SLR Parsers, LR (0) items

Bottom-up Parsers

- Simple Shift-reduce parsers has lot of Shift/Reduce conflicts
- Operator precedence parsers is for a small class of grammars
- Go for LR parsers

- LR(1) parsers recognize the languages in which one symbol of lookahead is sufficient to decide whether to shift or reduce
 - L: for left-to-right scan of the input
 - R : for reverse rightmost derivation
 - 1: for one symbol of look-ahead

- Read input, one token at a time
- Use stack to keep track of current state
 - The state at the top of the stack summarizes the information below.
 - The stack contains information about what has been parsed so far.

- Use parsing table to determine action based on current state and look-ahead symbol.
- Parsing table construction takes into account the shift, reduce, accept or error action

- SLR
 - Simple LR parsing
 - Easy to implement, but not powerful
 - Uses LR(0) items
- Canonical LR
 - Larger parser but powerful
 - Uses LR(1) items

• LALR

- Condensed version of canonical LR
- May introduce conflicts
- Uses LR(1) items

SLR Parsers - Handle

- As a SLR parser processes the input, it must identify all possible handles.
- For example, consider the usual expression grammar and the input string

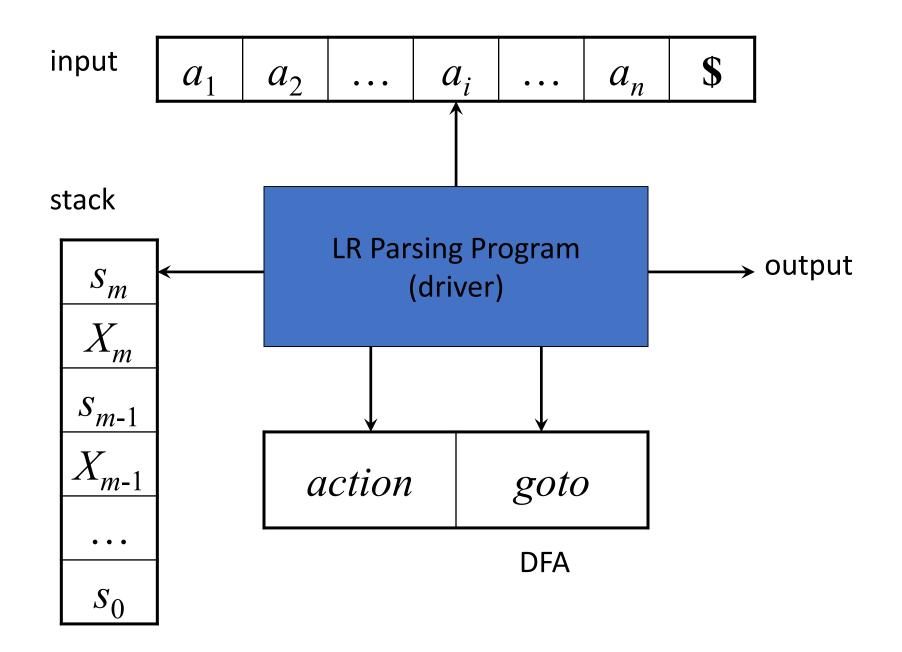
a + b.

- If the parser has processed 'a' and reduced it to E. Then, the current state can be represented by E +E where means
 - E has already been parsed and
 - +E is a potential suffix, which, if determined, yields to a successful parse.

SLR parsers

 Our ultimate aim is to finally reach state E+E●, which corresponds to an actual handle yielding to the reduction E→E+E

- LR parsing works by building an automata where each state represents what has been parsed so far and what we intend to parse after looking at the current input symbol. This is indicated by productions having a "." These productions are referred to as items.
- Items that has the "." at the end leads to the reduction by that production



SLR (1) Parser

- Form the augmented grammar
- Construction of LR(0) items
- Construct the follow() for all the non-terminals which requires construction of first() for all the terminals and nonterminals

SLR(1) parser

- Using this and the follow() of the grammar, construct the parsing table
- Using the parsing table, a stack and an input parse the input

LR (0) items

- An *LR(0) item* of a grammar *G* is a production of *G* with a at some position of the right-hand side
- Thus, a production

$$A \rightarrow X Y Z$$

has four items:

$$[A \rightarrow \bullet X Y Z]$$

$$[A \rightarrow X \bullet YZ]$$

$$[A \rightarrow X Y \bullet Z]$$

$$[A \rightarrow X Y Z \bullet]$$

• that production $A \to \varepsilon$ has one item $[A \to \bullet]$

LR (0) items

- The grammar is augmented with a new start symbol S' and production $S' \rightarrow S$
- Initially, set $C = closure(\{[S' \rightarrow \bullet S]\})$
- For each set of items $I \in C$ and each grammar symbol $X \in (N \cup T)$ such that $goto(I,X) \notin C$ and $goto(I,X) \neq \emptyset$,
 - add the set of items goto(I,X) to C
- Repeat until no more sets can be added to C

Closure (I)

- Start with closure(I) = I
- If $[A \rightarrow \alpha \bullet B\beta] \in closure(I)$ then for each production $B \rightarrow \gamma$ in the grammar, add the item $[B \rightarrow \bullet \gamma]$ to closure(I) if it is not already there
- Repeat 2 until no new items can be added to closure(I)

Goto (I, X)

- For each item $[A \rightarrow \alpha \bullet X\beta] \in I$, add the set of items $closure(\{[A \rightarrow \alpha X \bullet \beta]\})$ to goto(I,X) if not already there
- Repeat until no more items can be added to goto(I,X)
- Intuitively, goto(I,X) is the set of items that are valid for the viable prefix γX when I is the set of items that are valid for γ

Augmented Grammar

$$E' \rightarrow E$$

- 1. $E \rightarrow E + T$
- 2. $E \rightarrow T$
- 3. $T \rightarrow T * F$
- 4. $T \rightarrow F$
- 5. $F \rightarrow (E)$
- 6. $F \rightarrow id$

Augmented Grammar

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- E' → .E
- E → . E +T
- \bullet E \rightarrow .T
- \bullet T \rightarrow .T * F
- \bullet T \rightarrow .F
- $F \rightarrow . (E)$
- $F \rightarrow$. id

17: (noto (2, *) 7-77 x. F Gots (993) F7.(E) FJ.id 18: Goto (94, E)

F -> (E.) モンE·+T

29: Gota (96, T) とうモナて。 てって、*ド

1 16: Got (1-7,7) てつて炸。 1(1: Goto (18,)) F7(E).

Items

- I₀
- $E' \rightarrow .E$
- E → . E +T
- $\bullet E \rightarrow .T$
- T \rightarrow .T * F
- \bullet T \rightarrow .F
- $F \rightarrow . (E)$
- $F \rightarrow$. id

- $I_1 = Goto (I_0, E)$
- $E' \rightarrow E$.
- $E \rightarrow E . + T$

- $I_2 = Goto(I_0, T), Goto(I_4, T),$
 - $E \rightarrow T$.
 - $T \rightarrow T.*F$

- I₃ = Goto (I₀, F), Goto (I₄, F), Goto (I₆, F)
- T \rightarrow F.

I₅= Goto (I₀, id), Goto (I₄, id), Goto (I₆, id), Goto (I₇, id)
 F → id.

- I₄ = Goto (I₀, (), Goto (I₄, (), Goto (I₆, (), Goto (I₇,()
- $F \rightarrow (.E)$
- $E \rightarrow .E + T$
- $E \rightarrow .T$
- $T \rightarrow .T * F$
- $T \rightarrow .F$
- $F \rightarrow .(E)$
- $F \rightarrow .id$

Items

$$I_{6} = \operatorname{Goto}(I_{1}, +), \operatorname{Goto}(I_{8}, +), \qquad F \rightarrow (E.)$$

$$E \rightarrow E + . T \qquad E \rightarrow E . + T$$

$$T \rightarrow .T * F$$

$$T \rightarrow .F \qquad I_{9} = \operatorname{Goto}(I_{6}, T)$$

$$F \rightarrow .(E) \qquad E \rightarrow E + T.$$

$$T \rightarrow T * F$$

$$I_{7} : \operatorname{Goto}(I_{2}, *), \operatorname{Goto}(I_{9}, *) \qquad I_{10} : \operatorname{Goto}(I_{7}, F)$$

$$T \rightarrow T * . F$$

$$F \rightarrow .(E)$$

$$F \rightarrow .id \qquad I_{11} : \operatorname{Goto}(I_{8},))$$

$$F \rightarrow (E).$$

SLR Parsing Table

- Input: Augmented Grammar G'
- Output: SLR parsing table with functions, shift, reduce and accept
- Parsing table is between items and Terminals and nonterminals
- The non-terminals correspond to the goto() of the items set
- The terminals have the parsing table corresponding to the action – shift / reduce/accept

SLR Parsing Table

- Augment the grammar with $S' \rightarrow S$
- Construct the set $C=\{I_0,I_1,...,I_n\}$ of LR(0) items
- If $[A \rightarrow \alpha \bullet a\beta] \in I_i$ and $goto(I_i,a)=I_j$ then set action[i,a]=shift j, where a is a terminal
- If $[A \rightarrow \alpha \bullet] \in I_i$ then set action[i,a]=reduce $A \rightarrow \alpha$ for all $a \in FOLLOW(A)$ where $A \neq S'$)

SLR parsing table

- If $[S' \rightarrow S \bullet]$ is in I_i then set action[i, \$] = accept
- If $goto(I_i,A)=I_i$ then set goto[i,A]=i
- Repeat for all the items until no more entries added
- The initial state *i* is the I_i holding item $[S' \rightarrow \bullet S]$
- All other entries are error

Grammar

• $E' \rightarrow E$ $\bullet E \rightarrow E + T$ $_{\mathbf{v}} \cdot E \rightarrow T$ $_{ \boldsymbol{\mathsf{J}} }$ • T \rightarrow T * F $f \cdot L \rightarrow L$ $\varsigma \cdot F \rightarrow (E)$ **6** • F → id

Follow

- Follow (E) = {\$, +,) }
- Follow (T) = {\$, +, *,)}
- Follow (F) = {\$, +, *,)}

- si means shift state i
- rj means reduce by production numbered j
- Blank means error

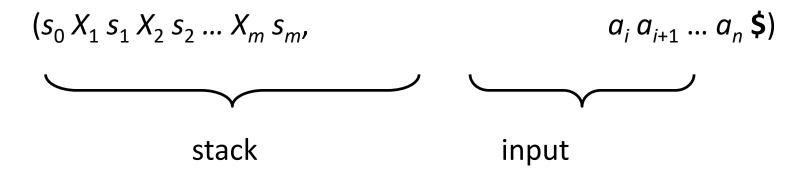
Shift, Accept, Reduce

State	Action					Goto			
	id	+	*	()	\$	Е	Т	F
0	s5			s4			1	2	3
1		s6				accept			
2		r2	s7		r2	r2			
3		r4	r4		r4	r4			
4	s5			s4			8	2	3
5		r6	r6		r6	r6			
6	s5			s4				9	3

Shift, Accept and Reduce

State	Action						Goto		
	id	+	*	()	\$	Е	Т	F
7	s5			s4					10
8		s6			s11				
9		r1	s7		r1	r1			
10		r3	r3		r3	r3			11
11		r <u>5</u>	r5		r5	r5			

SLR Parsing



Parsing action

- If $action[s_m, a_i] = shift s$, then push a_i , push s, and advance input: $(s_0 X_1 s_1 X_2 s_2 ... X_m s_m a_i s, a_{i+1} ... a_n \$)$
- If $action[s_m, a_i] = \text{reduce } A \rightarrow \beta \text{ and } goto[s_{m-r}, A] = s \text{ with } r = |\beta| \text{ then pop } 2r \text{ symbols, push } A, \text{ and push } s$:

$$(s_0 X_1 s_1 X_2 s_2 ... X_{m-r} s_{m-r} A s, a_i a_{i+1} ... a_n \$)$$

- If $action[s_m, a_i] = accept$, then stop
- If $action[s_m, a_i] = error$, then attempt recovery

Parsing algorithm

- Set input to point to the first symbol of w\$
- Repeat
 - Let s be the state on the top of the stack
 - Let a be the symbol pointed to by ip
 - If action [s, a] = shift s' then
 - Push a then s' on top of the stack
 - Move input to the next input symbol
 - Else if action [s, a] = reduce A \rightarrow β then
 - Pop 2 * | β | symbols off the stack
 - Let s' be the state now on the top of the stack
 - Push A then goto [s', A] on top of the stack
 - Output the production A \rightarrow β
 - Else if action[s, a] = accept then return;
 - Else error()

Parsing action

Stack	Input	Action
0	id * id + id \$	$[0, id] \rightarrow s5$, shift
0 id 5	* id + id \$	$[5, *] \rightarrow r6$, pop 2 symbols, Goto $[0, F] \rightarrow 4$
0 F 3	* id + id \$	$[3, *] \rightarrow r4$, pop 2 symbols, Goto $[0, T] \rightarrow 2$
0 T 2	* id + id \$	[2, *] → s7, shift
0 T 2 * 7	id + id \$	$[7, id] \rightarrow s5$, shift
0 T 2 * 7 id 5	+ id \$	$[5, +] \rightarrow r6$, pop 2 symbols, Goto $[7, F] \rightarrow 10$
0 T 2	+ id \$	$[2, +] \rightarrow r2$, pop 2 symbols and goto $[0, E] \rightarrow 1$

Parsing action

Stack	Input	Action
0 E 1	+ id \$	$[1, +] \rightarrow s6$, shift
0 E 1 + 6	id \$	[6, id] \rightarrow s5, shift
0 E 1 + 6 id 5	\$	$[5, \$] \rightarrow \text{r6, pop 2 symbols,}$ goto $[6, F] \rightarrow 3$
0 E 1 + 6 F 3	\$	$[3, \$] \rightarrow r4$, pop 2 symbols, goto $[6, T] \rightarrow 9$
0 E 1 + 6 T 9	\$	$[9, \$] \rightarrow r1$, pop 6 symbols, goto $[0, E] \rightarrow 1$
0 E 1	\$	[1, \$] → accept, hence successful parsing

Problems with SLR grammar

- Every SLR grammar is unambiguous, but not every unambiguous grammar is SLR
- Consider for example the unambiguous grammar

Example

- $S \rightarrow L = R$
- $\bullet S \rightarrow R$
- L \rightarrow * R
- L \rightarrow id
- $R \rightarrow L$

Items set

1.
$$S \rightarrow \bullet L=R$$

2.
$$S \rightarrow \bullet R$$

3.
$$L \rightarrow \bullet *R$$

4.
$$L \rightarrow \bullet id$$

5.
$$R \rightarrow \bullet L$$

•
$$I_1$$
: (I_0, S)
 $S' \rightarrow S$ •

•
$$I_2$$
: (I_0, L)
 $S \rightarrow L \bullet = R$
 $R \rightarrow L \bullet$

•
$$I_3$$
: (I_0, R)
 $S \rightarrow R$ •

Items set

- I_4 : $(I_0, *)$ $(I_4, *)$ $(I_6, *)$ $L \rightarrow * \cdot R$ $R \rightarrow \cdot L$ $L \rightarrow \cdot * R$ $L \rightarrow \cdot id$
- I_5 : (I_0 , id) (I_4 , id) (I_6 , id) $L \to id$ •
- I_9 : (I_6, R) $S \rightarrow L=R$ •

•
$$I_6$$
: $(I_2, =)$
 $S \rightarrow L = \bullet R$
 $R \rightarrow \bullet L$
 $L \rightarrow \bullet *R$
 $L \rightarrow \bullet \text{id}$

•
$$I_7$$
: (I_4, R)
 $L \rightarrow *R$ •

•
$$I_8$$
: $(I_4, L) (I_6, L)$
 $R \rightarrow L$ •

- Follow (S) = { \$}
- Follow (L) = { =, \$ }
- Follow (R) = { \$, =}

State	Action			Goto			
	id	=	*	\$	S	L	R
0	s5		s4		1	2	3
1				accept			
2		S6 /r5		r5			
3				r2			
4	s5		s4			8	7
5		r4		r4			
6	s5		s4			8	9

State	Action			Goto			
	id	=	*	\$	S	L	R
7		r3		r3			
8		r5		r5			
9				r1			

0 id =
$$*id$$
 \$ 35
0 id = $*id$ \$ 74 L $\rightarrow id$
0 L 2 = $*id$ \$ 75 R \rightarrow 1 Reduce \rightarrow Error
0 R 3 = $*id$ \$ 1 L \rightarrow id \$ 1 L

Conflict

- Shift / reduce conflict arises
- Because the grammar is not SLR(1)
- Follow information alone is not sufficient
- Hence, powerful parser is required

Summary

- Learnt to parse the SLR(1) grammar using the SLR(1) parsing algorithm
- Some grammar results in Shift / Reduce conflict