

Assignment - I

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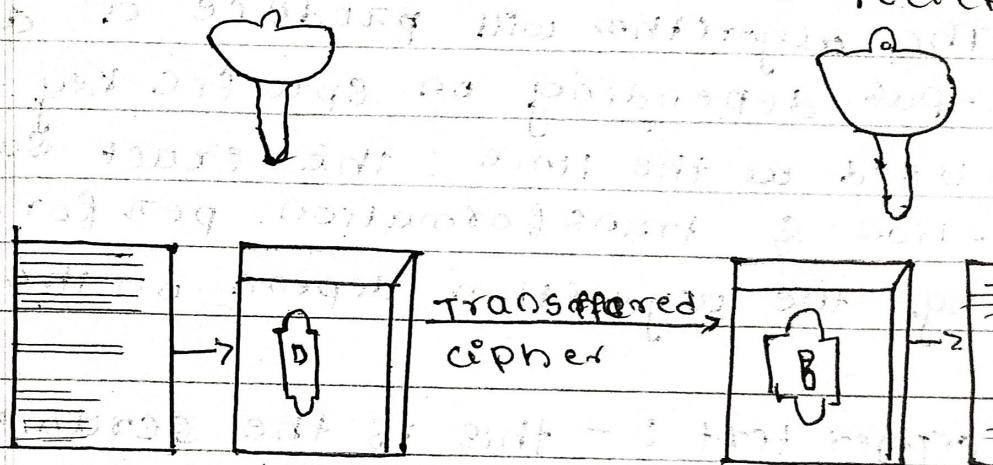
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1) Define cryptography & explain symmetric cipher model.?

→ It is a technique for providing a communication using confidentiality, integrity and security.

Symmetric cipher model :-

Secret key shared by sender and recipient



plaintext → encryption algorithm → cipher → decryption algorithm → plaintext
(eg. DES) (reverse of encryption algorithm)

A symmetric encryption scheme have five ingredients. They are:

plain text: This is the original intelligible message or data that is fed into the algorithm as input.

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Encryption algorithm :- The encryption algorithm performs various substitution and transformation on the plain text.

Secret key :- The secret key is also input to the encryption algorithm the key is a value independent of the plain text & of the algorithm.

The algorithm will produce a different output depending on specific key being used at the time. The exact substitution & transformation performed by the algorithm depends on the key.

Cipher text :- This is the scrambled message produced as output. It depends on the plain text and the secret key. For given message two different key will produce two different cipher texts.

The cipher text is an apparently random stream of data and as it stands is unintelligible.

Decryption algorithm : This is essential. The encryption algorithm run in

reverse it take the cipher text and the secret key and produces original plain text.

Q2) Explain Hill cipher and apply it to encrypt plain text = pay more money

with $K = \begin{bmatrix} 17 & 17 & 5 \\ 21 & 18 & 21 \\ 2 & 2 & 9 \end{bmatrix} \mod 26$

pay (15, 0, 24)

$$(C_1, C_2, C_3) = (15, 0, 24) \begin{bmatrix} 17 & 17 & 5 \\ 21 & 18 & 21 \\ 2 & 2 & 9 \end{bmatrix} \mod 26$$

$$= \begin{bmatrix} 15 \times 17 + 0 \times 21 + 24 \times 2 \\ 15 \times 17 + 0 \times 18 + 24 \times 2 \\ 15 \times 5 + 0 \times 21 + 24 \times 9 \end{bmatrix} \mod 26$$

$$= [303, 303, 531] \mod 26$$

$$= [17, 17, 11]$$

$$= R, R, L$$

mod (12, 14, 17)

$$= (12, 14, 17) \begin{bmatrix} 17 & 17 & 5 \\ 21 & 18 & 21 \\ 2 & 2 & 9 \end{bmatrix} \mod 26$$

$$\begin{aligned}
 &= [12 \times 17 + 14 \times 21 + 17 \times 2] \\
 &= [12 \times 17 + 14 \times 18 + 17 \times 2] \bmod 26 \\
 &= [12 \times 5 + 14 \times 21 + 17 \times 19] \\
 &= [532, 490, 677] \bmod 26
 \end{aligned}$$

$$\text{EMO} = [u, 12, 14]$$

$$\begin{aligned}
 &= [u, 12, 14] \cdot \begin{bmatrix} 17 & 17 & 5 \\ 21 & 18 & 21 \\ 2 & 2 & 19 \end{bmatrix} \bmod 26
 \end{aligned}$$

$$\begin{aligned}
 &= [u \times 17 + 12 \times 21 + 14 \times 2] \\
 &= [u \times 17 + 12 \times 18 + 14 \times 21] \bmod 26 \\
 &= [u \times 5 + 12 \times 21 + 14 \times 19]
 \end{aligned}$$

$$\begin{aligned}
 &= [348, 312, 583] \bmod 26 \\
 &= [10, 0, 18]
 \end{aligned}$$

= K.A.S

$$\text{key} = (13, u, 0)$$

$$\begin{aligned}
 &= (13, u, 0) \cdot \begin{bmatrix} 17 & 17 & 5 \\ 21 & 18 & 21 \\ 2 & 2 & 19 \end{bmatrix} \bmod 26
 \end{aligned}$$

$$\begin{aligned}
 &= \left[13 \times 17 + 14 \times 21 + 12 \times 24 \right] \\
 &\quad \left[13 \times 17 + 14 \times 18 + 12 \times 21 \right] \bmod 26 \\
 &\quad \left[13 \times 2 + 14 \times 2 + 12 \times 19 \right] \\
 \\
 &= [353, 341, 605] \bmod 26 \\
 &= (15, 317) \\
 &= (P, D, h)
 \end{aligned}$$

Ciphertext = RRLMWBKAS PDB

Another interesting multiletter cipher is Hill cipher developed by mathematician Lester Hill in 1929. The encryption algorithm takes in successive plain text letters and substitutes for them m cipher text letters. The substitutions are determined by a linear equations in which each character is assigned a numeric value ($a=0, b=1, \dots, z=25$). For $m=3$ the system can be described as followed: $c = kp \bmod 26$ where c = ciphertext, k = key, and p = plain text.

Q4) Explain Feistel encryption and decryption in detail.

→ Feistel cipher is the execution of two or more simple cipher in sequence in such a way that the final or product is cryptographically stronger than any of the component ciphers.

(F.E.S.T.E.L)

Feistel encryption (F.E.S.T.E.L)

- * The inputs to the encryption algorithm are a plaintext block of length 20 bits and a key k . The plaintext block is divided into two halves L_0 and R_0 .
- * The two halves of the data pass through n rounds of the data processing and then combine to produce the ciphertext block.
- * Each round i has inputs L_{i-1} and R_{i-1} derived from the previous round as well as subkey k_i derived from overall key k .
- * The subkey k_i are different from k and from each other.

Feistel decryption :-

- * The process of decryption with a Feistel cipher is essentially the same as encryption process.

- * The rule is as follows: use the ciphertext as input to the algorithm but use the subkeys k_i in reversed order
- * That is use k_0 in first round, k_{n-1} in the second round ... so on until k_1 is used in last round
- * The output of first round of the decryption process is equal to a 32-bit swap of the input to the 16th round of encryption process.
- * First consider encryption process

$$LE_{16} = RE_{15}$$

$$RE_{16} = LE_{15} \times F(RE_{15}, k_{16})$$

$$\text{On decryption side. } LD_1 = RD_0 = LE_{16} = \\ RE_{15}$$

$$RD_1 = LD_0 \times F(RE_{15}, k_{16})$$

$$= RE_{16} \times F(RE_{15}, k_{16})$$

$$= [(LE_{15} \times F(RE_{15}, k_{16})) \times F(RE_{15}, k_{16})]$$

= The XOR has the following properties:

$$[A \times B] \times C = A \times [B \times C] \quad D \times 0 = 0$$

$$E \times 0 = E$$

Then $LD_1 = RE_{15}$ and $RD_1 = LE_{15}$. The O/P of first round of decryption processor is $LE_{15} \parallel RE_{15}$ which is

32-bit swap of ip to 16th round

of encryption

for ith iteration of encryption algo

$$\text{with } \text{LE}_i = \text{RE}_i - I$$

$$\text{RE}_i = \text{LG}_i - 1 \times F(\text{RG}_i - 1, \text{R}_i)$$

rearranging terms, $\text{RE}_i - 1 = \text{LG}_i$

$$\text{LG}_i - 1 = \text{RG}_i \times F(\text{RG}_{i-1}, \text{R}_i)$$

$$\text{RG}_i \times F(\text{LG}_i, \text{R}_i) = \text{IP}$$

initial value of IP = 0x00000000

values of R_i = 0x00000000

values of LG_i = 0x00000000

values of RG_i = 0x00000000

values of IP = 0x00000000

last step of IP = 0x00000000

final calculation of IP = 0x00000000

values of R_i = 0x00000000

values of LG_i = 0x00000000

values of RG_i = 0x00000000

values of IP = 0x00000000

last step of IP = 0x00000000

values of R_i = 0x00000000

values of LG_i = 0x00000000

values of RG_i = 0x00000000

values of IP = 0x00000000

last step of IP = 0x00000000

values of R_i = 0x00000000

values of LG_i = 0x00000000

values of RG_i = 0x00000000

③ Explain Playfair cipher, and its rules for the following example :-

Ex:- Keyword: "MONARCHY" plain text:

a) ATTACK b) CRYPTOGRAPHY

→ A playfair algorithm is based on the use of 5x5 matrix of letters connected using a keyword.

Rules : Diagram

* Same row: if both letters are in same row replace each letter to its right

* Same column: if both letters are in same column replace each with below letter

* Rectangle: if letters form a rectangle replace each letter in same row but at the corner

a) Keyword: MONARCHY

plain text: ATTACK

M	O	N	A	R
C	H	Y	B	D
E	F	G	I	T
Z	P	Q	S	T
U	V	W	X	Z

Diagram: AT TA CR
RS SR DE

b) CRYPTOGRAPHY

M	O	N	A	R	I	S
C	H	I	X	B	D	E
G	F	Q	P	E	J	K
L	P	Q	S	T	U	V
U	V	W	X	Z	Y	A

Diagram: CR and XP TO AR, AP, HX
DM, HO, VP, RN, OS, YB

7) List and explain the block cipher design principles

→ There are three critical aspects of block cipher design:

- i) The number of rounds: the greater the number of rounds, the more difficult it is to perform encryption analysis - DES even for a relatively weak F.

+ The creation should be that the number of rounds is chosen so that known cryptanalytic efforts require greater effort than a simple brute-force key search attack

* If DES had 15 or fewer rounds, differential cryptanalysis would require less effort than brute-force key.

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ii) Design of Function F :-

- * The function F provides the element S of confusion in all feistel cipher, want it to be difficult to "unscramble" the substitution performed by F.
- * One obvious criterion is that F be nonlinear. The more nonlinear F, the more difficult any type of ~~cryptanalysis~~ will be.
- * One of the most intensive areas of research in the field of symmetric block ciphers is that of S-box design. It would like any change to the input vector to an S-box to result in random-looking changes to the output. The relationship should be non-linear and difficult to approximate with linear functions.

iii) Key Scheduling :-

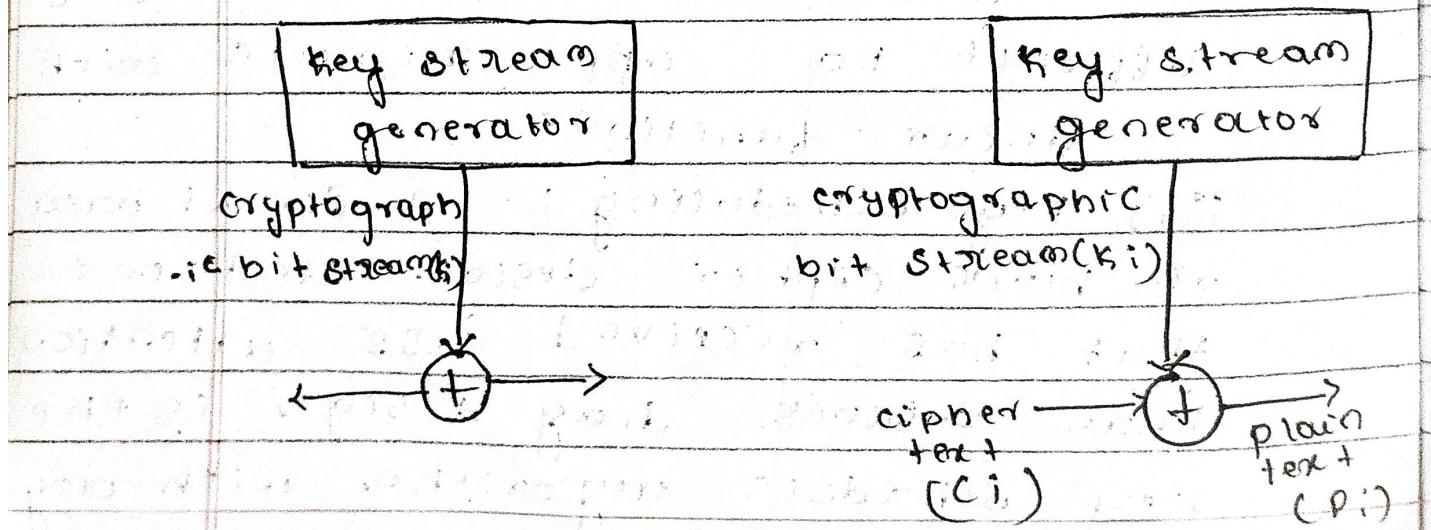
A final area of block cipher design and one that has received less attention than S-block design is the key schedule algorithm with any

feistel block cipher. The key schedule is used to generate a subkey for each round. * would like to select subkeys to minimize the difficulty of reducing individual subkeys and difficulty of working back to main key. The key schedule should guarantee key cipher text & strict available criterion and bit independence criterion.

8) Explain vernam cipher and OTP.

* The ultimate defense against such a cryptanalysis is to choose a keyword that is as long as the plaintext and has no statistical relationship to it.

* Such a system was introduced by AT&T engineer named Gilbert Vernam in 1918.



The system can be expressed succinctly as follows.

$$C_i = P_i \oplus K_i$$

where $P_i = i^{\text{th}}$ binary digit of plaintext

$K_i = i^{\text{th}}$ binary digit of key.

$C_i = i^{\text{th}}$ binary digit of ciphertext

\oplus = exclusive - or generated by per-

forming the bitwise XOR of the plaintext and key. Because of the properties of XOR, decryption simply involves the same bitwise operation:

$$P_i = C_i \oplus K_i$$

One-time pad

- * The key is to be used to encrypt and decrypt a single message, and then is discarded.

- * Each new message requires a new key of the same length as the new message. Such a scheme known as a one-time pad is unbreakable.

- * The one-time pad offers complete security, but in practical has two fundamental difficulties.

- i) There is the practical problem of making large quantities.

- ii) There is the practical problem of making large quantities.

of random keys.

ii) even more daunting is the problem of key distribution and protection. For every message to be sent, a key of equal length is needed by both sender and receiver.

10. List the difference b/w conventional and public key encryption.

Conventional

- Needed to work:
 - i. The same algorithm with the same key is used for encryption and decryption
 - ↳ the sender and receiver must share algorithm & key

public key

- needed to work:
 - i. One algorithm is used for encryption & related algorithm for decryption with a pair of keys. one for encryption and one for decryption
 - ↳ the sender and receiver must each have one of the matched pair of keys.

- Needed for security
 - ↳ the key must be kept secret
 - ↳ one of the two keys must be kept secret

- | | |
|--|--|
| * it must be impossible or at least impractical to decipher a message if the key is kept secret | * it must be impossible or at least impractical to decipher a message if the key is kept secret |
| * knowledge of the algorithm plus one samples of cipher text must be insufficient to determine the key | * knowledge of the algorithm plus one samples of cipher text must be insufficient to determine the other key |