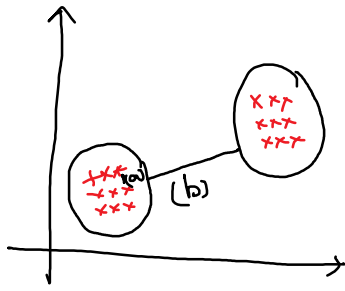


Unsupervised learning

$D \Rightarrow \{x_i, y_i\} \rightarrow$ supervised learning

$D = \{x_i\} \rightarrow$ unsupervised learning

Clustering
↓
KMeans

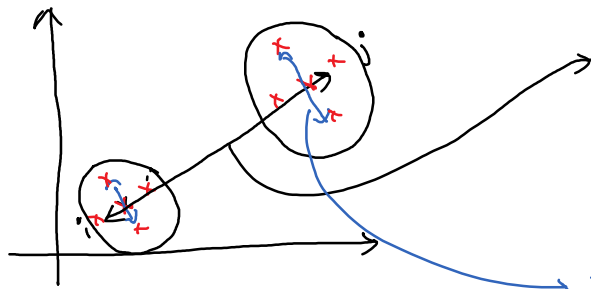


\Rightarrow Intercluster distance (b)

\Rightarrow Intracluster distance

Characteristics: a) \rightarrow intracluster distance should be small
(good cluster) b) \rightarrow intercluster distance should be large

Dunn's Index $\Rightarrow \frac{\max d(i, j) \rightarrow \text{intercluster distance}}{\max d'(k) \rightarrow \text{intracluster distance}}$



$\max d(i, j) \Rightarrow$ distance b/w farthest points in different cluster.

$\max d'(k) \Rightarrow$ distance b/w farthest points in same cluster

b) Silhouette's Score $\Rightarrow \frac{b-a}{\max(b, a)} \rightarrow b \Rightarrow \text{avg intercluster distance}$
 $[-1, +1]$ $a \Rightarrow \text{avg intracluster distance}$

\therefore

Case 1: a) $\Rightarrow \min \Rightarrow 0$ b) $\Rightarrow b$ (best scenario)

$$SS = \frac{b-0}{\max(b, 0)} = \frac{b}{b} = 1$$

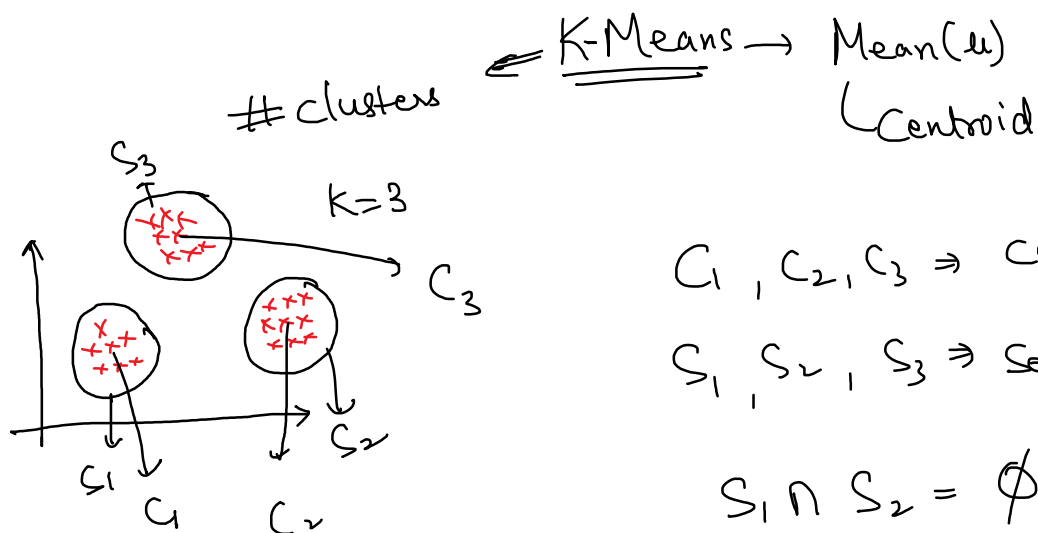
Case 2: $b < a$, $b = 0$, $a = a$

completely wrong

$$SS = \frac{0-a}{\max(0,a)} = -\frac{a}{a} = -1$$

Case 3: $a = b$

$$SS = \frac{a-a}{\max(a,a)} = \frac{0}{a} = 0$$



$$C = \frac{1}{n} \sum_{i=1}^n x_i \quad x_i \in S_i$$

$$S_1 \cap S_2 = \emptyset \quad S_3 \cap S_1 = \emptyset$$

$$S_2 \cap S_3 = \emptyset$$

$$\text{MOF} \Rightarrow C^* = \underset{C_1, C_2, C_3, \dots, C_k}{\operatorname{argmin}} \sum_{i=1}^k \sum_{x_i \in S_i} \|x_i - C_i\|^2$$

intracluster distance
 $x_i \in S_i$
 $S_i \cap S_j = \emptyset$

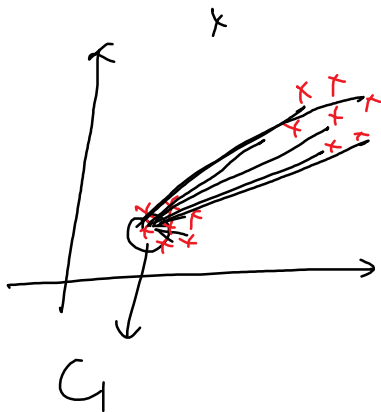
nphard
problem

Lloyd's Algorithm:

- ① Randomly choose k datapoints as centroids
- ② Assignment: for each point, select the nearest centroid with the help of distance & add that point to the corresponding cluster.
- ③ Update: Recalculate centroids,
$$C_i = \frac{1}{S_i} \sum_{i=1}^n x_i$$

$x_i \in S_i$
- ④ Repeat step ② & ③ till convergence

KMeans ++



| datapoints | distance |
|------------|----------|
| x_1 | d_1 |
| x_2 | d_2 |
| \vdots | \vdots |
| x_n | d_n |

distance \propto prob. of being picked as centroid

KMeans \Rightarrow affected by outliers