

$R(ABC)$ $f = \{ A \rightarrow B, B \rightarrow C \}$

$\phi^+ = \{ \phi \}$ → ①

$A^+ = \{ A, B, C \}$ → ④

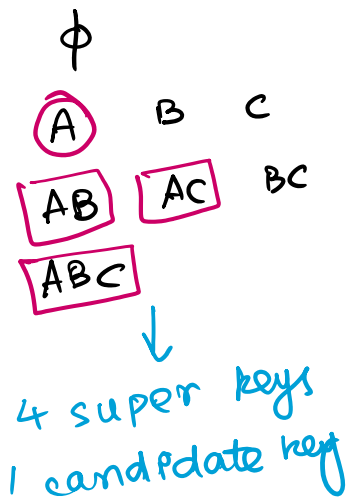
$B^+ = \{ B, C \}$ → ④

$C^+ = \{ C \}$ → ②

$BC^+ = \{ B, C \}$ → ④

$8 \times 4 = 32$

43 functional dependencies



candidate key

- ① attributes neither on left / right.
- ② attributes only on right.
- ③ attributes only on left.
- ④ 1 ∪ 3
- ⑤ Test if closure on ④ includes all attributes, if yes → candidate key

or

- (i) Find attributes that are on both sides
- (ii) Find closure of core attributes + one exterior attribute taken one at a time

$$R = \{ W, H, O, S, E \}$$

$$F = \{ WH \rightarrow S, HOS \rightarrow E \}$$

- ① ϕ ② E ③ WHO ④ WHO

$$(WHO)^+ = \{ W, H, O, S, E \}$$

↪ candidate key

$$R (A B C D E F G)$$

$$F = \{ AB \rightarrow F, AD \rightarrow E, F \rightarrow G \}$$

- ① C ② EG ③ ABD ④ $ABCD$

$$(ABCD)^+ = \{ A, B, C, D, E, F, G \}$$

$$R (A B C D)$$

$$F = \{ ABC \rightarrow D, D \rightarrow A \}$$

- ① ϕ ② ϕ ③ BC ④ BC

$$(BC)^+ = \{ B, C \}$$

- ⑤ (i) A, D

$$(ABC)^+ = \{ A, B, C, D \}$$

$$(BCD)^+ = \{ A, B, C, D \}$$

~~ABCD~~

3 super keys
& candidate keys

$$R (A B C D E F)$$

$$F = \{ DF \rightarrow C, BC \rightarrow F, E \rightarrow A, ABC \rightarrow E \}$$

- ② BD ④ BD

$$+ = \{ \text{D}, \text{F}, \text{C}, \text{E} \}$$

- ① ϕ ② ϕ ③ BD ④ BD

$$(\text{BD})^+ = \{ \text{B}, \text{D} \} \quad \text{X}$$

⑤ (i) ACEF

$$(\text{BDA})^+ = \{ \text{A}, \text{B}, \text{D} \} \quad \text{X}$$

$$(\text{BDC})^+ = \{ \text{B}, \text{C}, \text{D}, \text{F} \} \quad \text{X}$$

$$(\text{BDE})^+ = \{ \text{B}, \text{D}, \text{E} \} \quad \text{X}$$

$$(\text{BDF})^+ = \{ \text{B}, \text{D}, \text{F}, \text{C} \} \quad \text{X}$$

$$(\text{BDAC})^+ = \{ \text{A}, \text{B}, \text{C}, \text{D}, \text{E}, \text{F} \} \quad \checkmark$$

$$(\text{BD AE})^+ = \{ \text{A}, \text{B}, \text{D}, \text{E} \} \quad \checkmark$$

$$(\text{BD AF})^+ = \{ \text{A}, \text{B}, \text{D}, \text{F}, \text{C}, \text{E} \} \quad \checkmark$$

$$(\text{BD CE})^+ = \{ \text{B}, \text{C}, \text{D}, \text{E}, \text{F}, \text{A} \} \quad \checkmark$$

$$(\text{BD CF})^+ = \{ \text{B}, \text{C}, \text{D}, \text{F} \} \quad \text{X}$$

$$(\text{BDEF})^+ = \{ \text{B}, \text{D}, \text{E}, \text{F}, \text{C}, \text{A} \} \quad \checkmark$$

BDA

BDC

BDE

BDF

BDAC

BD AE

BD AF

BD CE

BD CF

BDEF

BDACE

BDACF

BD AEF

BDCEF

BDACEF

4 candidate keys

9 super keys

$R(\text{ABCDE}) \quad \{ \text{AB} \rightarrow \text{C}, \text{C} \rightarrow \text{D}, \text{B} \rightarrow \text{AE} \}$

- ① ϕ ② DE ③ B ④ B

$$\text{B}^+ = \{ \text{B}, \text{A}, \text{E}, \text{C}, \text{D} \}$$

candidate key = B

super keys = B

$[\text{A} + \text{R} + \text{D} + \text{E}]$

① candidate key

16 super keys