Quantum Teleportation Solutions

Vishal Bysani

June 2024

1 Quantum Teleportation

The task is to teleport an arbitrary qubit state $|\psi\rangle = \alpha|0\rangle + \beta|1\rangle$ from Alice to Bob with the help of only classical communication and a previously shared EPR state $|\Phi^+\rangle = \frac{1}{\sqrt{2}}(|00\rangle + |11\rangle)$ (each having one qubit). The teleportation protocol consists of four main steps:

- 1. Alice applies a CNOT gate on her two qubits, with $|\psi\rangle$ as the control qubit and her half of the entangled pair as the target qubit. She then applies a Hadamard gate to the control qubit.
- 2. Alice measures both qubits that she owns. She sends the measurement results to Bob.
- 3. Depending on the measurement results, Bob applies X and Z gates to his qubit.
- 4. The qubit in Bob's possession is now in the state $|\psi\rangle$.

2 Teleporting a Mixed State