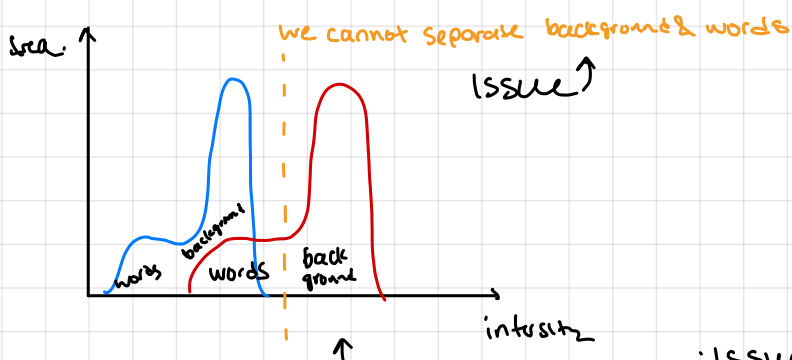
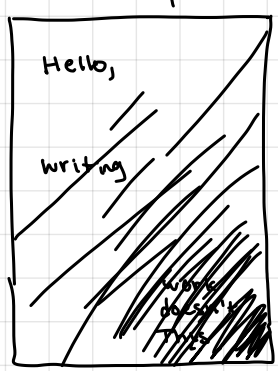


Adaptive Histogram Equalization - 1/23/2020



- apply different functions to different parts of image
- do histogram equalization in patches

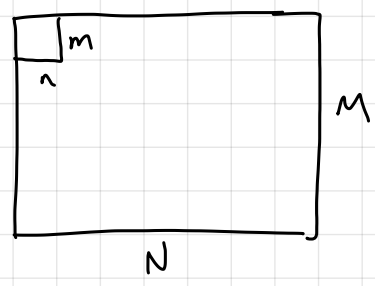


• Issue → edges formed by applying different transformations to different images

• solution: do it pixel by pixel?

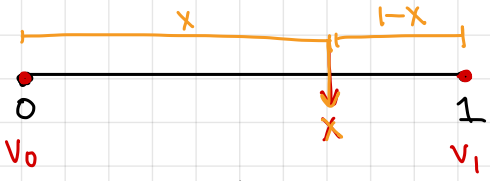
- ① Compute hist. of surrounding pixels
- ② histogram equalization
- ③ replace pixel

- computing histogram is $O(nm)$
- doing hist eq is $O(nm)$



Better way: bilinear interpolation

Linear interpolation:

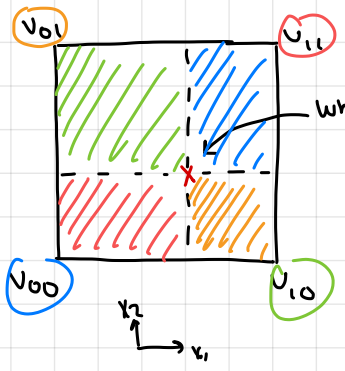


$$V_i = f(x_i)$$

$$V(x) = xV_1 + (1-x)V_0$$

value @ x

Bilinear interpolation



What value occurs here?

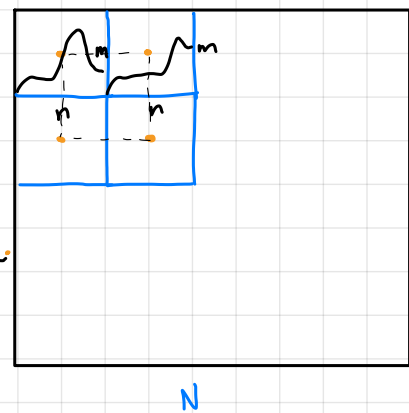
$$V(x) = x_1 x_2 V_{11} + x_1 (1-x_2) V_{10} + (1-x_1) x_2 V_{01} + (1-x_1)(1-x_2) V_{00}$$

Adaptive Hist Eq with bilinear interpolation:

- x_{ij} : orig intensity
- y_{ij} : resulting one
- f_{uw} : transform fn @ ctr of window

$$y_{ij} = x_{1j} x_{2j} f_{Lij} + x_{1j} (1-x_{2j}) f_{Lij} + (1-x_{1j}) x_{2j} f_{uw} + (1-x_{1j})(1-x_{2j}) f_{uw}$$

↑
fn to left of y



- apply transformations of surrounding blocks in prop to dist from center of surrounding blocks

• how does block sizing help/hurt?

doing this pixel by pixel

$$O(nmNM)$$

doing it block by block
 $O(NM)$ b/c just breaking up image & doing same thing over

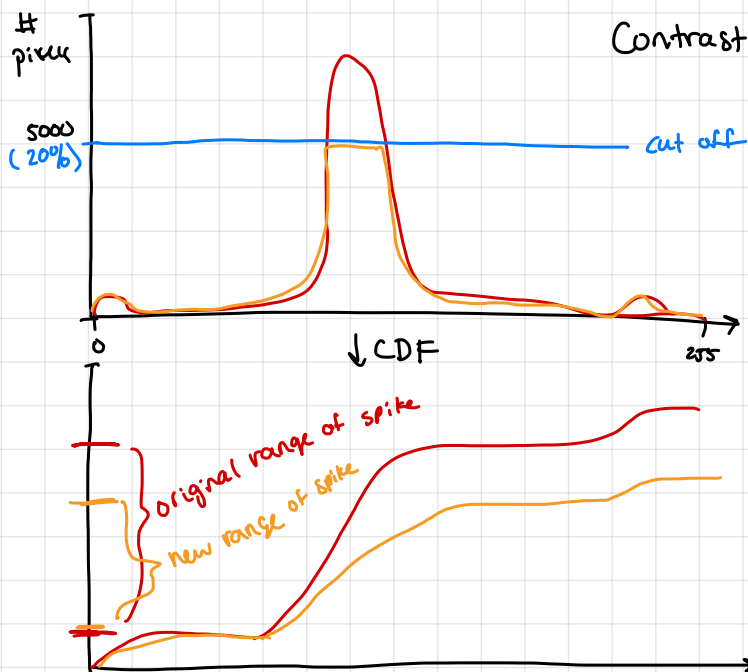
Issues with histogram equalization

- amplification of noise
- Introduces Contrast
but what if it introduces contrast where there shouldn't be?
↳ even worse with adaptive hist eq.
- Photo of wall:



Looks like not
a wall but gravel now

Determining areas of low contrast that we don't to amplify



Contrast-limited adaptive histogram equalization
(CLAHE)

↳ solves book problem

- high slope means we are stretching mapping out
- limiting height or dist limits slope and thus the spreading out of intensities and thus the contrast