

HW3

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Problem SET 1

Question 1:- What is the rank of the matrix A?

Ans :- The rank of a matrix is defined as

- (a) the maximum number of linearly independent column vectors in the matrix or
- (b) the maximum number of linearly independent row vectors in the matrix. Both definitions are equivalent.

```
A <- matrix(c(1,-1,0,5,2,0,1,4,3,1,-2,-2,4,3,1,-3),nrow=4,ncol=4)
```

```
4
```

```
## [1] 4
```

```
# Calculating rank of Matrix by using rankMatrix function of Matrix package.  
require(Matrix)
```

```
## Loading required package: Matrix
```

```
rankMatrix(A)[1]
```

```
## [1] 4
```

Both Answers match , hence Rank of matrix A is 4. As it is a full matrix and all 4 rows/columns are linearly independent of each other hence Rank is 4.

Question 2:- Given an $m \times n$ matrix where $m > n$, what can be the maximum rank? The minimum rank, assuming that the matrix is non-zero?

Answer :- a) The maximum Rank for $m \times n$ where $m > n$ will be n if all the n columns are linearly independent.
b) Minimum Rank for $m \times n$ where $m > n$ will be 1 as the matrix is non-zero so it will have 1 linear independent columns.

Question 3:- What is the rank of matrix B?

Answer :- The RANK of matrix B is 1, as row 2 is equal to row 1 * 3 . And row 3 is equal to row 1 times 2. Hence we have only one linear independent row. Hence Rank is 1. Next step we will calculate the rank of matrix B using r function rankMatrix to prove it.

```
B <- matrix (c(1,3,2,2,6,4,1,3,2),nrow=3, ncol=3)  
rankMatrix(B)[1]
```

```
## [1] 1
```

Hence proved that Rank of B is 1.

Problem SET 2

Question :-

Answer :- Answer by hand is attached as pdf(Solution_Problem_Set_HW3.pdf to cuny hw submission site) , herein R we will try to prove the same with r functions.

```
library(pracma)
```

```
## Warning: package 'pracma' was built under R version 3.5.3
```

```
##
```

```
## Attaching package: 'pracma'
```

```
## The following objects are masked from 'package:Matrix':
```

```
##
```

```
##      expm, lu, tril, triu
```

```
A <- matrix(c(1,0,0,2,4,0,3,5,6),nrow=3,ncol=3)
```

```
A
```

```
##      [,1] [,2] [,3]
```

```
## [1,]    1    2    3
```

```
## [2,]    0    4    5
```

```
## [3,]    0    0    6
```

```
charpoly(A)
```

```
## [1]    1 -11  34 -24
```

The values prove that our Characteristic polynomial is correct.

```
e <- eigen(A)
```

```
e$values
```

```
## [1]  6 4 1
```

This proves our eigen values are also correct

```
e$vectors
```

```
##      [,1]      [,2] [,3]
```

```
## [1,] 0.5108407 0.5547002    1
```

```
## [2,] 0.7981886 0.8320503    0
```

```
## [3,] 0.3192754 0.0000000    0
```

This proves our eigen vector values are also correct.