1. **Objective Function:**

• The function $f(x,y)=((x)2+y-11)2+((y)2+x-7)2f(x,y)=((x)^2+y-11)^2+((y)^2+x-7)^2f(x,y)=((x)^2+y-11)^2+((y)^2+x-7)^2$ is defined. This function has several local minima.

2. Gradient Computation:

• The gradient of the function is approximated using finite differences.

3. **Armijo Line Search:**

• The step size is adapted during the gradient descent process to ensure that the Armijo condition is met, providing a balance between sufficient decrease and step size reduction.

4. Gradient Descent:

- The algorithm iteratively updates the point (x1,x2)(x_1, x_2)(x1,x2) using the computed gradient and the step size from the line search.
- It tracks the path taken by the gradient descent and the corresponding function values.

5. Visualization:

- The code generates two plots:
 - 2D Contour Plot: Shows the contour lines of the function and the path taken by the gradient descent.
 - o **3D Surface Plot:** Shows the surface of the function and the descent path in 3D space.