

1. **(20 points)** Consider a three-layer feedforward neural network with *two* input neurons, *two* hidden neurons, and *two* output neurons, as illustrated below. The activation function of the hidden layer and the output layer is the *Sigmoid* function

$$f(x) = \frac{1}{1+e^{-x}} .$$

Given the initial model  $\mathbf{w} = \{w_{11}^{(1)}, w_{12}^{(1)}, w_{21}^{(1)}, w_{22}^{(1)}, w_{11}^{(2)}, w_{12}^{(2)}, w_{21}^{(2)}, w_{22}^{(2)}\} = \{0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8\}$ , where  $\{w_{11}^{(1)}, w_{12}^{(1)}, w_{21}^{(1)}, w_{22}^{(1)}\}$  correspond to the input-to-hidden layer weights and  $\{w_{11}^{(2)}, w_{12}^{(2)}, w_{21}^{(2)}, w_{22}^{(2)}\}$  correspond to the hidden-to-output layer weights. Suppose *Stochastic Backpropagation Algorithm* is used to train the neural network, and the randomly chosen training example is  $\mathbf{x}^1 = (3, -5)^t$  with  $\mathbf{t}_1 = (1, 0)$ . What is the learned model  $\mathbf{w}$  after training the neural networks? (Learning rate  $\eta = 1$ )

