

Probability Concepts

Principles of Counting

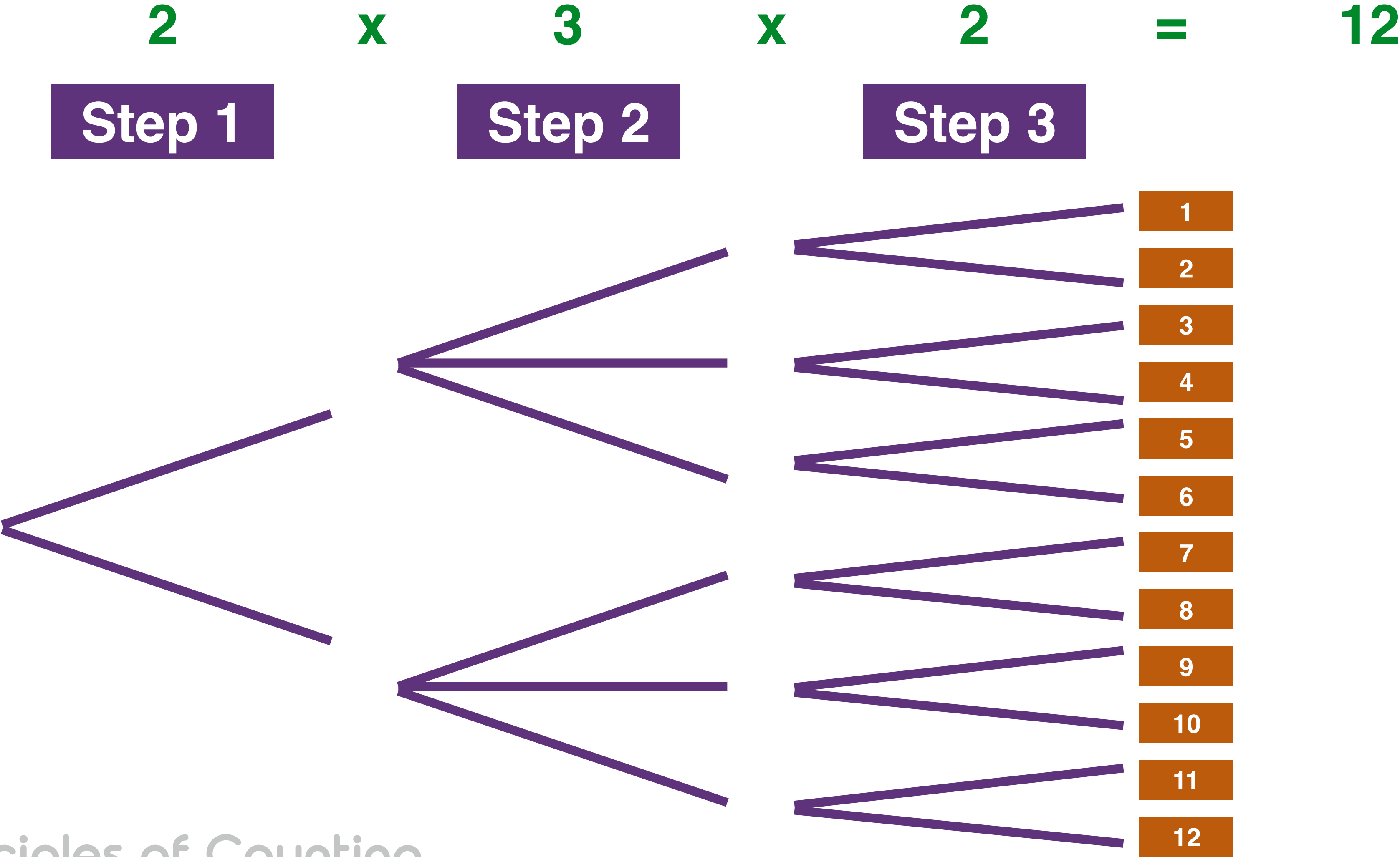
Principles of Counting

*help to determine the **total number of possibilities** in a problem*

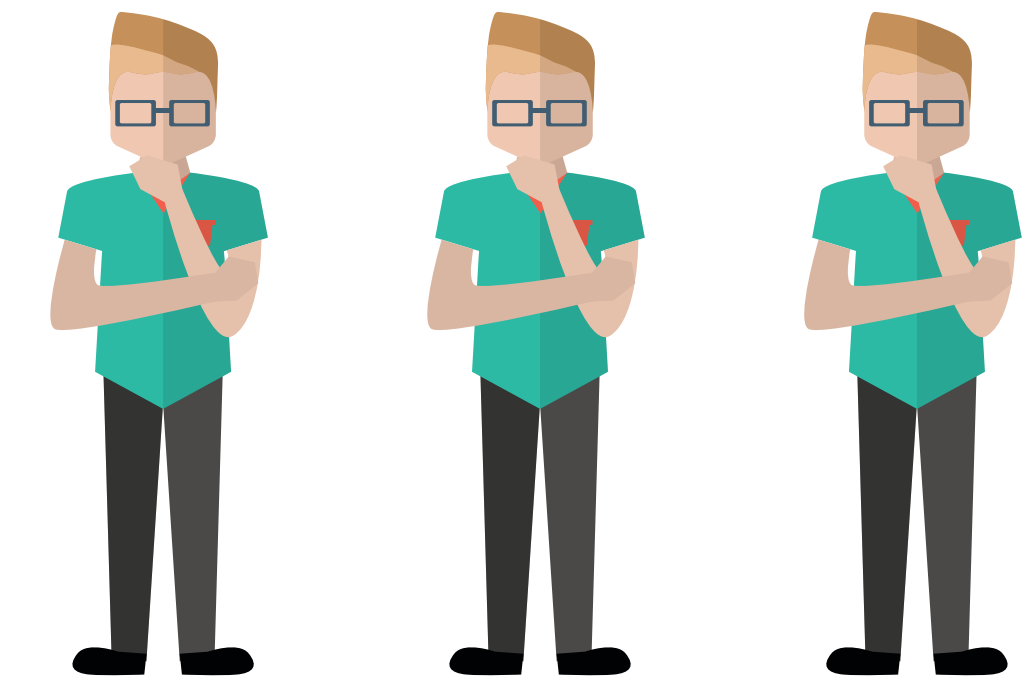


Principles of Counting

Multiplication Rule of Counting



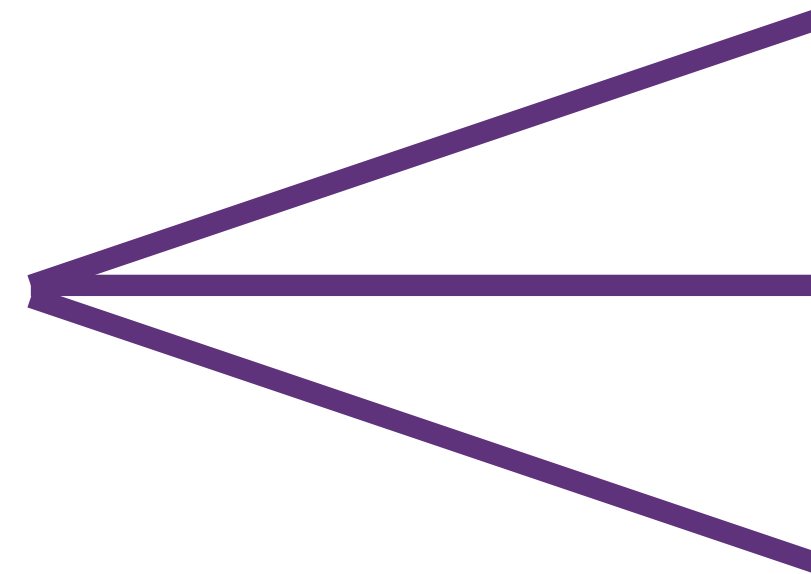
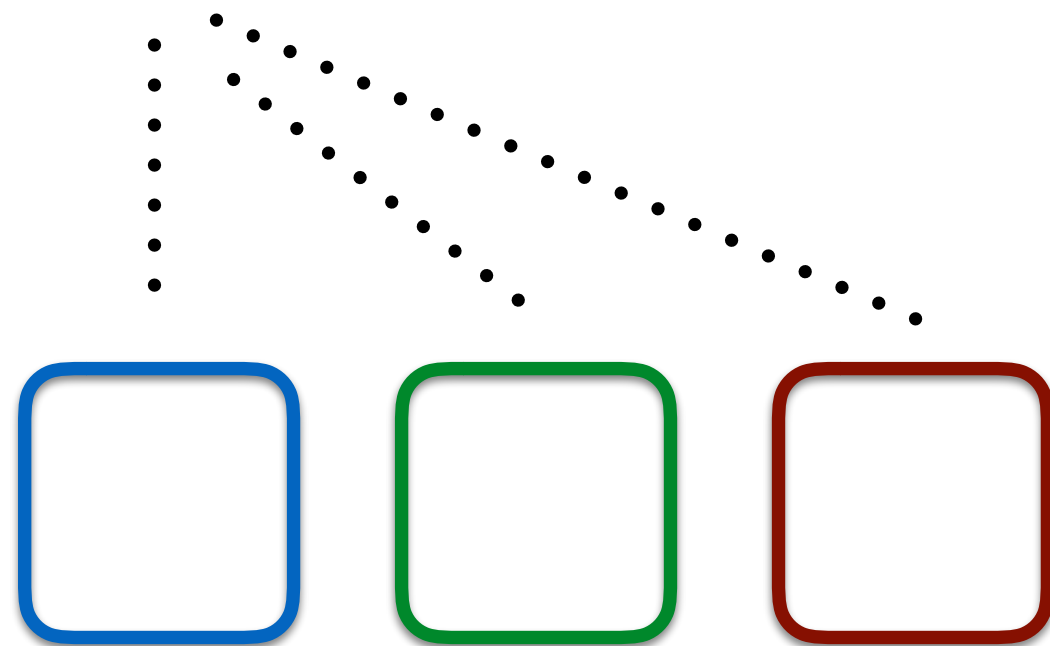
Multiplication Rule of Counting



Step 1

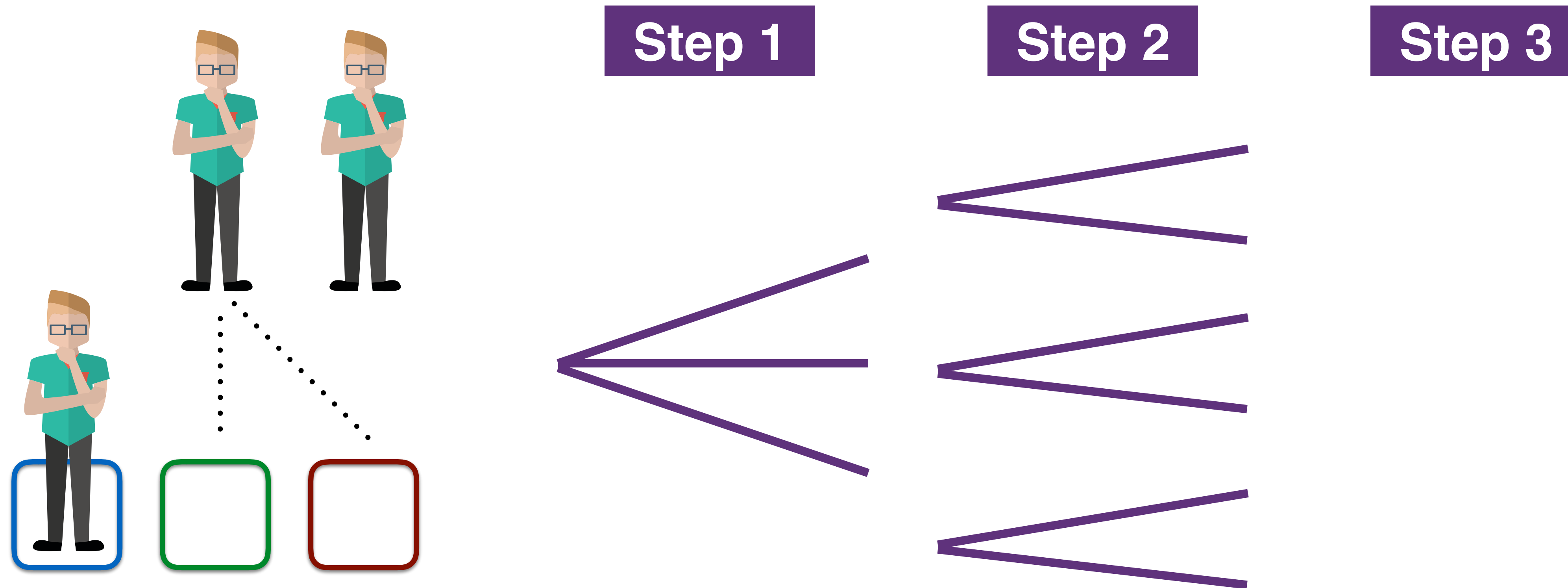
Step 2

Step 3



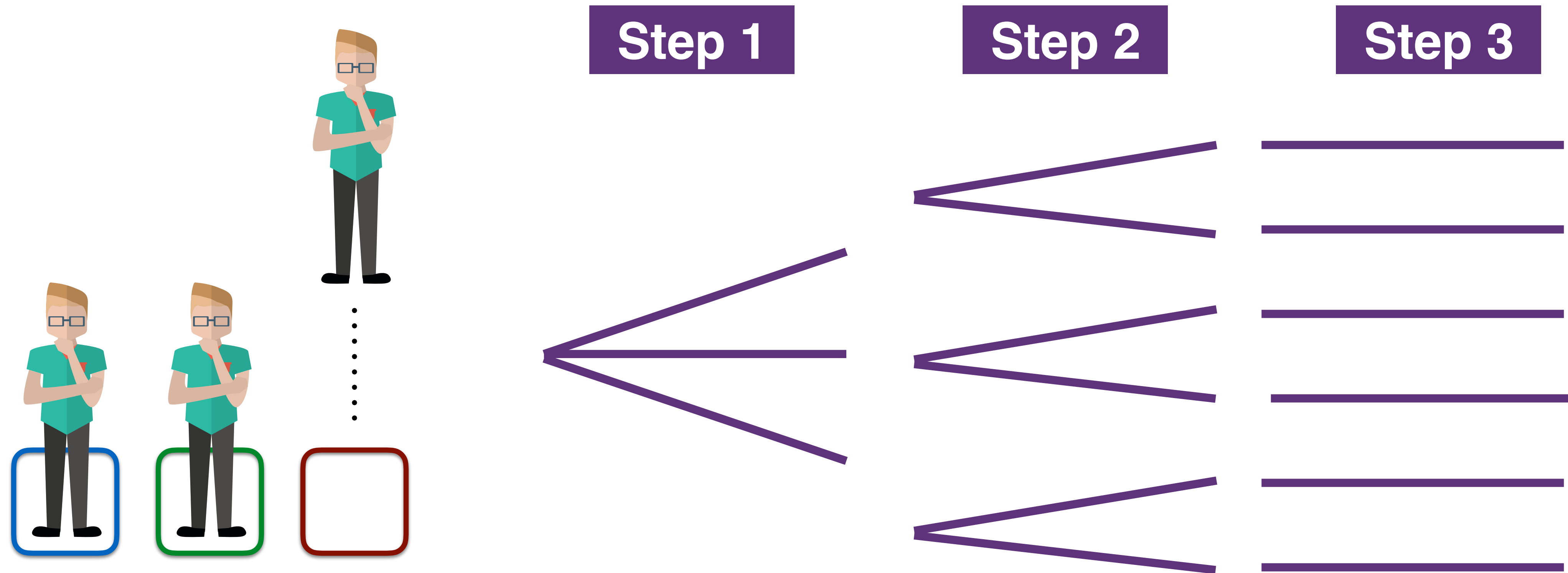
How many ways to assign?

Multiplication Rule of Counting



How many ways to assign?

Multiplication Rule of Counting



How many ways to assign?

Multiplication Rule of Counting

3

x

2

x

1

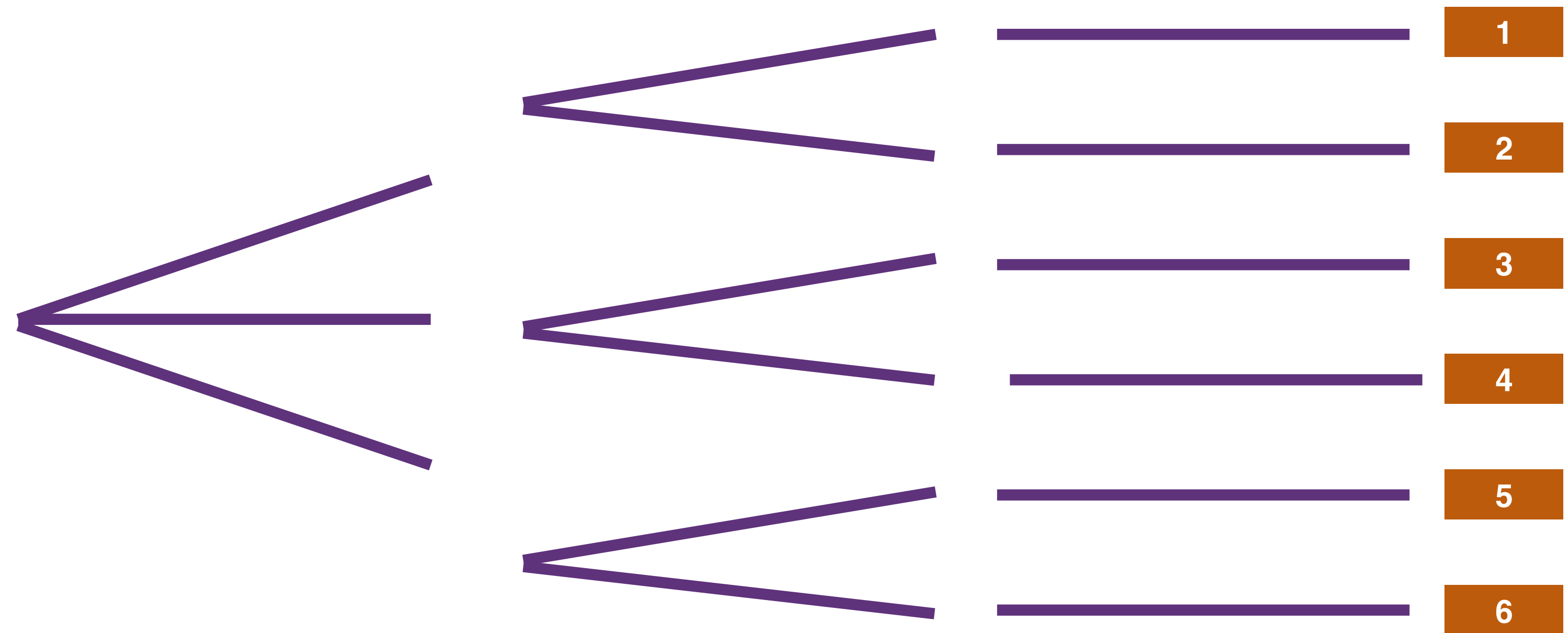
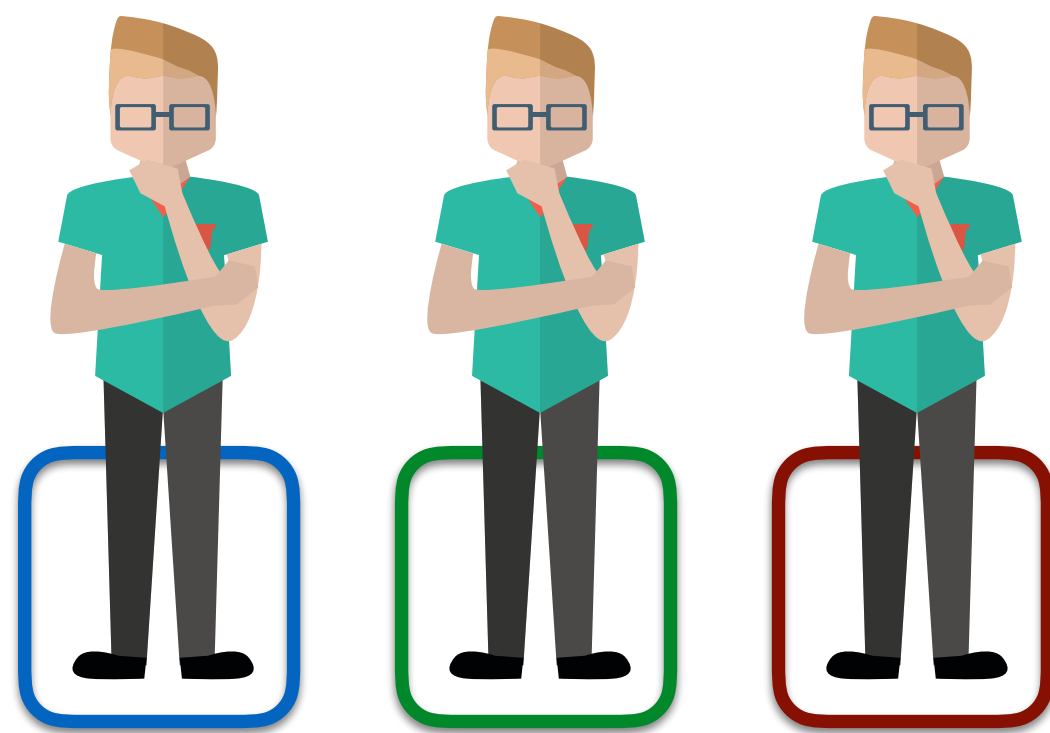
=

6

Step 1

Step 2

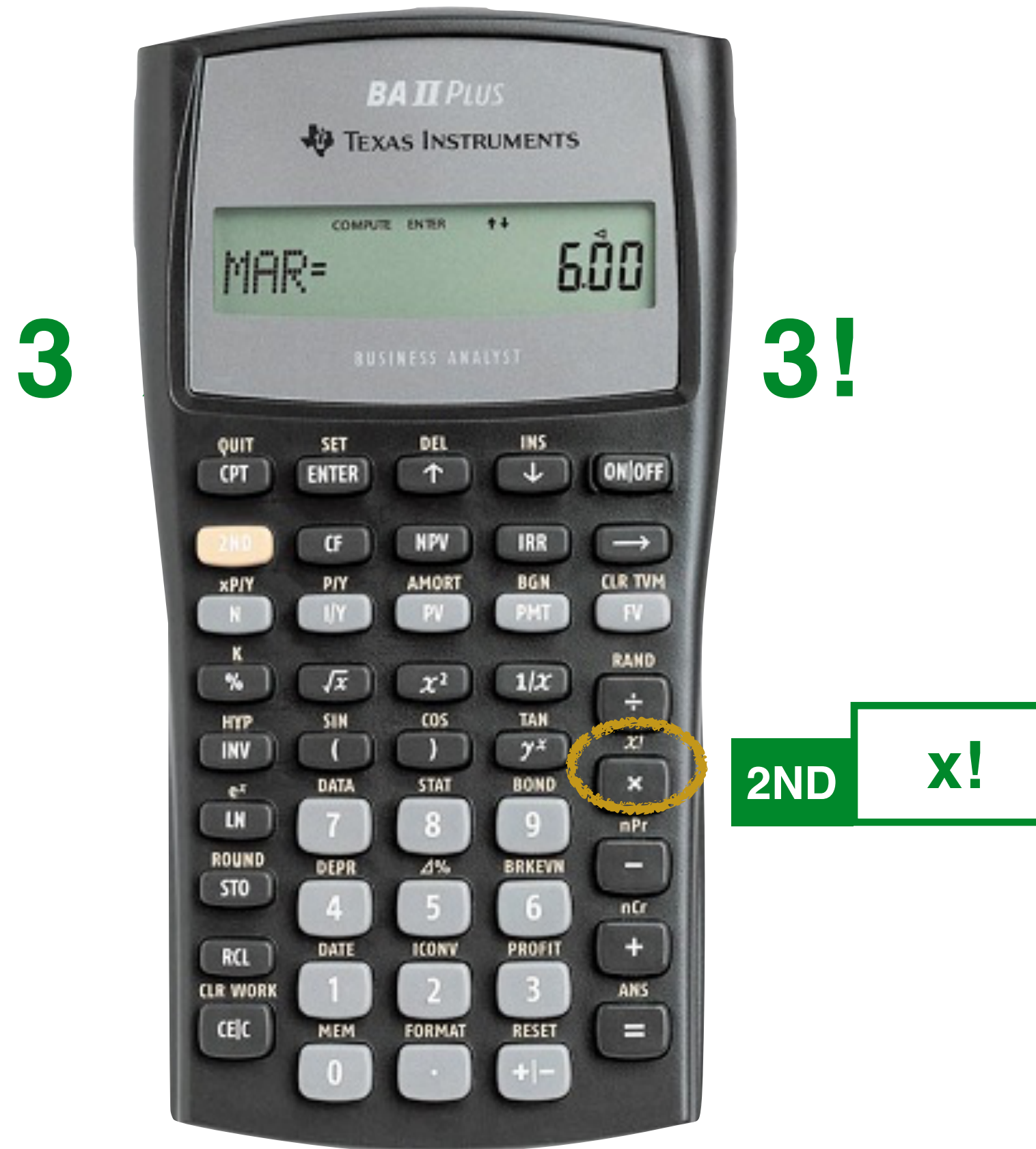
Step 3



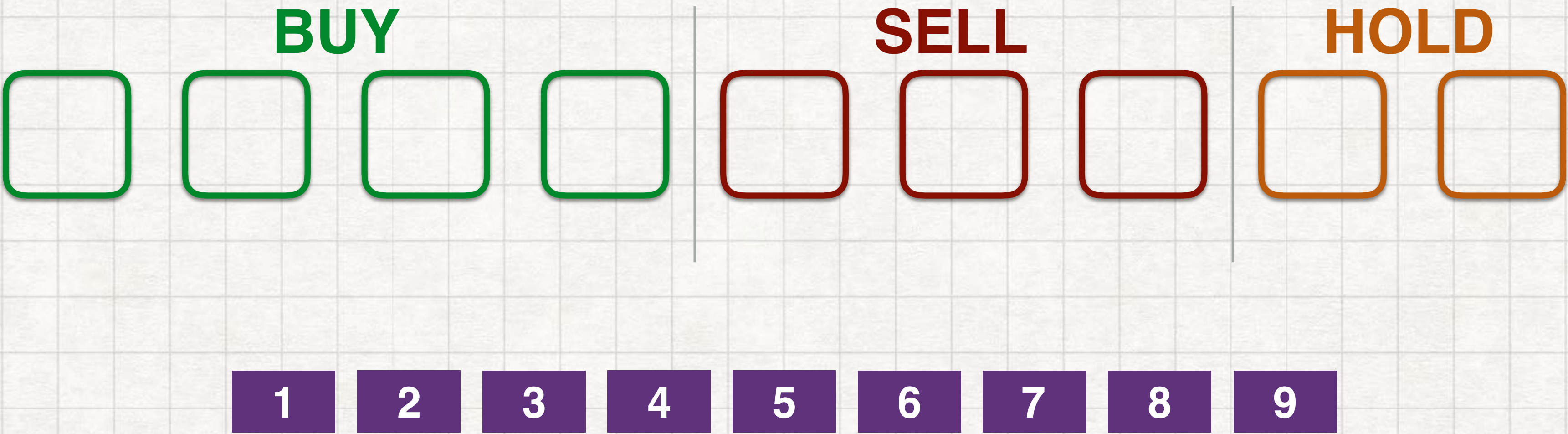
How many ways to assign?

Factorial

$$n \times (n-1) \times (n-2) \times \dots \times 1 = n!$$



You are an analyst covering 9 stocks. You are required to label 4 stocks as a “Buy”, 3 stocks as a “Sell” and 2 stocks as a “Hold”. How many ways can these 9 stocks be labeled?



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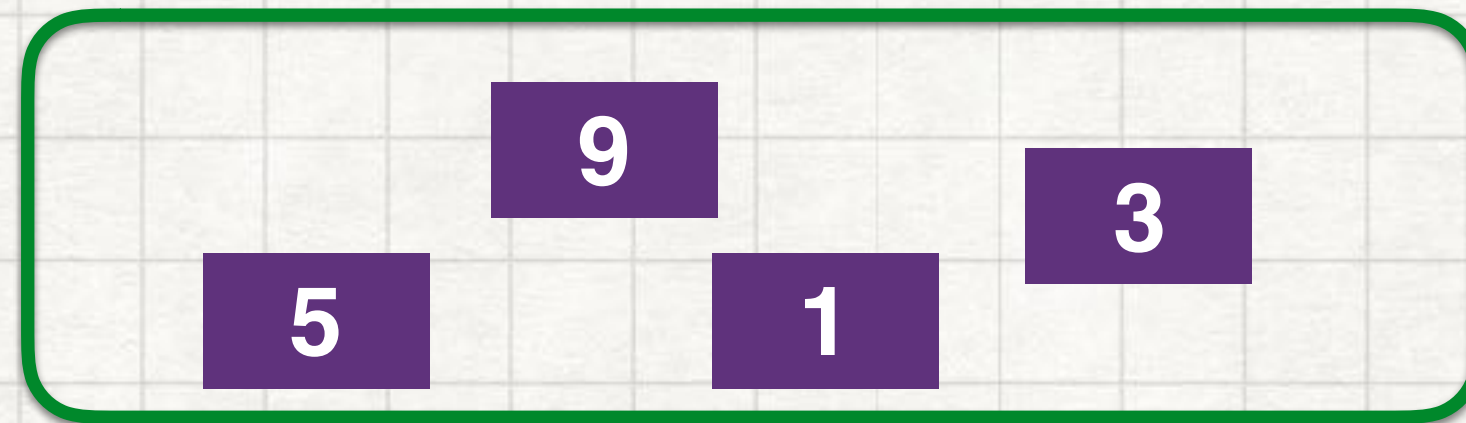


$$\text{Total Possible Sequences} = 9! = 362,880$$

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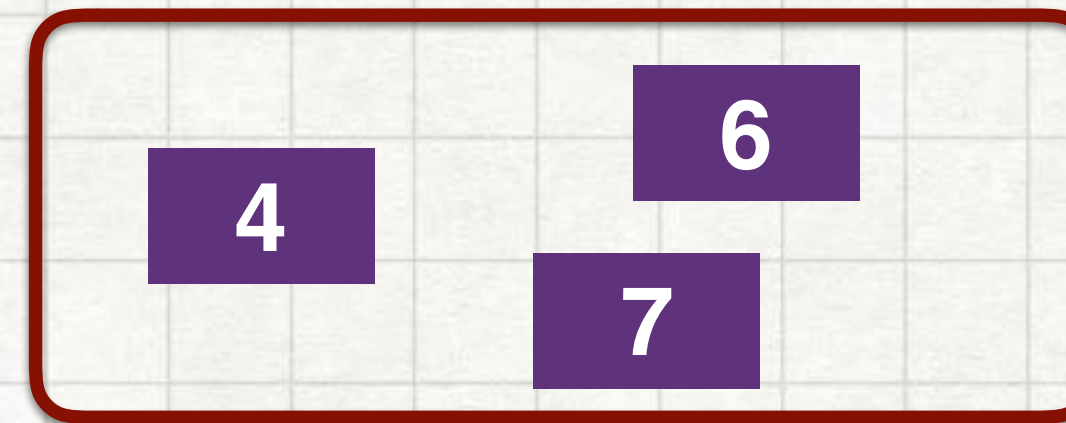
Sequence
does not
matter

BUY



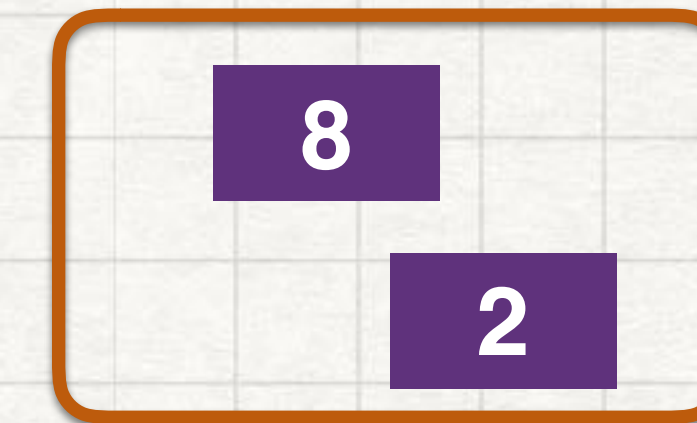
4!

SELL



3!

HOLD



2!

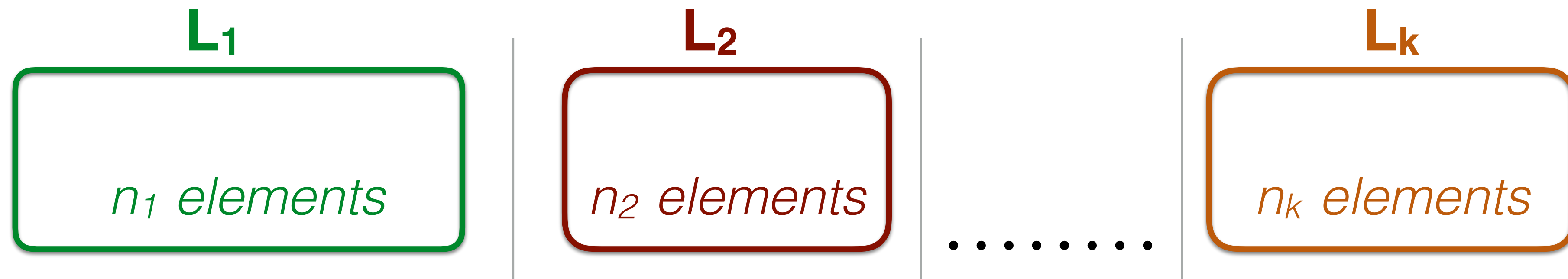
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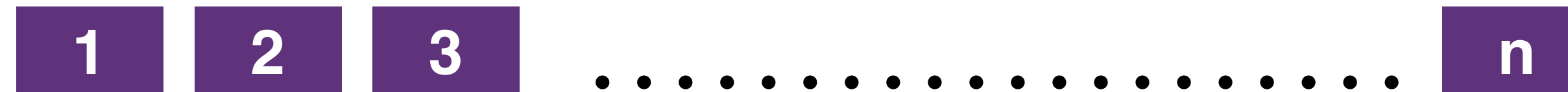


$$\begin{aligned} \text{Number of different ways to assign the 9 stocks} &= \frac{9!}{4! \times 3! \times 2!} = \frac{362,880}{24 \times 6 \times 2} \\ &= 1260 \end{aligned}$$

Multinomial Formula



$$n_1 + n_2 + \dots + n_k = n$$



$$\text{Num of Ways} = \frac{n!}{n_1! n_2! \dots n_k!}$$

Combination Formula



1 2 3 4

"n choose r" ${}_nC_r = \frac{n!}{r! (n-r)!}$

Combination Formula

Sequence is not important

Selected

2

4

1

3 stocks

Not Selected

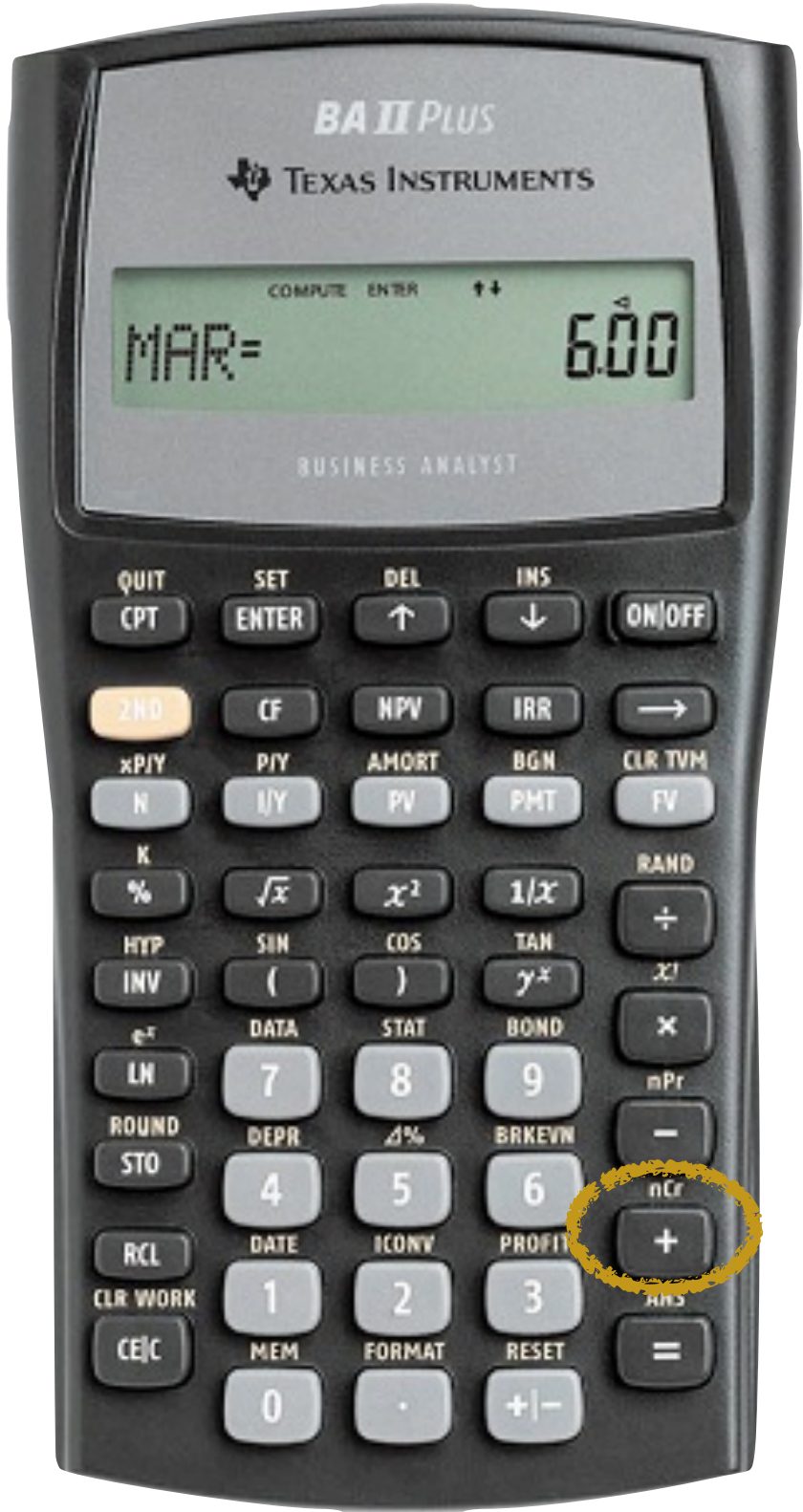
3

1 stock

${}_4C_3 = 4! / 3!1! = 4$

“n choose r”

${}_nC_r = \frac{n!}{r!(n-r)!}$



4

2NDnCr

3=

Permutation Formula

*Sequence is
IMPORTANT*

Selected



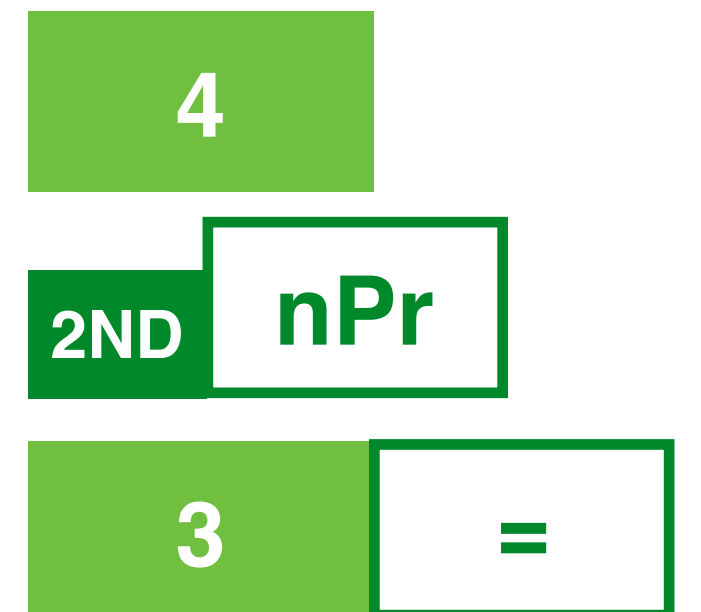
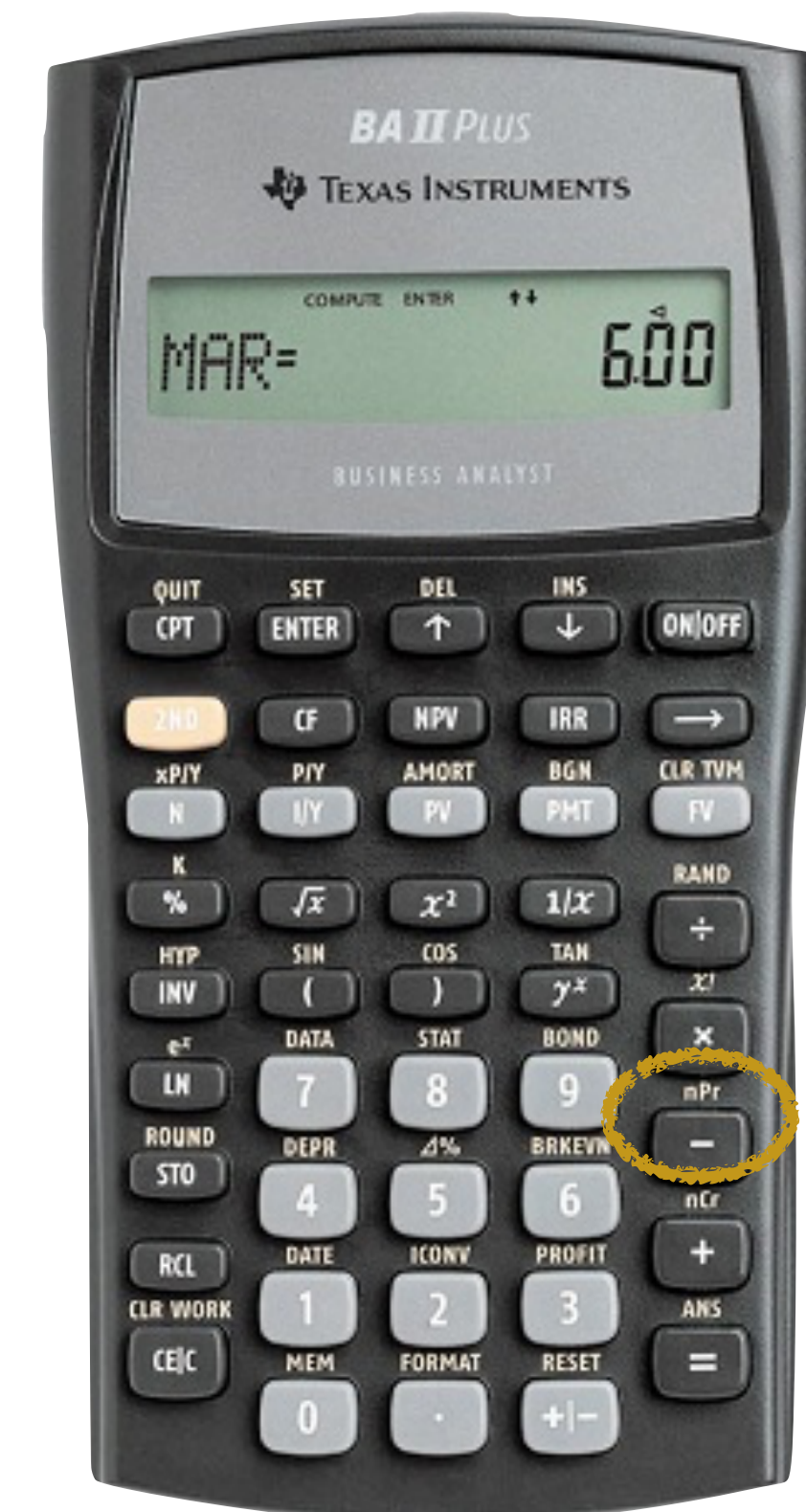
3 *stocks*

Not Selected



$${}_4P_3 = 4! / 1! = 24$$

$${}_nP_r = \frac{n!}{(n-r)!}$$





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