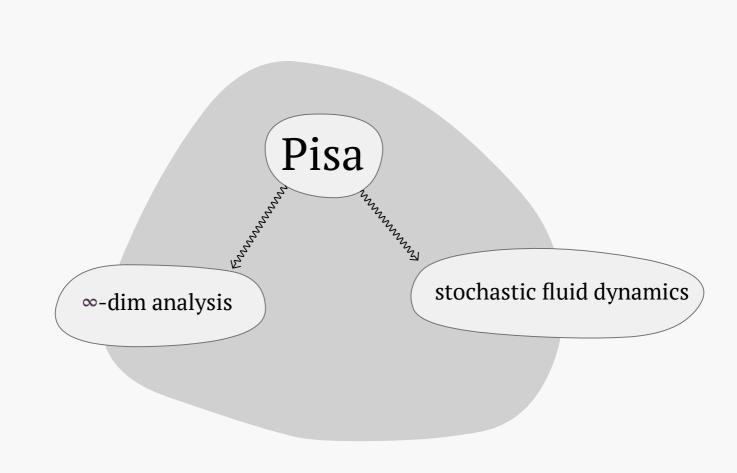
## the generator of some singular SPDEs



$$\partial_t u(t,x) = \Delta u(t,x) + \partial_x (u(t,x)^2) + \partial_x \xi(t,x), \qquad x \in \mathbb{T}, t \ge 0$$

with  $u(0) \sim \mu$  and  $\mu$  white noise on  $\mathbb{T}$  with zero mean.

► Formal generator

$$\mathcal{L}\varphi(u) = \underbrace{\int \partial_x^2 u(x) D_x \varphi(u) dx + \frac{1}{2} \text{Tr}[\partial_x \otimes \partial_x D^2 \varphi(u)]}_{\mathcal{L}_0} + \underbrace{\int (\partial_x u(x)^2) D_x \varphi(u) dx}_{\mathcal{L}_0}$$

$$\varphi(u) = \Phi(u(f_1), ..., u(f_n)) \qquad \Rightarrow \qquad D_x \varphi(u) = \sum_{i=1}^n \partial_k \Phi(u(f_1), ..., u(f_n)) f_k(x)$$

$$\mathcal{L}_{0}\boldsymbol{\varphi}(u) = \sum_{k=1}^{n} \partial_{k}\Phi(u(f_{1}),...,u(f_{n}))u(\Delta f_{k}) + \frac{1}{2}\sum_{k,\ell=1}^{n} \partial_{k}\partial_{\ell}\Phi(u(f_{1}),...,u(f_{n}))\langle\partial_{x}f_{k},\partial_{x}f_{\ell}\rangle$$

$$\mathcal{G}\varphi(u) = -\sum_{k=1}^{n} \partial_k \Phi(u(f_1), ..., u(f_n)) \int u(x)^2 \partial_x f_k(x) dx$$

▶ Problem:  $u^2(\partial_x f)$  is not a well-defined random variable – not even tested with  $\partial_x f$ .

$$\mathbb{E}[u^2(f)u^2(f)] \stackrel{\text{"="}}{\int} \delta(x-y)^2 f(x) f(y) dx dy \quad ?????$$

Indeed, it is a "distribution" on  $L^2(\mu)$ 

## diffusion with singular drift & regularisation by noise

[Assing ('03) (pre-generator), Flandoli-Russo-Wolf ('03), Delarue-Diel ('16), Allez-Chouk, Cannizzaro-Chouk]

## Gaussian space = symmetric Fock space

$$L^{2}(\mu) \approx \Gamma_{s}H = \bigotimes_{n \geq 0} H^{\bigotimes_{s} n}, \qquad H = L^{2}_{0}(\mathbb{T}) \approx \ell^{2}(\mathbb{N}_{\geq 0}), \qquad \mathbb{E}|\varphi(u)|^{2} = \sum_{n \geq 0} n! \|\varphi_{n}\|_{H^{\bigotimes_{n}}}^{2}$$

$$\varphi(u) = \sum_{n \geq 0} \underbrace{W_n(\varphi_n)}_{n-\text{th chaos}}, \qquad W_n(\varphi_n) = \sum_{k_1, \dots, k_n} \varphi_n(k_1, \dots, k_n) \underbrace{\llbracket \hat{u}(k_1) \cdots \hat{u}(k_n) \rrbracket}_{\text{Wick's product}}$$

$$\mathbb{E}(\overline{[\![\hat{u}(k_1)\cdots\hat{u}(k_n)]\!]}[\![\hat{u}(k_1')\cdots\hat{u}(k_n')]\!]) = \sum_{\sigma \in S_n} \mathbb{1}_{k_1 = k_{\sigma(1)}',\dots,k_n = k_{\sigma(n)}'}$$

$$D_k W_n(\boldsymbol{\varphi}_n) = n W_{n-1}(\boldsymbol{\varphi}_n(k, \cdots)) \qquad D_k^* W_n(\boldsymbol{\varphi}_n) = W_{n+1}(S(\mathbb{1}_k \otimes \boldsymbol{\varphi}_n))$$
destruction creation

$$\llbracket \hat{u}(k_1)\cdots\hat{u}(k_n)\rrbracket = D_{k_1}^*\cdots D_{k_n}^*1$$

$$u_k = D_k + D_k^*, \quad \overline{u_k} = u_{-k}, \quad D_k D_\ell^* = D_\ell^* D_k + \mathbb{1}_{\ell=k}$$

$$\mathcal{N} = \sum_{k} D_{k}^{*} D_{k}, \qquad \mathcal{L}_{0} = \sum_{k} k^{2} D_{k}^{*} D_{k} \qquad \mathcal{G} = \sum_{k+k_{1}+k_{2}=0} \iota k (D_{k_{1}} + D_{k_{1}}^{*}) (D_{k_{2}} + D_{k_{2}}^{*}) D_{k}$$

$$\mathcal{G} = \sum_{\substack{k+k_1+k_2=0\\ =0}} \iota k D_{k_1} D_{k_2} D_k + \sum_{\substack{k+k_1+k_2=0\\ =0}} \iota k \underbrace{D_{k_1}^* D_{k_2}^* D_k}_{1 \text{ particle}} + 2 \sum_{\substack{k+k_1+k_2=0\\ =0}} \iota k \underbrace{D_{k_1}^* D_{k_2} D_k}_{2 \text{ particles}} + 1 \text{ particle}$$

$$\sum_{k+k_1+k_2=0} \iota k D_{k_1} D_{k_2} D_k = \sum_{k+k_1+k_2=0} \iota \frac{k_1+k_2+k_3}{3} D_{k_1} D_{k_2} D_k = 0$$

$$u_k = D_k + D_k^*, \quad \overline{u_k} = u_{-k}, \quad D_k D_\ell^* = D_\ell^* D_k + \mathbb{1}_{\ell=k}$$

$$\mathcal{N} = \sum_{k} D_{k}^{*} D_{k}, \qquad \mathcal{L}_{0} = \sum_{k} k^{2} D_{k}^{*} D_{k} \qquad \mathcal{G} = \sum_{k+k_{1}+k_{2}=0} \iota k (D_{k_{1}} + D_{k_{1}}^{*}) (D_{k_{2}} + D_{k_{2}}^{*}) D_{k}$$

$$\mathcal{G} = \underbrace{\sum_{k+k_1+k_2=0} \iota k D_{k_1} D_{k_2} D_k}_{=0} + \underbrace{\sum_{k+k_1+k_2=0} \iota k}_{1 \text{ particle}} \iota k \underbrace{D_{k_1}^* D_{k_2}^* D_k}_{1 \text{ particles}} + 2 \underbrace{\sum_{k+k_1+k_2=0} \iota k}_{2 \text{ particles}} \iota k \underbrace{D_{k_1}^* D_{k_2} D_k}_{2 \text{ particles}}$$

$$\mathscr{G} = \mathscr{G}^+ - \mathscr{G}^-, \qquad (\mathscr{G}^{\pm})^* = \mathscr{G}^{\mp}$$

► Creation and destruction are unbounded operators

$$||D_k \varphi||^2 = \sum_{n \geq 0} n! ||(n+1)\varphi_{n+1}(k,\cdot)||^2 = \sum_{n \geq 0} (n+1)! ||(n+1)^{1/2} \varphi_{n+1}(k,\cdot)||^2 \leq ||(\mathcal{N}+1)^{1/2} \varphi||^2$$

$$D_k, D_k^*, u_k \approx \mathcal{N}^{1/2}$$

•  $\mathcal{G}^-$  is nice:

$$(\mathcal{G}^{-}\boldsymbol{\varphi})_{n} = \sum_{k+k_{1}+k_{2}=0} \iota k_{1} (D_{k_{1}}^{*} D_{k_{2}} D_{k} \boldsymbol{\varphi})_{n} = -\sum_{k+k_{1}+k_{2}=0} \iota (k+k_{2}) S(\mathbb{1}_{k_{1}} \otimes \boldsymbol{\varphi}_{n+1}(k,k_{2},\cdot))$$

So if  $k, k_2$  are bounded,  $k_1$  is also bounded and this function is in  $(\ell_0^2)^{\otimes n}$ .

 $\blacktriangleright \mathcal{G}^+$  is **not**:

$$(\mathcal{G}^+\boldsymbol{\varphi})_n = \sum_{k+k_1+k_2=0} \iota k_1 (D_{k_1}^* D_{k_2}^* D_k \boldsymbol{\varphi})_n = -\sum_{k+k_1+k_2=0} \iota \frac{k}{2} S(\mathbb{1}_{k_1} \otimes \mathbb{1}_{k_2} \otimes \boldsymbol{\varphi}_{n-1}(k, \cdot))$$

No chance that

$$\sum_{k+k_1+k_2=0} \mathbb{1}_{k_1} \otimes \mathbb{1}_{k_2} = \sum_{p \in \mathbb{Z}_0: p \neq 0, k} \mathbb{1}_{k-p} \otimes \mathbb{1}_p$$

$$k-p$$

is in  $\ell^2 \otimes \ell^2$ . Too many different possibilities for the created particles, irrespective of the test function  $\varphi$ .

 $\mathcal{G}^+$  is not a well-defined operator in  $\Gamma H$ .

•  $\mathscr{G} \varphi$  is only a (Hida) distribution

$$\|(-\mathcal{L}_0)^{-1/4}\mathcal{G}\boldsymbol{\varphi}\| \lesssim \|(\mathcal{N}+1)(-\mathcal{L}_0)^{1/2}\boldsymbol{\varphi}\|$$

▶ It looses both 1 degree of regularity in  $\mathcal{N}$  and 3/4 in  $(-\mathcal{L}_0)$ . However we "gain" one from  $\mathcal{L}_0$ ... so it remains  $(-\mathcal{L}_0)^{1/4}$  to spare.

► Useful in ¶<sub>|𝒢₀|≥𝒩</sub>αΓΗ:

$$\|\mathcal{N} \mathbb{1}_{|\mathcal{L}_0| \geqslant L \mathcal{N}^{\alpha}} \boldsymbol{\varphi} \| \lesssim L^{-1/\alpha} \| (-\mathcal{L}_0)^{1/\alpha} \mathbb{1}_{|\mathcal{L}_0| \geqslant \mathcal{N}^{\alpha}} \boldsymbol{\varphi} \| \lesssim L^{-1/\alpha} \| (-\mathcal{L}_0)^{1/\alpha} \boldsymbol{\varphi} \|$$

$$\|(-\mathscr{L}_0)^{-1/2}1_{\|\mathscr{L}_0\|\geqslant I_*\mathscr{N}} \alpha\mathscr{G} \boldsymbol{\varphi}\| \lesssim \delta \|(-\mathscr{L}_0)^{1/2} \boldsymbol{\varphi}\|$$

$$\mathcal{L}_0 \boldsymbol{\varphi} \approx -\mathcal{G}^- \boldsymbol{\varphi}$$

▶ To use  $\mathcal{L}_0 \varphi$  to compensate for  $\mathscr{G}^- \varphi$ : we look for "controlled"  $\varphi$  such that

We don't need to be greedy.

$$\mathscr{G}^{>} := \mathbb{1}_{|\mathscr{L}_{0}| \geq L, \mathcal{N}^{\alpha}} \mathscr{G}, \qquad \mathscr{G}^{<} = \mathscr{G} - \mathscr{G}^{>}$$

 $\mathscr{G}^{>}$  models the large momentum behaviour of  $\mathscr{G}$  . L is a cutoff to be chosen later.

$$oldsymbol{arphi} = -\mathcal{L}_0^{-1} \mathcal{G}^{\succ} oldsymbol{arphi} + oldsymbol{arphi}^{\#}, \qquad oldsymbol{arphi} = \mathcal{K} oldsymbol{arphi}^{\#}$$

$$\mathcal{L} \varphi = \mathcal{L}_0 \varphi + \mathcal{G} \varphi = \mathcal{L}_0 \varphi^{\#} + \mathcal{G}^{\checkmark} \varphi$$

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For 
$$\gamma \in (1/4, 1/2]$$

$$\|w(\mathcal{N})(-\mathcal{L}_0)^{\gamma - 1} \mathcal{G}^{>} \boldsymbol{\varphi}\| \lesssim \varepsilon |w| \|(-\mathcal{L}_0)^{\gamma} w(\mathcal{N}) \boldsymbol{\varphi}\|$$

 $\|w(\mathcal{N})(-\mathcal{L}_0)^{\gamma-1}\mathcal{G}^{\succ}\varphi\|\lesssim \varepsilon|w|\|(-\mathcal{L}_0)^{\gamma}w(\mathcal{N})\varphi\|$ 

so  $\mathcal{L}\varphi = \mathcal{L}_0\varphi^{\#} + \mathcal{G}^{\checkmark}\varphi$  is well defined for controlled functions.

is dense in  $w(\mathcal{N})^{-1}\Gamma H$  and  $\mathcal{D}(\mathcal{L}) = \mathcal{D}_1(\mathcal{L})$ .

► For all  $\gamma \ge 0$   $\delta > 0$ 

 $\|(-\mathcal{L}_0)^{\gamma}w(\mathcal{N})\mathcal{K}\boldsymbol{\varphi}^{\sharp}\| + (|w|\boldsymbol{\varepsilon})^{-1}\|(-\mathcal{L}_0)^{\gamma}w(\mathcal{N})(\mathcal{K}\boldsymbol{\varphi}^{\sharp} - \boldsymbol{\varphi}^{\sharp})\| \lesssim \|(-\mathcal{L}_0)^{\gamma}w(\mathcal{N})\boldsymbol{\varphi}^{\sharp}\|$ 

 $\|w(\mathcal{N})(-\mathcal{L}_0)^{\gamma}\mathcal{G}^{\prec}\boldsymbol{\varphi}\| \lesssim \|w(\mathcal{N})(1+\mathcal{N})^{9/2+7\gamma}(-\mathcal{L}_0)^{1/4+\delta}\boldsymbol{\varphi}^{\#}\|$ 

 $\mathcal{D}_{w}(\mathcal{L}) = \{ \boldsymbol{\varphi} = \mathcal{K} \boldsymbol{\varphi}^{\sharp} : \| w(\mathcal{N})(-\mathcal{L}_{0})\boldsymbol{\varphi}^{\sharp} \| + \| w(\mathcal{N})(1+\mathcal{N})^{9/2}(-\mathcal{L}_{0})^{1/2}\boldsymbol{\varphi}^{\sharp} \| \}$ 

Densely defined operator

$$(\mathscr{L},\mathscr{D}(\mathscr{L}))$$

$$\blacktriangleright \mathcal{L}$$
 is dissipative

$$\langle \boldsymbol{\varphi}, \mathcal{L} \boldsymbol{\varphi} \rangle = -\|(-\mathcal{L}_0)^{1/2} \boldsymbol{\varphi}\|^2 \leq 0, \qquad \boldsymbol{\varphi} \in \mathcal{D}(\mathcal{L})$$

$$\langle \psi, \mathcal{L} \varphi \rangle = \langle \mathcal{L}^{(-1)} \psi, \varphi \rangle, \qquad \varphi \in \mathcal{D}(\mathcal{L})$$
 $\langle \psi, \mathcal{L} \varphi \rangle = \langle \mathcal{L}^{(-1)} \psi, \varphi \rangle, \qquad \varphi \in \mathcal{D}(\mathcal{L}), \psi \in \mathcal{D}(\mathcal{L}^{(-1)})$ 

▶For  $\mathcal{L}^{(\lambda)} = \mathcal{L}_0 + \lambda \mathcal{G}$  with  $\lambda \in \mathbb{R}$  similar construction:  $\mathcal{D}(\mathcal{L}^{(\lambda)}) \cap \mathcal{D}(\mathcal{L}^{(\lambda')}) = \{\text{constants}\}...$ 

•  $\mathcal{L}^m$  Galerkin approximation for  $\mathcal{L}$ ,  $(T_t^m)_t$  Markov semigroup

$$\partial_t \boldsymbol{\varphi}^m(t) = \mathcal{L}^m \boldsymbol{\varphi}^m(t)$$

 $\frac{1}{2}\partial_t \|w(\mathcal{N})\boldsymbol{\varphi}^m(t)\|^2 + \|w(\mathcal{N})(-\mathcal{L}_0)^{1/2}\boldsymbol{\varphi}^m(t)\|^2 = \langle \boldsymbol{\varphi}^m(t), w(\mathcal{N})^2 \mathcal{G}^m \boldsymbol{\varphi}^m(t) \rangle$ 

• We have for  $\gamma > 1/4$  and uniformly in m

$$\|w(\mathcal{N})(-\mathcal{L}_0)^{-\gamma}\mathcal{G}_+^m\psi\| \lesssim \|w(\mathcal{N})\mathcal{N}(-\mathcal{L}_0)^{3/4-\gamma}\psi\| \qquad (roughly)$$

$$\langle \varphi^{m}(t), w(\mathcal{N})^{2} \mathcal{G}^{m} \varphi^{m}(t) \rangle = \langle \varphi^{m}(t), w(\mathcal{N})^{2} (\mathcal{G}_{+}^{m} + \mathcal{G}_{-}^{m}) \varphi^{m}(t) \rangle$$

$$= \langle \varphi^{m}(t), w(\mathcal{N})^{2} \mathcal{G}_{+}^{m} \varphi^{m}(t) \rangle + \langle \varphi^{m}(t), \mathcal{G}_{-}^{m} w(\mathcal{N} + 1)^{2} \varphi^{m}(t) \rangle$$

$$= \langle \varphi^{m}(t), [w(\mathcal{N})^{2} - w(\mathcal{N} + 1)^{2}] \mathcal{G}_{+}^{m} \varphi^{m}(t) \rangle \approx \langle \varphi^{m}(t), w(\mathcal{N}) \underbrace{w'(\mathcal{N})}_{\approx w(\mathcal{N}) \mathcal{N}^{-1}} \mathcal{G}_{+}^{m} \varphi^{m}(t) \rangle$$

$$\leq \delta \| w(\mathcal{N}) (-\mathcal{L}_0)^{1/2} \boldsymbol{\varphi}^m(t) \|^2 + c_{\delta} \| w(\mathcal{N}) (-\mathcal{L}_0)^{-1/2} \mathcal{N}^{-1} \mathcal{G}_+^m \boldsymbol{\varphi}^m(t) \|^2$$

$$\leq \delta \| w(\mathcal{N}) (-\mathcal{L}_0)^{1/2} \boldsymbol{\varphi}^m(t) \|^2 + c_{\delta} \| w(\mathcal{N}) (-\mathcal{L}_0)^{1/4} \boldsymbol{\varphi}^m(t) \|^2$$

$$\frac{1}{2}\partial_t \|w(\mathcal{N})\boldsymbol{\varphi}^m(t)\|^2 + \delta \|w(\mathcal{N})(-\mathcal{L}_0)^{1/2}\boldsymbol{\varphi}^m(t)\|^2 \leq c_\delta' \|w(\mathcal{N})\boldsymbol{\varphi}^m(t)\|^2$$

▶ To pass to the limit in the Kolmogorov equation we need further regularity to put  $\lim_{m} \varphi^{m}$  in the domain of  $\mathscr{L}$ . We need control of

$$\varphi^{m,\#}(t) = \varphi^m(t) + \mathcal{L}_0^{-1} \mathcal{G}^{m,*} \varphi^m(t)$$

▶ The equation for  $\varphi^{m,\#}$  gives the required apriori estimates

$$\partial_t \varphi^{m,\#}(t) = \mathcal{L}^m \varphi^m(t) + \mathcal{L}_0^{-1} \mathcal{G}^{m,*} \partial_t \varphi^m(t) = \mathcal{L}_0 \varphi^{m,\#}(t) + \mathcal{G}^{m,*} \varphi^m(t) + \mathcal{L}_0^{-1} \mathcal{G}^{m,*} \partial_t \varphi^m(t)$$

For  $\gamma \in (3/8, 5/8)$ , exists  $p(\alpha)$  s.t.

$$\|(1+\mathcal{N})^{\alpha}(-\mathcal{L}_{0})^{1+\gamma}\varphi^{m,\#}(t)\|+\|(1+\mathcal{N})^{\alpha}(-\mathcal{L}_{0})^{\gamma}\partial_{t}\varphi^{m,\#}(t)\|\lesssim \|(1+\mathcal{N})^{p(\alpha)}(-\mathcal{L}_{0})^{1+\gamma}\varphi^{m,\#}(0)\|$$

▶ Given

$$\|(1+\mathcal{N})^{p(\alpha)}(-\mathcal{L}_0)^{1+\gamma}\boldsymbol{\varphi}(0)\| < \infty$$

with  $\alpha > 9/2$  and  $\gamma \in (3/8, 5/8)$  then

$$\partial_t \boldsymbol{\varphi}(t) = \mathcal{L} \boldsymbol{\varphi}(t)$$

has a solution

$$\varphi \in C(\mathbb{R}_+, \mathcal{D}(\mathcal{L})) \cap C^1(\mathbb{R}_+, \Gamma H)$$

• Unique by dissipativity (but we cannot define flow  $e^{t\mathscr{L}}$ )

▶ By Galerkin approximation we can construct a stationary process  $(u_t^m)_t$  such that

$$\varphi^m(u^m(t)) = \varphi^m(u^m(0)) + \int_0^t \mathcal{L}^m \varphi^m(u^m(s)) ds + M_t^{m,\varphi}$$

- Compactness by energy solution methods.
- ► For all  $\varphi \in \mathcal{D}(\mathcal{L}) \subseteq \Gamma H$

$$\varphi(u(t)) = \varphi(u(0)) + \int_0^t \mathcal{L} \varphi(u(s)) ds + M_t^{\varphi}$$

- ▶ This makes sense only if Law(u(t))  $\ll \mu$ . Incompressible solutions.
- - ▶ Uniqueness by duality with the backward equation

 $\mathbb{E}[\varphi(u_t)\psi(u_s)] = \mathbb{E}[(\varphi(t-s,u_t) + \int_s^t (\partial_r + \mathcal{L})\varphi(t-r,u_r)dr)\psi(u_s)] = \mathbb{E}[\varphi(t-s,u_s)\psi(u_s)]$ 

▶ Multi-component Burgers eq. [Funaki-Hoshino '17, Kupiainen-Marcozzi '17]

$$\partial_t u^i = \Delta u^i + \sum_{j,k} \Gamma^i_{jk} \partial_x (u^j u^k) + \partial_x \xi^i$$

under "trilinear condition" [Funaki-Hoshino '17]:  $\Gamma_{jk}^i = \Gamma_{kj}^i = \Gamma_{ki}^j$ .

▶ Fractional Burgers eq. [G.-Jara '13]

$$\partial_t u = -(-\Delta)^{\theta} u + \partial_x u^2 + (-\Delta)^{\theta/2} \xi$$

for  $\theta > 3/4$ ; note that  $\theta = 3/4$  is critical,  $\infty$  expansion in reg. str.!

▶ 2d NS with small hyperdissipation and energy invariant measure (G., Turra, in prep.)  $\kappa > 0$ 

$$\partial_t u = -(-\Delta)^{1+\kappa} u + u \cdot \nabla u + (-\Delta)^{(1+\kappa)/2} \mathcal{E}, \quad u: \mathbb{T}^2 \to \mathbb{R}^2$$

ightharpoonupLimitations: need Gaussian invariant measure (quasi-invariance should work), once use antisymmetry of  $\mathscr{G}$ ; might be avoided.

- ► Weak universality for fractional Burgers [Sethuraman '16, Gonçalves-Jara '18] and multi-component Burgers [Bernardin-Funaki-Sethuraman '19+]
- ▶ Burgers on  $\mathbb{R}$  is ergodic (extension to KPZ Perkowski, Zhu-Zhu).
- ▶ Burgers on T is exponentially ergodic [Gubinelli-P. '18]:

$$\int |\mathbb{E}_{u}[\varphi(u_{t})] - \int \varphi \, d\mu|^{2} \, d\mu(u) \leq e^{-8\pi^{2}t} \int \varphi^{2} \, d\mu$$

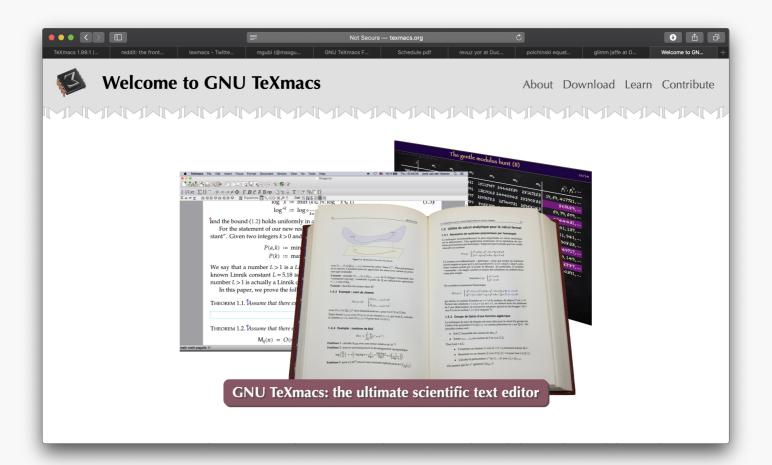
Ergodicity on T known by [Hairer-Mattingly '18.]

▶ (Multi-component / fractional) KPZ on  $\mathbb{T}$  has Gaussian fluctuations (*Perkowski*, *Canniz-zaro*). Tracy-Widom fluctuations on  $\mathbb{R}$  [Sasamoto-Spohn '10, Amir-Corwin-Quastel '11].

- ▶ Probabilistic theory for singular SPDEs  $\leftrightarrow \infty$ -dim singular operator  $\mathcal{L} = \mathcal{L}_0 + \mathcal{G}$ .
- ▶ Under Gaussian (invariant) measure: use chaos decomposition → work on Fock space
- ▶ Construct  $\mathcal{D}(\mathcal{L})$  via ideas from paracontrolled distributions.
- ▶ Existence for martingale problem via Galerkin approximation.
- ▶ Existence for backward equation  $\partial_t \varphi = \mathcal{L} \varphi$  via energy estimates.
- ▶ Duality gives uniqueness for martingale prob. and backward eq.
- ▶ (multi-component, fractional) Burgers, down to criticality.
- ▶ Need Gaussian measure. beyond: unclear.

Buon compleanno, Franco!





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