

Ques. 1] Plot a histogram.

{ 10, 13, 18, 22, 27, 32, 38, 40, 45, 51, 56
57, 88, 90, 92, 94, 99 }

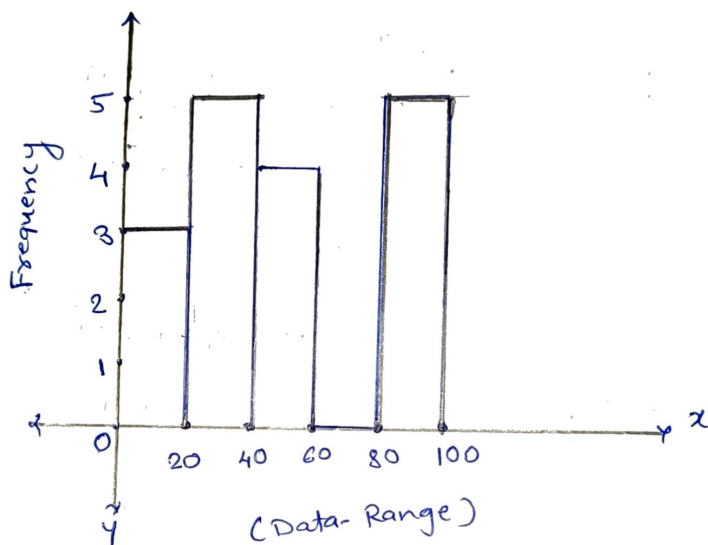
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$$\text{Bins} = 5$$

$$\therefore \text{Bin Size} = \frac{100}{5}$$

$$\text{Bin Size} = 20$$

$$[0 - 100]$$



Ques. 2] In a quant test of CAT Exam, the population standard deviation is known to be 100. A sample of 25 test taken has a mean of 520. Construct an 80% CI about the mean?

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Given

$$\sigma = 100 \text{ (population standard deviation)}$$

$$n = 25 \text{ (sample of test)}$$

$$\bar{x} = 520 \text{ (mean)}$$

$$C.I = 80\%$$

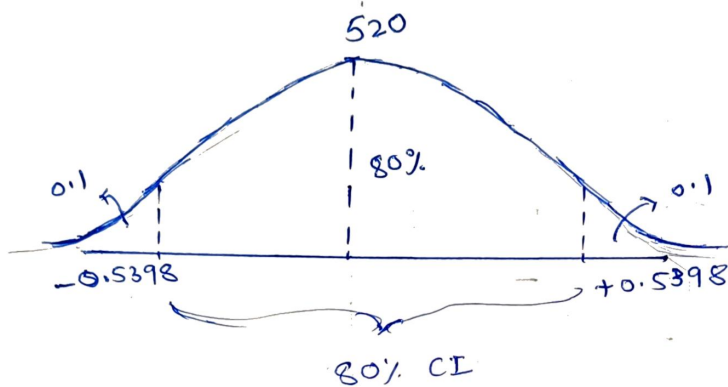
$$q = 1 - C.I$$

$$= 1 - 0.80$$

$$q = 0.2$$

$$\begin{aligned} \frac{Z_{\alpha}}{2} &= Z \frac{0.2}{2} \\ &= Z 0.1 \\ &= 0.5398 \end{aligned}$$

ques. 3]

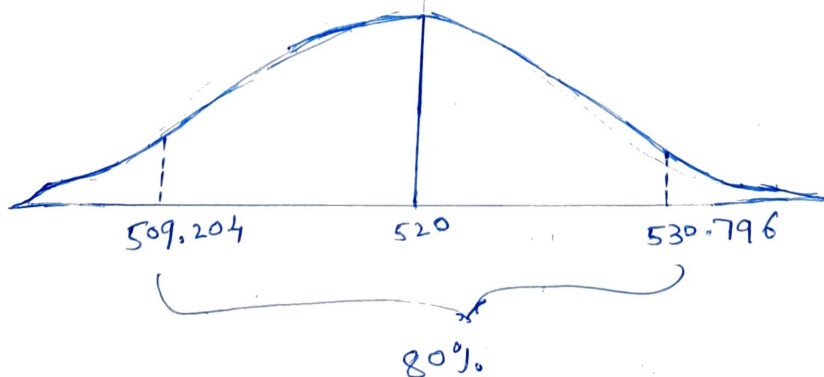


Lower fence

$$\begin{aligned} \bar{x} &= \bar{x} - \frac{Z_{\alpha}}{2} \times \frac{\sigma}{\sqrt{n}} \\ &= 520 - 0.5398 \times \frac{100}{\sqrt{25}} \\ &= 509.204 \end{aligned}$$

Higher fence

$$\begin{aligned} &= \bar{x} + \frac{Z_{\alpha}}{2} \times \frac{\sigma}{\sqrt{n}} \\ &= 520 + 0.5398 \times \frac{100}{\sqrt{25}} \\ &= 530.796 \end{aligned}$$



Ques. 3] A car believes that the percentage of citizens in city ABC that owns a vehicle is 60% or less. A sales manager disagrees with this. He conducted a hypothesis testing surveying 250 residents & found that 170 residents responded yes to owning a vehicle.

- State the null & alternate hypothesis
- At a 10% significance level, is there enough evidence to support the idea that vehicle owner in ABC city is 60% or less.

Null hypothesis

$$H_0: P_0 \leq 60\%$$

$$H_1: P_0 > 60\%$$

$$n = 250$$

$$x = 170$$

$$\hat{p} = \frac{x}{n} = \frac{170}{250} = 0.68$$

$$\begin{aligned} q_0 &= 1 - p_0 \\ &= 1 - 0.6 \\ &= 0.4 \end{aligned}$$

Null hypotheses (H_0)

It claim that there is no effect in the population

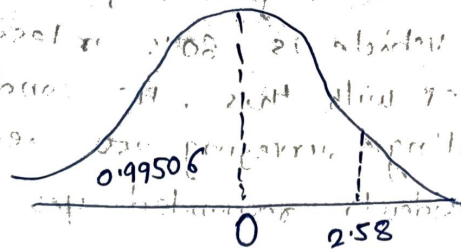
Alternate hypotheses (H_1)

A claim that there is an effect in the population

Z-test

$$\begin{aligned} Z &= \frac{\hat{p} - p_0}{\sqrt{\frac{p_0 q_0}{n}}} = \frac{0.68 - 0.6}{\sqrt{\frac{0.6 \times 0.4}{250}}} = \frac{0.08}{\sqrt{\frac{0.24}{250}}} = \frac{0.08}{\sqrt{0.00096}} \\ &= \frac{0.08}{0.030983} = 2.58 \end{aligned}$$

$$\boxed{Z = 0.99506}$$



$$CI = 10\% \quad p\text{-value} = 1 - 0.99506$$

$$CI = 0.1$$

$$p\text{-value} = 0.0494$$

$$p\text{-value} < \text{significant value}$$

$$0.0494 < 0.10$$

∴ Reject the Null Hypothesis.

we can say that the sales manager is correct

ques 4) what is the value of 99 percentile?

2, 2, 3, 4, 5, 5, 5, 6, 7, 8, 8, 8, 8, 8, 8, 9, 9, 10

11, 11, 12

$$\text{Value} = \frac{\text{Percentile}}{100} \times S$$

$$\text{Sample size (S)} = 20$$

$$P_{99} = \frac{99}{100} \times 20$$

$$= 19.8 \approx 20$$

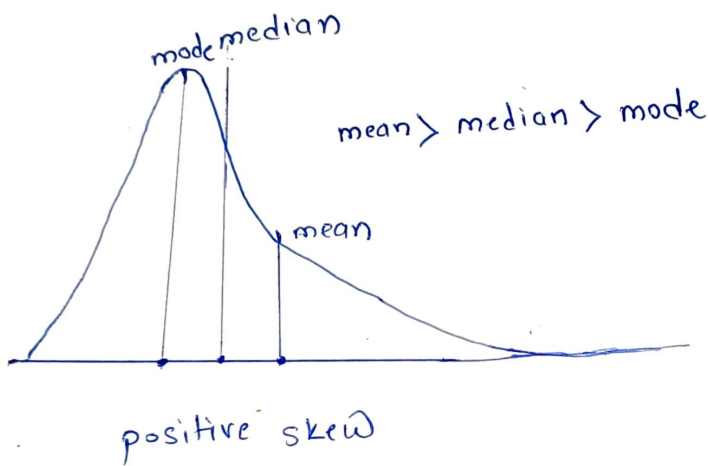
The 99th percentile will be at index 20.

Thus the 99th percentile value is 12

Ques-5] In left & Right skewed data, what is the relationship between mean, median & mode?
Draw the graph to represent the same

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* Right skewed :-

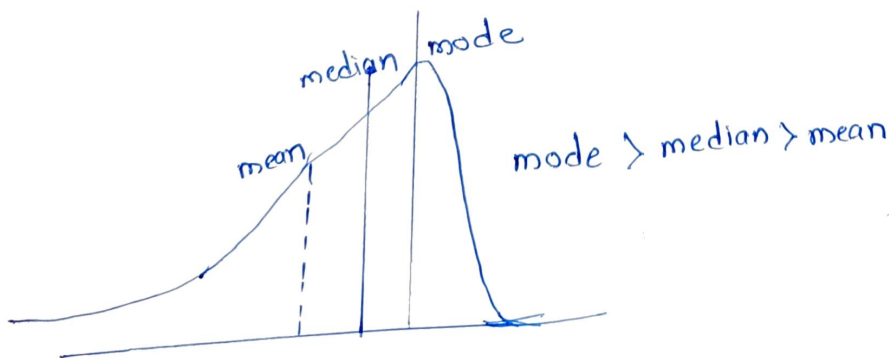
A Right skewed distribution is longer on the right side of its peak than on its left. Right skewed also refer as a positive skewed.



The mean of a Right skewed distribution is always greater than its median.

* left skewed

left skewed distribution is longer on a left side of its peak than on Right side. left skewed also refer as negative skew



The mean of a left-skewed distribution is almost always less than its median