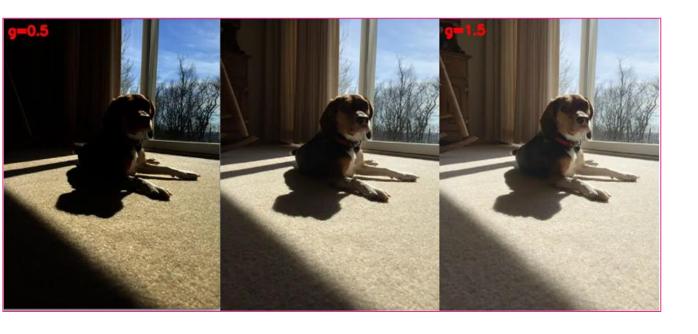
Image Enhancement:

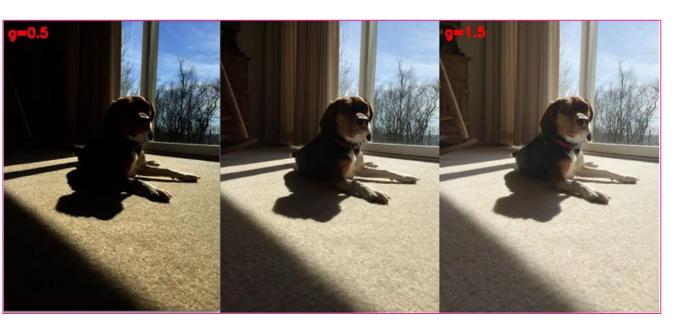
Spatial domain

Dr. Tushar Sandhan

Introduction



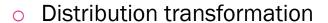
Introduction

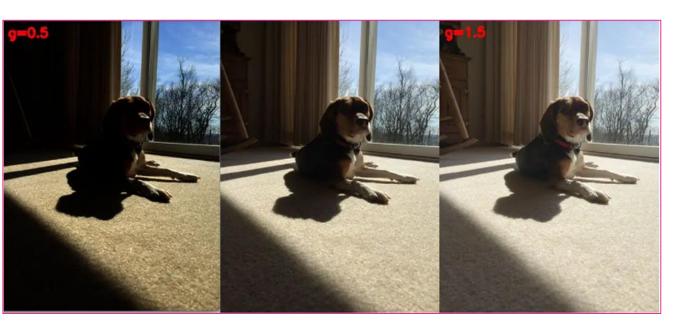




Introduction

Intensity transformations





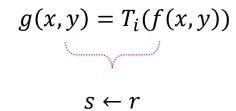


- Transformations
 - intensity transformations
 - negatives
 - logs
 - power-law (gamma)
 - contrast stretching
 - level slicing
 - bit-plane slicing
 - distribution transformations
 - histogram equalization
- Spatial filtering
 - image filtering

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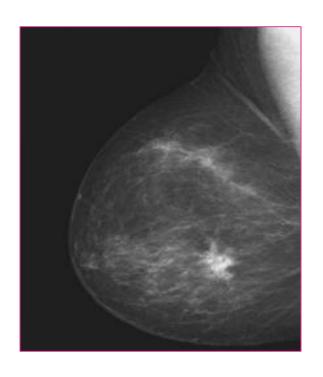
$$g(x,y) = T_i(f(x,y))$$

$$s \leftarrow r$$

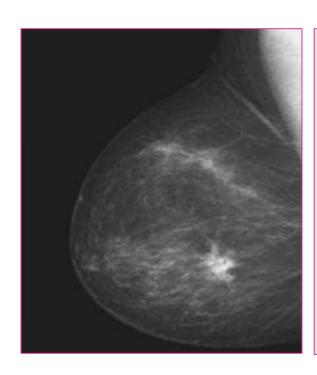
$$g(x,y) = T_i \left(p(f(x,y)) \right)$$

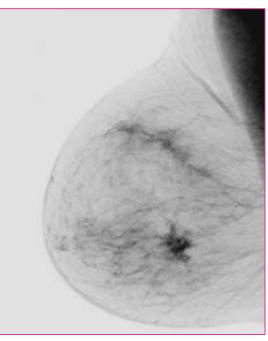
$$s = L - 1 - r$$

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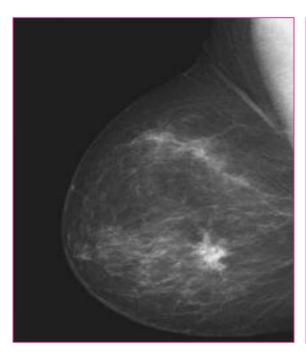


$$s = L - 1 - r$$





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$$s = c \cdot log(1+r)$$

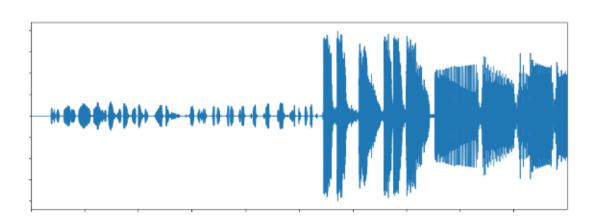
- Log transformations
 - used to expand values of dark pixels
 - o simultaneously compressing bright pixels
 - o compresses dynamic range of images
 - Fourier spectrum





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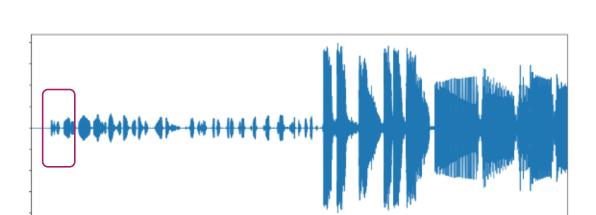






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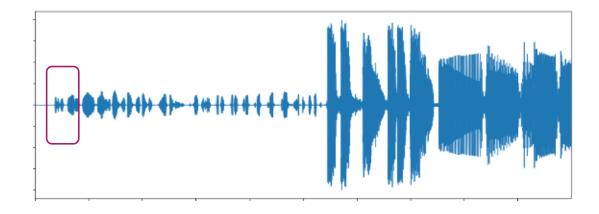


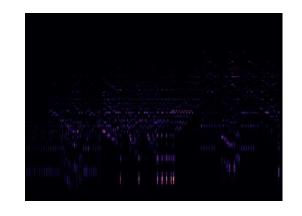
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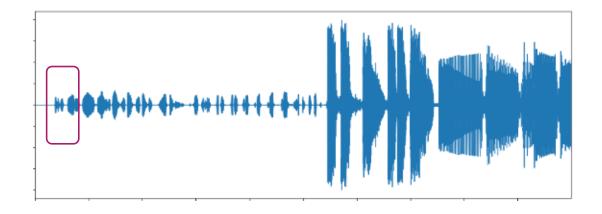


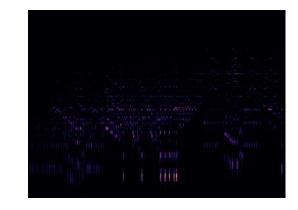
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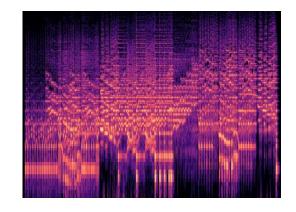
- Log transformations
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 $s = c \cdot r^{\gamma}$

- Power-law transformations
 - o sensors respond according to power law
 - CMOS, scanners, printing, displays
 - CRT: intensity to voltage response as power function ($\gamma' = 1.8 \sim 2.5$)
 - o gamma correction
 - \circ device dependent γ
 - \circ γ variation also varies the color ratios
 - \circ correct color reproduction needs knowledge of γ
 - gamma injection
 - o post image processing for contrast manipulation

 $s = c \cdot r^{\gamma}$

Power-law transformations

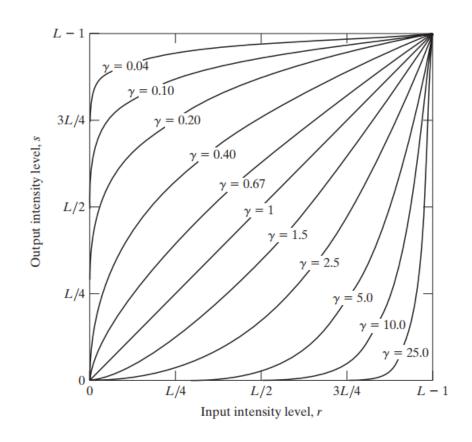
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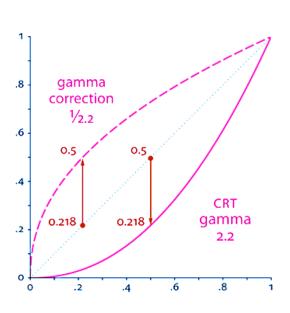
o gamma injection

o post image processing for contrast manipulation



 $s = c \cdot r^{\gamma}$

• γ correction





 $s = c \cdot r^{\gamma}$

lacksquare γ injection









 $s = c \cdot r^{\gamma}$

• γ injection









 $s = c \cdot r^{\gamma}$

• γ injection

















 $s = c \cdot r^{\gamma}$

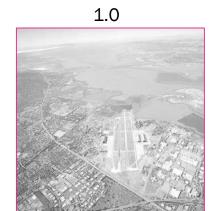
• γ injection











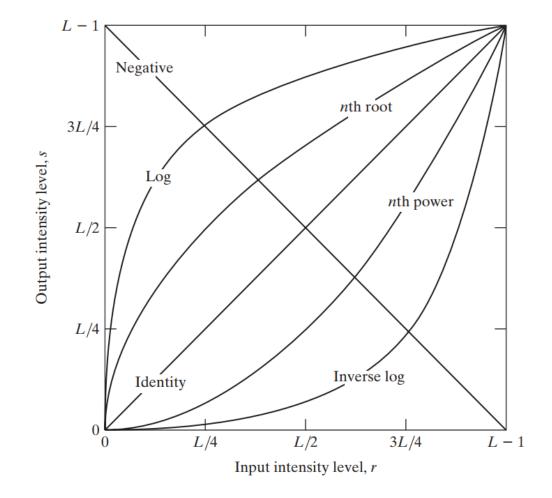






Transformations

- Compositions
 - o piecewise combinations
 - piecewise linear
 - many T_i formulated with this
 - need more user input paras



Contrast

- low contrast images
 - due to poor illumination, low dynamic range sensors
 - wrong setting of lens aperture



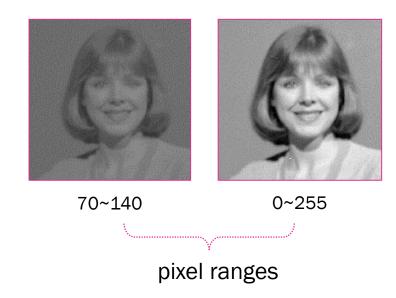


- o full range stretching
 - $(r_1, s_1) = (r_{min}, 0)$
 - $(r_2, s_2) = (r_{max}, L 1)$
- thresholding

•

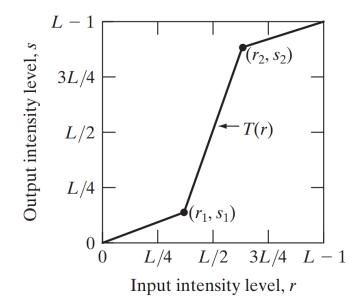
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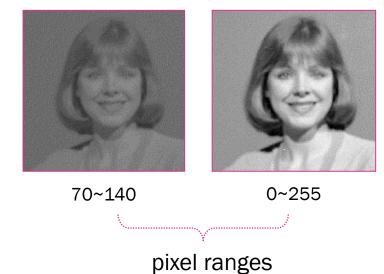
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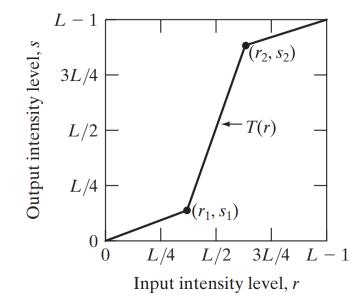
•

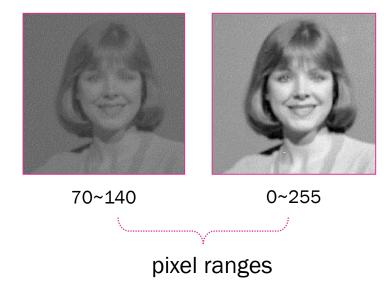




Contrast

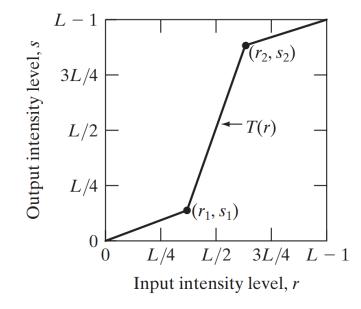
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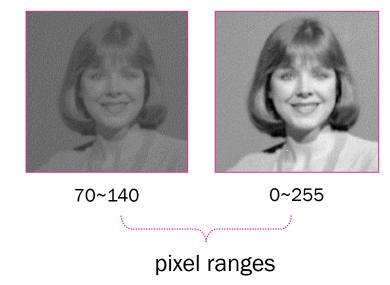


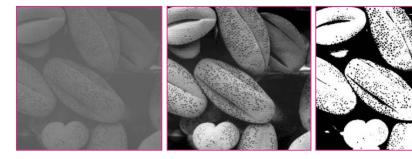


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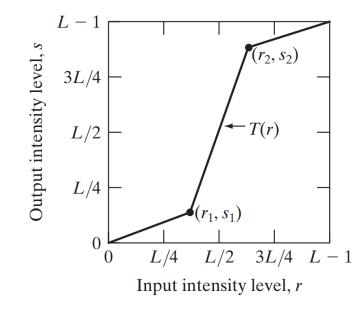


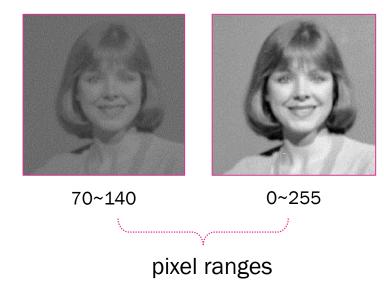




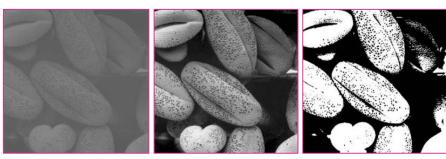
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SEM image of pollen grains



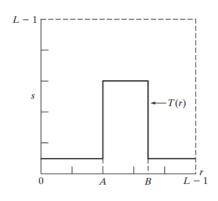
- Intensity levels
 - o local thresholding, stretching
 - o enhancing only specific intensities
 - e.g. detecting water, wetland in sat. images

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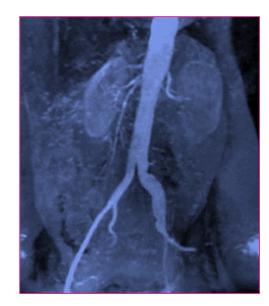


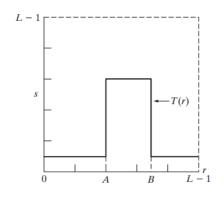
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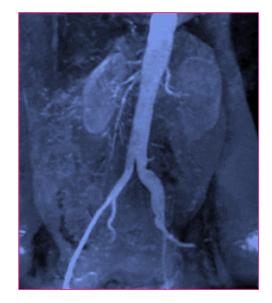
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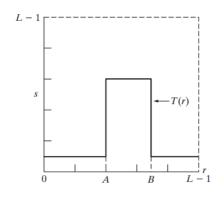


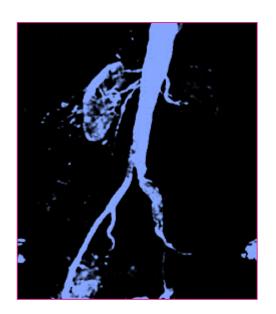


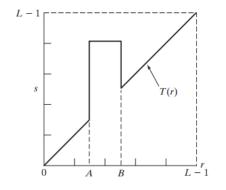


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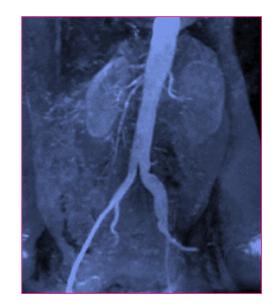


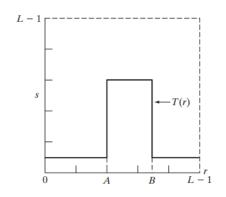




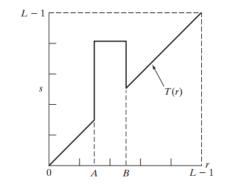
Level slicing

- Intensity levels
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 - o enhancing only specific intensities
 - e.g. detecting water, wetland in sat. images



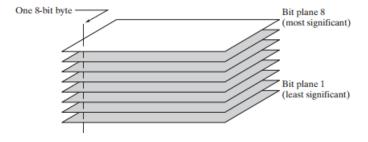








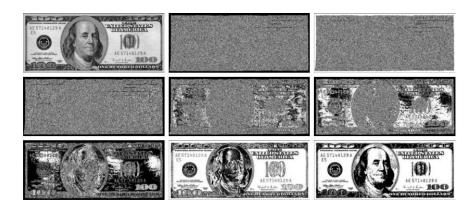
- Bitplanes
 - contribution of each bit for total image appearance
 - o gives clue for a compression

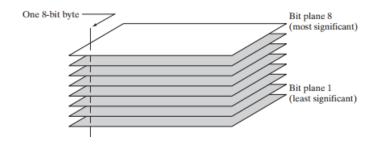


Bitplanes

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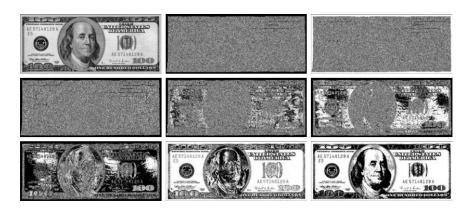
slicing

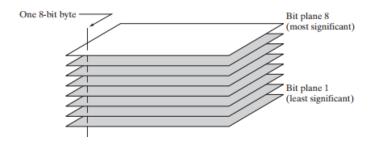




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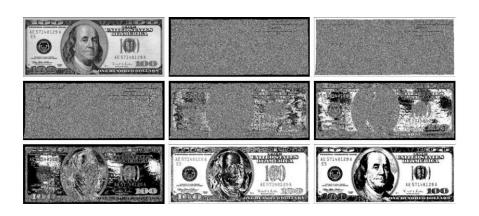


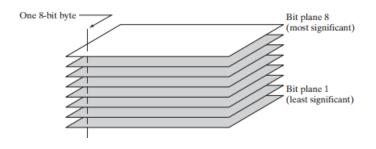


reconstruction

- Bitplanes
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 - o gives clue for a compression







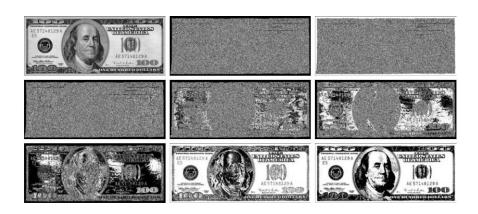
reconstruction

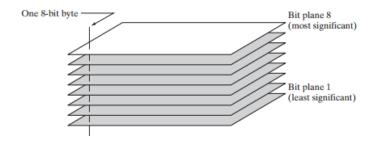


bitplanes (8+7)

- Bitplanes
 - contribution of each bit for total image appearance
 - o gives clue for a compression







reconstruction



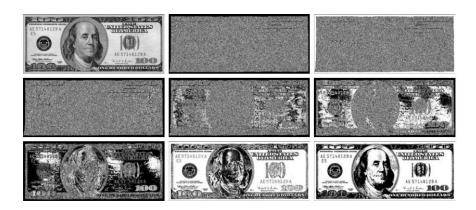
• bitplanes (8+7)

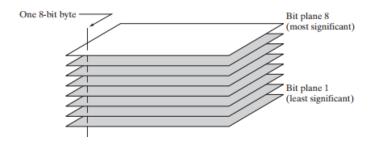


bitplanes (8+7+6)

- Bitplanes
 - contribution of each bit for total image appearance
 - o gives clue for a compression







reconstruction







- bitplanes (8+7)
- bitplanes (8+7+6)
- bitplanes (8+7+6+5)

Spatial domain enhancements

- Transformations
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 - logs
 - power-law (gamma)
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- Spatial filtering
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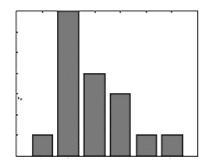
$$g(x,y) = T_i(f(x,y))$$

$$s \leftarrow r$$

$$g(x,y) = T_i(p(f(x,y)))$$

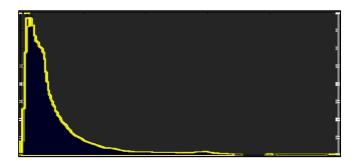
- distribution of discrete intensities
 - o distribution is also discrete

4	1	3	2
3	1	1	1
0	1	5	2
1	1	2	2

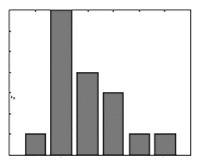


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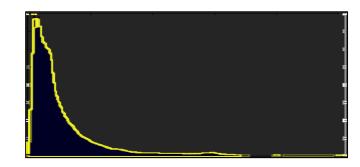


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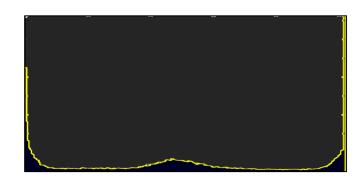


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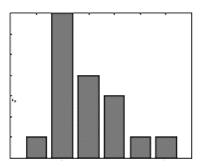








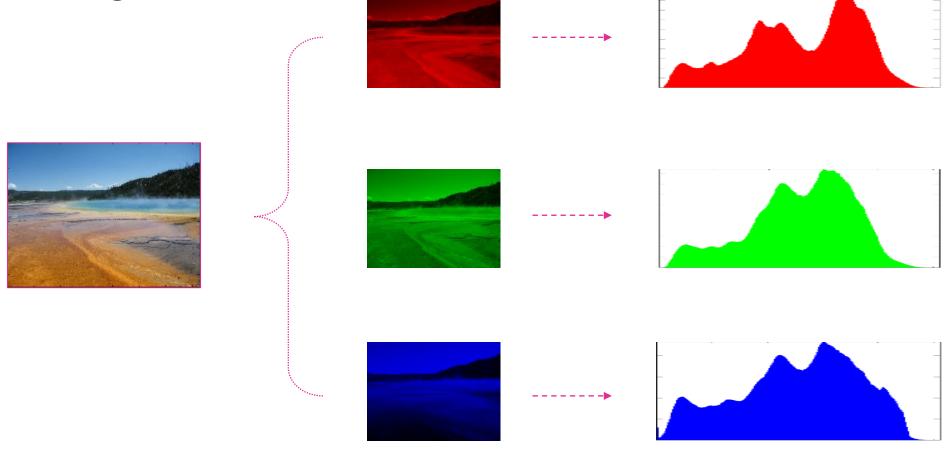
4	1	3	2
3	1	1	1
0	1	5	2
1	1	2	2



Color images



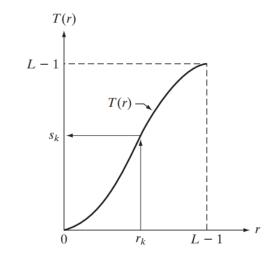
Color images

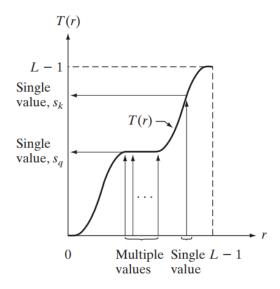


s = T(r)

- Assume
 - \circ T(r) is monotonic ↑
 - o bounded $0 \le T(r) \le L 1$
 - o variable equivalence
 - to cover all notations

$$0 \le r \le L - 1$$



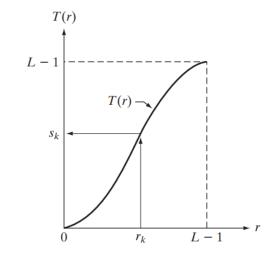


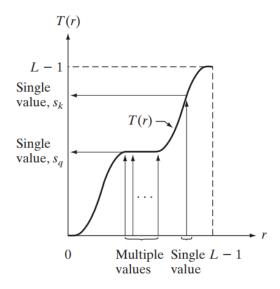
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$$Y = T(X)$$

$$s = T(r)$$

$$0 \le r \le L - 1$$



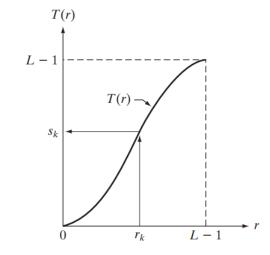


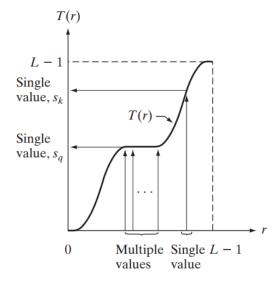
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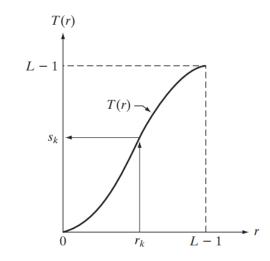
$$Y = T(X)$$

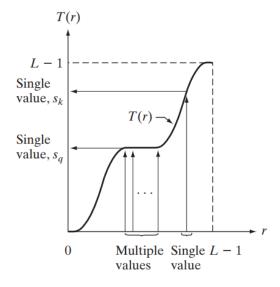
$$s = T(r)$$

$$\downarrow$$

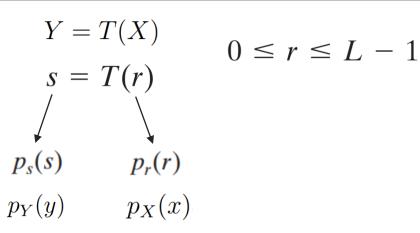
$$p_s(s) \qquad p_r(r)$$

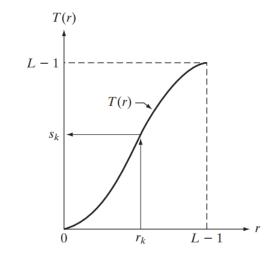
$$0 \le r \le L - 1$$

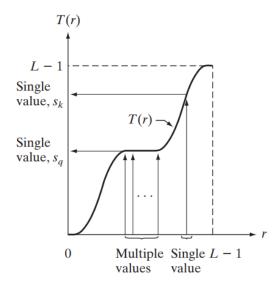




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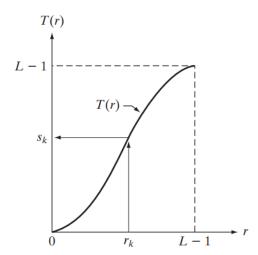
$$\downarrow$$

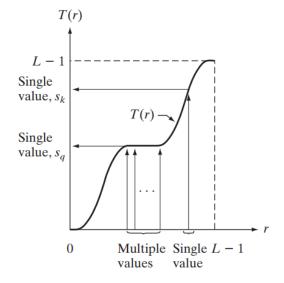
$$p_s(s) \qquad p_r(r)$$

$$p_Y(y) \qquad p_X(x)$$

$$0 \le r \le L - 1$$

T(r) is cts & differentiable



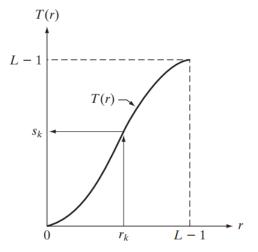


- Assume
 - \circ T(r) is monotonic ↑
 - o bounded $0 \le T(r) \le L 1$
 - o variable equivalence
 - to cover all notations

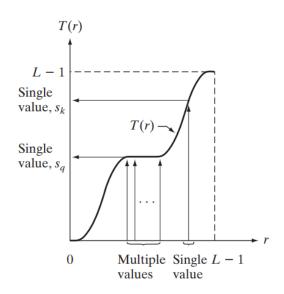
Y = T(X) s = T(r) $p_s(s) \qquad p_r(r)$ $p_Y(y) \qquad p_X(x)$

$$0 \le r \le L - 1$$

T(r) is cts & differentiable



• cumulative function satisfies above properties for T(r)



- Assume
 - \circ T(r) is monotonic ↑
 - o bounded $0 \le T(r) \le L 1$
 - variable equivalence
 - to cover all notations

• cumulative function satisfies above properties for T(r)

$$Y = T(X)$$

$$s = T(r)$$

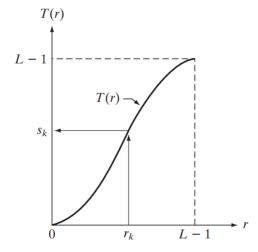
$$\downarrow$$

$$p_s(s) \qquad p_r(r)$$

$$p_Y(y) \qquad p_X(x)$$

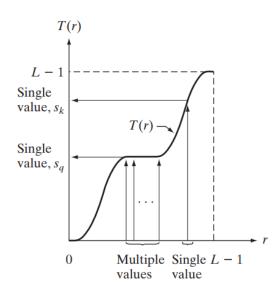
$$0 \le r \le L - 1$$

T(r) is cts & differentiable



$$s = T(r) = (L - 1) \int_0^r p_r(w) dw$$

$$Y = T(X) = (L-1) \int_0^X p_X(x) dx$$



- Assume
 - \circ T(r) is monotonic ↑
 - o bounded $0 \le T(r) \le L 1$
 - variable equivalence
 - to cover all notations

$$Y = T(X)$$

$$S = T(r)$$

 $p_r(r)$

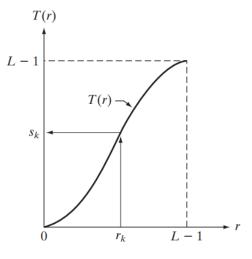
 $p_X(x)$

 $p_s(s)$

 $p_Y(y)$

$$0 \le r \le L - 1$$

T(r) is cts & differentiable



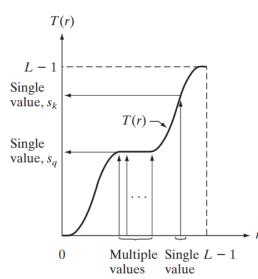
• cumulative function satisfies above properties for T(r)

$$s_k = T(r_k) = (L - 1) \sum_{j=0}^k p_r(r_j)$$

$$= \frac{(L-1)}{MN} \sum_{j=0}^{k} n_j \qquad k = 0, 1, 2, \dots, L-1$$

$$s = T(r) = (L - 1) \int_0^r p_r(w) dw$$

$$Y = T(X) = (L-1) \int_0^X p_X(x) dx$$



$$Y = T(X) = (L - 1) \int_0^X p_X(x) dx$$

$$Y = T(X)$$

$$\downarrow \qquad \qquad \downarrow$$

$$p_Y(y) \qquad p_X(x)$$

Y = T(X) T(X) is cts & differentiable

What is $p_Y(y)$?

$$Y = T(X) = (L-1) \int_0^X p_X(x) dx$$

$$Y = T(X)$$

$$\downarrow$$

$$p_Y(y) \qquad p_X(x)$$

Y = T(X) T(X) is cts & differentiable

$$\int_0^y p_Y(z)dz = \text{ probability that } 0 \le Y \le y$$

$$Y = T(X) = (L - 1) \int_0^X p_X(x) dx$$

$$Y = T(X)$$

$$\downarrow$$

$$p_Y(y) \qquad p_X(x)$$

Y = T(X) T(X) is cts & differentiable

$$\int_0^y p_Y(z)dz = \text{ probability that } 0 \le Y \le y$$

$$= \text{ probability that } 0 \le X \le T^{-1}(y)$$

$$Y = T(X) = (L-1) \int_0^X p_X(x) dx$$

$$\int_0^y p_Y(z)dz = \text{ probability that } 0 \le Y \le y$$

= probability that
$$0 \le X \le T^{-1}(y)$$

$$=\int_{0}^{T^{-1}(y)} p_X(w)dw$$

$$Y = T(X) = (L-1) \int_0^X p_X(x) dx$$

$$Y = T(X)$$

$$\downarrow \qquad \qquad \downarrow$$

$$p_Y(y) \qquad p_X(x)$$

Y = T(X) T(X) is cts & differentiable

$$\int_0^y p_Y(z)dz = \int_0^{T^{-1}(y)} p_X(w)dw$$

$$Y = T(X) = (L - 1) \int_0^X p_X(x) dx$$

$$Y = T(X)$$

$$\downarrow$$

$$p_Y(y) \qquad p_X(x)$$

Y = T(X) T(X) is cts & differentiable

$$\int_{0}^{y} p_{Y}(z)dz = \int_{0}^{T^{-1}(y)} p_{X}(w)dw$$

$$\frac{d}{dy} \left(\int_0^y p_Y(z) dz \right)$$

$$Y = T(X) = (L - 1) \int_0^X p_X(x) dx$$

$$Y = T(X)$$

$$\downarrow$$

$$p_Y(y) \qquad p_X(x)$$

Y = T(X) T(X) is cts & differentiable

$$\int_{0}^{y} p_{Y}(z)dz = \int_{0}^{T^{-1}(y)} p_{X}(w)dw$$

$$\frac{d}{dy}\left(\int_0^y p_Y(z)dz\right) = p_X(T^{-1}(y))\frac{d}{dy}(T^{-1}(y))$$

$$Y = T(X) = (L - 1) \int_0^X p_X(x) dx$$

$$Y = T(X)$$

$$\downarrow$$

$$p_Y(y) \qquad p_X(x)$$

Y = T(X) T(X) is cts & differentiable

$$\int_0^y p_Y(z)dz = \int_0^{T^{-1}(y)} p_X(w)dw$$

$$\frac{d}{dy}\left(\int_0^y p_Y(z)dz\right) = p_X(T^{-1}(y))\frac{d}{dy}(T^{-1}(y))$$

$$p_Y(y)$$

$$Y = T(X) = (L - 1) \int_0^X p_X(x) dx$$

$$Y = T(X)$$

$$\downarrow$$

$$p_Y(y) \qquad p_X(x)$$

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$$p_Y(y) = p_X(T^{-1}(y)) \frac{d}{dy}(T^{-1}(y))$$

$$Y = T(X) = (L - 1) \int_0^X p_X(x) dx$$

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$$\downarrow \qquad \qquad \downarrow$$

$$p_Y(y) \qquad p_X(x)$$

Y = T(X) T(X) is cts & differentiable

$$p_Y(y) = p_X(T^{-1}(y)) \frac{d}{dy}(T^{-1}(y))$$

$$= \frac{1}{L-1} \cdot \frac{dT}{dx}|_{x=T^{-1}(y)} \frac{d}{dy} (T^{-1}(y))$$

$$Y = T(X) = (L-1) \int_0^X p_X(x) dx$$

$$Y = T(X)$$

$$\downarrow \qquad \qquad \downarrow$$

$$p_Y(y) \qquad p_X(x)$$

Y = T(X) T(X) is cts & differentiable

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$$\frac{d}{dy}T(T^{-1}(y)) = \frac{d}{dy}y = 1$$

$$Y = T(X) = (L-1) \int_0^X p_X(x) dx$$

$$Y = T(X)$$

$$\downarrow \qquad \qquad \downarrow$$

$$p_Y(y) \qquad p_X(x)$$

Y = T(X) T(X) is cts & differentiable

$$p_Y(y) = p_X(T^{-1}(y)) \frac{d}{dy}(T^{-1}(y))$$

$$= \frac{1}{L-1} \cdot \frac{dT}{dx}|_{x=T^{-1}(y)} \frac{d}{dy} (T^{-1}(y))$$

$$\frac{d}{dy}T(T^{-1}(y)) = \frac{d}{dy}y = 1$$

$$=\frac{1}{L-1}$$

$$Y = T(X) = (L-1) \int_0^X p_X(x) dx$$

$$Y = T(X)$$

$$\downarrow \qquad \qquad \downarrow$$

$$p_Y(y) \qquad p_X(x)$$

Y = T(X) T(X) is cts & differentiable

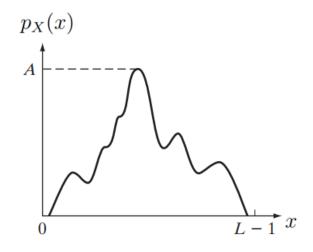
$$Y = T(X) = (L-1) \int_0^X p_X(x) dx$$

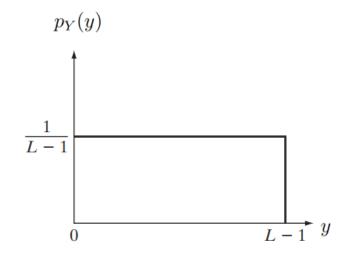
$$Y = T(X)$$

$$\downarrow \qquad \qquad \downarrow$$

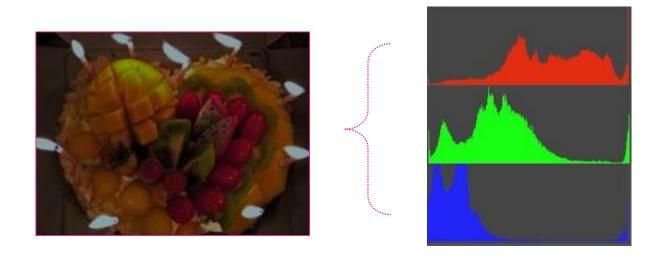
$$p_Y(y) \qquad p_X(x)$$

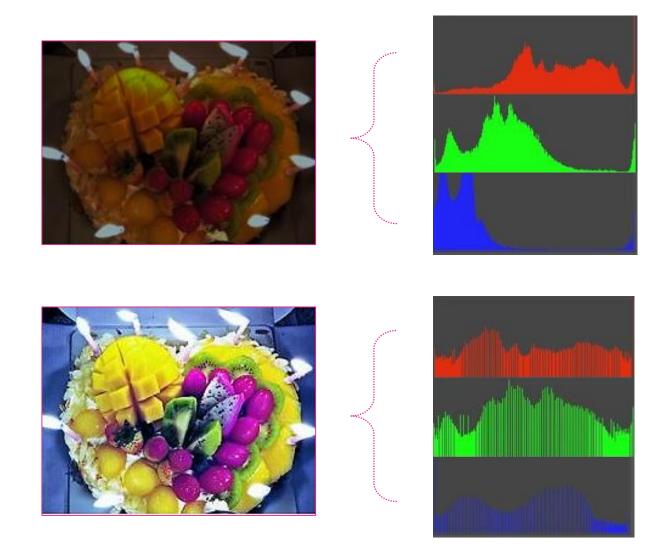
Y = T(X) T(X) is cts & differentiable

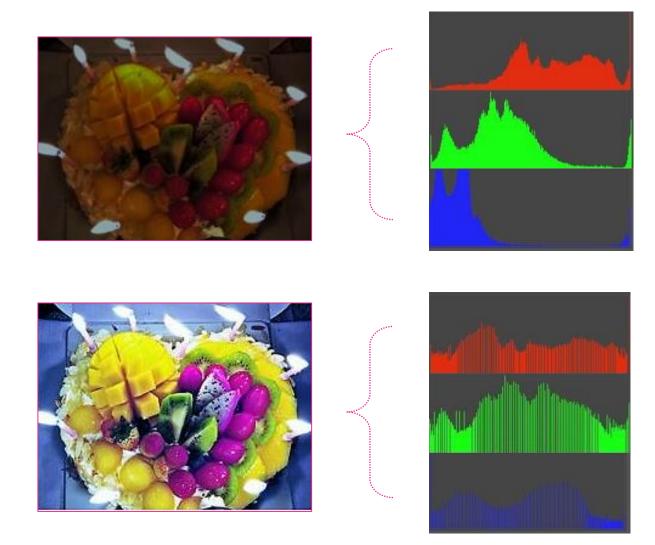






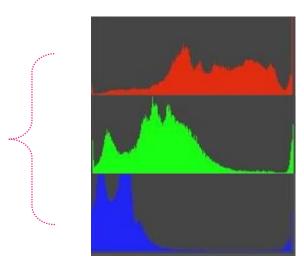






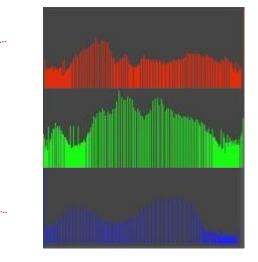


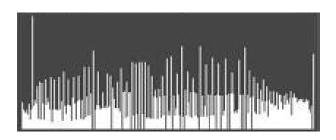




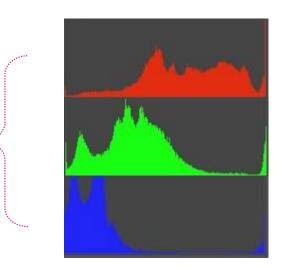




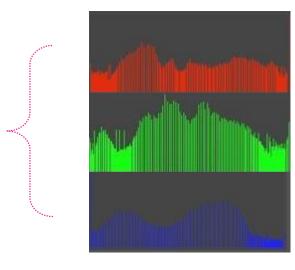






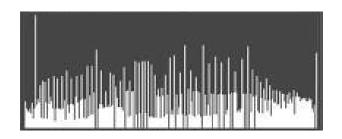


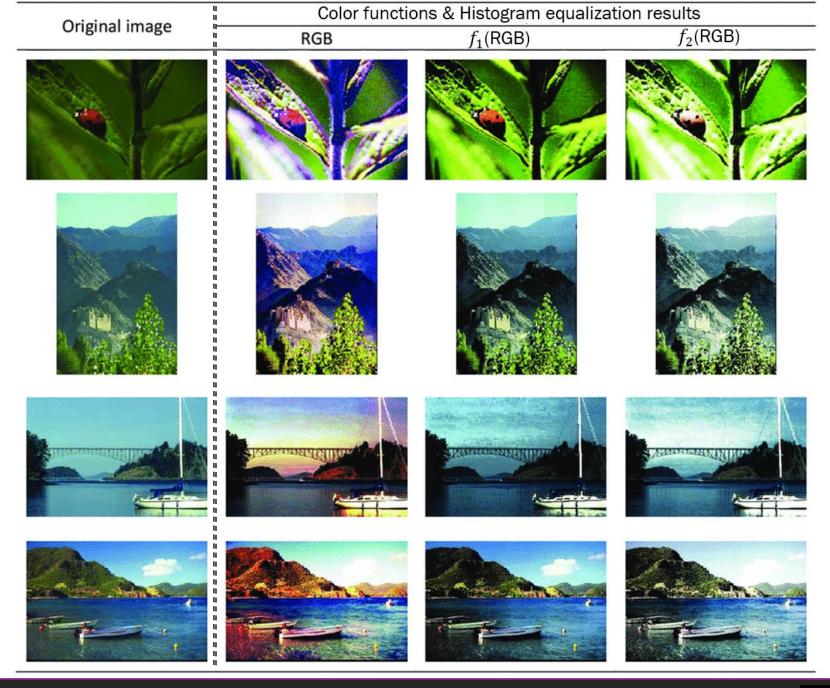




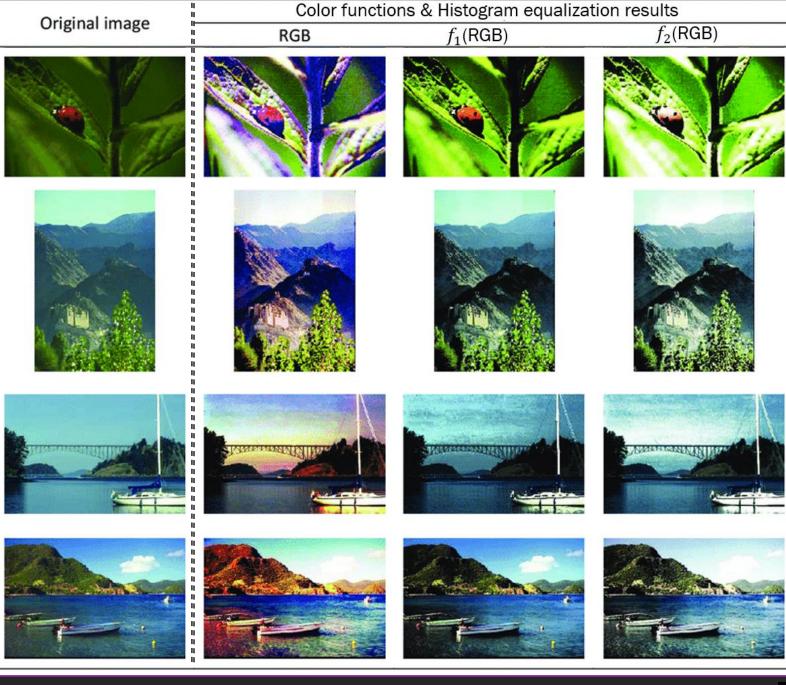




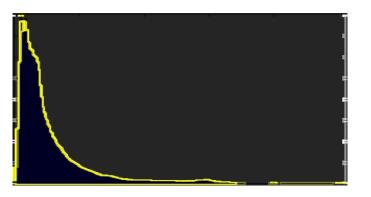


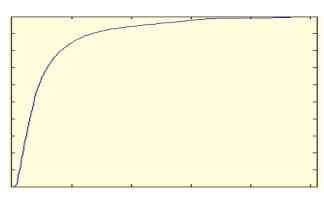


- Color conversions
 - colors can be mapped with certain functions
 - mapped images then histogram equalized

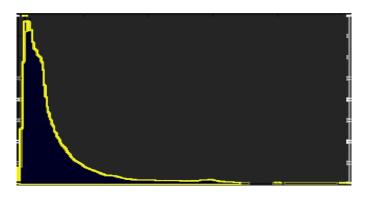


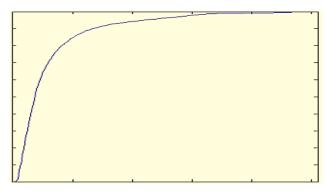




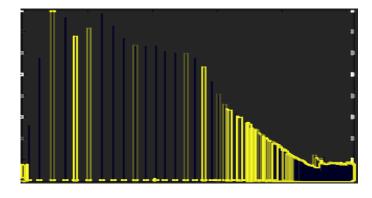


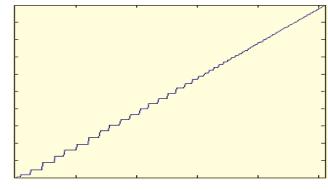












Conclusion

- Intensity transforms
- Distribution transforms

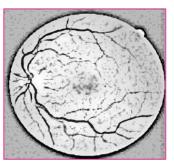
Conclusion

- Intensity transforms
- Distribution transforms









EE604: IMAGE PROCESSING

Conclusion

- Intensity transforms
- Distribution transforms

- ☐ Intensity transformations
 - negatives
 - logs
 - power-law (gamma)
 - contrast stretching
 - level slicing
 - bit-plane slicing

- Distribution transformations
 - Histogram equalization

