

## RELATIONSHIP BETWEEN $\lambda_g$ and $\lambda_0$ .

**Objective:** To provide the relation

$$\frac{1}{\lambda_g^2} - \frac{1}{\lambda_a^2} = \frac{1}{(2a)^2}$$

where  $\lambda_a$  is the wavelength in free space,  $\lambda_g$  is the wavelength in waveguide and 'a' is the broad dimension of the waveguide.

### Theory:

The best way to prove this relationship is to measure  $\lambda_g$  and  $\lambda_a$  and then plot the values of  $(1/\lambda_a)^2$  against the corresponding values of  $(1/\lambda_g)^2$ . This should result in a straight line graph which cuts the  $(1/\lambda_a)^2$  axis at a value equal to  $(1/2a)^2$ . If this graph allows the determination of a value of width of the broad wall of the guide which agrees with the actual value as measured by Calipers then this surely is a proof of the validity of the relationship expressed in the above equation.

To measure the waveguide wavelength,  $\lambda_g$ , standing waves are produced by improperly terminating the waveguide. Secondly, the radiation is allowed to leave the waveguide and the wavelength of the standing wave in free space ( $\lambda_a$ ) is compared with the wavelength in the waveguide ( $\lambda_g$ ). To produce standing wave in the waveguide and in the air, a horn is attached to the waveguide and a sheet of metal is placed a certain distance away from the horn. The electromagnetic radiation will then leave the waveguide via the horn into the air. It will be reflected from the sheet of metal and produce a standing wave between the horn and the sheet with a wavelength,  $\lambda_a$ . As the reflected wave will re-enter the waveguide there will be a standing wave produced in the waveguide but with a wavelength  $\lambda_g$ .

If the sheet is moved relative to the horn keeping its plane at right angles to the axis of the waveguide the standing wave will move. Therefore, the signal at the stationary probe of the standing wave detector will vary as the standing wave moves past it. The distance moved by the sheet to repeat the output on the meter (i.e. to have the probe at the ext corresponding position on the standing wave) is half a free space wavelength  $\lambda_a/2$ . The voltage of the sanding wave must always be at a minimum at the sheet because it is a good conductor. Consequently, moving the sheet moves the pattern. Therefore, when the sheet has moved a distance  $\lambda_a/2$ , the voltage at the stationary probe of the standing wave detector will be repeated. A measurement of the amount of movement of the sheet determination  $\lambda_a/2$  at particular frequency.

To determine the guide wavelength  $\lambda_g/2$  at the same frequency all that is necessary is to kept the sheet still and move the standing wave detector probe. The patter will remain stationary and the probe will explore that pattern in the waveguide which repeats every half guide wavelength  $\lambda_g/2$ . Recording the distance between two adjacent minima by noting the reading on the scale of the sanding wave detector gives  $\lambda_g/2$ .

Now knowing  $\lambda_g/2$  and  $\lambda_a/2$  at one frequency, these values are recorded and the whole experiment is repeated at a new frequency. This procedure is repeated for measurement at a number of frequencies. The values of  $(1/\lambda_g)^2$  and  $(1/\lambda_a)^2$  for each frequency are plotted and from the intersection of the graph with the  $1/\lambda_a^2$  axis a value of the inside broad dimension of the waveguide can be obtained, and compared with the measured value.

### Pre-Experiment Quiz

1. Derive the relation  $\frac{1}{\lambda_g^2} = \frac{1}{\lambda_a^2} - \frac{1}{(2a)^2}$  for a rectangular waveguide.
2. What is the cut-off wavelength for a rectangular waveguide?
3. What modification, if any, may be required in the relation in question 1, for a circular waveguide?

4. Rewrite the relation in question 1 so that it holds good for any mode supported by a rectangular waveguide.

**Procedure:**

1. The experimental arrangement to be made is shown in Fig.1

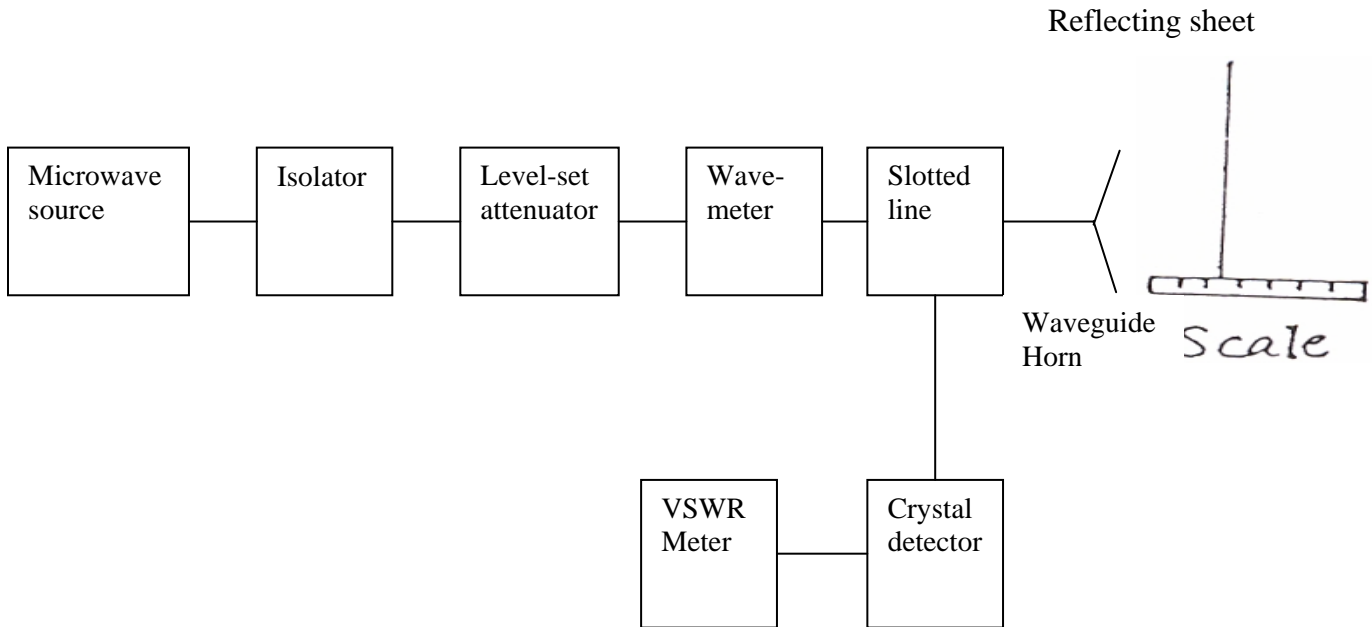


Fig.1 Experimental arrangement for measuring  $\lambda_g$  and  $\lambda_a$

2. Microwave signal generator is turned on and set at, say 9 GHz. The frequency may be measured using the wavemeter and its calibration chart.
3. The metal sheet is placed about 20 cms. from the waveguide horn.
4. Leaving the slotted-line probe fixed in one position, slowly move the metal sheet towards the horn until the probe output is a minimum. Do this 2-3 times and mark an average location of the sheet corresponding to the minimum output. Let the distance of the sheet at this location be  $x_1$  cm from some reference point along the normal to the sheet (towards the horn). Now, gradually move the sheet towards the horn till a minimum output reading, as before, is obtained. Let the sheet now

be at a distance  $x_2$  cms from the reference. Similarly, for successive minima,  $x_3, x_4$  etc. can be noted. So, at this frequency

$$\frac{\lambda_a}{2} = x_1 - x_2 = x_3 - x_4 = \frac{x_4 - x_1}{3} \text{ etc.}$$

5. Leaving the sheet fixed in this position, move the probe in the slotted line and obtain  $\lambda_g/2$  as the separation between successive minima. Record these values of frequency,  $\lambda_a$  and  $\lambda_g$  in table.
6. Change the frequency in small steps, say 200 MHz. Measure the corresponding  $\lambda_a$  and  $\lambda_g$ . Do this to cover a frequency range of, say, 9-11 GHz.
7. Plot a graph of  $\frac{1}{\lambda_g}2$  (y-axis) vs.  $\frac{1}{\lambda_a}2$  (x-axis). The intersection of the graph with x-axis equals  $1/(2a)^2$ , enabling one to arrive at an estimate of a. This estimate may be compared with the actual value.

### Post Experiment Quiz

1. What care may be taken to improve the accuracy of measurement of  $\lambda_a$  and  $\lambda_g$ ?
2. Can one utilize maxima values instead of minima values of the standing wave pattern?
3. Can one use a plane dielectric sheet in place of the metal sheet?
4. List some source of error which may cause a discrepancy between the estimated and measured value of a, the broad dimension of the waveguide.