

STATS 112 HW1

Viraj Vijaywargiya

2023-04-13

```
library(lattice)
library(nlme)
library(lme4)
```

```
## Loading required package: Matrix
```

```
##
```

```
## Attaching package: 'lme4'
```

```
## The following object is masked from 'package:nlme':
```

```
##
```

```
##      lmList
```

```
library(survival)
library(tidyverse)
```

```
## -- Attaching packages ----- tidyverse 1.3.2 --
```

```
## v ggplot2 3.3.6      v purrr  0.3.5
## v tibble  3.1.8      v dplyr  1.0.10
## v tidyr   1.2.1      v stringr 1.4.1
## v readr   2.1.3      v forcats 0.5.2
```

```
## -- Conflicts ----- tidyverse_conflicts() --
```

```
## x dplyr::collapse() masks nlme::collapse()
## x tidyr::expand()   masks Matrix::expand()
## x dplyr::filter()   masks stats::filter()
## x dplyr::lag()       masks stats::lag()
## x tidyr::pack()      masks Matrix::pack()
## x tidyr::unpack()    masks Matrix::unpack()
```

```
1. epilepsy = read.table("/Users/virajvijaywargiya/Downloads/epilepsy.txt", header=TRUE)
   epilepsy[,4] = epilepsy[,4]/8
   epilepsy[,c(5:8)] = epilepsy[,c(5:8)]/2
   epi.long = reshape(epilepsy, idvar="ID", varying=list(4:8), v.names="Rate", timevar="Time", times=c(
```

1a)

```
tapply(epi.long$Rate, list(epi.long$Time,epi.long$trt), mean)
```

```
##      Placebo Progabide
## 0 3.848214  3.955645
## 2 4.678571  4.290323
## 4 4.142857  4.209677
## 6 4.392857  4.064516
## 8 4.000000  3.370968
```

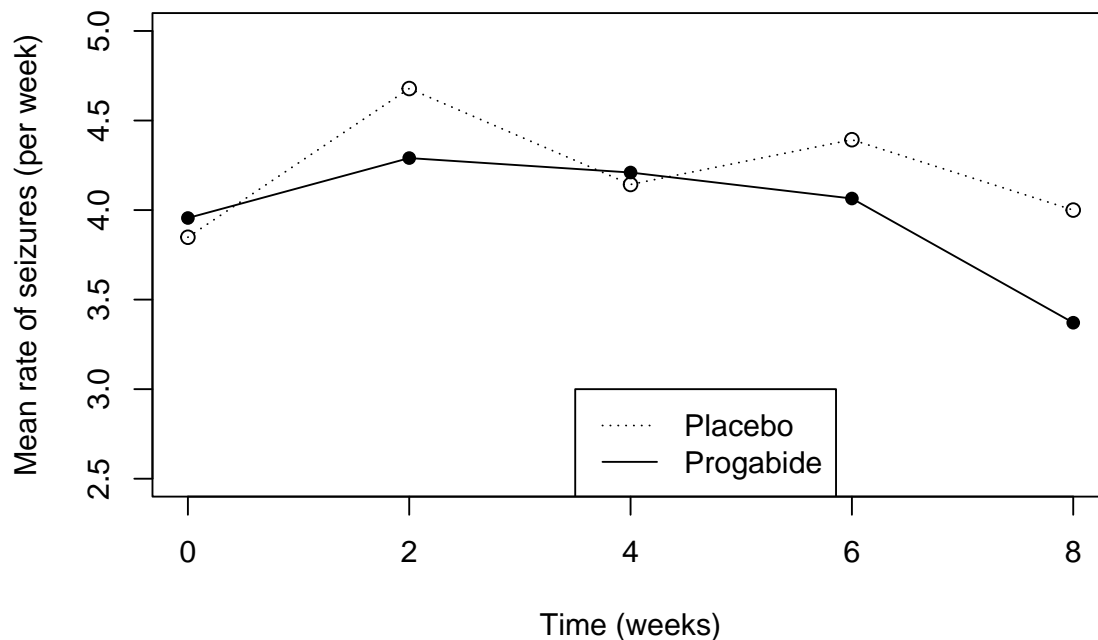
1b)

```
means = tapply(epi.long$Rate,list(epi.long$Time,epi.long$trt),mean)
```

```
matplot(c(0,2,4,6,8),means,col=c(1,1),lty=c(3,1),type="o",pch=c(1,16),xlab="Time (weeks)",ylab="Mean rate of seizures (per week)")
```

```
legend(3.5,3.0, c("Placebo","Progabide"), lty=c(3,1))
```

Mean Rate of Seizures by Treatment Group



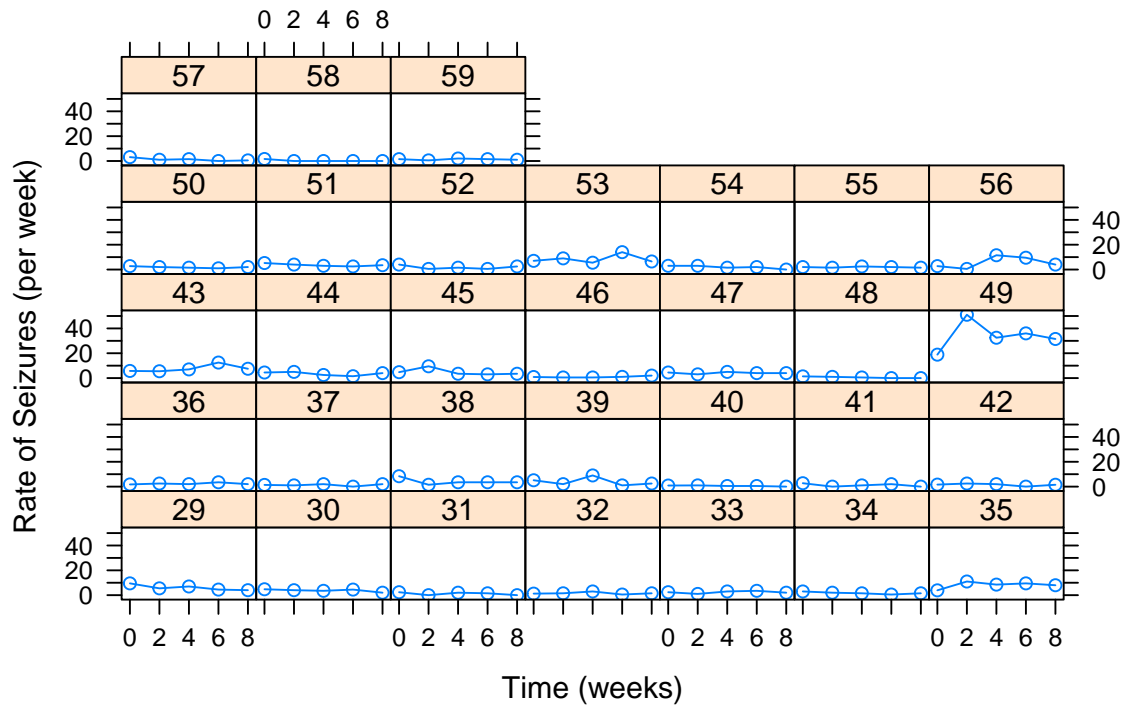
1c)

```
Prog = epi.long[epi.long$trt=="Progabide",]
Plac = epi.long[epi.long$trt=="Placebo",]
```

```
# Progabide group
```

```
xyplot(Rate ~ Time | factor(ID), data=Prog, type="o",main="Response Trajectories in Progabide Group")
```

Response Trajectories in Progabide Group

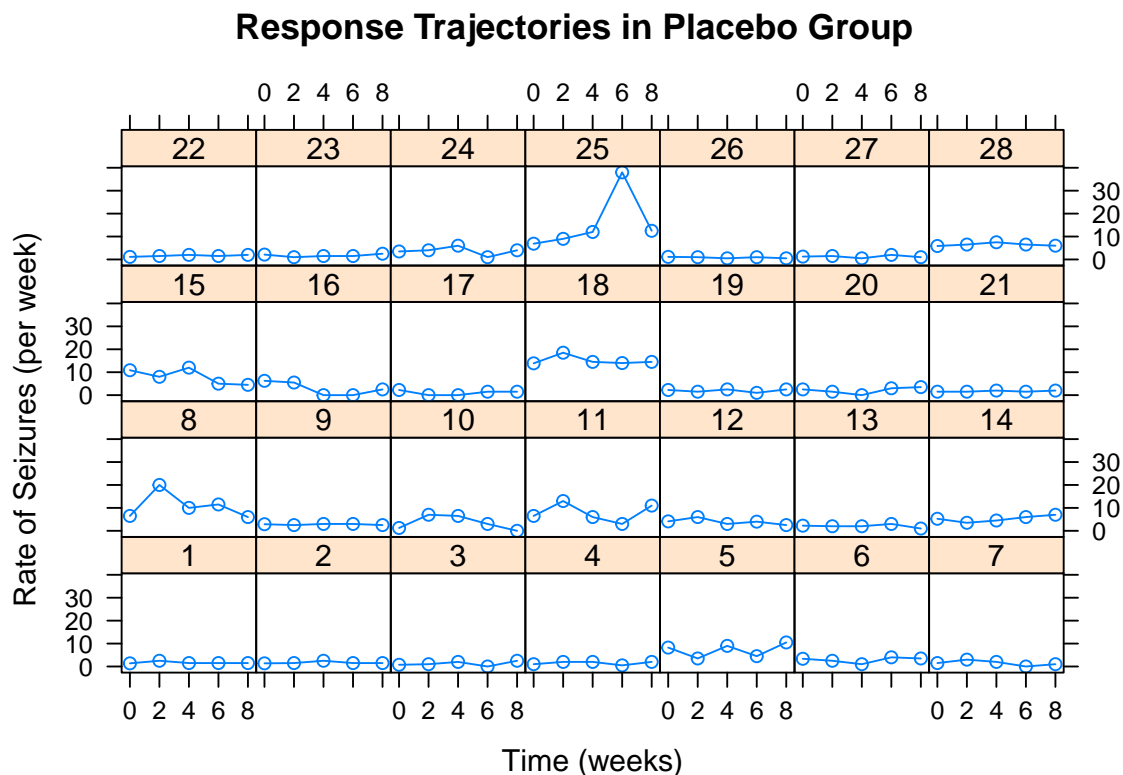


There seems to be a slight downwards trend with time moving on.

1d)

```
# Placebo group
```

```
xyplot(Rate ~ Time | factor(ID), data=Plac, type="o", main="Response Trajectories in Placebo Group",
```



This also seems to have a slight downwards trend with time moving on.

1e) Sample Covariance matrix for the Placebo group:

```
cov(epilepsy[epilepsy$trt=="Placebo",4:8])
```

```
##           Week0      Week2      Week4      Week6      Week8
## Week0  10.64740  12.30820  11.07341  11.80489  10.18519
## Week2  12.30820  25.68915  16.18651  18.85317  13.06481
## Week4  11.07341  16.18651  16.66402  19.79365  12.12963
## Week6  11.80489  18.85317  19.79365  53.82143  18.89815
## Week8  10.18519  13.06481  12.12963  18.89815  14.48148
```

Sample covariance matrix for the Progabide group:

```
cov(epilepsy[epilepsy$trt=="Progabide",4:8])
```

```
##           Week0      Week2      Week4      Week6      Week8
## Week0  12.24432  27.24872  17.54919  20.28421  17.18575
## Week2  27.24872  83.17957  49.05376  57.81398  49.83038
## Week4  17.54919  49.05376  35.16290  38.10269  31.55296
## Week6  20.28421  57.81398  38.10269  48.26237  37.20860
## Week8  17.18575  49.83038  31.55296  37.20860  31.66613
```

The sample covariance between weeks vary quite a bit across time. They seem somewhat similar across the time lags in the placebo group, however, they differ quite a bit in the Progabide group. For example: In the Progabide group, the sample covariance at the baseline is 12.24 but in week 2 it jumps to 83.18.

1f)

```
Pro.W0 = epilepsy$Week0[epilepsy$strtr=="Progabide"]
Pro.W8 = epilepsy$Week8[epilepsy$strtr=="Progabide"]
t.test(Pro.W0, Pro.W8, paired=T, alternative="two.sided")
```

```
##
## Paired t-test
##
## data: Pro.W0 and Pro.W8
## t = 1.054, df = 30, p-value = 0.3003
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -0.5482002 1.7175551
## sample estimates:
## mean of the differences
## 0.5846774
```

Null Hypothesis $H_0: u(d) = 0$ vs Alternate Hypothesis $H_A: u(d) \neq 0$. Test statistic $t = 1.054$, p-value = 0.3003.

Therefore, we fail to reject the null, and conclude that the mean change in rate of seizures from the baseline to the last week of the study is equal to zero.

1g)

```
Diffs = epilepsy$Week8 - epilepsy$Week0
Pro.D = Diffs[epilepsy$strtr=="Placebo"]
Pla.D = Diffs[epilepsy$strtr=="Progabide"]
t.test(Pla.D, Pro.D, mu=0, alternative="two.sided")
```

```
##
## Welch Two Sample t-test
##
## data: Pla.D and Pro.D
## t = -1.0656, df = 53.99, p-value = 0.2913
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -2.1220927 0.6491664
## sample estimates:
## mean of x mean of y
## -0.5846774 0.1517857
```

Null Hypothesis $H_0: u_1 = u_2$ vs Alternate Hypothesis $H_A: u_1 \neq u_2$ (u_1 is the mean change for Placebo and u_2 is the mean change for Progabide). Test statistic $t = -1.0656$. p-value = 0.2913.

Therefore, we fail to reject the null hypothesis and conclude that the mean change in rate of seizures from the baseline to the last week of the study is the same in both groups.

2. 2a)

```
exercise = read.csv("/Users/virajvijaywargiya/Downloads/exercise.csv")
summary(exercise)
```

```
##          id          program          week_0          week_1
## Min.      : 1  Length:37      Min.      :74.00  Min.      :75.00
## 1st Qu.:10  Class :character  1st Qu.:79.00  1st Qu.:79.00
```

```
## Median :19   Mode  :character   Median :80.00   Median :81.00
## Mean    :19                               Mean  :80.46   Mean    :81.42
## 3rd Qu.:28                               3rd Qu.:83.00   3rd Qu.:84.00
## Max.    :37                               Max.    :87.00   Max.    :91.00
##                                     NA's    :1
##      week_2      week_3      week_4
## Min.    :76.00   Min.    :75.00   Min.    :75.0
## 1st Qu.:80.00   1st Qu.:80.00   1st Qu.:80.0
## Median :82.00   Median :82.00   Median :82.0
## Mean    :82.08   Mean    :81.88   Mean    :81.8
## 3rd Qu.:84.00   3rd Qu.:84.00   3rd Qu.:85.0
## Max.    :90.00   Max.    :91.00   Max.    :87.0
## NA's    :1      NA's    :3      NA's    :7
```

From the output we can see that the averages for each week are around 80-82, and the inter-quartile ranges are similar. In addition, there are missing observations in week 1, 2, 3, 4.

2b)

```
library(GGally)
```

```
## Registered S3 method overwritten by 'GGally':
##   method from
##   +.gg      ggplot2
```

```
ggpairs(select(exercise, -id))
```

```
## Warning: Removed 1 rows containing non-finite values (stat_boxplot).
## Removed 1 rows containing non-finite values (stat_boxplot).

## Warning: Removed 3 rows containing non-finite values (stat_boxplot).

## Warning: Removed 7 rows containing non-finite values (stat_boxplot).

## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.

## Warning in ggally_statistic(data = data, mapping = mapping, na.rm = na.rm, :
## Removing 1 row that contained a missing value

## Warning in ggally_statistic(data = data, mapping = mapping, na.rm = na.rm, :
## Removing 1 row that contained a missing value

## Warning in ggally_statistic(data = data, mapping = mapping, na.rm = na.rm, :
## Removed 3 rows containing missing values

## Warning in ggally_statistic(data = data, mapping = mapping, na.rm = na.rm, :
## Removed 7 rows containing missing values

## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.

## Warning: Removed 1 rows containing non-finite values (stat_bin).

## Warning: Removed 1 rows containing missing values (geom_point).
```

```

## Warning: Removed 1 rows containing non-finite values (stat_density).

## Warning in ggally_statistic(data = data, mapping = mapping, na.rm = na.rm, :
## Removed 2 rows containing missing values

## Warning in ggally_statistic(data = data, mapping = mapping, na.rm = na.rm, :
## Removed 4 rows containing missing values

## Warning in ggally_statistic(data = data, mapping = mapping, na.rm = na.rm, :
## Removed 7 rows containing missing values

## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.

## Warning: Removed 1 rows containing non-finite values (stat_bin).

## Warning: Removed 1 rows containing missing values (geom_point).

## Warning: Removed 2 rows containing missing values (geom_point).

## Warning: Removed 1 rows containing non-finite values (stat_density).

## Warning in ggally_statistic(data = data, mapping = mapping, na.rm = na.rm, :
## Removed 4 rows containing missing values

## Warning in ggally_statistic(data = data, mapping = mapping, na.rm = na.rm, :
## Removed 8 rows containing missing values

## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.

## Warning: Removed 3 rows containing non-finite values (stat_bin).

## Warning: Removed 3 rows containing missing values (geom_point).

## Warning: Removed 4 rows containing missing values (geom_point).
## Removed 4 rows containing missing values (geom_point).

## Warning: Removed 3 rows containing non-finite values (stat_density).

## Warning in ggally_statistic(data = data, mapping = mapping, na.rm = na.rm, :
## Removed 9 rows containing missing values

## 'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.

## Warning: Removed 7 rows containing non-finite values (stat_bin).

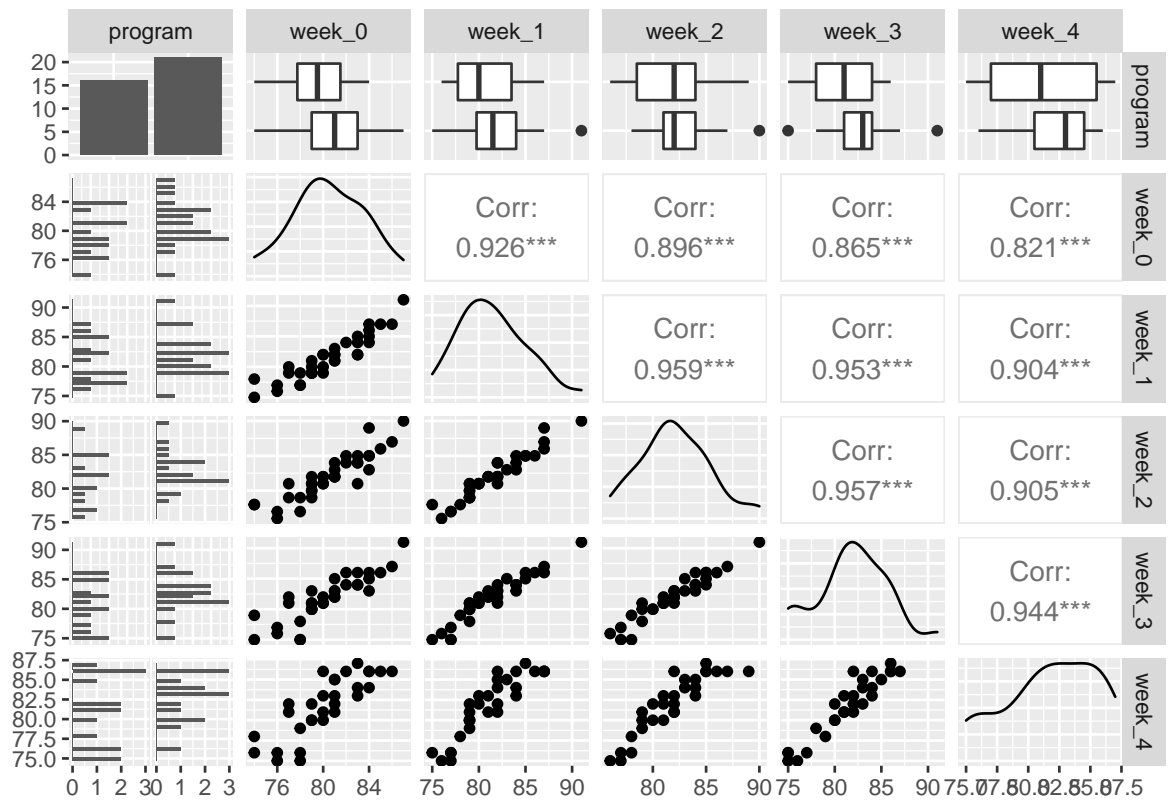
## Warning: Removed 7 rows containing missing values (geom_point).
## Removed 7 rows containing missing values (geom_point).

## Warning: Removed 8 rows containing missing values (geom_point).

## Warning: Removed 9 rows containing missing values (geom_point).

```

```
## Warning: Removed 7 rows containing non-finite values (stat_density).
```

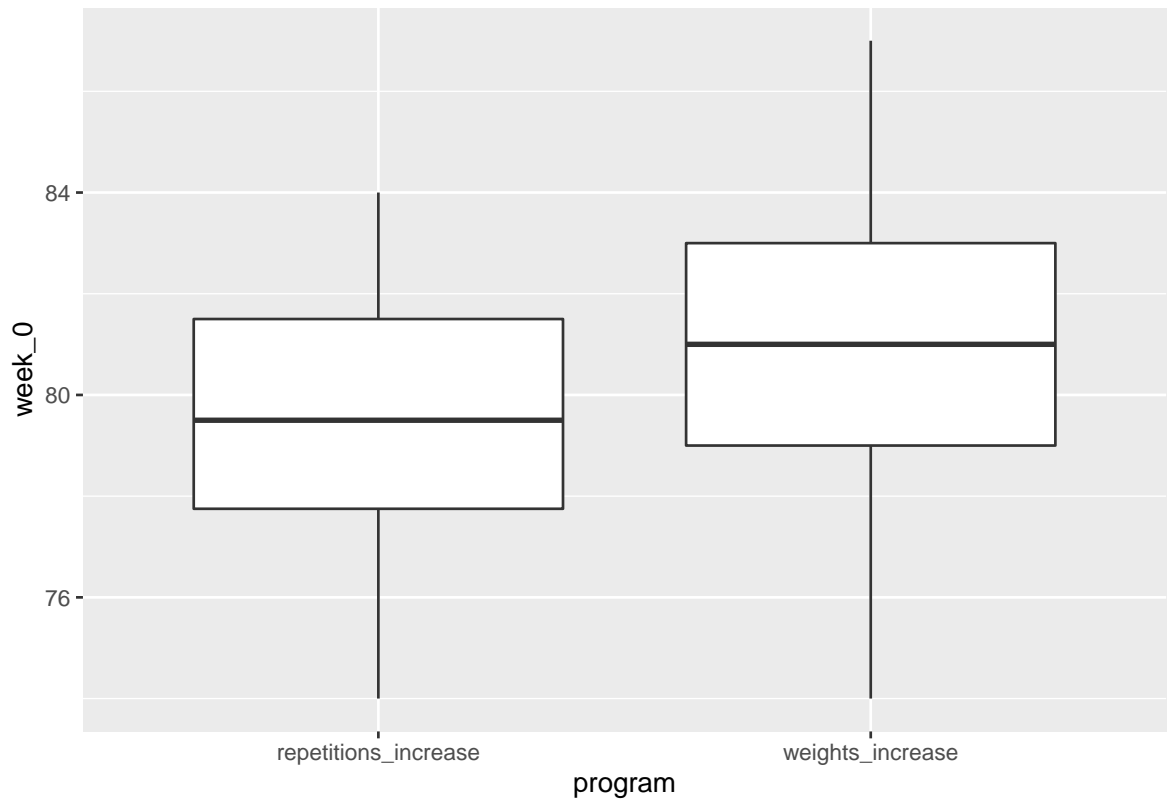


This plot shows all the possible two-way relationships. It will do a scatterplot if both variables from the dataset are quantitative, for example, week measurements. The top row shows boxplots of the weekly measurements by different groups.

We are excluding the IDs because it plays no role in the dataset as a covariate.

2c)

```
exercise %>%
  ggplot(aes(x = program, y = week_0)) + geom_boxplot()
```

From the boxplots above, we can see that the weights_increase group has a slightly higher muscle strength measurement than the repetitions_increase group, for week 0.

2d)

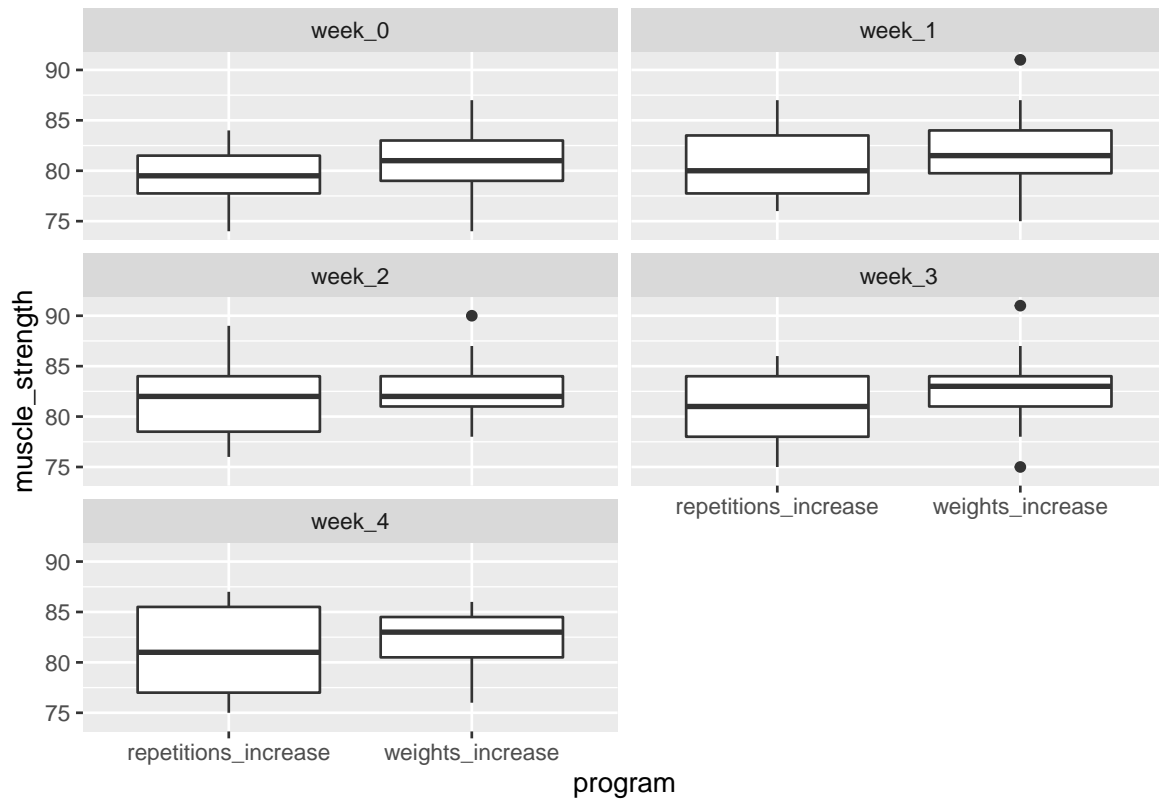
```
long_exercise <- exercise %>%
  pivot_longer(cols = starts_with("week"),
    names_to = "week",
    values_to = "muscle_strength")
glimpse(long_exercise)
```

```
## Rows: 185
## Columns: 4
## $ id      <int> 1, 1, 1, 1, 1, 2, 2, 2, 2, 2, 3, 3, 3, 3, 3, 4, 4, 4, ~
## $ program <chr> "repetitions_increase", "repetitions_increase", "repet~
## $ week    <chr> "week_0", "week_1", "week_2", "week_3", "week_4", "wee~
## $ muscle_strength <int> 79, 79, 80, 80, 80, 83, 85, 85, 86, 87, 81, 82, 82, 83~
```

2e)

```
long_exercise %>%
  ggplot(aes(x = program, y = muscle_strength)) + geom_boxplot() +
  facet_wrap(~week, nrow = 3)
```

```
## Warning: Removed 12 rows containing non-finite values (stat_boxplot).
```



For the repetitions_increase group, the average muscle strength across the weeks does not have much difference, it is mainly similar. However, the range for the muscle strength increases across the week, reaching maximum around 85.

2f)

```
long_exercise %>%
  group_by(program, week) %>%
  summarize(mean_muscle_strength = mean(muscle_strength, na.rm = TRUE),
            sd_muscle_strength = sd(muscle_strength, na.rm = TRUE))
```

```
## 'summarise()' has grouped output by 'program'. You can override using the
## '.groups' argument.
```

```
## # A tibble: 10 x 4
## # Groups:   program [2]
##   program          week mean_muscle_strength sd_muscle_strength
##   <chr>           <chr>           <dbl>           <dbl>
## 1 repetitions_increase week_0             79.7             3.11
## 2 repetitions_increase week_1             80.8             3.58
## 3 repetitions_increase week_2             81.3             3.68
## 4 repetitions_increase week_3             80.8             3.84
## 5 repetitions_increase week_4             81.1             4.32
## 6 weights_increase   week_0             81.0             3.11
## 7 weights_increase   week_1             81.9             3.57
## 8 weights_increase   week_2             82.6             2.85
## 9 weights_increase   week_3             82.7             3.46
## 10 weights_increase   week_4             82.5             2.90
```

This output relates to what was stated in part e as from the output we can see that the `mean_muscle_strength` is approximately the same across the weeks, however, the `sd_muscle_strength` increases across the weeks.

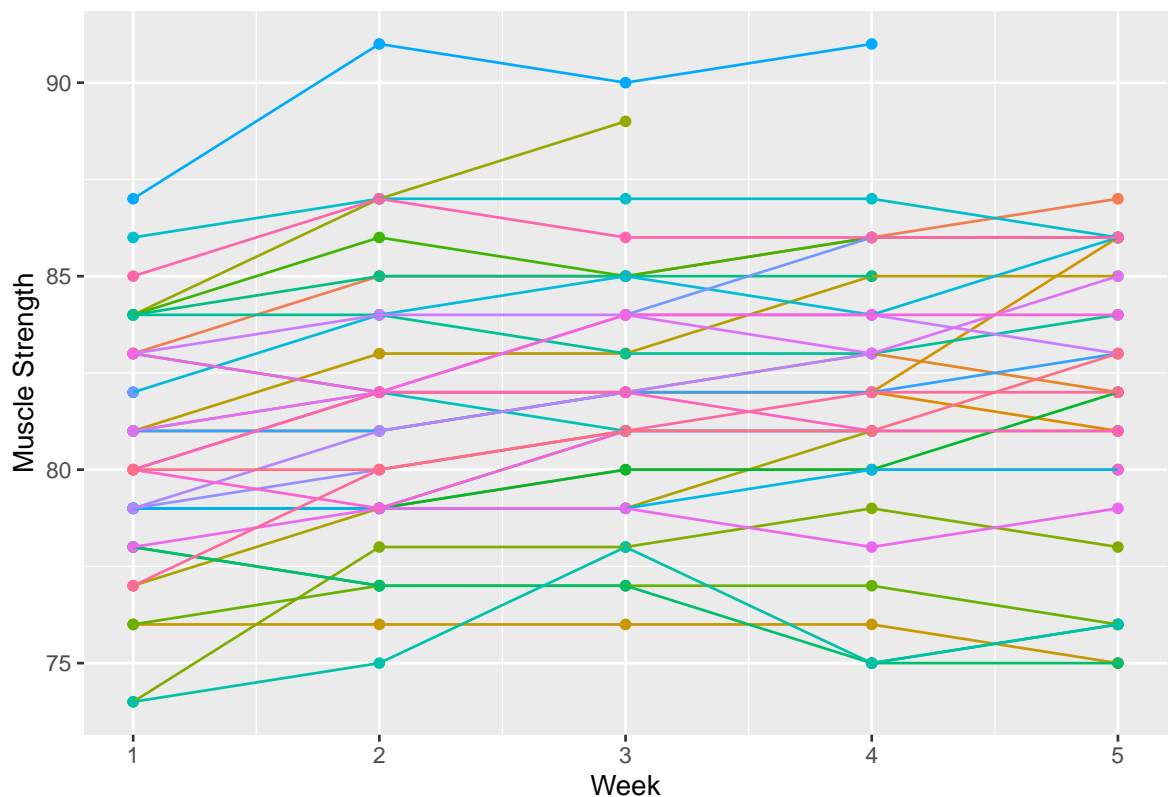
2g)

```
long_exercise <- long_exercise %>%
  mutate(week_numeric = str_sub(week, 5, 6),
         week_numeric = as.numeric(as.factor(week_numeric))) %>%
  relocate(week_numeric, .after = week)

long_exercise %>%
  ggplot(aes(x = week_numeric, y = muscle_strength,
            group = id, color = factor(id))) + geom_point(show.legend = FALSE) +
  geom_line(show.legend = FALSE) + labs(x = "Week", y = "Muscle Strength")
```

```
## Warning: Removed 12 rows containing missing values (geom_point).
```

```
## Warning: Removed 8 row(s) containing missing values (geom_path).
```



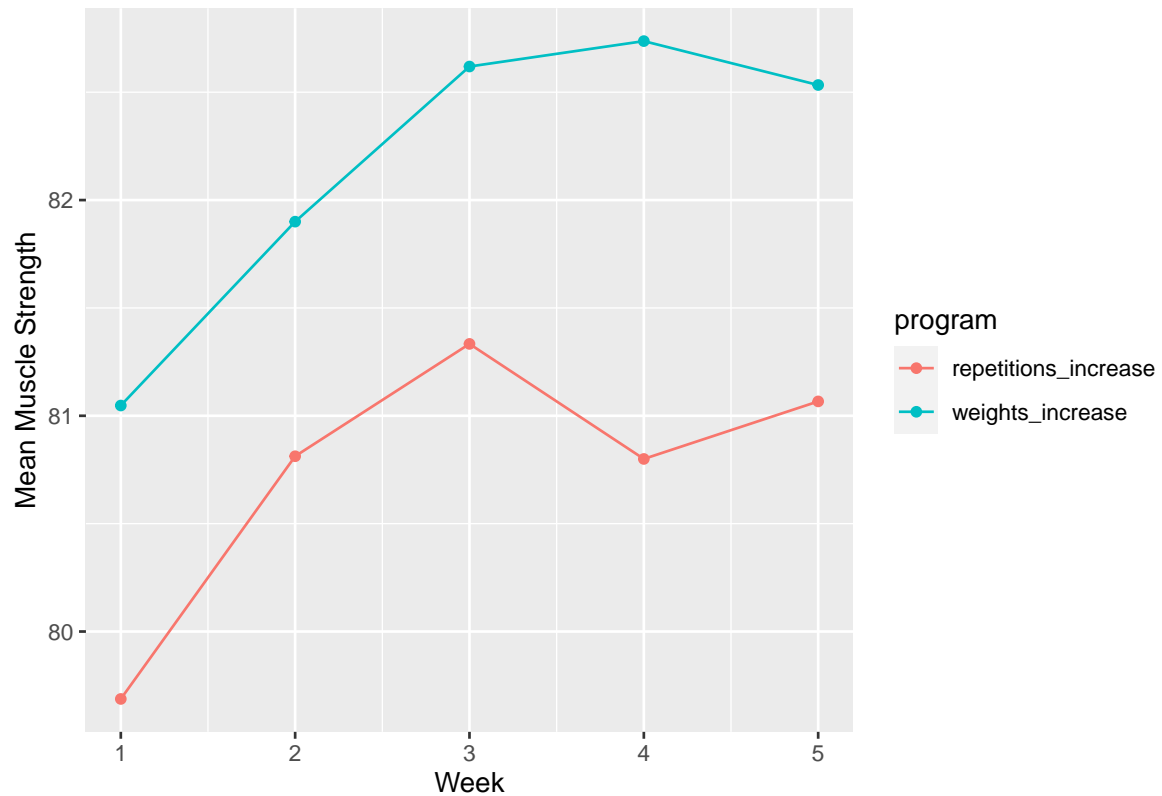
There isn't any fixed trend in the time plot above, some increase across weeks and some decrease. The time trends are all over the place.

2h)

```
long_exercise %>%
  group_by(week_numeric, program) %>%
  summarize(mean_muscle_strength = mean(muscle_strength, na.rm = TRUE)) %>%
```

```
ggplot(aes(x = week_numeric, y = mean_muscle_strength, color = program)) + geom_point() +  
geom_line() +  
labs(x = "Week", y = "Mean Muscle Strength")
```

'summarise()' has grouped output by 'week_numeric'. You can override using the
'.groups' argument.



The mean muscle strength for both groups increase as the weeks increase, therefore, there is an increase in the time trend.