# CS339: Abstractions and Paradigms for Programming

Environment Model

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### Problems brought by assignments

➤ Procedures are no longer mathematical functions!

- ➤ Substitution model of procedure application no longer works!
  - ➤ Reason: Variables are no longer simply names for expressions!



#### Substitution model revisited

#### > Evaluating a combination:

- ➤ Evaluate the subexpressions of the combination.
- ➤ Apply the value of the operator subexpression to the values of the operand subexpressions.

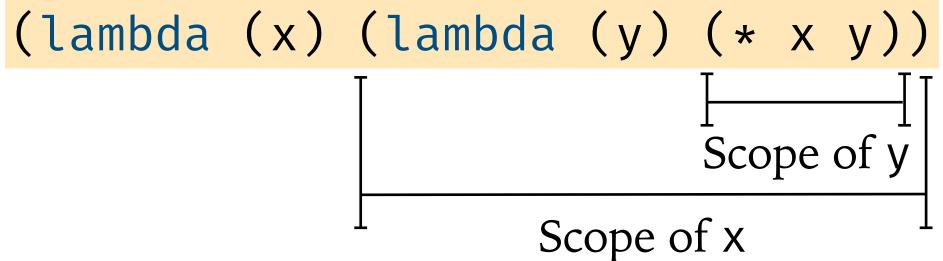
#### > Applying a procedure:

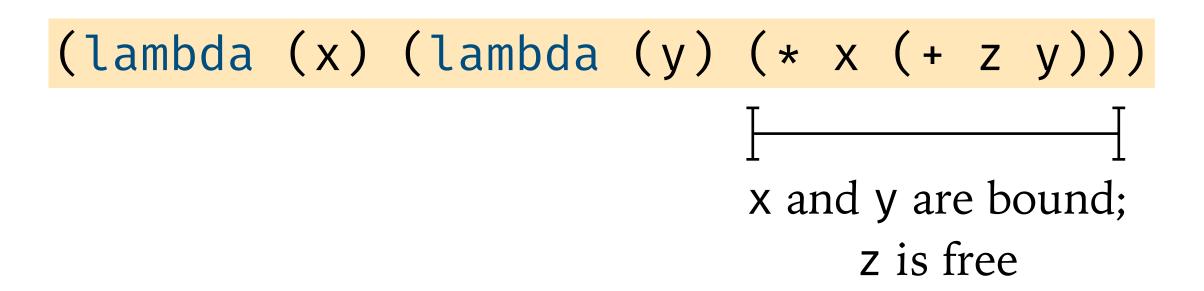
➤ To apply a compound procedure to arguments, evaluate the body of the procedure with each formal parameter replaced by the corresponding actual argument.



# Bindings and scope revisited

This lambda binds 'x' binds 'y'





The only way to create a binding is via a lambda!



#### Lambda — The Ultimate Binder

```
(let ((var1 expr1)
                                     ((lambda (var1 var2)
       (var2 expr2))
                                          <body>)
   <body>)
                                          expr1 expr2)
                                         (define foo
   (define (foo x)
                                           (lambda (x)
     <body>)
                                             <body>))
(define (foo x)
                                      (define (foo x)
                                        (let ((var expr))
  (define (var expr))
                                          <body>))
    <body>)
```



# The Environment Model



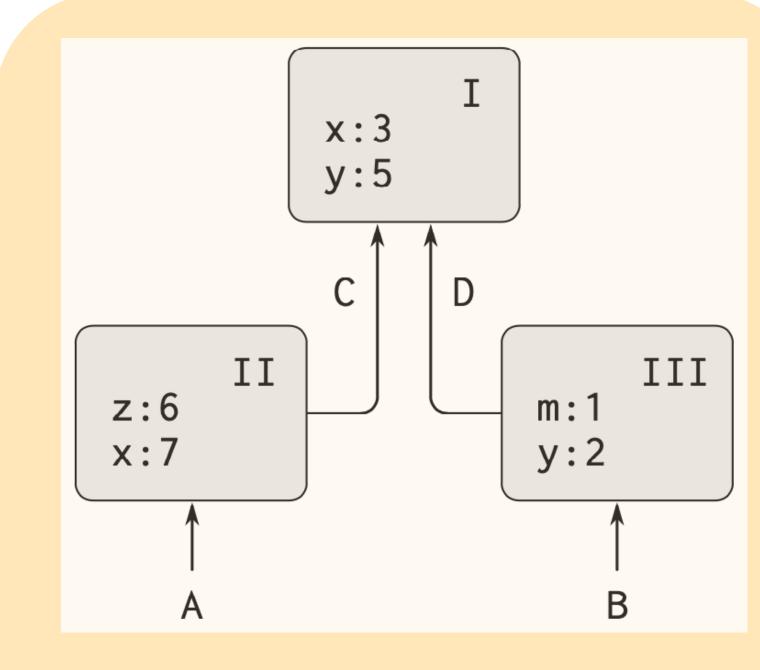
#### Frames and environments

I, II, III: Frames

#### Environment 'A':

• x: 7, y: 5, z: 6

• m: unbound



Environments as chains of frames

• z: unbound

A, B, C, D: Environments

Environment 'B':

• x: 3, y: 2, m: 1

#### Environments 'C', 'D':

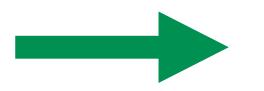
• x: 3, y: 5

• z, m: unbound

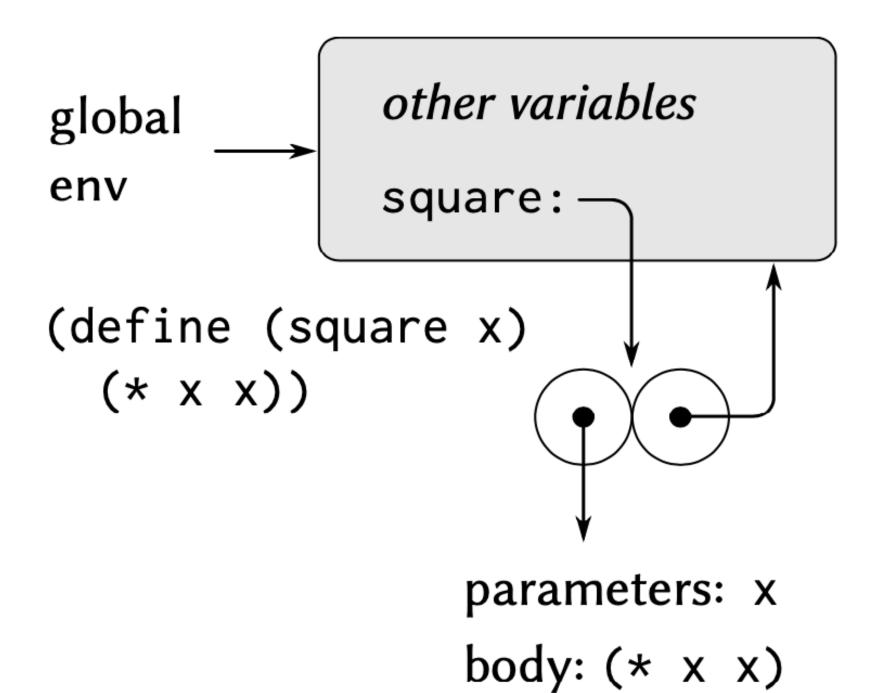


# Evaluating procedure definitions

```
(define (square x)
  (* x x))
```



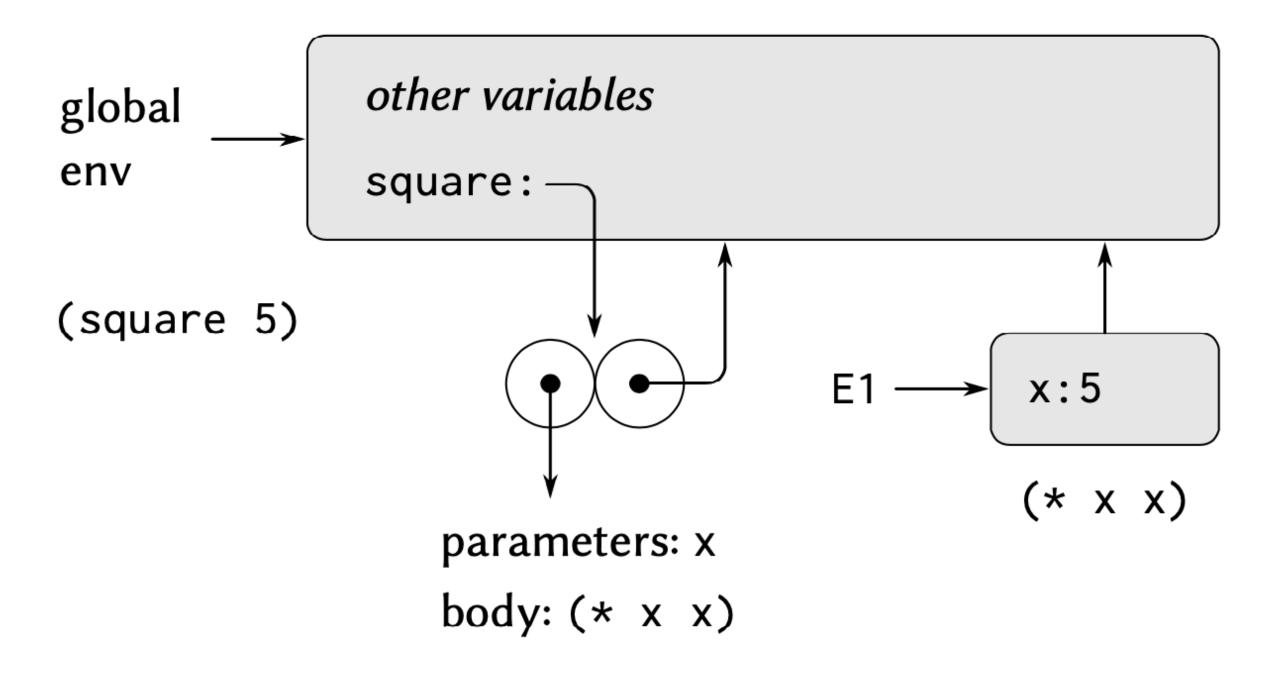
```
(define square
  (lambda (x) (* x x)))
```





# Evaluating procedure applications

```
(define (square x)
  (* x x))
> (square 5)
```



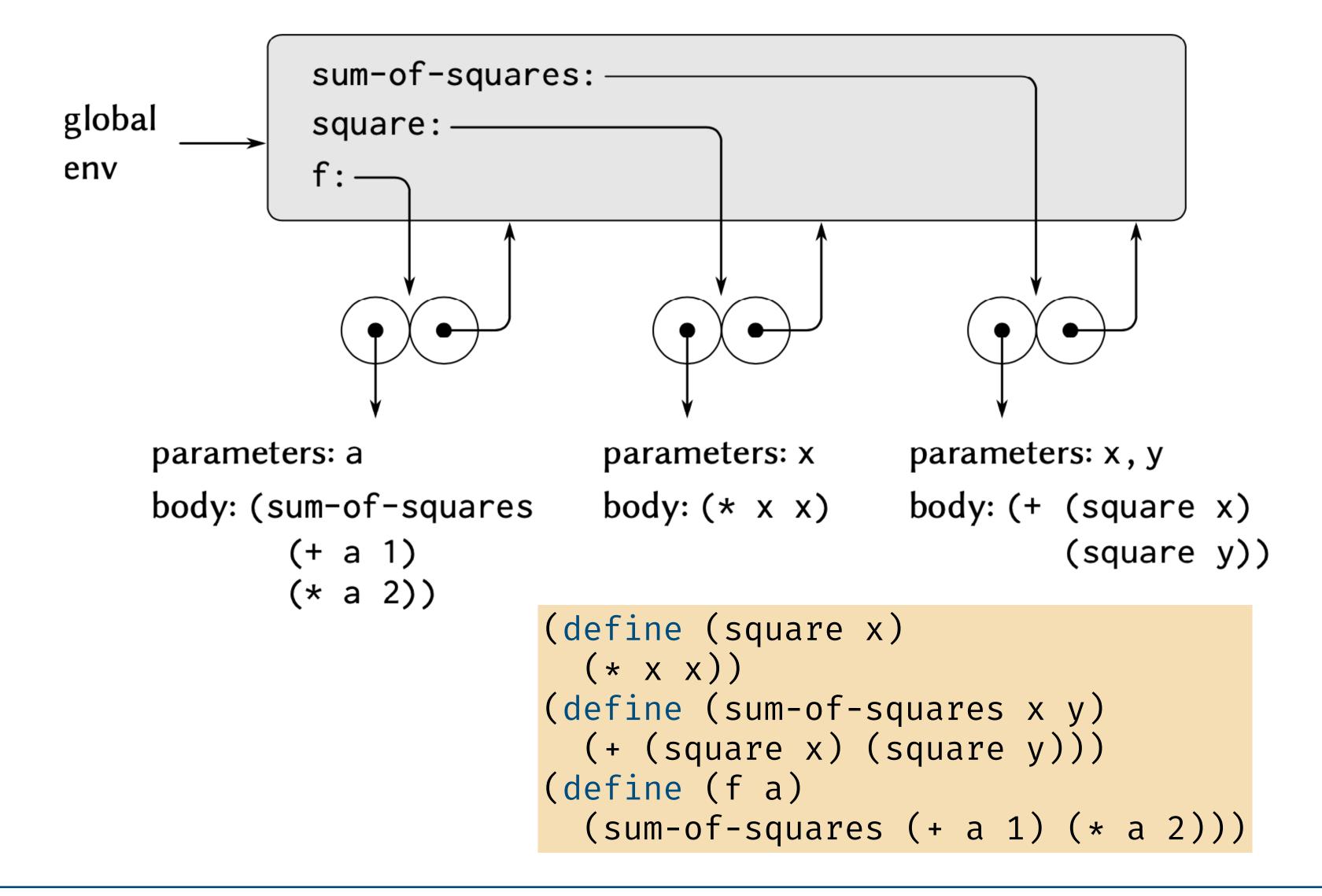


# The Environment Model: Summary

- ➤ Evaluating a combination: Same as the substitution model
  - ➤ Evaluate the subexpressions of the combination.
  - ➤ Apply the value of the operator subexpression to the values of the operand subexpressions.
- ➤ Evaluating a procedure definition:
  - ➤ Create a procedure object by evaluating a lambda-expression relative to a given environment.
- ➤ Evaluating a procedure application:
  - ➤ Create a new environment containing a frame that binds the parameters to the arguments, and then evaluate the body of the procedure in the new environment.

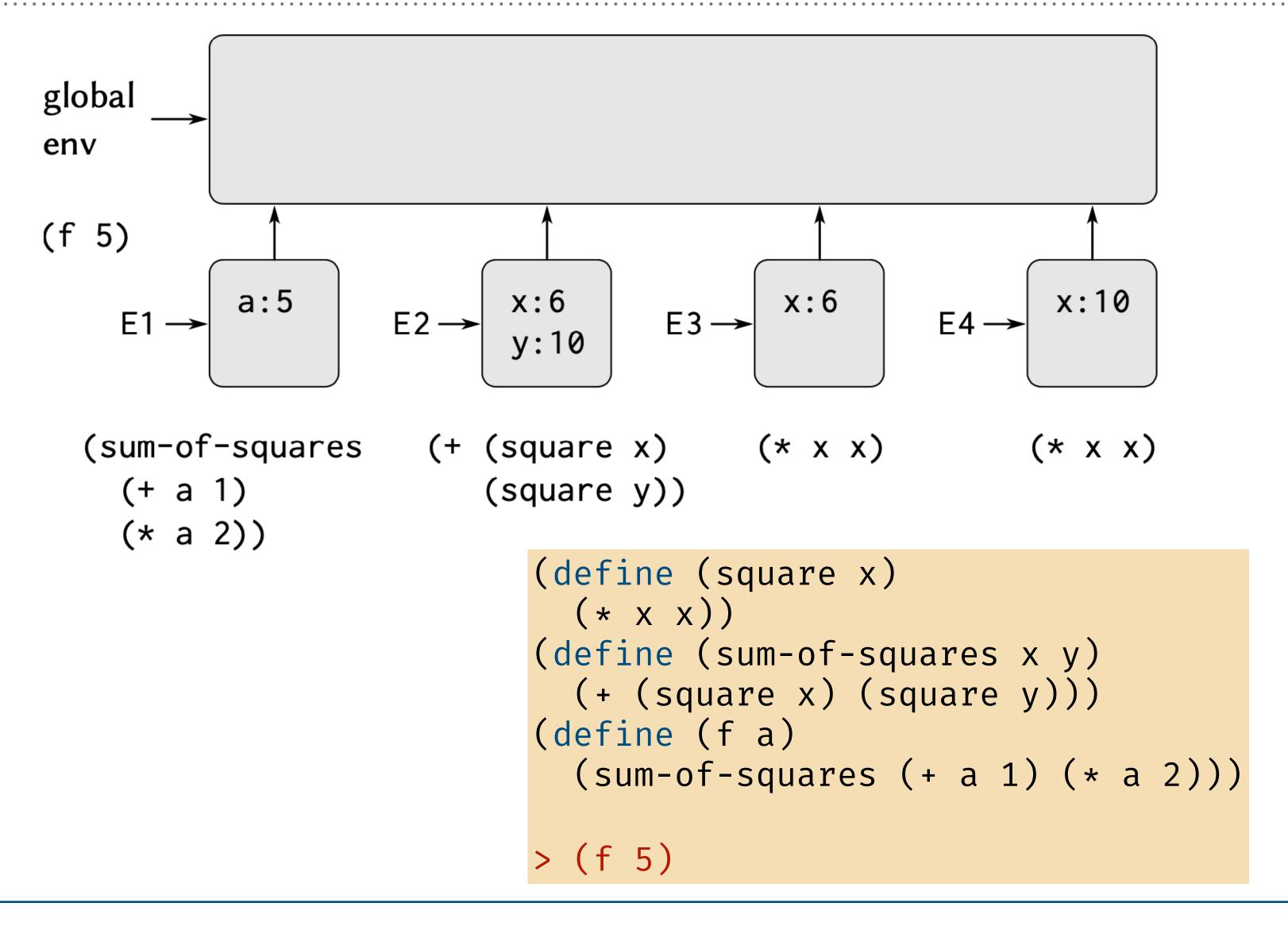


# Extended example 1: Definition





### Extended example 1: Application





#### EE2 Def: Local states in frames

```
global
           make-withdraw:
env
  parameters: balance
  body: (lambda (amount)
          (if (>= balance amount)
              (begin (set! balance (- balance amount))
                     balance)
              "insufficient funds"))
 (define (make-withdraw balance)
   (lambda (amount)
      (if (>= balance amount)
        (begin (set! balance (- balance amount))
               balance)
        "insufficient funds")))
```



### EE2 App1

```
make-withdraw: -
global
env
            W1: —
                           balance: 100
                                         parameters: balance
                                         body: ...
parameters: amount
body: (if (>= balance amount)
          (begin (set! balance (- balance amount))
                 balance)
          "insufficient funds")
         (define W1 (make-withdraw 100))
```

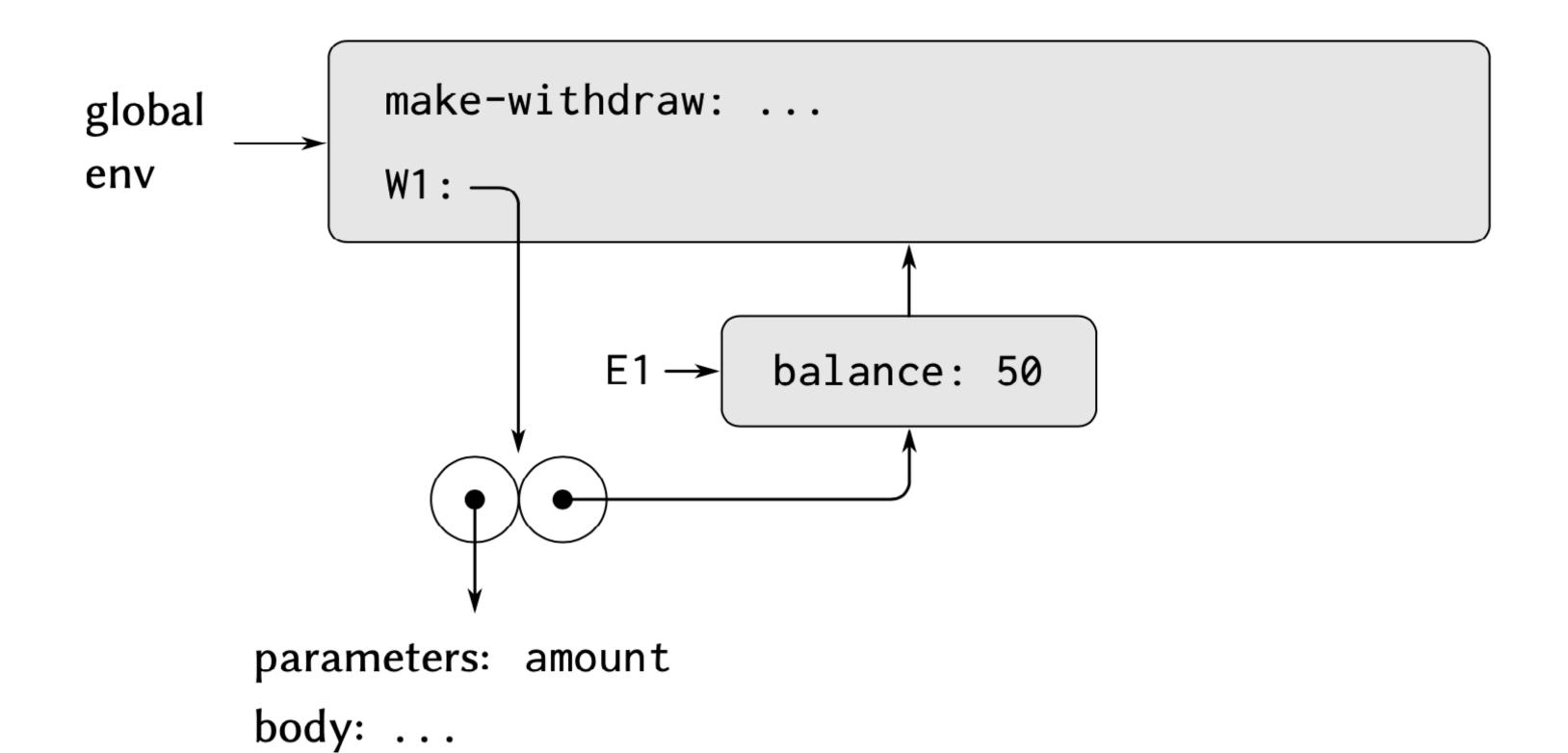


# EE2 App1 (Cont.)

```
make-withdraw: ...
global
env
             W1: —
                                               Here is the balance
                              balance: 100
                                               that will be changed
                                               by the set!
                                       amount: 50
                         (if (>= balance amount)
parameters: amount
                             (begin (set! balance
body: ...
                                           (- balance amount))
                                    balance)
                             "insufficient funds")
                         > (W1 50)
```



# EE2 App1 (Cont.)



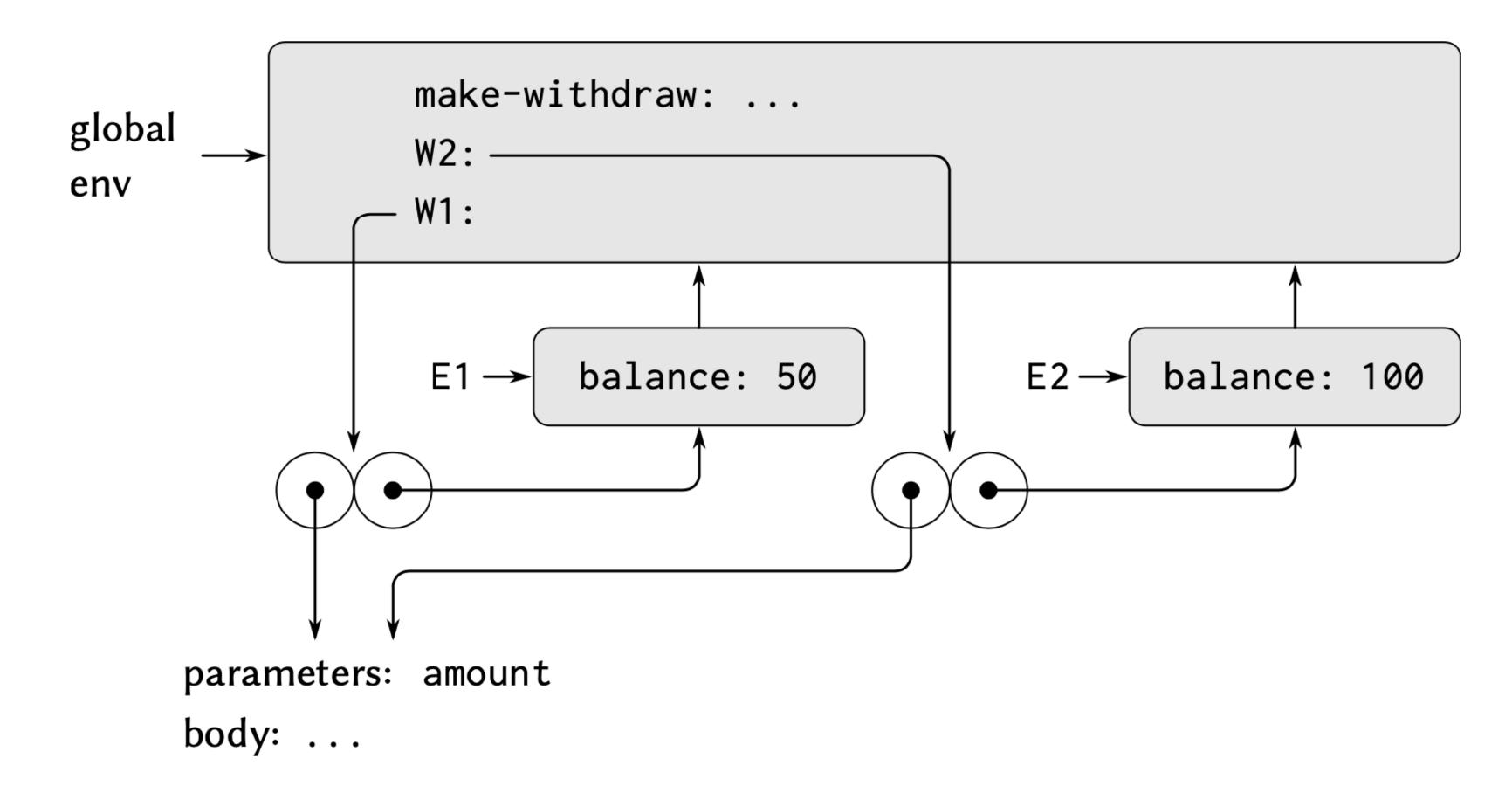
After (W1 50)



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# EE2 App2



(define W2 (make-withdraw 100))



#### Internal Definitions

> (sqrt 2)

```
global
             sqrt:
env
                                        x:2
                                        good-enough?: -
                                        improve: ...
parameters: x
                                        sqrt-iter: ...
body: (define good-enough? ...)
      (define improve ...)
      (define sqrt-iter ...)
      (sqrt-iter 1.0)
                                guess: 1
                                                parameters: guess
                           call to sqrt-iter
                                                body: (< (abs ...)
                                         guess:
                                    call to good-enough?
```

