

Given 3 integers  $n$ ,  $a$  &  $b$  return  $\eta$ th magical no.  
 Since one no. may be very large return  $1e9+7\%$ .  
 A no. is magical if it is divisible by either  $a$  or  $b$ .

Test cases  $\eta=1, a=2, b=3$        $\eta=4, a=2, b=3$   
 $\text{ans} = 2$                                    $\text{ans} = 6$

Constraints:  $\eta \leq 1e9$        $a \leq b \leq 1e4$ .

Ans → We will use binary search as one such opn as one rel. of  $\eta$  & no. by to achieve  $O(\log n)$  time complexity.

Start of binary search range

$$\text{left} = \text{gcd}(a, b) * \eta$$

End of binary search range

$$\text{right} = \min(a, b) * n$$

Now, while ( $\text{left} \leq \text{right}$ ) we find

$$\text{mid} = (\text{right} - \text{left}) / 2 + \text{left}$$

$$d = \min(\text{mid} \% a, \text{mid} \% b)$$

$$k = (\text{mid} - d)$$

$$\text{curr} = k/a + k/b - k/\text{lcm}(a, b);$$

If ( $\text{curr} == n$ ) return  $\text{curr} \% (1e9 + 7)$ ;

else if ( $\text{curr} < n$ )  $\text{left} = \text{mid} + 1$ ;

else  $\text{right} = \text{mid} - 1$ ;

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