H.C.F. and L.C.M. of Numbers

COMMON FACTOR

A *common factor* of two or more numbers is a number which divides each of them exactly. For example, 4 is a common factor of 8 and 12.

HIGHEST COMMON FACTOR

Highest common factor of two or more numbers is the greatest number that divides each one of them exactly. For example, 6 is the highest common factor of 12, 18 and 24. Highest Common Factor is also called *Greatest Common Divisor* or *Greatest Common Measure*.

Symbolically, these can be written as H.C.F. or G.C.D. or G.C.M., respectively.

METHODS OF FINDING H.C.F.

I. Method of Prime Factors

Step 1 Express each one of the given numbers as the product of prime factors.

[A number is said to be a *prime number* if it is exactly divisible by 1 and itself, but not by any other number, e.g., 2, 3, 5, 7, etc. are prime numbers]

Step 2 Choose common factors.

Step 3 Find the product of these common factors. This is the required H.C.F. of given numbers.

Illustration 1: Find the H.C.F. of 70 and 90.

Solution: $70 = 2 \times 5 \times 7$

$$90 = 2 \times 5 \times 9$$

Common factors are 2 and 5.

 \therefore H.C.F. = 2 × 5 = 10.

Illustration 2: Find the H.C.F. of 3332, 3724 and 4508.

Solution: $3332 = 2 \times 2 \times 7 \times 7 \times 17$

 $3724 = 2 \times 2 \times 7 \times 7 \times 19$

 $4508 = 2 \times 2 \times 7 \times 7 \times 23$

 \therefore H.C.F. = 2 × 2 × 7 × 7 = 196.

Illustration 3: Find the H.C.F. of 360 and 132.

Solution: $360 = 2^3 \times 3^2 \times 5$

 $132 = 2^2 \times 3^1 \times 11$

 \therefore H.C.F. = $2^2 \times 3^1 = 12$.

Electration 4: If $x = 2^3 \times 3^5 \times 5^9$ and $y = 2^5 \times 3^7 \times 5^{11}$, find H.C.F. of x and y.

Solution: The factors common to both x and y are 2^3 , 3^5 and 5^9 .

$$\therefore \text{ H.C.F.} = 2^3 \times 3^5 \times 5^9.$$

II. Method of Division

A. For two numbers:

Step 1 Greater number is divided by the smaller one.

Step 2 Divisor of (1) is divided by its remainder.

Step 3 Divisor of (2) is divided by its remainder.

This is continued until no remainder is left.

H.C.F. is the divisor of last step.

Illustration 5: Find the H.C.F. of 3556 and 3444.

$$\begin{array}{r}
3444)\overline{3556}(1) \\
\underline{3444} \\
112)\overline{3444}(30) \\
\underline{3360} \\
84)112(1) \\
\underline{84} \\
28)84(3) \\
\underline{84} \\
344
\end{array}$$

 \therefore H.C.F. = 28.

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2.2 Chapter 2

B. For more than two numbers:

- Step 1 Any two numbers are chosen and their H.C.F. is obtained.
- Step 2 H.C.F. of H.C.F. (of (1)) and any other number is obtained.
- Step 3 H.C.F. of H.C.F. (of (2)) and any other number (not chosen earlier) is obtained. This process is continued until all numbers have been chosen. H.C.F. of last step is the required H.C.F.

Illustration 6: Find the H.C.F. of 13915, 9499 and 2553 by division method.

Solution:

Solution:

9499)
$$13915$$
 (1
9499) 4416) 9499 (2
8832) 667) 4416 (6
4002) 414) 667 (1
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9

Now, in the next step, we will find the H.C.F. of 23 and 2553.

$$\begin{array}{c}
23 \overline{\smash)2553} \ (111) \\
\underline{23} \\
25 \\
\underline{23} \\
\underline{23} \\
\underline{23} \\
\underline{\times}
\end{array}$$

Thus, H.C.F. of 13915, 9499 and 2553 = 23.

Illustration 7: Find the greatest possible length which can be used to measure exactly the lengths 7 m, 3 m 85 cm, 12 m 95 cm.

Solution: Required length

= (H.C.F. of 700, 385, 1295) cm = 35 cm.

COMMON MULTIPLE

A common multiple of two or more numbers is a number which is exactly divisible by each one of them.

For example, 32 is a common multiple of 8 and 16. $8 \times 4 = 32$

$$16 \times 2 = 32$$
.

LEAST COMMON MULTIPLE

The least common multiple of two or more given numbers is the least or lowest number which is exactly divisible by each of them.

For example, consider the two numbers 12 and 18.

Multiples of 12 are 12, 24, 36, 48, 60, 72, ...

Multiples of 18 are 18, 36, 54, 72, ...

Common multiples are 36, 72, ...

:. Least common multiple, i.e., L.C.M. of 12 and 18 is 36.

METHODS OF FINDING L.C.M.

I. Method of Prime Factors

- **Step 1** Resolve each given number into prime factors.
- **Step 2** Take out all factors with highest powers that occur in given numbers.
- Find the product of these factors. This Step 3 product will be the L.C.M.

Illustration 8: Find the L.C.M. of 32, 48, 60 and 320.

Solution: $32 = 2^5 \times 1$ $48 = 2^4 \times 3$ $60 = 2^2 \times 3 \times 5$ $320 = 2^6 \times 6$ \therefore L.C.M. = $2^6 \times 3 \times 5 = 960$.

II. Method of Division

- The given numbers are written in a line Step 1 separated by common.
- Step 2 Divide by any one of the prime numbers 2, 3, 5, 7, 11, ... which will divide at least any two of the given numbers exactly. The quotients and the undivided numbers are written in a line below the first.
- Step 3 Step 2 is repeated until a line of numbers (prime to each other) appears.
- Find the product of all divisors and numbers in the last line, which is the required L.C.M.

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Illustration 9: Find the L.C.M. of 12, 15, 20 and 54.

L.C.M. =
$$2 \times 2 \times 3 \times 5 \times 1 \times 1 \times 1 \times 9$$

= 540.

Note:

Before finding the L.C.M. or H.C.F., we must ensure that all quantities are expressed in the same

SOME USEFUL SHORTCUT METHODS

1. H.C.F. and L.C.M. of Decimals

- Make the same number of decimal places in all the given numbers by suffixing zero(s) if necessary.
- Step 2 Find the H.C.F./L.C.M. of these numbers without decimal.
- **Step 3** Put the decimal point (in the H.C.F./L.C.M. of Step 2) leaving as many digits on its right as there are in each of the numbers.

Illustration 10: Find the L.C.M. of 1.2, 0.24 and 6. **Solution:** The given numbers can be written as 1.20, 0.24 and 6.00.

Now, ignoring the decimal we find the L.C.M. of 120, 24 and 600.

L.C.M. = $2 \times 2 \times 2 \times 3 \times 5 \times 1 \times 5 = 600$ Thus, the required L.C.M. = 6.00, i.e., 6.

Illustration 11: Find the H.C.F. of 6.16 and 13. **Solution:** The given numbers can be written as 6.16 and 13.00.

Now, ignoring the decimals we find the H.C.F. of 616 and 1300.

H.C.F. of 616 and 1300 is 4. Thus, the required H.C.F. = 0.04.

2. L.C.M. and H.C.F. of Fractions

 $L.C.M = \frac{L.C.M. \text{ of the numbers in numerators}}{L.C.M. \text{ of the numbers in numerators}}$ H.C.F. of the numbers in denominators

Q.C.F. of the numbers in numerators L.C.M. of the numbers in denominators

Illustration 12: Find the L.C.M. of $\frac{2}{5}$, $\frac{3}{10}$ and $\frac{6}{25}$.

Solution: L.C.M. of numerators 2, 3 and 6 is 6. H.C.F. of denominators 5, 10 and 25 is 5.

Required L.C.M. = $\frac{\text{L.C.M. of Numerators}}{\text{H.C.F. of Denominators}}$

Illustration 13: Find the H.C.F. of $\frac{4}{9}$, $\frac{10}{21}$ and $\frac{20}{63}$

Solution: H.C.F. of numerators 4, 10 and 20 is 2. L.C.M. of denominators 9, 21 and 63 is 63.

 $\therefore \text{ Required H.C.F} = \frac{\text{H.C.F. of Numerators}}{\text{L.C.M. of Denominators}} = \frac{2}{63}$

Notes:

- 1. If the given set of numbers includes fractions as well as whole numbers, treat whole number too as fraction with 1 in its denominator.
- 2. The H.C.F. of a number of fractions is always a fraction, but the L.C.M. may be a fraction or an integer.

3. Product of two numbers

= L.C.M. of the numbers \times H.C.F. of the numbers

Illustration 14: The H.C.F. and the L.C.M. of any two numbers are 63 and 1260, respectively. If one of the two numbers is 315, find the other number.

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Solution: The required number

$$=\frac{\text{L.C.M.} \times \text{H.C.F.}}{\text{First Number}} = \frac{1260 \times 63}{315} = 252.$$

4. To find the greatest number that will exactly divide x, y and z.

Required number = H.C.F. of x, y and z.

Illustration 15: Find the greatest number that will exactly divide 200 and 320.

Solution: The required greatest number

= H.C.F. of 200 and 320 = 40.

5. To find the greatest number that will divide x, yand z leaving remainders a, b and c, respectively. Required number = H.C.F. of (x - a), (y - b) and (z-c).

Illustration 16: Find the greatest number that will divide 148, 246 and 623 leaving remainders 4, 6 and 11, respectively.

Solution: The required greatest number

= H.C.F. of
$$(148 - 4)$$
, $(246 - 6)$ and $(623 - 11)$, i.e., H.C.F. of 144 , 240 and $612 = 12$.

i.e., H.C.F. of 144, 240 and 612 = 12.

6. To find the least number which is exactly divisible by x, y and z. Required number = L.C.M. of x, y and z.

Illustration 17: What is the smallest number which is exactly divisible by 36, 45, 63 and 80?

Solution: The required smallest number

=
$$I_0$$
C M. of 36, 45, 63 and 80
= 5040

- 7. To find the least number which when divided by x, y and z leaves the remainders a, b and c, respectively. It is always observed that (x - a)= (y - b) = (z - c) = k(say)
 - \therefore Required number = (L.C.M. of x, y and z) k.

Illustration 18: Find the least number which when divided by 36, 48 and 64 leaves the remainders 25, 37 and 53, respectively.

Solution: Since, (36-25) = (48-37) = (64-53) = 11,

therefore, the required smallest number

$$= (L.C.M. \text{ of } 36, 48 \text{ and } 64) - 11$$

= $576 - 11 = 565$.

8. To find the least number which when divided by x, y and z leaves the same remainder r in each case.

Required number = (L.C.M. of x, y and z) + r.

Illustration 19: Find the least number which when divided by 12, 16 and 18, will leave in each case a remainder 5.

Solution: The required smallest number

$$= (L.C.M. of 12, 16 and 18) + 5$$

= 144 + 5 = 149.

- **9.** To find the greatest number that will divide x, y and z leaving the same remainder in each case.
 - (a) When the value of remainder r is given: Required number = H.C.F. of (x - r), (y - r)and (z-r).
 - (b) When the value of remainder is not given: Required number = H.C.F. of |(x - y)|, |(y - y)|(-z) and |(z-x)|

Illustration 20: Find the greatest number which will divide 772 and 2778 so as to leave the remainder 5 in each case.

Solution: The required greatest number

$$=$$
 H.C.F. of $(772 - 5)$ and $(2778 - 5)$

= 59.

Illustration 21: Find the greatest number which on dividing 152, 277 and 427 leaves equal remainder.

Solution: The required greatest number

$$=$$
 H.C.F. of $|(x - y)|$, $|(y - z)|$ and $|(z - x)|$

$$=$$
 H.C.F. of $|(152 - 277)|$, $|(277 - 427)|$ and

$$|(427 - 152)|$$

- **10.** To find the *n*-digit greatest number which, when divided by x, y and z,
 - (a) leaves no remainder (i.e., exactly divisible)

Step 1 L.C.M. of
$$x$$
, y and $z = L$

Step 2
$$\frac{L n\text{-digit greatest number}}{Remainder} = R$$

Step 3 Required number

$$= n$$
-digit greatest number $- R$

- (b) leaves remainder K in each case Required number
 - = (n-digit greatest number -R) + K.

Illustration 22: Find the greatest number of 4-digit number which, when divided by 12, 18, 21 and 28 leaves 3 as a remainder in each case.

Solution: L.C.M. of 12, 18, 21 and 28 = 252.

$$\begin{array}{r}
252\overline{\smash{\big)}9999} \ \ (39) \\
\underline{9828} \\
171
\end{array}$$

 \therefore The required number = (9999 - 171) + 3 = 9931.

Illustration 23: Find the greatest number of four digits which, when divided by 12, 15, 20 and 35 leaves no remainder.

Solution: L.C.M. of 12, 15, 20 and 35 = 420.

$$420)9999(23)$$

$$\frac{9660}{339}$$

The required number = 9999 - 339= 9663.

- 11. To find the *n*-digit smallest number which when divided by x, y and z
 - (a) leaves no remainder (i.e., exactly divisible)

Step 1 L.C.M. of
$$x$$
, y and $z = L$

Step 2
$$\frac{L n$$
-digit smallest number (

Step 3 Required number

- = n-digit smallest number + (L R).
- (b) leaves remainder *K* in each case. Required number = n-digit smallest number + (L - R) + K.

Illustration 24: Find the least number of four digits which is divisible by 4, 6, 8 and 10.

Solution: L.C.M. of 4, 6, 8 and 10 = 120.

$$120)1000(8)$$

$$\frac{960}{40}$$

The required number = 1000 + (120 - 40)

Illustration 25: Find the smallest 4-digit number, such that when divided by 12, 18, 21 and 28, it leaves remainder 3 in each case.

Solution: C.M. of 12, 18, 21 and 28 = 252.

$$252)1000 (3)$$

$$\frac{756}{244}$$

The required number = 1000 + (252 - 244) + 3= 1011.

EXERCISE-I

- 1. What is the H.C.F. of 27, 18 and 36?
 - (a) 7
- (b) 11
- (c) 9
- (d) None of these
- 2. Determine the L.C.M of $\frac{2}{5}$, $\frac{3}{10}$ and $\frac{6}{25}$.

- (d) None of these
- **3.** What is the L.C.M. of 25, 30, 35 and 40?
 - (a) 3800
 - (b) 4200
 - (c) 4400
 - (d) None of these

- **4.** What is the greatest number which divides 852, 1065 and 1491 exactly?
 - (a) 193
- (b) 183
- (c) 223
- (d) 213
- **5.** What is the H.C.F. of $\frac{4}{9}$, $\frac{10}{21}$ and $\frac{20}{30}$?

- (d) None of these
- 6. Find the least number which when divided by 16, 18, 20 and 25 leaves 4 as remainder in each case but when divided by 7 leaves no remainder.
 - (a) 8004
- (b) 13004
- (c) 18004
- (d) 18014

2.6 Chapter 2

7	Area of three fields is 165 m ² , 195 m ² and 85 m ² ,
/٠	
	respectively. In each of the fields a flower bed of
	equal length has to be made. If flower bed in each
	of the fields is 3 m wide then what is the maximum
	length of the flower bed in each of the fields?
	() 7

(a) 7 m

(b) 9 m

(c) 5 m

(d) None of these

8. Find the greatest number which will divide 2112 and 2792 leaving the remainder 4 in each case.

(a) 78

(b) 68

(c) 65

(d) 63

9. The H.C.F. of two numbers is 12 and their difference is 12. The numbers are:

(a) 66, 78

(b) 70, 82

(c) 94, 106

(d) 84, 96

10. A merchant has 435 litres, 493 litres and 551 litres of three different kinds of milk. Find the least number of casks of equal size required to store all the milk without mixing.

(a) 51

(b) 61

(c) 47

(d) 45

11. Find the greatest number which will divide 25, 73 and 97 so as to leave the same remainder in each case.

(a) 12

(b) 18

(c) 24

(d) 32

12. The sum of two numbers is 216 and their H.C.F. is 27. The numbers are:

(a) 54, 162

(b) 108, 118

(c) 27, 189

(d) None of these

13. How often will five bells toll together in one hour if they start together and toll at intervals of 5, 6, 8, 12, 20 seconds, respectively?

(a) 29

(b) 30

(c) 31

(d) 120

14. Find the greatest number that will divide 964, 1238 and 1400 leaving remainders 41, 31 and 51, respectively.

(a) 71

(b) 81

(c) 61

(d) 73

15. Find the side of the largest square slabs which can be paved on the floor of a room 5 m 44 cm long and 3 m 74 cm broad.

(a) 56

(b) 42

(c) 38

(d) 34

16. The traffic lights at three different road crossings change after every 48 seconds, 72 seconds and 108 seconds, respectively. If they all change simultaneously at 8:20:00 hours; then they will again change simultaneously at:

(a) 8:27:12 hours

(b) 8:27:24 hours

(c) 8:27:36 hours

(d) 8:27:48 hours

17. The product of two numbers is 6760 and their H.C.F. is 13. How many such pairs can be formed?

(a) 2

(b) 3

(c) 4

(d) only one

18. Find the greatest number of four digits which when divided by 10, 15, 21 and 28 leaves 4, 9, 15 and 22 as remainders, respectively.

(a) 9654

(b) 9666

(c) 9664

(d) 9864

19. The number of prime factors in the expression $(6)^{10} \times (7)^{17} \times (11)^{27}$ is:

(a) 54

(b) 64

(c) 71

(d) 81

20. Find the greatest number which will divide 3962, 4085 and 4167 leaving the same remainder in each case.

(a) 37 (c) 41 (b) 39 (d) 43

21. A wholesale tea dealer has 408 kilograms, 468 kilograms and 516 kilograms of three different qualities of tea. He wants it all to be packed into boxes of equal size without mixing. Find the capacity of the largest possible box.

(a) 50

(b) 36

(c) 24

(d) 12

22. A room is 4 m 37 cm long and 3 m 23 cm broad. It is required to pave the floor with minimum square slabs. Find the number of slabs required for this purpose.

(a) 485

(b) 431

(c) 391

(d) 381

23. The least perfect square number which is divisible by 3, 4, 5, 6 and 8:

(a) 900

(b) 1200

(c) 2500

(d) 3600

24. Find the least number of five digits which when divided by 12, 16, 21, 36 and 40 leaves remainder 8 in each case.

(a) 10088

(b) 10072

(c) 10080

(d) None of these

25.	Three pieces of timber 42 m, 49 m and 63 m long
	have to be divided into planks of the same length.
	What is the greatest possible length of each plank?

(a) 7 m

(b) 14 m

(c) 42 m

(d) 63 m

26. Three men start together to travel the same way around a circular track of 11 kilometres in circumference.

Their speeds are 4, $5\frac{1}{2}$ and 8 Km/h, respectively.

When will they meet at the starting point?

(a) 11 hours

(b) 12 hours

(c) 23 hours

(d) 22 hours

27. Five bells begin to toll together and toll at intervals of 36, 45, 72, 81 and 108 seconds. After what interval of time will they keep on tolling together?

(a) 3240 seconds

(b) 3080 seconds

(c) 3140 seconds

(d) 3200 seconds

- **28.** Three different containers contain different quantities of mixture of milk and water, whose measurements are 403 Kg, 434 Kg and 465 Kg. What biggest measure must be there to measure all the different quantities exactly?
 - (a) 1 Kg

(b) 7 Kg

(c) 31 Kg

(d) 41 Kg

29. The L.C.M. and G.C.D. of two numbers are 1530 and 51, respectively. Find how many such pairs are possible?

(a) 2

(c) 4

(d) Only one

30. Find the least number of the digits which when divided by 63, 56 and 42 leaves remainder 1 in each case.

(a) 10082

(b) 10081

(c) 10001

31. The H.C.F. and L.C.M. of two numbers are 44 and 264, respectively. If the first number is divided by 2, the quotient is 44. The other number is:

(a) 33

(b) 66

(c) 132

(d) 264

32. The largest natural number which exactly divides the product of any four consecutive natural numbers, is:

(a) 6

(b) 12

(c) 24

(d) 120

33. Find the least number of six digits which is exactly divisible by 15, 21 and 28:

(a) 100480

(b) 100270

(c) 100380

(d) 100340

34. Find the greatest number of five digits which when divided by 12, 15, 21, 25 and 28 leaves 5, 8, 14, 18 and 21 as remainders, respectively.

(a) 98696

(b) 98700

(c) 97693

(d) 98693

35. What is the smallest number which when increased by 3 is divisible by 16, 24, 30 and 32?

(a) 480

(b) 475

(c) 472

(d) 477

36. The least number of square tiles required to cover the ceiling of a room 15 m 17 cm long and 9 m 2 cm broad, is:

(a) 656

(b) 738

(c) 814

37. Find the least number which when divided by 2, 3, 4, 5 and 6 leaves 1, 2, 3, 4 and 5 as remainders, respectively, but when divided by 7 leaves no remainder.

(a) 210

(b) 119

(c) 126

(d) 154

Find the greatest number of five digits which when divided by 4, 6, 10 and 15 leaves the same remainder 3 in each case.

(a) 99993

(b) 99063

(c) 90093

(d) 99963

39. Find the least number which is a multiple of 31 and when divided by 15, 24 and 32 leaves the remainders 2, 11 and 19, respectively.

(a) 2418

(b) 2387

(c) 2356

(d) 2325

40. Find the two largest numbers of four digits having 531 as their H.C.F.

(a) 9231, 9762

(b) 9027, 9558

(c) 9037, 9568

(d) 9127, 9658

41. Find the greatest number of five digits which becomes exactly divisible by 10, 12, 15 and 18 when 3769 is added to it.

(a) 99811

(b) 99911

(c) 98911

(d) 99011

42. Find the least number which when decreased by 11 is divisible by 14, 15, 21, 32 and 60.

(a) 4371

(b) 3271

(c) 3371

(d) 3360

2.8 Chapter 2

- **43.** Find the least number of five digits which when divided by 8, 12, 16 and 20 leaves remainders 1, 5, 9 and 13, respectively.
 - (a) 10003
- (b) 10093
- (c) 10073
- (d) 10013
- **44.** The H.C.F. of two numbers is 11 and their L.C.M. is 693. If one of the numbers is 77, find the other.
 - (a) 909
- (b) 119
- (c) 66
- (d) 99
- **45.** Find the greatest number of four digits which is exactly divisible by 24, 28, 30 and 35.
 - (a) 9225
- (b) 9240
- (c) 9250
- (d) 9260
- **46.** Find the greatest number of four digits which must be added to 5231 so that the final number becomes exactly divisible by 12, 15, 27, 32 and 40.
 - (a) 7929
- (b) 7829
- (c) 9729
- (d) 7729

- **47.** A heap of stones can be made up into groups of 21. When made up into groups of 16, 20, 25 and 45, there are 3 stones left in each case. How many stones at least can there be in the heap?
 - (a) 7203
- (b) 2403
- (c) 3603
- (d) 4803
- **48.** Find the greatest number of five digits which when divided by 8, 9 and 10 leaves 3 as remainder in each case.
 - (a) 99996
 - (b) 99723
 - (c) 99983
 - (d) None of these
- 49. What is the least number of cut pieces of equal length that can be cut out of two lengths 10 m 857 mm and 15 m 87 mm?
 - (a) 174
- (b) 172
- (c) 164
- (d) 184

EXERCISE-2 (BASED ON MEMORY)

- 1. The sum of two numbers is 45. Their difference is $\frac{1}{9}$ of their sum. Their L.C.M. is:
 - (a) 200
- (b) 250
- (c) 100
- (d) 150

[SSC (GL) Prol Examination, 2007]

- 2. The sum of the H.C.F. and L.C.M. of two numbers is 680 and the L.C.M. is 84 times the H.C.F. If one of the numbers is 56, then the other is:
 - (a) 84
- (b) 12
- (c) 8
- (d) 96

[SSC (GL) Prel. Examination, 2005]

- **3.** The L.C.M. and H.C.F. of the numbers 28 and 42 are in the ratio:
 - (a) 6:1
- (b) 2:3
- (c) 3:2
- (d) 7:2

[SSC (GL) Prel. Examination, 2000]

- **4.** The L.C.M. of two numbers is 1820 and their H.C.F. is 26. If one number is 130 then the other number is:
 - (a) 70
- (b) 1690
- (c) 364
- (d) 1264

[SSC (GL) Prel. Examination, 2002]

- **5.** H.C.F. and L.C.M. of two numbers are 7 and 140, respectively. If the numbers are between 20 and 45, the sum of the numbers is:
 - (a) 70
- (b) 77
- (c) 63
- (d) 56

[SSC (GL) Prel. Examination, 2003]

- **6.** The L.C.M. of two numbers is 14560 and their H.C.F. is 13. If one of them is 416, then the other is:
 - (a) 460
- (b) 455
- (c) 450
- (d) 446

[SSC (GL) Prel. Examination, 2002]

- 7. The ratio of two numbers is 3:4 and their H.C.F. is 4. Their L.C.M. is:
 - (a) 12
- (b) 16
- (c) 24
- (d) 48

[SSC (GL) Prel. Examination, 2002]

- **8.** The H.C.F. of two numbers is 16 and their L.C.M. is 160. If one of the numbers is 32, then other number is:
 - (a) 48
- (b) 80
- (c) 96
- (d) 112

[SI of Police Rec. Examination, 1997]

9.	9. The H.C.F. of two numbers is 24. The number, which							
	can be their L.C.M., is:							
	(a) 84	(b) 120						
	(c) 128	(d) 148						
	[Assitant's	Grade Examination, 1997]						
10.	. H.C.F. of 4 \times 27 \times 3125, 8 \times 9 \times 25 \times 7 and 16 \times							
	$81 \times 5 \times 11 \times 49$ is:							
	(a) 180	(b) 360						
	(c) 540	(d) 1260						
	[SI of Police Rec. Examination, 1997							
11.	1. The sum of two numbers is 528 and their H.C.F.							
	3. The number of suc	h pairs is:						
	(a) 2	(b) 3						
	(c) 4	(d) 5						
	[SI of Police Rec. Examination, 1997							
12.	The L.C.M. of two nur	nbers is 1920 and their H.C.F.,						
	is 16. If one of the n	umbers is 128, find the other						
	number.							
	(a) 204	(b) 240						
	(c) 260	(d) 320						
	[SI of Poli	ce Rec. Examination, 1997]						
13.	The H.C.F. and L.C.M	1. of two numbers are 11 and						
	385 respectively. If on	e number lies between 75 and						
	125, then that number	is:						
	(a) 77	(b) 88						
	(c) 99	(d) 110						
[SI Rec. COP Examination, 19								
14.	The sum of two numb	pers is 2000 and their L.C.M.						
	is 21879. The two nur	A \						
	(a) 1993, 7	(b) 1991, 9						
	(c) 1989, 11	(d) 1987, 13						
		Grade Examination, 1998						
15.	The L.C.M. of two nu	mbers is 495 and their H.C.F.						
	7/)~	vo numbers is 100 then their						
difference is:								
	(a) 10	(b) 46						
	(c) 70	(d) 90						
	3 7) Prel. Examination, 1999						
16.	ers is 225 and their H.C.F. is							
5. If one number is 25, the other number wil								
	(a) 5	(b) 25						
	(c) 45	(d) 225						

- 18. The L.C.M. of two numbers is 1820 and their H.C.F. is 26. If one number is 130 then the other number is:
 - (a) 70

(b) 1690

(c) 364

(d) 1264

[SSC (GL) Prel. Examination, 2002]

- 19. H.C.F. and L.C.M. of two numbers are 7 and 140, respectively. If the numbers are between 20 and 45, the sum of the numbers is:
 - (a) 70

(c) 63

(d) 56

[SSC (GL) Prel. Examination, 2003]

- 20. L.C.M. of two numbers is 495 and their H.C.F. is 5. If the sum of two numbers is 100 then their difference is:
 - (a) 10

(b) 46 (d) 90

(c) 70

[SSC (GL) Prel. Examination, 1999]

- 21. Philip, Tom and Brad start jogging around a circular field and complete a single round in 18 seconds, 22 seconds and 30 seconds, respectively. In how much time, will they meet again at the starting point?
 - (a) 3 minutes 15 seconds
 - (b) 21 minutes
 - (c) 16 minutes 30 seconds
 - (d) 12 minutes

[Indian Bank PO, 2011]

- 22. Amit, Sucheta and Neeti start running around a circular track and complete one round in 18 seconds, 24 seconds and 32 seconds, respectively. In how many seconds will the three meet again at the starting point if they all have started running at the same time?
 - (a) 196

(b) 288

(c) 324

(d) Cannot be determined

[Bank of India PO, 2010]

- 23. Three friends A, B and C start running around a circular stadium and complete a single round in 24 seconds, 36 seconds and 30 seconds, respectively. After how many minutes will they meet again at the starting point?
 - (a) 12

(b) 6

(c) 8

(d) 15

[IDBI PO, 2009]

24. Seema, Meena and Reena start jogging around a circular stadium and complete one round in 54 seconds, 42 seconds and 63 seconds, respectively. Approximately after how many minutes they will meet again at the starting point?

[SSC (GL) Prel. Examination, 2000]

[SSC (GL) Prel. Examination, 1999]

17. The H.C.F. of two numbers is 8. Which one of the

(b) 48

(d) 60

following can never be their L.C.M.?

(a) 24

(c) 56

2.10 Chapter 2

- (a) 8
- (b) 10
- (c) 3
- (d) 6

[Syndicate Bank PO, 2010]

25. L.C.M. and H.C.F. of two numbers x and y are 3 and 105, respectively. If x + y = 36, the value of $\frac{1}{x} + \frac{1}{x}$ is:

- (a) 1
- (b) $\frac{1}{6}$
- (c) $\frac{12}{315}$
- (d) $\frac{4}{35}$

[UPPCS, 2012]

- **26.** The greatest number, which when subtracted from 5834, gives a number exactly divisible by each of 20, 28, 32 and 35, is:
 - (a) 1120
- (b) 4714
- (c) 5200
- (d) 5600

[SSC (GL), 2010]

- **27.** H.C.F. and L.C.M. of two numbers are 8 and 48, respectively. If one of the numbers is 24, then the other number is:
 - (a) 48
- (b) 36
- (c) 24
- (d) 16

[SSC (GL.), 2010]

- **28.** Two numbers are in the ratio 3:4. Their L.C.M. is 84. The greater number is:
 - (a) 21
- (b) 24
- (c) 28
- (d) 84

[SSC (GL), 2010]

- **29.** H.C.F. and L.C.M. of two numbers are 12 and 924, respectively. Then the number of such pairs is:
 - (a) 0
- (b) 1
- (c) 2
- (d) 3

[SSC (GL), 2011]

- **30.** What is the least number which, when divided by 5, 6, 7, 8 gives the remainder 3 but is divisible by 9?
 - (a) 1463
- (b) 1573
- (c) 1683
- (d) 1793

[SSC (GL), 2011]

- **31.** L.C.M. of two numbers is 120 and their H.C.F. is 10. Which of the following can be the sum of those two numbers?
 - (a) 140
- (b) 80
- (c) 60
- (d) 70

[SSC (GL), 2011]

- **32.** The traffic lights at three different road crossings change after 24 seconds, 36 seconds and 54 seconds, respectively. If they, all change simultaneously at 10:15:00 am, then at what time will they again change simultaneously?
 - (a) 10:16:54 am
- (b) 10:18:36 am
- (c) 10:17:02 am
- (d) 10:22:12 am

[SSC (GL), 2011]

- **33.** Find the least number which when divided separately by 15, 20, 36 and 48 leaves 3 as remainder in each case.
 - (a) 183
- (b) 243
- (c) 483
- (d) 72

[SSC, 2014]

34. If the L.C.M. and H.C.F. of two expressions are $(x^2 + 6x + 8)(x + 1)$ and (x + 1), respectively and one

of the expressions is $x^2 + 3x + 2$, find the other.

- (a) $x^2 + 5x + 4$
- (b) $x^2 5x + 4$
- (c) $x^2 + 4x + 5$
- (d) $x^2 4x + 5$

[SSC, 2014]

- **35.** What is the smallest number by which 625 must be divided so that the quotient is a perfect cube?
 - (a) 125
- (b) 5
- (c) 2
- (d) 3

[SSC, 2014]

- **36.** Find the greatest number which exactly divides 200 and 320.
 - (a) 10
- (b) 20
- (c) 16
- (d) 40

[SSC, 2014]

- **37.** The greatest 4-digit number exactly divisible by 10, 15 and 20 is:
 - (a) 9990
- (b) 9960
- (c) 9980
- (d) 9995

[SSC, 2013]

- **38.** If the students of 9th class are arranged in rows of 6, 8, 12 or 16, no student is left behind. The possible number of students in the class is:
 - (a) 60
- (b) 72
- (c) 80
- (d) 96

[SSC, 2013]

39. If A and B are the H.C.F. and L.C.M., respectively of two algebraic expressions x and y, and A + B = x + y, then the value of $A^3 + B^3$ is:

- (a) $x^3 v^3$
- (b) x^{3}
- (c) y^3
- (d) $x^3 + v^3$

[SSC Assistant Grade III, 2013]

- **40.** The greatest number that divides 411, 684, 821 and leaves 3, 4 and 5 as remainders, respectively is:
 - (a) 254
- (b) 146
- (c) 136
- (d) 204

[SSC Assistant Grade III, 2013]

- **41.** Given: $\sqrt[3]{4}$, $\sqrt{3}$, $\sqrt[6]{25}$ and $\sqrt[12]{289}$, the greatest and least of them are respectively:
 - (a) $\sqrt[12]{289}$ and $\sqrt[3]{4}$
 - (b) $\sqrt{3}$ and $\sqrt[3]{4}$
 - (c) $\sqrt[6]{25}$ and $\sqrt{3}$
 - (d) $\sqrt[3]{4}$ and $\sqrt[6]{25}$

[SSC Assistant Grade III, 2012]

- **42.** In four consecutive prime numbers that are in ascending order, the product of the first three is 385 and that of the last three is 1001. The largest given prime number is:
 - (a) 11
- (b) 13
- (c) 17
- (d) 19

SSC, 2012

43. H.C.F. of $\frac{2}{3}$, $\frac{4}{5}$ and $\frac{6}{7}$ is:

- (a) $\frac{48}{105}$
- (b) $\frac{2}{105}$
- (c) $\frac{1}{105}$
- (d) $\frac{24}{105}$

[SSC, 2012]

- **44.** There are five bells which start ringing together at intervals of 3, 6, 9, 12 and 15 seconds respectively. In 36 minutes, how many times will the bells ring simultaneously?
 - (a) 13
- (b) 12
- (c) 6
- (d) 5

[SSC, 2012]

- **45.** Two numbers are in the ratio 5:6. If their H.C.F. is 4, then their L.C.M. will be:
 - (a) 90
- (b) 96
- (c) 120
- (d) 150

[SSC, 2010]

- **46.** A number, when divided successively by 4, 5 and 6, leaves remainders 2, 3 and 4 respectively. The least such number is:
 - (a) 50
- (b) 53
- (c) 58
- (d) 214

[SSC, 2010]

- **47.** The greatest number that divides 43, 91 and 183 so as to leave the same remainder in each case, is:
 - (a) 9
- (b) 8
- (c) 4
- (d) 3

[SSC, 2010]

ANSWER KEYS

Exercise-I

- 1. (c) 2. (a) 3. (b) 4. (d) 5. (c) 6. (c) 7. (c) 8. (b) 9. (d) 10. (a) 11. (c) 12. (c) 13. (c)
- 14. (a) 15. (d) 16. (a) 17. (a) 18. (a) 19. (b) 20. (c) 21. (d) 22. (c) 23. (d) 24. (a) 25. (a) 26. (d)
- 27. (a) 28. (c) 29. (c) 30. (b) 31. (c) 32. (c) 33. (c) 34. (d) 35. (d) 36. (e) 37. (b) 38. (d) 39. (b)
- **40.** (b) **41.** (b) **42.** (c) **43.** (c) **44.** (d) **45.** (b) **46.** (d) **47.** (a) **48.** (b) **49.** (d)

Exercise-2

- 1. (c) 2. (d) 3. (a) 4. (c) 5. (c) 6. (b) 7. (d) 8. (b) 9. (b) 10. (c) 11. (c) 12. (b) 13. (a)
- 14. (c) 15. (a) 16. (c) 17. (d) 18. (c) 19. (c) 20. (a) 21. (c) 22. (b) 23. (b) 24. (d) 25. (d) 26. (b)
- 27. (d) 28. (c) 29. (c) 30. (c) 31. (d) 32. (b) 33. (d) 34. (a) 35. (a) 36. (d) 37. (b) 38. (d) 39. (d)
- **40.** (c) **41.** (b) **42.** (b) **43.** (b) **44.** (a) **45.** (c) **46.** (c) **47.** (c)

EXPLANATORY ANSWERS

EXERCISE-I

1. (c) H.C.F. of 27, 18 and 36

$$\begin{array}{c|c}
18 & 27 & 1 \\
 \hline
 & 18 \\
 \hline
 & 9 & 18 & 2 \\
 \hline
 & 18 \\
 \hline
 & \times
\end{array}$$

∴ H.C.F. of 27 and 18 is 9 Now, H.C.F. of 9 and 36

9) 36 (4

∴ H.C.F. of 9 and 36 is 9

Therefore, the required H.C.F of 27, 18 and 36 is 9.

- **2.** (a) L.C.M. of $\frac{2}{5}$, $\frac{3}{10}$ and $\frac{6}{25}$
 - $= \frac{\text{L.C.M. of 2, 3 and 6}}{\text{H.C.F. of 5, 10 and 25}}$
 - \therefore L.C.M. of 2, 3 and 6 = 6

and, H.C.F. of 5, 10 and 25 = 5

- $\therefore \text{ Required L.C.M.} = \frac{6}{5}$
- - $\therefore \text{ Required L.C.M.} = 2 \times 5 \times 5 \times 3 \times 7 \times 4$ = 4200.
- **4. (d)** H.C.F. of 852 and 1065 is 213. H.C.F. of 213 and 1491 is 213.
- 5. (c) H.C.F. of $\frac{4}{9}$, $\frac{10}{21}$ and $\frac{20}{63}$
 - $= \frac{\text{H.C.F. of 4, 10 and 20}}{\text{L.C.M. of 9, 21 and 63}}$

 \therefore H.C.F. of 4, 10 and 20 = 2 and L.C.M. of 9, 21 and 63 = 63

- \therefore Required H.C.F. = $\frac{2}{63}$
- **6. (c)** L.C.M. of 16, 18, 20 and 25 is 3600.

Required number =
$$3600 \times K + 4$$

= $(7 \times 514 + 2)K + 4$
= $(7 \times 514)K + 2K + 4$

Now (2K + 4) is divisible by 7 for K = 5.

 $\therefore \text{ Required number} = 5 \times 3600 + 4$ = 18004.

7. (c) H.C.F. of 165, 195 and 85 will be maximum area of each of the flower beds.

H.C.F. of 165 and 195:

:. H.C.F. of 165 and 195 is 15

Also, now, H.C.F. of 15 and 85 is 5.

- **8. (b)** Subtract 4 from each of the numbers 2112 and 2792 and then take the H.C.F, i.e., H.C.F of 2108 and 2788.
- 9. (d) The difference of requisite numbers must be 12 and each one must be divisible by 12. So, the numbers are 84, 36.
- 10. (a) Since minimum number of casks are required, the size of the cask is greatest. Also the cask in three cases are of equal size. The size of the cask is the H.C.F. of 435, 493 and 551 which is 29.

Now, the number of casks required for storing the milk $= (493 + 435 + 551) \div 29 = 51$.

11. (c) 73 - 25 = 48

$$97 - 73 = 24$$

$$97 - 25 = 72$$

H.C.F. of 48, 24 and 72 is 24.

12. (c) Let the numbers be 27a and 27b

Then,
$$27a + 27b = 216$$
 or, $27(a + b) = 216$

or,
$$a + b = \frac{216}{27} = 8$$

 \therefore Values of co-primes (with sum 8) are (1, 7) and (3, 5)

So, the numbers are $(27 \times 1, 27 \times 7)$,

i.e., (27, 189).

13. (c) The time after which the bells will ring together is the L.C.M. of 5, 6, 8, 12 and 20 seconds, i.e., 120 seconds. The number of times they will toll together in one hour

$$= (3600 \div 120) + 1$$

= 30 + 1 = 31.

14. (a) 964 - 41 = 923

$$1238 - 31 = 1207$$

$$1400 - 51 = 1349$$

H.C.F. of 923 and 1207 is 71.

H.C.F. of 71 and 1349 is 71.

- 15. (d) The side of the square slab is the H.C.F. of 544 and 374 cm, i.e., 34.
- **16.** (a) Interval of change = (L.C.M. of 48, 72, 108) seconds = 432

So, the lights will change after every 432 seconds, i.e., 7 minutes and 12 seconds.

So, the next simultaneous change will take place at 8:27:12 hours.

17. (a) Let the numbers be 13x and 13y.

$$13x \times 13y = 6760$$

$$\therefore x \times y = 6760 \div (13 \times 13) = 40$$

Possible values of (x, y) are

(1, 40); (2, 20); (4, 10); (5, 8)

Only two acceptable values are (1, 40) and (5, 8).

- 18. (a) First, find the greatest number of four digits that is divisible by the L.C.M. of 10, 15, 21 and 28 and then subtract 6 from it to get the required number.
- 19. (b) Since 2, 3, 7, 11 are prime numbers and the given expression is $2^{10} \times 3^{10} \times 7^{17} \times 11^{27}$, the number of prime factors in the given expression is (10 + 10 + 17)+27) = 64.
- **20.** (c) 4085 3962 = 1234167 - 4085 = 824167 - 3962 = 205H.C.F. of 123, 82 and 205 is 41.
- 21. (d) The capacity of the box is H.C.F. of 408, 468 and 516, i.e., 12.
- **22.** (c) Length = 437 cmBreadth = 323 cm.

The side of the square slab is the H.C.F. of 437 and 323,

 \therefore Area of square slab = 19 cm × 19 cm = 361 cm²

The number of slabs = $\frac{\text{Area of the room}}{\text{Area of the slab}}$

$$= \frac{437 \times 323 \text{ cm}^2}{361 \text{ cm}^2}$$

$$= 391$$

23. (d) 2 | 3, 4, 5, 6, 8 2 3, 2, 5, 3,

L.C.M. of 3, 4, 5, 6, 8 = 120

Required number = $2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 5 \times 5$ = 3600

24. (a) Required number = the least number of 5 digits divisible by the L.C.M. of 12, 16, 21, 36, 40 + the remainder 8.

25. (a) Greatest possible length of each plank

$$= (H.C.F. \text{ of } 42, 49, 63) \text{ m} = 7 \text{ m}.$$

26. (d) Time for one revolution by each of three men

$$=\frac{11}{4}, \frac{11}{5\frac{1}{2}}, \frac{11}{8}$$
 hours

$$=\frac{11}{4}, \frac{2}{1}, \frac{11}{8}$$
 hours

.. The time when they will meet at the starting point

= L.C.M. of
$$\frac{11}{4}$$
, $\frac{2}{1}$, $\frac{11}{8}$ which is $\frac{22}{1}$, i.e., 22 hours.

27. (a) The interval of time is L.C.M. of the numbers 36, 45, 72, 81 and 108.

	_								
2	36,	45,	72,	81,	108				
2	18	45,	36,	81,	54				
3	9,	45,	18,	81,	27				
3	9,	45,	9,	81,	27				
3	3,	15,	3,	27,	9				
3	1,	5,	1,	9,	3				
	1,	5,	1,	3,	1				

idia Education L.C.M. (36, 45, 72, 108) = 3240.

- **28.** (c) Biggest measure = H.C.F. of (403, 434, 465) = 31 Kg.
- **29.** (c) Let the numbers be 51x and 51y where x and y are

Now,
$$51x \times 51y = 51 \times 1530$$

$$\therefore x \times y = 30$$

Possible pairs are (1, 30); (2, 15); (3, 10) and (5, 6).

30. (b) L.C.M. of 63, 56 and 42 is 504.

Least number of 5 digits divisible by 504:

$$\begin{array}{r}
504 \overline{\smash{\big)}\ 10000} (19) \\
\underline{-504} \\
4960 \\
\underline{-4536} \\
424
\end{array}$$

$$= 1000 + (504 - 424) = 10080$$

- :. Required number = 10080 + 1 = 10081.
- **31.** (c) First number = $2 \times 44 = 88$

Second number =
$$\frac{44 \times 264}{88}$$
 = 132.

- **32.** (c) $1 \times 2 \times 3 \times 4 = 24$
 - ∴ Required number = 24.

2.14 Chapter 2

33. (c) L.C.M. of 15, 21 and 28 is 420.

Least number of 6 digits = 100000

$$\begin{array}{r}
420 \overline{\smash{\big)}\ 100000} \ (238) \\
\underline{-840} \\
1600 \\
-1260 \\
\underline{-3360} \\
40
\end{array}$$

Remainder = 40.

- \therefore Least number = 100000 + (420 40)= 100380.
- 34. (d) Find the greatest number of five digits which is divisible by the L.C.M. of 12, 15, 21, 25 and 28 and then subtract 7 from it to get the required number.
 Required number = 98700 7 = 98693.
- 35. (d) Required number

= (L.C.M. of 16, 24, 30 and 32)
$$- 3$$

= $480 - 3 = 477$.

- **36.** (c) Side of each tile = (H.C.F. of 1517 and 902) cm = 41 cm
 - $\therefore \text{ Number of tiles} = \frac{1517 \times 902}{41 \times 41} = 814.$
- **37. (b)** L.C.M. of 2, 3, 4, 5, 6 is 60.

One of the numbers satisfying the first condition is 60 - 59

$$60 + 59 = 119$$
, etc.

But 119 is also divisible by 7.

38. (d) L.C.M. of 4, 6, 10, 15 = 60

Greatest number of five digits which is divisible by 60 = 99960.

- \therefore Required number = 99960 + 3 = 99963.
- **39. (b)** L.C.M. of 15, 24, 32 is 480

Required number = 480K - 13

$$= 15 \times 31K + (15K - 13)$$

(15K - 13) is divisible by 31 for K = 5

- \therefore Least number = $480 \times 5 13 = 2387$.
- **40. (b)** The greatest number of four digits divisible by 531 is 9558, so the other number is 9558 531 = 9027. Thus, the numbers are 9558 and 9027.
- **41. (b)** L.C.M. of 10, 12, 15 and 18 = 540. Dividing (99999 + 3769) by 540, the remainder is 88.
 - \therefore Required number = 99999 88 = 99911.
- 42. (c) Required number

= (L.C.M. of 14, 15, 21, 32, 60) + 11 =
$$3360 + 11 = 3371$$
.

- **43. (c)** Least number of five digits divisible by L.C.M. of 8, 12, 16, 20 is 10080.
 - :. Required number = 10080 7 = 10073.

- **44.** (d) Required number = $\frac{\text{L.c.M.} \times \text{H.c.f.}}{\text{Given number}}$ = $\frac{693 \times 11}{77} = 99$.
- **45. (b)** L.C.M. of 24, 28, 30 and 35

$$= 2 \times 2 \times 2 \times 3 \times 5 \times 7 = 840$$

Greatest number of four digits

= 9999

Quotient when 9999 is divided by 840 is 11 and remainder is 759.

- ∴ Greatest number of four digits in this case = 9999 - 759 = 9240.
- **46.** (d) L.C.M. of 12, 15, 27, 32, 40 = 4320. Let us add 5231 to the greatest number of four digits and then divide by 4320 to find the remainder.

$$4320)15230(3)$$

$$\frac{12960}{2270}$$

Required greatest number of four digits

$$= 9999 - 2270$$

= 7729.

47. (a) L.C.M. of 16, 20, 25, 45 = 3600

1st number = $3600 \times 1 + 3$

= 3603 which is not divisible by 21.

2nd number = $3600 \times 2 + 3$

= 7203 which is divisible by 21.

48. (b) L.C.M. of 8, 9, 10 = 360

Greatest number of five digits which is divisible by 360 = 99999 - 279 = 99720

- :. Required number = 99729 + 3 = 99723.
- **49. (d)** H.C.F. of 10857 and 15087 is 141.

The least number of cut pieces

$$= (10857 + 15087) \div 141$$

= 184.

Exercise-2 (Based on Memory)

- (d) Let x be the H.C.F. of two numbers 56 and k.
 Let y be the L.C.M. of two numbers 56 and k.
 To find k.
 - $\therefore xy = 56k$ Also x + y = 680 y = 84x [Given]
 - \Rightarrow 85 $x = 680 \Rightarrow x = 8$
 - $\Rightarrow y = 673$
 - \Rightarrow 56 $k = 8 \times 672$
 - $\Rightarrow k = 96$
 - \therefore The other number = 96
- **3.** (a) L.C.M. of 28, 42 = 84 H.C.F. of 28, 42 = 14
 - \therefore Required ratio = 84:14 = 6:1.
- **4.** (c) Required number = $\frac{1820 \times 26}{130} = 364$.
- **5. (c)** Since the H.C.F. is 7 therefore, possible numbers could be 21, 28, 35 and 42. L.C.M. of the numbers does not have the factor of 3. But 21 and 42 are the numbers which have 3 as a factor. So, 21 and 42 will not be the numbers. If 21 and 42 are not the numbers, then the numbers are 28 and 35.
 - \therefore Sum of the numbers = 28 + 35 = 63.
- **6. (b)** $\frac{14560 \times 13}{416} = 455$.
- **8. (b)** H.C.F. \times L.C.M. = Product of the numbers,

i.e.,
$$16 \times 160 = 32 \times K \implies K = 80$$

- 10. (c) $4 \times 27 \times 3125$

 - $= 2 \times 2 \times 2 \times 3 \times 3 \times 5 \times 5 \times 7 \ 16 \times 81 \times 5 \times 11 \times 49$
 - $= 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 5 \times 7 \times 7 \times 11$
 - $\therefore \text{ H.C.F.} = 2 \times 2 \times 3 \times 3 \times 3 \times 5 = 540.$
- **11.** (c) (33, 495); (99, 429); (165, 363); (231, 297)
- **12. (b)** $128 \times K = 1920 \times 16 \implies K = 240$.
- 13. (a) Let the numbers be x and y
 - $\therefore xy = 11 \times 385 = 11 \times 5 \times 7 \times 11 = 77 \times 55.$
- **14. (c)** From the given choices we can see that L.C.M. of 1989 and 11 is 21879.

Therefore, required numbers are 1989, 11.

- 15. (a) Let the two numbers be x and (100 x)
 - $L.C.M. \times H.C.F. = Product of the numbers$

$$495 \times 5 = x(100 - x)$$

or,
$$x^2 - 100x + 2475 = 0$$

or,
$$x^2 - 55x - 45x + 2475 = 0$$

or,
$$(x - 55)(x - 45) = 0$$
 or $x = 45$ or $x = 55$

Thus, the numbers are 45 and 55.

When x = 55, we get 100 - x = 45 and vice versa.

Hence, their difference = 55 - 45 = 10.

- **16.** (c) Other number = $\frac{225 \times 5}{25}$ = 45.
- 17. (d) Non-multiples of 8 are not the L.C.M.
- **18.** (c) Required number = $\frac{1820 \times 26}{130}$ = 364.
- 19. (c) Since the H.C.F. is 7 therefore, possible numbers could be 21, 28, 35 and 42. L.C.M. of the numbers does not have the factor of 3. But 21 and 42 are the numbers which have 3 as a factor. So, 21 and 42 will not be the numbers. If 21 and 42 are not the numbers, then the numbers are 28 and 35.
 - \therefore Sum of the numbers = 28 + 35 = 63.
- **20.** (a) Let the two numbers be x and (100 x).
 - $L.C.M. \times H.C.F. = Product of the numbers$

$$495 \times 5 = x(100 - x)$$

or,
$$x^2 - 100x + 2475 = 0$$

or,
$$x^2 - 55x - 45x + 2475 = 0$$

or,
$$(x - 55)(x - 45) = 0$$

or,
$$x = 45$$
 or $x = 55$

Thus, the numbers are 45 and 55.

When x = 55, we get 100 - x = 45 and vice versa.

Hence, their difference = 55 - 45 = 10.

21. (c) The L.C.M. of 18, 22, 30 is 990.

So, they will meet each other after 990, i.e., 16 minutes and 30 seconds.

22. (b) Time taken,

 $2 \times 2 \times 2 \times 3 \times 3 \times 4 = 288$ seconds.

2.16 Chapter 2

23. (b)
$$24 = 2 \times 2 \times 2 \times 3$$

 $36 = 2 \times 2 \times 3 \times 3$
 $30 = 2 \times 3 \times 5$
L.C.M. = $2 \times 2 \times 2 \times 3 \times 3 \times 5 = 360$

Hence, all three friends will meet again after 360 seconds.

i.e.,
$$\frac{360}{60} = 6$$
 minutes

24. (d) L.C.M. of 54, 42,
$$63 = 378$$
 seconds

$$\frac{378}{60} \approx 6.3 \text{ minutes} \approx 6 \text{ minutes}$$

25. (d) Multiple of two numbers

= Multiple of L.C.M. and H.C.F. of that numbers

$$\therefore xv = 3 \times 105$$

$$\frac{1}{x} + \frac{1}{y} = \frac{x+y}{xy} = \frac{36}{3 \times 105}$$
$$= \frac{12}{105} = \frac{4}{35}$$

26. (b) Number divisible by 20, 28, 32 and 35 is L.C.M. of these numbers

$$20 = 4 \times 5$$

$$28 = 4 \times 7$$

$$32 = 5 \times 4 \times 2$$

$$35 = 4 \times 7$$
L.C.M. = $4 \times 5 \times 7 \times 8$
= 1120

Required number = 5834 - 1120 = 4714

- 27. (d) Product of the numbers = $H.C.F. \times L.C.M.$
 - $\Rightarrow \text{ Second number} = \frac{8 \times 48}{24} \implies 16$
- **28.** (c) The numbers are 21 and 28.
- **29.** (c) Let the numbers be 12x and 12y respectively, where x and y are prime to each other.

Therefore, L.C.M =
$$12xy$$

so,
$$12xy = 924$$

$$\Rightarrow \qquad xy = \frac{924}{12} = 77$$

Hence, possible pairs are (1, 77) and (7, 11)

30. (c) L.C.M. of 5, 6, 7, $8 = 35 \times 24 = 840$

Therefore, the required number = 840x + 3, which is exactly divisible by 9.

For x = 2, it is divisible by 9.

Hence,

Required number =
$$840x + 3$$

= $840 \times 2 + 3$
= 1683

31. (d) Let the number be 10x, and 10y, respectively and xand y are prime to each other.

Therefore, L.C.M. = 10xy

$$\Rightarrow$$
 10xy = 120

$$\Rightarrow xy = \frac{120}{10} = 12$$

Possible pairs = (3, 4) or (1, 12)

Hence, sum of the numbers

$$= 30 + 40 = 70$$

32. (b) L.C.M. of 24 seconds, 36 seconds and 54 seconds = 216 seconds = 3 min 36 seconds

Required time = 10:18:36 am

33. (d) Required number = (L.C.M. of 15, 20, 36 and 48) + 3

L.C.M. =
$$2 \times 2 \times 3 \times 5 \times 3 \times 4 = 720$$

34. (a)
$$x^2 + 6x + 8 = x^2 + 4x + 2x + 8$$

$$= x(x+4) + 2(x+4)$$

$$= (x+2)(x+4)$$

$$x^2 + 3x + 2 = x^2 + 2x + x + 2$$

$$= x(x+2) + 1(x+2)$$

$$= (x+2)(x+1)$$

First expression \times Second expression = H.C.F. \times L.C.M.

$$\Rightarrow (x^2 + 3x + 2) \times \text{Second expression} = (x^2 + 6x + 8)$$
$$(x + 1) \times (x + 1)$$

$$\Rightarrow (x+2)(x+1) \times \text{Second expression} = (x+2)(x+4)$$
$$(x+1)(x+1)$$

$$\Rightarrow \text{ Second expression} = \frac{(x+2)(x+4)(x+1)(x+1)}{(x+2)(x+1)}$$

$$=(x+4)(x+1)=x^2+4x+x+4=x^2+5x+4$$

35. (a)
$$5 \mid 625$$

$$5 \mid 125$$

$$5 \mid 25$$

$$\therefore 625 = 5 \times 5 \times 5 \times 5 = 5^3 \times 5$$

For the smallest cube number, 625 should be divided 5,

$$625 \div 5 = 125 = 5^3$$

36. (d) Required number = H.C.F. of 200 and 320 = 40

80

40)80(2 <u>80</u> ×

37. (b) L.C.M. of 10, 15 and 20 = 60

Greatest 4-digit number = 9999

$$\begin{array}{r} \therefore 60)9999(166) \\ \underline{60} \\ 399 \\ \underline{360} \\ 399 \\ \underline{360} \\ 39 \end{array}$$

- :. Required number = 9999 39 = 9960
- **38.** (d) Required number of students = L.C.M. of 6, 8, 12 and 16 = 48

$$= 2 \times 2 \times 2 \times 2 \times 3 = 48$$

- \therefore Required answer = multiple of 48 = 96
- **39.** (d) If x = 2, y = 4 then A = 2, B = 4 $\therefore x + y = A + B$

$$A^3 + B^3 = x^3 + y^3$$

40. (c) Required number = H.C.F. of 411 - 3 = 408; 684 - 4 = 680 and 821 - 5 = 816

H.C.F. of 408 and 816 = 408

H.C.F. of 408 and 680 = 136

$$\frac{408}{272},408(1)$$

$$\frac{272}{136},272(2)$$

$$\frac{272}{136},272(2)$$

:. Required number = 136

41. (b) L.C.M. of indices of surds = 12

$$3\sqrt{4} = \sqrt[12]{4^4} = \sqrt[12]{256}$$

$$\sqrt{3} = \sqrt[12]{3^6} = \sqrt[12]{729}$$

$$\sqrt[6]{25} = \sqrt[12]{625}$$

¹²√289

- \therefore The largest number = $\sqrt{3}$ and the smallest number = $\sqrt[3]{4}$
- **42. (b)** Let the four consecutive prime numbers be a, b, c and d: where a < b < c < d.
 - \therefore abc = 385 and bcd = 1001
 - \therefore H.C.F. = bc

- $\therefore bc = 77$
- $\therefore bcd = 1001$

$$d = \frac{bcd}{bc} = \frac{1001}{77} = 13$$

43. (b) H.C.F. of $\frac{2}{3}$, $\frac{4}{5}$ and $\frac{6}{7}$ H.C.F. of 2,4 and 6

$$= \frac{\text{H.C.F. of 2,4 and 6}}{\text{L.C.M. of 3,5 and 7}} = \frac{2}{105}$$

- **44.** (a) L.C.M. of 3, 6, 9, 12 and 15 = 180 seconds
 - :. Required answer

$$=\frac{36\times60}{180}+1=12+1=13$$

45. (c) Let the first number be 5x and the second number be 6x

Now, according to the question,

$$H.C.F. = 4$$

- \therefore x = 4
- \Rightarrow First number = $5 \times 4 = 20$
- \Rightarrow Second number = $6 \times 4 = 24$
- :. Required. L.C.M. = 120
- 46. (c) Quicker Method:

$$4 - 2 = 5 - 3 = 6 - 4 = 2$$

Now, L.C.M. of 4, 5, 6 = 60

 \therefore Required number = 60 - difference = 60 - 2 = 58

2.18 Chapter 2

47. (c) Let the greatest number be x

$$\therefore 43 = nx + k \qquad \cdots (1)$$

$$\Rightarrow 91 = mx + k \qquad \cdots (2) \qquad \Rightarrow 140 = (l - n)x$$

$$\Rightarrow$$
 183 - $lx + k$...(3) \therefore x = H.C.F. of 48, 92, and 140 = 4

 \Rightarrow 48 = (m - n)x

 \Rightarrow 92 = (l - m)x

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