

## Project 1 – Algorithm 4 Pseudocode

```
MAX-SUBARRAY-LINEAR( $A$ )
   $n = A.length$ 
   $max-sum = -\infty$ 
   $ending-here-sum = -\infty$ 
  for  $j = 1$  to  $n$ 
     $ending-here-high = j$ 
    if  $ending-here-sum > 0$ 
       $ending-here-sum = ending-here-sum + A[j]$ 
    else  $ending-here-low = j$ 
       $ending-here-sum = A[j]$ 
    if  $ending-here-sum > max-sum$ 
       $max-sum = ending-here-sum$ 
       $low = ending-here-low$ 
       $high = ending-here-high$ 
  return ( $low, high, max-sum$ )
```

The variables are intended as follows:

- $low$  and  $high$  demarcate a maximum subarray found so far.
- $max-sum$  gives the sum of the values in a maximum subarray found so far.
- $ending-here-low$  and  $ending-here-high$  demarcate a maximum subarray ending at index  $j$ . Since the high end of any subarray ending at index  $j$  must be  $j$ , every iteration of the for loop automatically sets  $ending-here-high = j$ .
- $ending-here-sum$  gives the sum of the values in a maximum subarray ending at index  $j$ .

The first test within the for loop determines whether a maximum subarray ending at index  $j$  contains just  $A[j]$ . As we enter an iteration of the loop,  $ending-here-sum$  has the sum of the values in a maximum subarray ending at  $j - 1$ . If  $ending-here-sum + A[j] > A[j]$ , then we extend the maximum subarray ending at index  $j - 1$  to include index  $j$ . (The test in the if statement just subtracts out  $A[j]$  from both sides.) Otherwise, we start a new subarray at index  $j$ , so both its low and high ends have the value  $j$  and its sum is  $A[j]$ . Once we know the maximum subarray ending at index  $j$ , we test to see whether it has a greater sum than the maximum subarray found so far, ending at any position less than or equal to  $j$ . If it does, then we update  $low$ ,  $high$ , and  $max-sum$  appropriately.