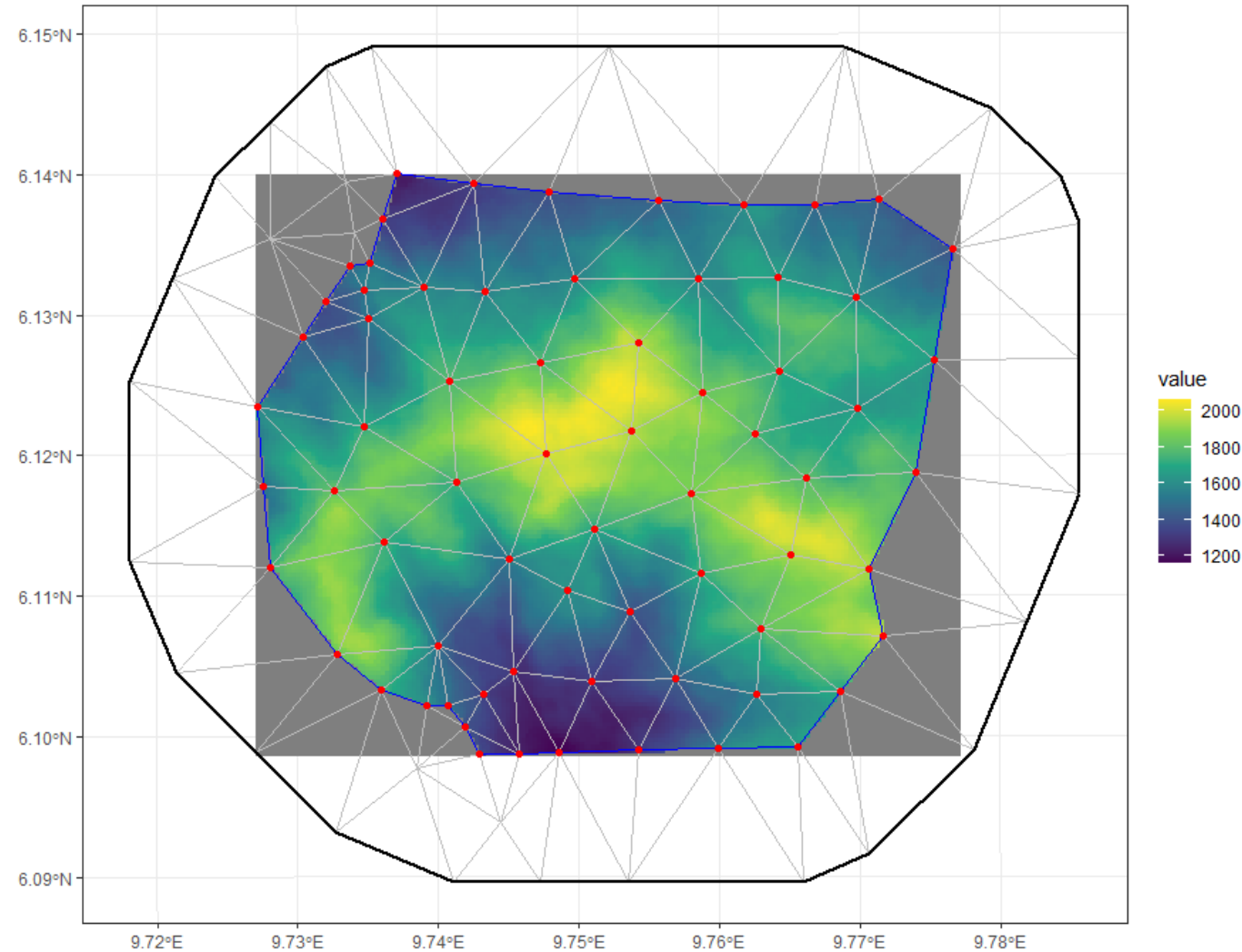
The mesh: what does it really do?



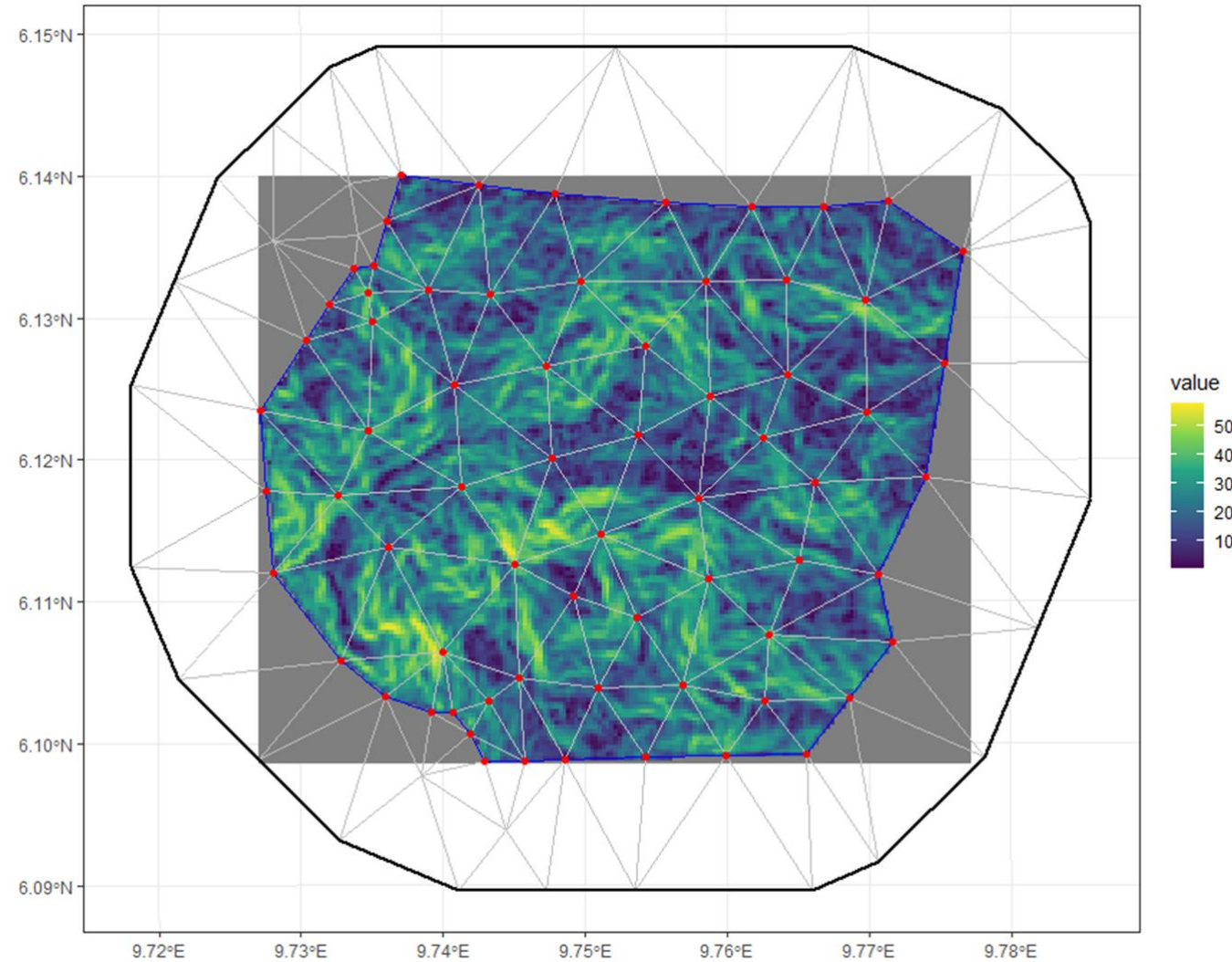
The mesh: what does it really do?



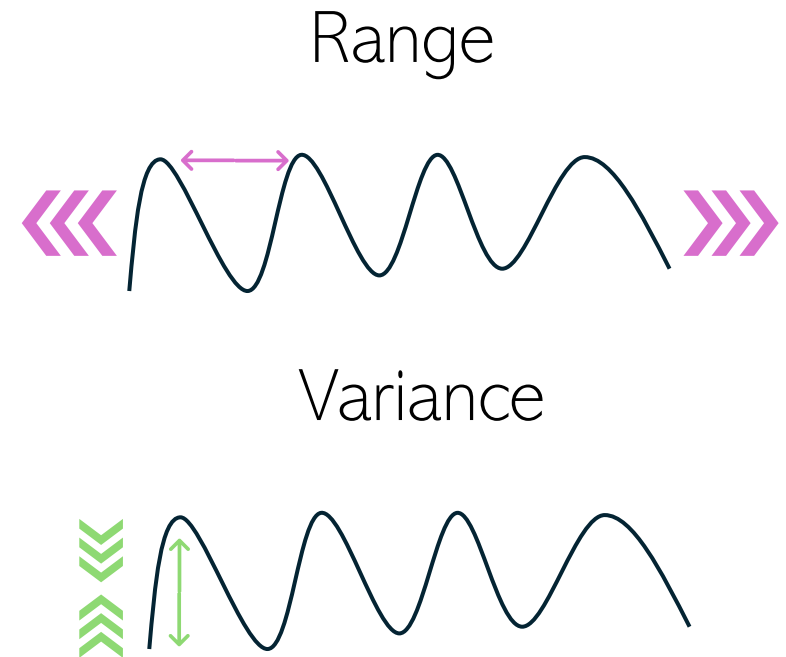
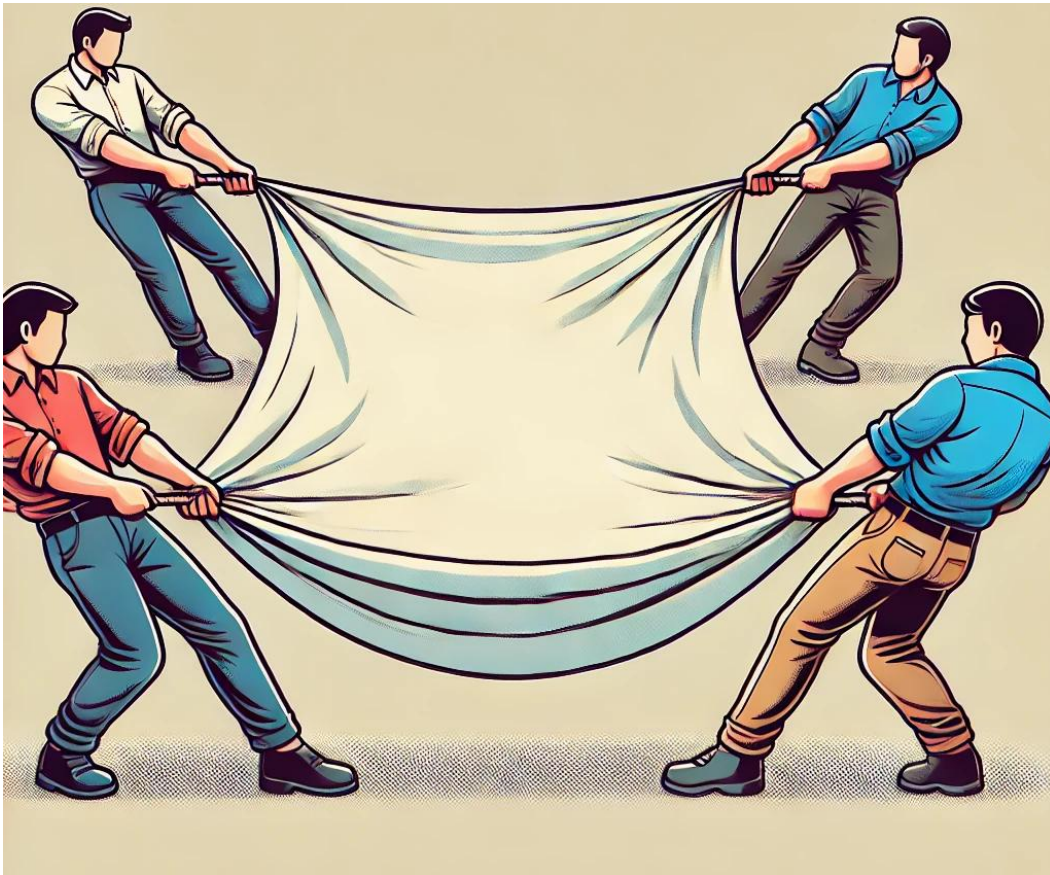
The mesh: what does it really do?



The mesh: what does it really do?



PC priors: inference's best friend



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