

SUPER KEY | CANDIDATE KEY | PRIMARY KEY

04 October 2023 19:44

SID	Name	Marks	Dept	course
1	a	78	CS	C ₁
2	b	60	EE	C ₂
3	a	78	CS	C ₂
4	b	60	EE	C ₃
5	c	80	IT	C ₂

⚡ Get record with name = a

↳ 2 records exist

⚡ something to uniquely identify records required. → key concept

↳ S. No is a key

⚡ Is {Dept, course} a key?

Eg {CS, C₁} → no other combo

✓ (EE, C₁) (CS, C₂) (EE, C₃) (IT, C₂)
 ↳ all unique, so {Dept, course} is a key

⚡ Is {Name, marks} a key?

✗ (a, 78) is repeated twice.

\otimes $(a, 78)$ is superkey

$\Leftrightarrow \{ \text{name, marks, dept, course} \}$
a key? YES ✓
taking all attributes will definitely form a key.

DEFN: A key is a single attribute or a set of attributes that uniquely identify a record in a table.

TYPES OF KEYS

① superkey \equiv key [same defn]

eg $SID \rightarrow SK$ ✓
 $SID, name \rightarrow SK$ ✓

If α is a sk, all combinations with α will definitely be a sk

$SID, marks \rightarrow SK$

$\{ \text{name, marks, dept} \} \rightarrow \times$ ($a, 78, CS$) repeated

$\{ \text{marks, course, dept} \} \rightarrow \checkmark SK$

minimum no. of superkeys in a table

Q : Maximum no. of superkeys in a relation

$$5c_1 + 5c_2 + 5c_3 + 5c_4 + 5c_5 \\ = 2^5 - 1 = 32 - 1 = 31$$

[remember $nCr = \frac{m}{n \cdot r(r)}$]

If there are 4 attributes

$$4c_1 + 4c_2 + 4c_3 + 4c_4 = 2^4 - 1 = 15$$

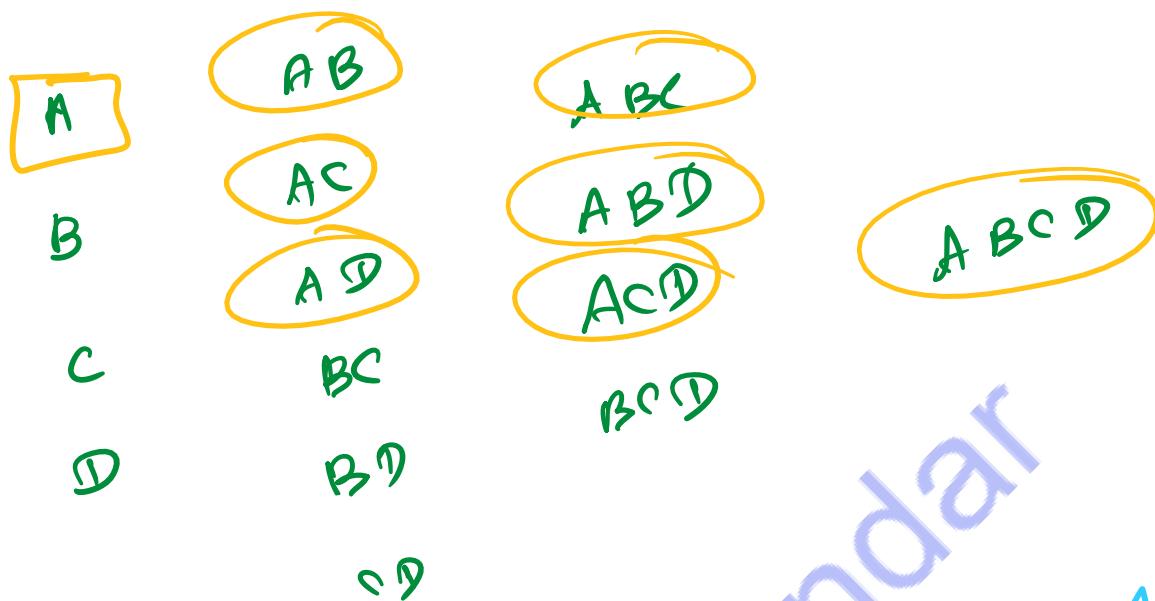
In general, a relation with n attributes can have a maximum of $2^n - 1$ superkeys

$R(A, B, C, D)$

A	B	C	D
1	1	5	1
2	1	7	1
3	1	7	1
4	2	7	1
5	2	5	1
6	2	5	2

and the total no. of superkeys

Find the total no. of relation



superkeys $\rightarrow \{A, AB, AC, AD, ABC, ABD, ACD, ABCD\}$

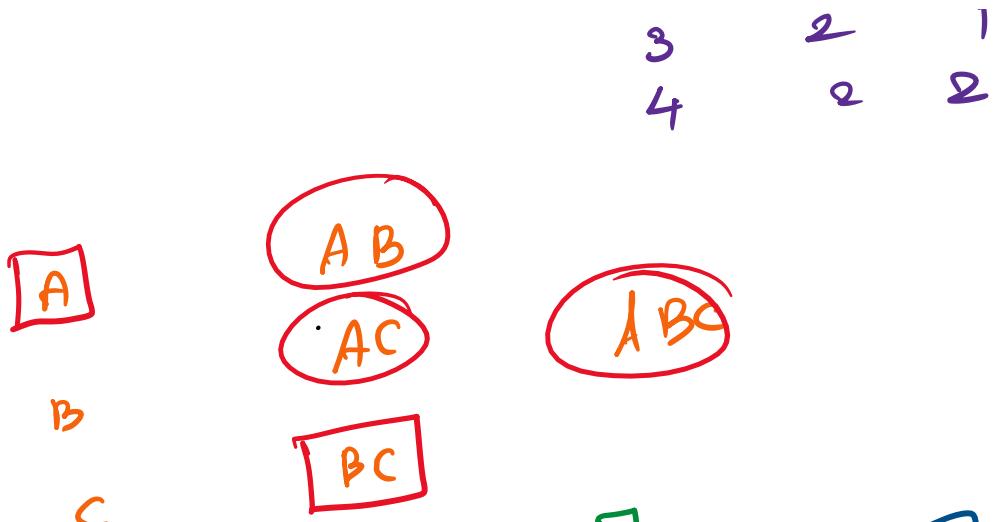
8 superkeys are present

② candidate keys

DEFN: A candidate key is a superkey whose proper subsets are not superkeys
= minimal super-key

$R(A, B, C)$

A	B	C
1	1	1
2	1	2
3	2	1
1.	2	2



[candidate keys = 2]
super keys = 5
 $\square + \circ$

$\square \rightarrow$ candidate keys
 $\circ \rightarrow$ non-minimal super keys

* Minimal \rightarrow as minimum as possible

* Minimum \rightarrow having minimum no. of attributes

* Every candidate key is a super key, but every super key need not be a candidate key.



③ PRIMARY KEY

- * Any one candidate key is chosen and made as the primary key.
- * The chosen primary key must have no NULL values.
- * Remaining candidate keys will be considered as secondary keys / alternate keys.
- * A relation can have more than one super key & candidate key but must have only one primary key.

$R(A, B, C)$ A is candidate key.
Find the total no. of super keys.

A with all combos of BC
 $\hookrightarrow \frac{2}{2} = [4 \text{ super keys}]$

$R(A, B, C)$ AC is a candidate key.
Find total no. of super keys.

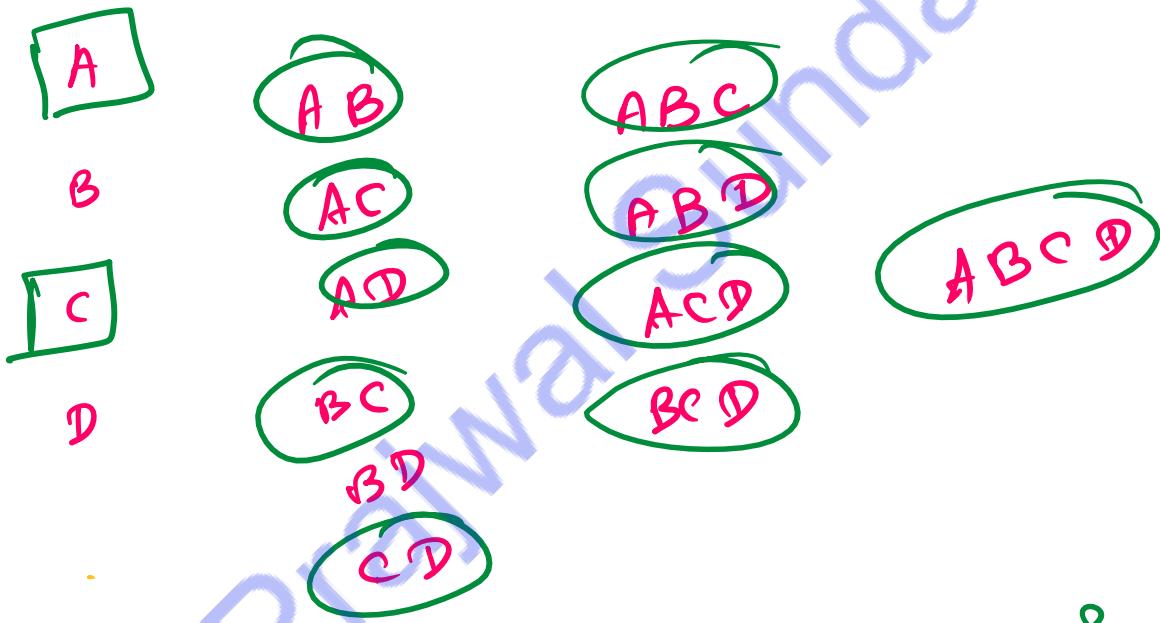
R(A, B, C, D)

Find total no. of super keys.

Ac with all combos of B

$\hookrightarrow 2^4 = 16$ super keys

R(A, B, C, D) A & D are candidate keys. Find the total no. of super keys



no. of candidate keys = 6
 no. of super keys = 12

FUNCTIONAL DEPENDENCIES

04 October 2023 20:20

$$FD : x \rightarrow y$$

If value of x
is known, y
can be uniquely
determined

x	y
:	:
:	:
:	:

relation
given

It doesn't mean y can be computed
functionally using value of x .
 $y = x^2 + 5x$ nothing like this.

x \longrightarrow y dependant
determinant

x	y
1	1
2	1
3	2
4	3

$$x = 2 : y = 1 \text{ uniquely}$$

$$x = 3 : y = 2 \text{ uniquely}$$

$$x \rightarrow y \text{ exists } \checkmark$$

x	y
1	1
2	1
3	2
4	3
2	5

Here if $x = 2$:
 $y = 1$ (or) 5
 cannot be uniquely determined

so $x \rightarrow y \times$ does not exist

$$y = x^2$$

$$x = 5 \rightarrow y = 25$$

$$x = -5 \rightarrow y = 25$$

$$y = 25 \rightarrow x = \pm 5$$

But

so $x \rightarrow y$ exists
 $y \rightarrow x$ does not exist

$x \rightarrow y$

For functional dependency $x \rightarrow y$
 to exist, if the same x value
 exists in 2 or more records, the
 corresponding y values must also
 match.

In a class

$R\text{no} \rightarrow \text{name}$ exists ✓

But in a seminar hall

$R\text{no} \rightarrow \text{name}$ ✗ does not exist
 many students

Rno → name \oplus
[RCE 15, ECE 15, many students
with the same rno may exist]

R no , Dept \rightarrow name exists ✓

FD : $x \rightarrow y$ is true
if $t_1 \cdot x = t_2 \cdot x$
then $t_1 \cdot y = t_2 \cdot y$

x	y
1	1
2	1
3	2
4	3
2	5

$$t_1 = (1, 1) \quad t_2 = (2, 1)$$

$t_1 \cdot x \neq t_2 \cdot x \Rightarrow$ no need to check if

$t_1 = (2, 1)$ $t_2 = (2, 5)$
 $t_1 \cdot \alpha = t_2 \cdot \alpha$ but $t_1 \cdot \gamma \neq t_2 \cdot \gamma$
 $\alpha \rightarrow \gamma$ \otimes does not exist

x	y
1	1
2	1
3	2
4	3

Well $d \rightarrow r$ functional dependency exists

R No	Name	Marks	Dept	course
1	a	78	CS	C1
2	b	60	EE	C1
3	a	78	CS	C2
4	b	60	EE	C3
5	c	80	IT	C3
6	d	80	EC	C2

check if the functional dependencies exist :

① $R\text{ NO} \rightarrow Name$
 as no gno is
 $t_1.x \neq t_2.x \Rightarrow$
 Dependency exists

duplicated
 no need to
 check if
 $R\text{ NO} \rightarrow Name$ (✓)

② $Name \leftrightarrow R\text{ NO}$

$t_1 = (a, 1) \quad t_2 = (a, 3)$
 $t_1.x = t_2.x$ but $t_1.y \neq t_2.y$

Dependency does not exist (✗)

③

$R\text{ NO} \rightarrow marks$

✓

④ $\text{Dept} \rightarrow \text{course}$

$$t_1 = (\text{CS}, \text{C}_1) \quad t_2 = (\text{CS}, \text{C}_2)$$

$$t_1 \cdot x = t_2 \cdot x \quad \text{but} \quad t_1 \cdot y \neq t_2 \cdot y$$

dependency does not exist \times

⑤ $\text{course} \rightarrow \text{Dept}$

$$t_1 = (\text{C}_1, \text{CS}) \quad t_2 = (\text{C}_1, \text{EE})$$

$$t_1 \cdot x = t_2 \cdot x \quad \text{but} \quad t_1 \cdot y \neq t_2 \cdot y$$

dependency does not exist \times

⑥ $\text{marks} \rightarrow \text{Dept}$

in all cases where $t_1 \cdot x = t_2 \cdot x$

$t_1 \cdot y = t_2 \cdot y$ holds true

dependency exists \checkmark

$\text{marks} \rightarrow \text{Dept}$

⑦ $\underbrace{\text{Rno, name}}_x \rightarrow \underbrace{\text{marks}}_y$

No gno repetition

exists \checkmark

so no x repetition

$\text{gno, name} \rightarrow \text{marks}$

⑧ name \rightarrow marks
FD exists $\text{name} \rightarrow \text{marks}$

⑨ name, marks \rightarrow dept
 $t_1 = (a 78, CS)$ $t_2 = (a 78, CS)$
only place where $t_1 \cdot x = t_2 \cdot x$
here $t_1 \cdot y = t_2 \cdot y \Rightarrow$ no problem
 $\text{name, marks} \rightarrow \text{dept}$

⑩ name, marks \rightarrow dept, course
 $t_1 = (a 78, CS C_1)$
 $t_2 = (a 78, CS C_2)$
 $t_1 \cdot x = t_2 \cdot x$ but $t_1 \cdot y \neq t_2 \cdot y$
dependency does not exist.

⑪ ~~g1 no~~ \rightarrow name, marks

✓

✓

⑫ dept, course \rightarrow name

✓

⑬ g1 no, marks \rightarrow dept

⑭ name \rightarrow course \times

⑮ name, marks, dept \rightarrow g1 no \times

(15)

name , marks, dept → 91% 😊

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ARMSTRONG'S AXIOMS IN DBMS

04 October 2023 22:06

Types of Functional Dependencies

- ① Trivial
- ② Non-Trivial
- ③ Multi-valued
- ④ Transitive

FD : $x \rightarrow y$

$$\text{if } t_1 \cdot x = t_2 \cdot x$$

$$\text{then } t_1 \cdot y = t_2 \cdot y$$

① TRIVIAL FD

FD : $x \rightarrow y$

if $y \subseteq x \Rightarrow x \rightarrow y$ is a
trivial functional dependency

Rno \rightarrow Rno

Rno, name \rightarrow Name

Rno, name \rightarrow Rno

trivial FD
always valid

No use in writing these FD
[understood by default]

② NON TRIVIAL FDs

$\vee \cap \cup - \Delta$

(e) $\text{NON} \cap \text{FL} = \emptyset$
 $X \rightarrow Y$ and $X \cap Y = \emptyset$
 $R\text{No} \rightarrow \text{Name} \rightarrow$ may / may not
 be valid \rightarrow use table to check

$X \rightarrow Y \quad Y \not\subseteq X \Rightarrow$ semi trivial FD

$R\text{No}, \text{Name} \rightarrow \text{Name, Marks}$

C check table to check validity

ARMSTRONG'S AXIOMS / RULES

INFERENCE

RNO	Name	Marks	Dept	Course
1	a	78	CS	C ₁
2	b	60	EE	C ₁
3	a	78	CS	C ₂
4	b	60	EE	C ₃
5	c	80	IT	C ₂

① REFLEXIVITY

$$X \rightarrow X \quad X \rightarrow Y \quad Y \subseteq X$$

... - onto $\text{Name} \rightarrow \text{Name}$

R NO → R NO

Marks → Marks

course → course

Name → Name

Dept → Dept

R no, name → R NO

② TRANSITIVITY

If $(x \rightarrow y \text{ and } y \rightarrow z)$ then $(x \rightarrow z)$ exists

Ram is sibling of Shyam

Shyam is sibling of Mohan

↓
Ram is sibling of Mohan

Name → Marks

Marks → Dept

Name → Dept

If a new tuple $(6, d, 80, Er, c4)$

Name → Marks ✓

But Marks → Dept ✗

Nothing can be directly commented
about Name → Dept
on checking table \Rightarrow it exists ✓

③ AUGMENTATION

③ AUGMENTATION

If $X \rightarrow Y$ then $XA \rightarrow YA$

If $RNO \rightarrow \text{name}$,
 $RNO, \text{marks} \rightarrow \text{Name, Marks}$

④ UNION

If $X \rightarrow Y$ and $X \rightarrow Z$ then $X \rightarrow YZ$

If $RNO \rightarrow \text{name}$ and
 $RNO \rightarrow \text{marks}$ then
 $RNO \rightarrow \text{Name, Marks}$

⑤ DECOMPOSITION / SPLITTING:

If $X \rightarrow YZ$ then $X \rightarrow Y$ and $X \rightarrow Z$

If $XY \rightarrow Z$ then $\begin{matrix} X \rightarrow Z \\ Y \rightarrow Z \end{matrix} \quad X$
 (wrong)

The determinant side (LHS) can never be split. only the RHS can be split.

$\text{name, marks} \rightarrow \text{dept, course}$

$\overset{H}{\text{name}} \quad \text{marks} \rightarrow \text{dept}$

name, marks \xrightarrow{u} dept
name, marks \xrightarrow{v} course

⑥ PSEUDO TRANSITIVITY

If $x \rightarrow y$ and $y \rightarrow z \rightarrow A$
then $xz \rightarrow A$

Rno \rightarrow name

Name, Marks \rightarrow Dept

then Rno, marks \rightarrow Dept

⑦ COMPOSITION

If $x \rightarrow y$ and $A \rightarrow B$ then
 $xA \rightarrow yB$

ATTRIBUTE CLOSURE

09 October 2023 19:12

$R(A, B, C, D, E)$

$FD: \{ A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow E \}$

$A \rightarrow A$ (reflexivity)

$A \rightarrow B, B \rightarrow C \Rightarrow A \rightarrow C$ (transitivity)

$A \rightarrow C, C \rightarrow D \Rightarrow A \rightarrow D$

$A \rightarrow D, D \rightarrow E \Rightarrow A \rightarrow E$

so $A \rightarrow ABCDE$

$A^+ = \{ A, B, C, D, E \}$

attribute closure of A

similarly for B:

$B \rightarrow B, B \rightarrow C, B \rightarrow D, B \rightarrow E$

$B \not\rightarrow A$ not possible

(C)

$B^+ = \{ B, C, D, E \}$

Also $C^+ = \{ C, D, E \}$

$D^+ = \{ D, E \}$

$E^+ = \{ E \}$

In simple words :

+ ... and a set of attributes, n

X^+ contains a set of attributes determined by X [$X \Rightarrow$ set of attributes]

$$A^+ = \{A, B, C, D, E\}$$

$$AD^+ = \{A, B, C, D, E\}$$

By augmentation property:

$$A \rightarrow B \Rightarrow AD \rightarrow BD \Rightarrow AD \rightarrow D$$

... $AD \rightarrow A B C D E$ can be proved
attribute closure of AD

super key w/ attribute closure:

set of attributes whose closure contains all attributes of the relation.

$$A^+ = \{A, B, C, D, E\} \Rightarrow \text{super key } \checkmark$$

$$AD^+ = \{A, B, C, D, E\} \Rightarrow \text{super key } \checkmark$$

$$AB^+ = \{A, B, C, D, E\} \Rightarrow \text{super key } \checkmark$$

$$B^+ = \{B, C, D, E\} \Rightarrow \text{not a super key } \times$$

A $\{B, C, D, E\}$
 super key
 all combinations = $\frac{4}{2} = 16$ super keys

$BCDE^+ = \{B, C, D, E\} \Rightarrow \times$
 ↳ no subset of this can be
 a super key.

candidate key : minimal super key
 Here A is the only candidate

$R(A, B, C, D, E)$

$FD : \{A \rightarrow B, D \rightarrow E\}$

$A^+ = \{A, B\}$

$BC^+ = \{B, C\}$

$ABCDE^+ = \{A, B, C, D, E\}$

all attributes
 of the relation
 all obviously
 form a
 super key.

$ABDE^+ = \{A, B, D, E\} \Rightarrow \times$

$ACDE^+ = \{A, C, D, E, B\}$

super key

$ACD^+ = \{A, C, D, B, E\}$

HCK

- T " -- -- --)
super key.
also \Rightarrow minimal \rightarrow candidate key

$A^+ = \{A, B\}$ $C^+ = \{C\}$ $D^+ = \{D, E\}$
 $AC^+ = \{A, B, C\}$ $AD^+ = \{A, B, D\}$ $CD^+ = \{C, D, E\}$

$ACD \Rightarrow$ 1 candidate key

BE combos $\Rightarrow 2^2 = 4$ super keys

CANDIDATE KEYS

09 October 2023 19:35

$$R(A, B, C, D, E) \quad FD = \{ A \rightarrow B, D \rightarrow E \}$$

Find all candidate keys and super keys.

$$ABCDEF^+ = \{ A, B, C, D, E \}$$

↪ by reflexivity property (each attribute can determine itself)

Remove dependent attrs :

$$A \cancel{B} C D E$$

$$A C D F$$

$A \rightarrow B$, so discard B.

$D \rightarrow E$, so discard E.

$(ACD) \Rightarrow$ nothing

also it can see \checkmark verified that no proper subset is a super key \Rightarrow so ACD is a candidate key.

Prime Attributes

those attributes which are a part of the candidate key.

In the previous Qn,
prime attributes = {A, C, D}

A CD → candidate key.

Now check if any of the prime attributes appear on the right hand side (RHS) of any functional dependency. If no → there will be only one candidate key.

A, C, D → none of them appear in the RHS. so ACD is the only candidate key.

R(A, B, C, D) FD = {A → B, B → C, C → A}

$$A^{+} = \{A, B, C, D\}$$

$$ACD^{+} = \{A, C, D, B\}$$

$$AD^{+} = \{A, B, C, D\}$$

↳ no more attributes can be discarded.

$$A^{+} = \{A, B, C\} \quad D^{+} = \{D\}$$

so $AD \Rightarrow$ candidate key

$$\dots \text{thus} - \{A, D\}$$

Q6

Prime attributes = {A, D}

A is present on the RHS of a FD.

so AD is not the only candidate key.

$C \rightarrow A$ so CD is a SK

$B \rightarrow C$ so BD is a SK

now checking proper subsets

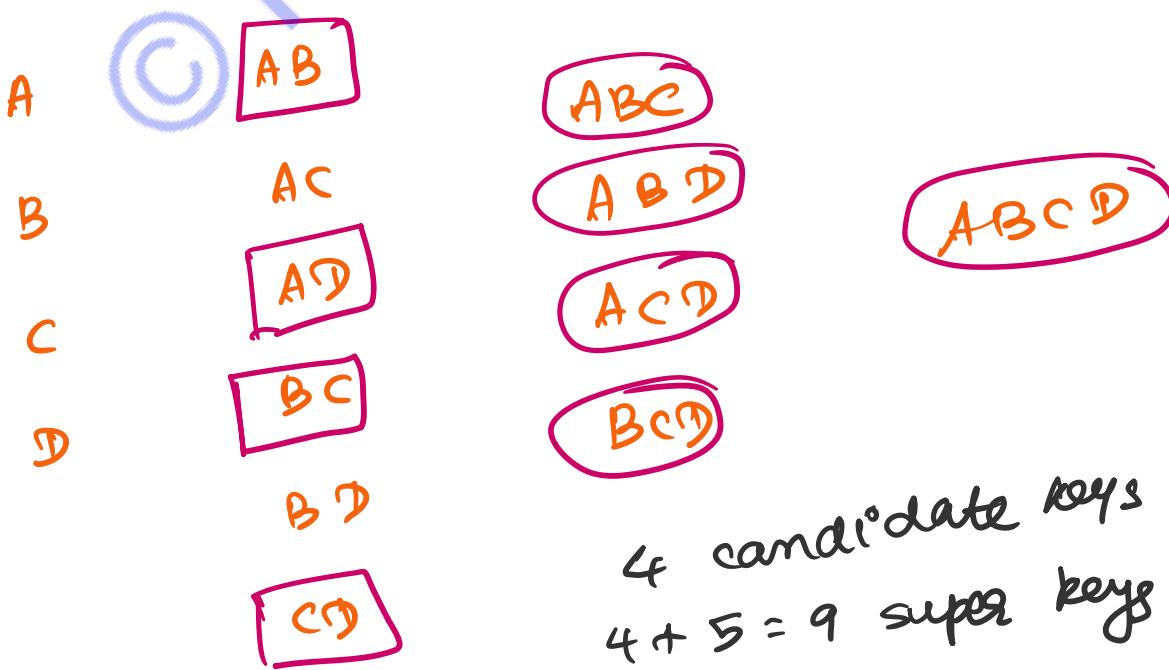
C^+ = {A, B, C} = B^+ = D^+ = {D}

candidate keys = {AD, BD, CD}

prime attributes = {A, B, C, D}

R(A, B, C, D)

FD: {AB \rightarrow CD, D \rightarrow B, C \rightarrow A}



4 candidate keys

4 + 5 = 9 super keys

$R(A, B, C, D, E, F)$

$FD = \{ AB \rightarrow C, C \rightarrow DE, E \rightarrow F, D \rightarrow A, C \rightarrow B \}$

$A B \not\subset D E F^+ = \{ A, B, C, D, E, F \}$

$A B \not\subset D E F^+ = \{ A, B, C, D, E, F \}$

$ABF^+ = \{ A, B, C, D, E, F \}$

$AB^+ = \{ A, B, C, D, E, F \}$

$A^+ = \{ A \}$ $B^+ = \{ B \}$

so AB is a candidate key.

For now prime attributes = $\{ A, B \}$

more candidate keys are present

$D \rightarrow A$ $D^+ = \{ A, B, C, D, E, F \}$

$BD^+ = \{ B \}$ $D^+ = \{ A, D \}$

so BD is a candidate key

Now prime attributes = $\{ A, B, D \}$

$C \rightarrow B$, so



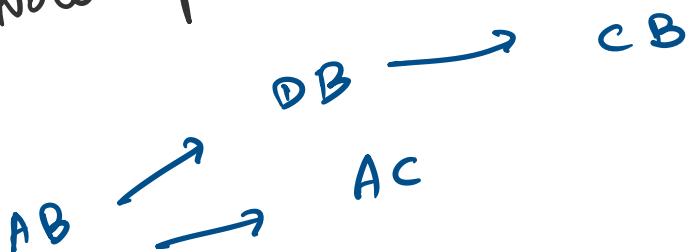
$AC^+ = \{ A, B, C, D, E, F \}$

$AC^+ = \{A, B, C, D, E, F\}$
 $A^F = \{A\}$
 super key but
 not candidate
 key

$c^+ = \{C, D, E, F, A, B\}$
 super key

candidate key

Now prime attributes = $\{A, B, C, D\}$



$\textcircled{X} BC^+ = \{A, B, C, D, E, F\}$
 not candidate key

so

candidate keys \Rightarrow	AB, B^D, C
prime attributes =	$\{A, B, C, D\}$
non-prime attributes =	$\{E, F\}$

Alternate Path:

~~$ABCFDEF$~~ = $\{A, B, C, D, E, F\}$
 +

 $B^D E F = \{A, B, C, D, E, F\}$

without using transitive rule, we
 are left with 3 attributes (earlier
 there were only 2).

there were only 2).

check all proper subsets of BDE-

$$B\bar{D}^+ = \{B, D, A, C, E, F\}$$

super key + candidate key also

$B\bar{D}$, then C , then AC
[same answer irrespective of path taken]

NORMALIZATION

09 October 2023 21:55

student

SID	SName	Credits	Dept Name	Building	Room No
1	Rahul	5	CSE	B1	101
2	Jiya	8	CSE	B1	101
3	Jenny	9	FD	B2	201
4	Payal	9	FD	B2	201
5	Ankita	7	CIVIL	B1	110
6	Aakash	7	ECE	B1	115
7	Vanshika	8	CIVIL	B1	101
8	Tanshika	7	CSE	B1	101

Dept Building & Room No → repeated
 all tuples
 ↳ large schema leads to more redundancy.

Problems that occur due to redundancy

- ① insertion anomaly
- ② update anomaly
- ③ deletion anomaly

Anomaly : when a data has multiple copies, and we update the data at one location but forget to update another location.

one location but forget to update that data at another location.

Insertion Anomaly

Eg: only a new Dept MME with Building B1 and Room 120 needs to be inserted. But it is not possible as there is no student yet.

updation Anomaly

updation @ many locations
eg if CSE Room 301
updating it in one location & forgetting to update it in another → leads to data inconsistency.

Delete Anomaly

If only one student is there in a dept & the student leaves, when that tuple is deleted, simultaneously all data of that department is also lost.

SOLN: Decomposition into 2 tables

sid	sname	credits	dept name	→ foreign key
=			rse	

SID	Name	Group	Branch	key
1	Rahul	5	CSE	
2	Jiya	8	CSE	
3	Jenny	9	FD	
4	Payal	9	FD	
5	Ankur	7	civil	
6	Aakash	7	ECE	
7	Vanshika	8	civil	
8	Tanishka	7	CSE	

(Primary key) Dept Name	B welding	Room No
CSE	B1	101
civil	B1	110
FD	B2	201
ECE	B1	115

[Tables are related to each other using FOREIGN KEY]

- ① Insertion Anomaly → solved
 we can insert a new dept without adding any student.

adding any ^{or -}
(MME, B1, 120)

② update Anomaly → solved
only one tuple needs to be updated, eg while changing the room no. of a department.

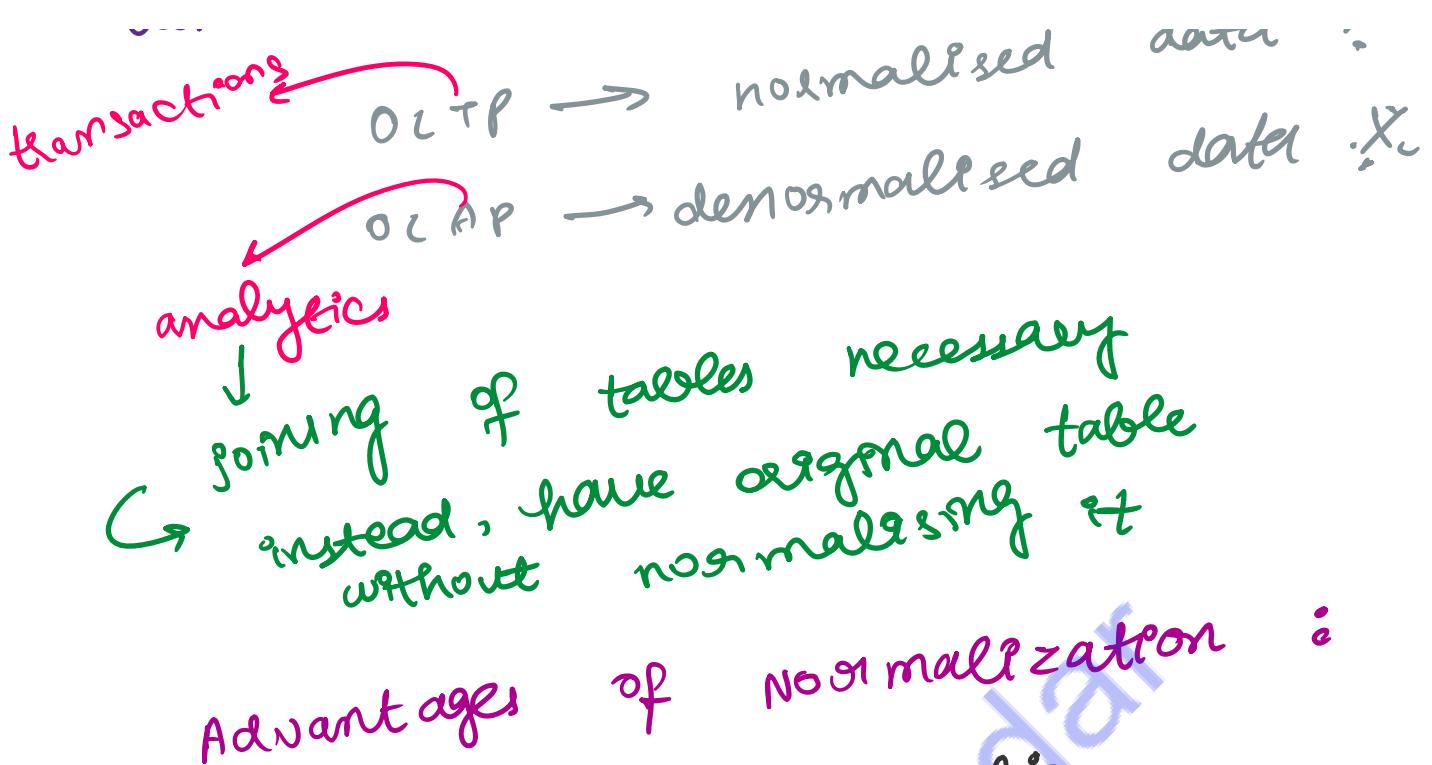
③ delete Anomaly → solved
Deleting student data doesn't erase information about the department

Normalization

process of making table free of insertion, updation and deletion anomalies. It also helps save space by reducing redundant data

But it is not always the best idea to normalize data. sometimes, denormalisation is better.

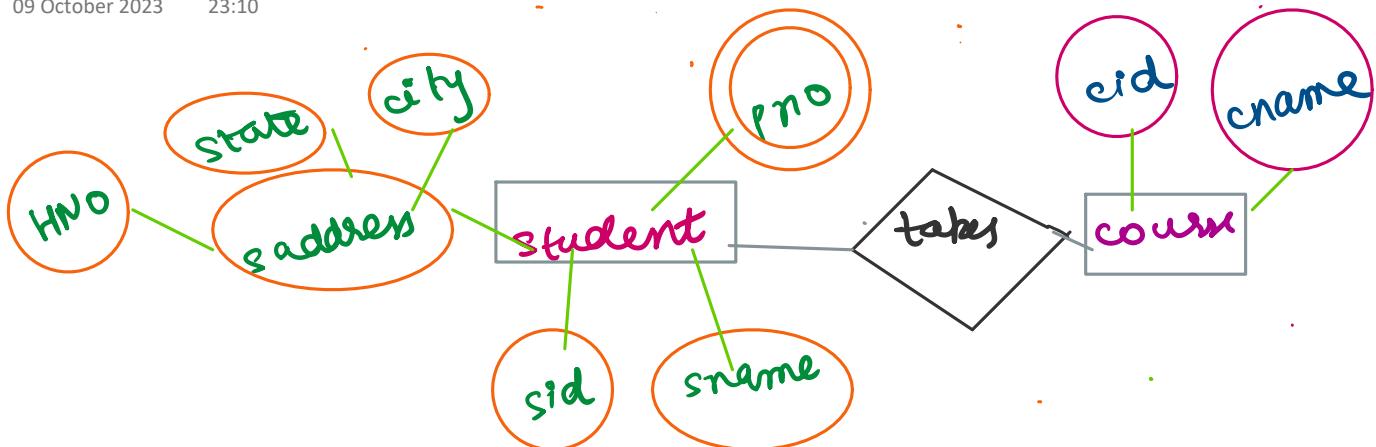
relations \rightarrow normalised data



- ① removal of anomalies
- ② reduction of redundancy & saving of space
- ③ minimization of NULL values
- ④ easier understanding of table schema

FIRST NORMAL FORM

09 October 2023 23:10



student

SID	SName	SAdd	PNO
1	Jenny	Haryana India	P ₁ , P ₂
2	Jiya	Punjab India	P ₃
3	Payal	Rajasthan India	P ₄ , P ₅
4	Shamini	Haryana India	P ₇

First Normal Form (1NF):
A table is said to be in 1NF iff
all attributes have atomic domains.
Rule - 1
[each cell must contain exactly
ONE value only]

Individual units which
cannot be further
decomposed.

↓

For composite attributes :
 make separate attributes for each,
 eg state & country as 2 attributes

To get multi-valued attributes :
 make one new tuple for each value
 in the multi-valued set.

SID	sName	state	country	Phone No
1	Jenny	HR	INDIA	P1
1	Jenny	HR	INDIA	P2
2	Tiya	PUNJAB	INDIA	P3
3	Payal	RAJ	INDIA	P4
3	Payal	RAJ	INDIA	P5

Rule - 2

↓
 A column must contain values from
 the same domain.
 of same type

Rule - 3

↓
 Column should have a unique name.

↓
Each column should have a unique name.

rule - 4

→ no ordering to the rows and columns must be applicable.

Rule - 5

→ no duplicate rows must be present.

Primary key

↳ Here (sid, phoneno)

Good ER diagram → Relational schema will be in INF by default

If not → bad design of ER diagram.

INF is an essential property in a relational schema.

Decomposing the above table into 2 :

sid	gname	State	country
1	Jenny	HR	IN

1	Jenny	HR	IN
2	Jyoti	PB	IN
3	Payal	RJ	IN

foreign key

SNO	PN ^o
1	P ₁
1	P ₂
2	P ₃
3	P ₄
3	P ₁

SNO, PN^o

primary key

[many
to
one
relationship
exists]

Note : integers are atomic values . but
a set of integers isn't.

123 → atomic
but 1,2,3 → non-atomic (can be split
into 3 parts)

(CS 00) → non-atomic → CS
→ 001

Having schema as :
(SNO, Sname, state, country, phone1, phone2)

↓
partially solves the problem , but it
fails if one person has more than
2 phone numbers , and therefore is
not recommended .

SECOND NORMAL FORM

10 October 2023 14:08

$$R(A, B, C, D, E \rightarrow F)$$

$$FD = \{ A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow E \}$$

[in overwhelming majority of situations,
it will already be in 1NF]

A relation is said to be in 2NF if:

- ① it is in 1NF.
- ② no partial dependency exists in the relation.

partial dependency Format:

proper subset of \rightarrow non-prime attribute
any candidate key

For the given relation, $A B C D E F$
candidate key = $A F$ = 1
super keys = $A F (B C D E)$ = 16

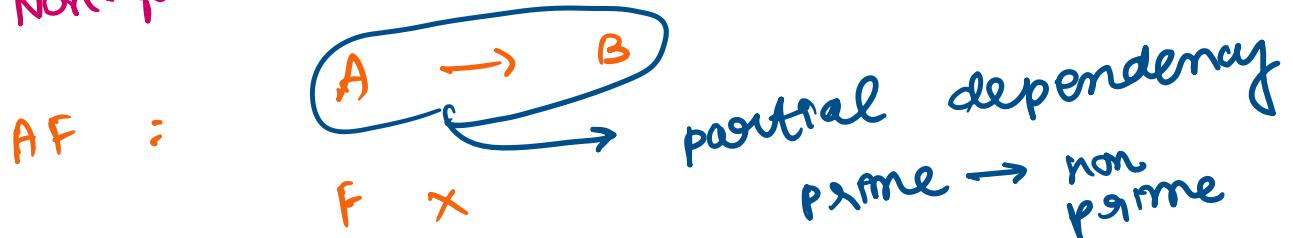
$A^+ = A B C D E$ } so $A F$ is a CK
 $F^+ = F$

prime attributes = { A, F }

non-prime attributes = { B, C, D, E }

not in RHS
only 1 CK

Non-prime attributes - $\{D, C\}$

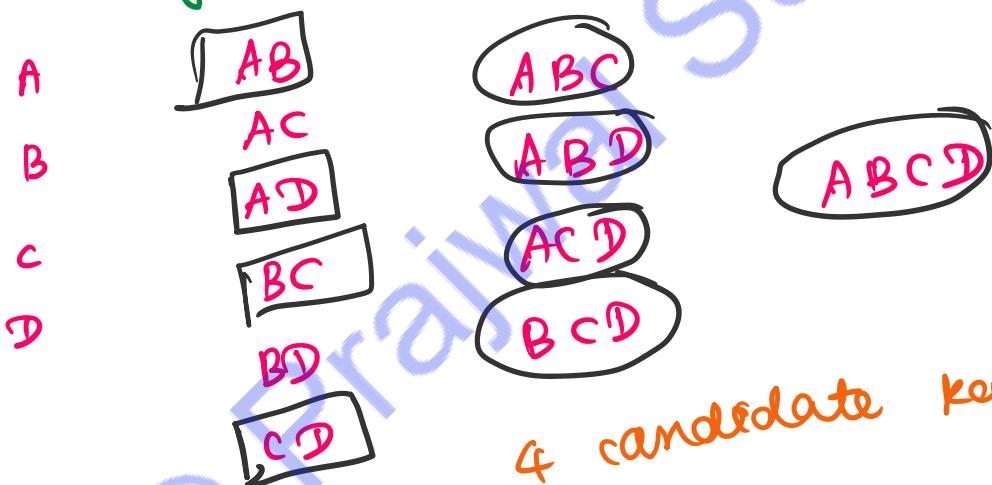


Partial dependency is present. So the relation is not in 2NF.

$R(A, B, C, D)$

$$FD = \{AB \rightarrow CD, C \rightarrow A, D \rightarrow B\}$$

finding candidate keys:



4 candidate keys

prime attributes = $\{A, B, C, D\}$

no non-prime attribute

$\hookrightarrow \checkmark$ It is in 2NF

$R(A, B, C, D)$

$$FD : \{A \rightarrow B, B \rightarrow C, C \rightarrow D\}$$

candidate keys  $A^+ = \{A, B, C, D\}$

$C \rightarrow D$ not in RHS
only 1 into

candidate key A - " "
 prime attributes = $\{A\}$ not " only ① candidate key
 non-prime attributes = $\{B, C, D\}$
 There is no proper subset of the
 candidate key $A \rightarrow$ so, definitely,
 the given relation is in 2NF

$R(A, B, C, D)$

$FD = \{A \rightarrow B, B \rightarrow D\}$

Candidate key:

AC^+

$= \{A, C, B, D\}$

prime attributes = $\{A, C\}$

prime

attributes

not in the RHS of any FD
so it is the only candidate key.

non-prime attributes = $\{B, D\}$

non-prime attributes

A is a proper subset of AC .

$A \rightarrow B$

B

non-prime attribute

partial functional dependency exists.

is

therefore the relation
not in 2NF

Therefore the relation
not in 2NF

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THIRD NORMAL FORM

10 October 2023 19:22

^{PK} SID	sname	DOB	state	country	Pin code	Total credits
1	A	-	HR	IN	122001	-
2	B	-	HR	IN	122001	-
3	C	-	HR	IN	122001	-
4	D	-	PB	IN	123456	-

↳ this relation is in 2NF as the candidate key has only one attribute.

Based on the no. of attributes present in the candidate key, there are 2 types of keys:

- ① simple candidate key (1 attribute)
- ② composite key (≥ 2 attributes)

partial dependency condition :

proper subset
of candidate key \rightarrow non-prime
attribute

Even if a relation is in 2NF, it isn't considered to be good enough.
... so ... it can arise :

1. Non-prime candidate

problems that can arise:

e.g. pincode → state, country

If pincode is changed → corresponding state and country also need to be changed.

↳ update anomaly exists.

also redundancy exists

soln: form another table

state	country	pincode
HR	IN	122001

cause of problem:

Non-prime attribute → Non-prime attribute

Transitive dependency

A relation is said to be in 3NF if

① It is in 2NF.

② no transitive dependency exists for non-prime attributes

A table is in 3NF iff. for each of its non-trivial functional dependences, at least one of the following conditions holds:

① LHS is super key.

② RHS is prime attribute.

$R(A, B, C, D)$

$FD: \{ A \rightarrow B, B \rightarrow C, C \rightarrow D \}$

Candidate key: $A^+ = \{ A, B, C, D \}$

Prime attributes: $\{ A \}$

Non-prime attributes: $\{ B, C, D \}$

Candidate key has only a single attribute

↳ relation is in 2NF.

But $B \rightarrow C$ non-prime attribute \rightarrow non-prime attribute

same for

$C \rightarrow D$

so this relation is not in 3NF

1NF	2NF	3NF
✓	✓	✗

∴ alternate approach:

(con't) alternate approach:

$A \rightarrow B$ LHS is superkey \checkmark

$\times B \rightarrow C \times$ both conditions failed \times

$\times C \rightarrow D \times$ both conditions failed \times

Relation is not in 3NF

$R(A, B, C, D, E, F)$

FD: $\{AB \rightarrow CDEF, BD \rightarrow F\}$

candidate key

$AB^+ = \{A, B, C, D, E, F\}$

\hookrightarrow only candidate key

prime attributes = $\{A, B\}$

Non-prime attributes = $\{C, D, E, F\}$

$AB \rightarrow CDEF$

full candidate key

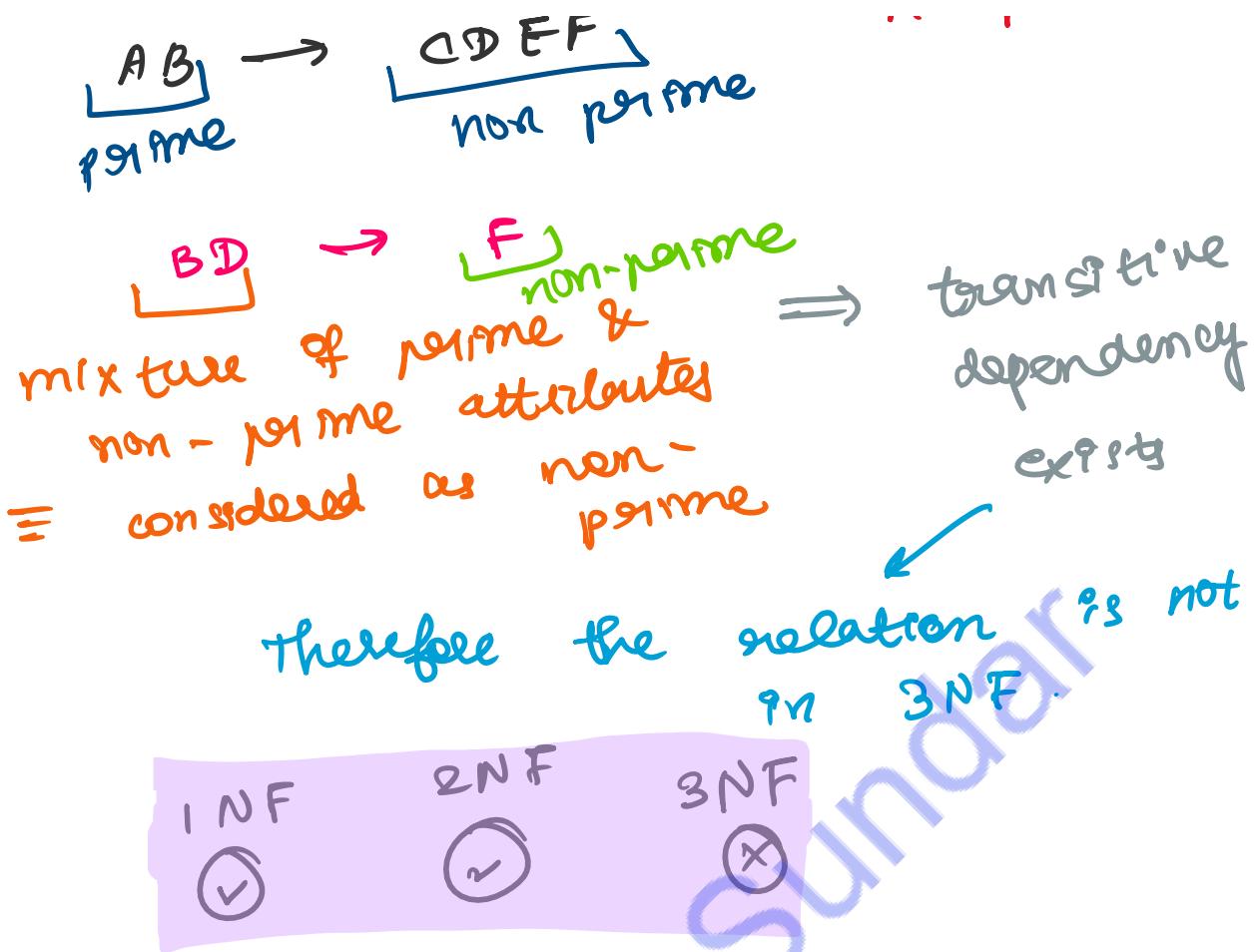
both are not partial dependencies.

\therefore Relation is in 2NF.

$BD \rightarrow F$

not of a proper subset
of candidate key

$AB \rightarrow CDEF$ → no problem
prime



Advantages of 3NF over 2NF:

2NF had some anomalies (insert, update, remove) \rightarrow all of them are removed in 3NF.

then it is a good database design.

$R(A, B, C, D, E)$

FD: $\{ A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A \}$

candidate keys :

AE, BE, CE, DE

AE , BE , CE , DE

prime attributes = { A, B, C, D, E }

non-prime attributes = \emptyset

As there are no non-prime attributes, the relation is in

2NF and 3NF

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BOYCE CODD NORMAL FORM

10 October 2023 20:00

Drawbacks in 3NF :

when multiple overlapping candidate keys are present

A B BC CD

To handle these cases, a stronger form of 3NF known as was developed.

Developed by E. F. Codd and Raymond F. Boyce

father of DBMS, also developed 1, 2, 3 NFs

BCNF

A relation R is said to be in BCNF iff:

- ① It is in 3NF.
- ② For each non-trivial functional dependency, the LHS is a super key.

$R(A, B, C)$

FD: $\{A \rightarrow B, B \rightarrow C, C \rightarrow A\}$

$R(A, B, C)$ $\Gamma: A \rightarrow B, D \rightarrow E$

candidate keys : A, B, C

prime attributes = $\{A, B, C\}$

Non-prime attributes = \emptyset

then \downarrow 2NF \checkmark 3NF \checkmark

$A \rightarrow B$
SK \checkmark

$B \rightarrow C$
SK \checkmark

$C \rightarrow A$
SK \checkmark

↳ therefore the given relation
in BCNF \checkmark

$R(A, B, C, D, E)$

$\Gamma: A \rightarrow BCDE, BC \rightarrow ACE, D \rightarrow E$

candidate keys : A, BC

prime attributes = $\{A, B, C\}$

non-prime attributes = $\{D, E\}$

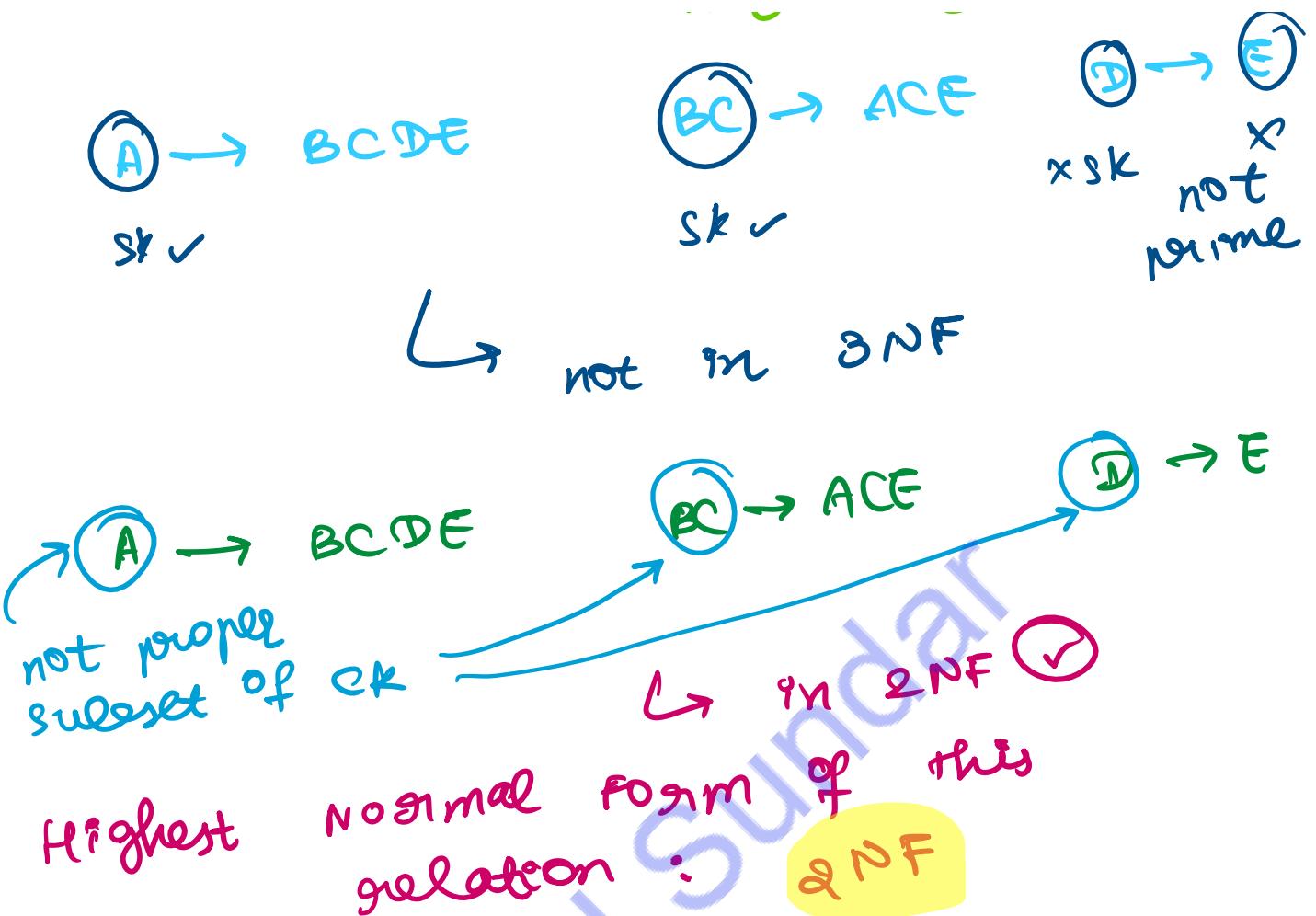
$A \rightarrow BCDE$
SK \checkmark

$BC \rightarrow ACE$
SK \checkmark

$D \rightarrow E$
X SK

↳ not in BCNF

∴ \downarrow 2NF $D \rightarrow E$



$R(A, B, C, D, E)$
 $f: \{AB \rightarrow CDE, D \rightarrow A\}$

candidate keys : $\{AB, BD\}$

prime attributes = $\{A, B, D\}$

non-prime attributes = $\{C, E\}$

$AB \rightarrow CDE$ SK ✓
 $D \rightarrow A$ not SK ✗

not in BCNF.

$D \rightarrow A$ 3NF ✓

A B → CDE
prime

D → A
prime

3NF ✓

A B → C D E
not a subset of CK non prime

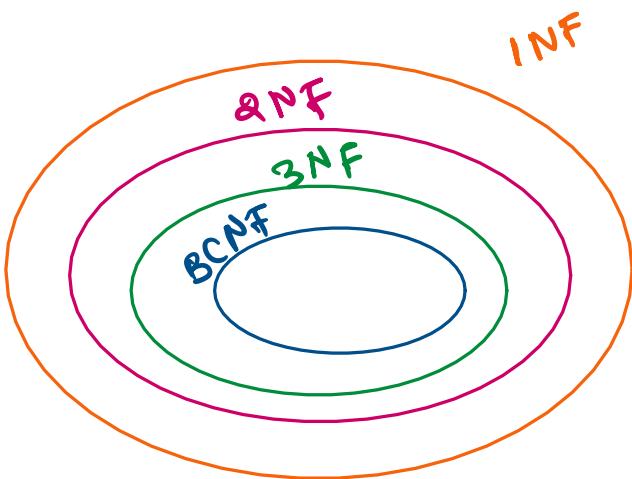
D → A
not a subset of CK

2NF ✓

Highest normal form : 3NF

HIGHEST NORMAL FORM OF A RELATION

10 October 2023 20:32



$R(A B C D E F G H)$

FD: $\{ABC \rightarrow DE, E \rightarrow GH, H \rightarrow G, G \rightarrow H,$
 $A B C D \rightarrow E F\}$

candidate key:

prime attributes = $\{A, B, C\}$

non-prime attributes = $\{D, E, F, G, H\}$

checking for 2NF:

↳ no LHS has proper subset of
 $ABC \rightarrow \text{so } 2NF \checkmark$

checking for 3NF:

↳ $E \rightarrow GH$ \Rightarrow transitive functional dependency exists \times
non-prime non-prime

P.J.I

so, the relation is in **2NF**

$R(A B C D)$

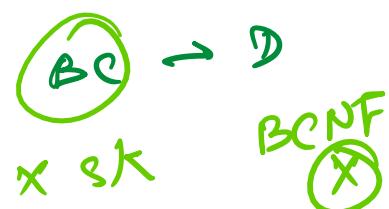
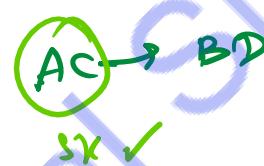
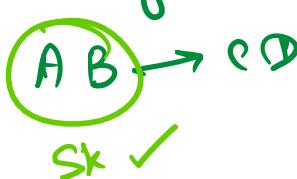
$F.D. : \{ AB \rightarrow CD, AC \rightarrow BD, BC \rightarrow D \}$

Candidate keys : AB , AC

Prime attributes = $\{ A, B, C \}$

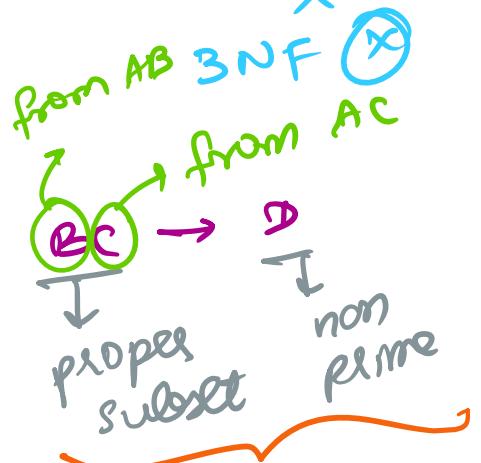
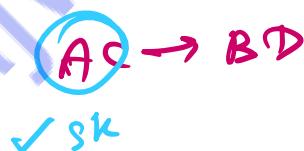
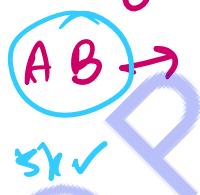
Non-prime attributes = $\{ D \}$

Checking for BCNF :



BCNF X

Checking for 3NF :



Checking for 2NF :

$AB \rightarrow CD$
not proper subset

$AC \rightarrow BD$
not proper subset

2NF X

partial dependency
(proper subset. ungen is also proper subset.)

∴ the given relation
is in **1NF** only.

∴ The given relation is in **1NF** only. (proper subset of ck also proper subset)

Points to note :

- ① If all candidate keys are simple (single attributes) then it would be in **2NF**.
- ② If all attributes of a relation are prime attributes, it would be in **3NF**.
- ③ If relation is in **3NF** & all candidate keys are simple, then it is in **BCNF**.

$R(A B C D E)$

FD: $\{AB \rightarrow CDE, D \rightarrow BE\}$

candidate keys : **AB, AD**

2NF :

$AB \rightarrow CDE$

↳ **2NF X**

$D \rightarrow$
subset of AD
 $BE \downarrow$
non-prime attribute

relation is in **1NF**

$R(ABCDE)$
 $FD: \{ AE \rightarrow BC, AC \rightarrow D, CD \rightarrow BE, D \rightarrow E \}$
 candidate keys : AC , AD , AE non prime
 $AE \rightarrow BC$ $AC \rightarrow D$ $CD \rightarrow BE$ $D \rightarrow E$
2NF ✓ proper subset X proper subset ✓
 Not even 2NF.
 Relation is in 1NF.

$R(ABCD)$
 $FD: \{ AB \rightarrow C, ABD \rightarrow C, ABC \rightarrow D, AC \rightarrow D \}$
 candidate key : AB
 $2NF:$ $AB \rightarrow C$ $ABD \rightarrow C$ $ABC \rightarrow D$ $AC \rightarrow D$
no proper subsets of AB candidate key
2NF ✓
 $3NF:$ $AB \rightarrow C$ $ABD \rightarrow C$ $ABC \rightarrow D$ $AC \rightarrow D$
prime non prime non prime non prime non prime non non non non
transitive dependencies not in 3NF ✗
 Relation is in 1NF.

\therefore Relation is in 2NF

$R(A B C D)$

$F_D : \{ A \rightarrow BCD, BC \rightarrow AD, D \rightarrow B \}$

Candidate keys : A, B^P, C^D

all attributes are prime
attributes \rightarrow 3NF.

Checking BCNF :

$(A) \rightarrow BCD$
SK ✓

$(BC) \rightarrow AD$
SK ✓

$(D) \rightarrow B$
 \times not SK

not in BCNF \otimes

3NF.

\therefore The relation is in 3NF.

$R(A B C)$

$F_D : \{ A \rightarrow B, B \rightarrow AC \}$

Candidate keys : A, B

2NF :

$A \rightarrow B$

no proper subset of candidate key

$B \rightarrow AC$

\hookrightarrow 3NF ✓

no proper \hookrightarrow \Rightarrow 2NF ✓

3NF :

$A \rightarrow B$
prime

$B \rightarrow AC$
prime

no transitive
dependency ✓

3NF ✓

BCNF :

$(A) \rightarrow B$
SK ✓

$(B) \rightarrow AC$
SK ✓

BCNF ✓

∴ Given relation

in BCNF

R(ABCDE)

FD: $\{ A \rightarrow BC, BC \rightarrow AD, D \rightarrow E \}$

candidate keys : A, BC

2NF:

$A \rightarrow BC$

$BC \rightarrow AD$

$D \rightarrow E$

none are proper subsets of any candidate key, so it is in 2NF ✓

3NF:

$A \rightarrow BC$
prime

$BC \rightarrow AD$
prime

$D \rightarrow E$
non prime
non prime

prime prime
 non prime prime
 transitive dependency
 $\exists \text{ N.F. } \times$
 ∴ The given relation is in 2NF.

$R(A B C D E)$
 $FD: \{ A \rightarrow B, BC \rightarrow D, DE \rightarrow A \}$
 candidate keys: ACD, BCD, CDE
 ↳ As all attributes are prime attributes, the given relation is in 3NF.
 BCNF:
 $A \rightarrow B$ $BC \rightarrow E$ $DE \rightarrow A$
 SK ✓ X SK X SK
 × not in BCNF
 therefore the given relation is in 3NF

$R(A B C D E)$
 $FD: \{ B \rightarrow A, A \rightarrow C, BC \rightarrow D, AC \rightarrow BE \}$
 candidate keys: A, B
 ↳ 2 candidate keys are simple, 1NF.

→ all candidate keys are simple,
so the relation is in 2NF.

3NF:

$$\boxed{B} \rightarrow A$$

prime

$$\boxed{A} \rightarrow C$$

prime

$$\boxed{BC} \rightarrow D$$

non prime

$$\boxed{AC} \rightarrow \boxed{BE}$$

non prime

3NF X

transitive

dependencies
exist

∴ The given relation is in 2NF

2NF



DEPENDENCY PRESERVING DECOMPOSITION

11 October 2023 20:08

$R(A, B, C)$

1	1	1
2	1	2
3	2	1
4	2	2

$R(A B C D)$

$R_1(AB)$

$R_2(CD)$

can't just decompose,
need to follow some
rules

① dependency preserving

② lossless

For given table

$fD: \{ A \rightarrow B, A \rightarrow C \}$

decomposing the table :

$R_1(A, B)$

1	1
2	1
3	2
4	2

$R_2(B, C)$

1	1
1	2
2	1
2	2

$fD: \{ A \rightarrow B \}$

$\hookrightarrow F_1$

$\hookrightarrow F_2$ no functional dependency

Logically $F_1 \cup F_2 = f$ must hold

... here $F_1 \cup F_2 = \{ A \rightarrow B \}$

But here $F_1 \cup F_2 = \{ A \rightarrow B \}$
 ↳ so this decomposition is not a
 dependency preserving relation

In general, if a relation R is divided into $R_1(F_1) R_2(F_2) \dots R_n(F_n)$:

The decomposition is said to be dependency preserving if

$$F_1 \cup F_2 \cup F_3 \cup \dots \cup F_n = F$$

$R(A B C D E)$

$$F = \{ A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A \}$$

$R_1(A B C)$

$R_2(C D E)$

$$\left\{ \begin{array}{l} A^+ = \cancel{A B C D} \\ B^+ = \cancel{A B C D} \\ C^+ = \cancel{A B C D} \end{array} \right.$$

$$\begin{array}{l} C^+ = \cancel{A B C D} \\ D^+ = \cancel{A B C D} \\ E^+ = E \end{array}$$

$$\begin{array}{l} A \rightarrow BC \\ B \rightarrow AC \\ C \rightarrow AB \end{array}$$

$$\left\{ \begin{array}{l} C \rightarrow BD \\ D \rightarrow C \end{array} \right.$$

(candidate keys)

(candidate keys)

(candidate key)

no need to write
other functional
dependencies

now performing $F_1 \cup F_2$

$$F_1 \cup F_2 = \{ A \rightarrow BC, B \rightarrow AC, \\ C \rightarrow ABD, D \rightarrow C \}$$

check if every member of F is
a member of $F_1 \cup F_2$

$$F = \{ A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A \}$$

$$\overbrace{F_1 \cup F_2}^G \equiv F$$

check $\leftarrow G$ covers F $G \supseteq F$
 F covers G → always true

Note: while decomposing, it always
will not lead to a dependency
preserving decomposition.

Up to 3NF → dependency preserving
BCNF → exceptional case

Find the highest normal form:

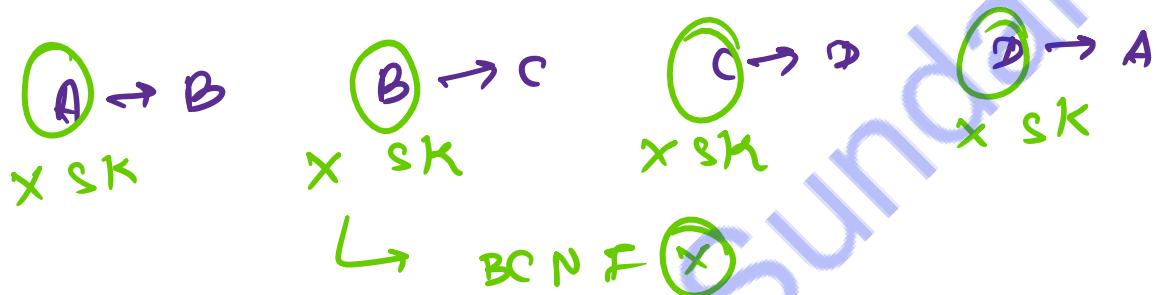
R (ABCDE)

$R(A B C D E)$

$F: \{ A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A \}$

candidate keys: AE, BE, CE, DE

As all attributes in the relation are prime attributes, the relation is in 3NF.



$R(C A B C D E)$

$F: \{ A \rightarrow BC^D, B \rightarrow AE, BC \rightarrow AED, D \rightarrow E, C \rightarrow DE \}$

$R_1(C A B)$

$$\{ A^+ = ABCDEF \\ B^+ = ABCDEF \}$$

$B^+ = ABCDEF$
candidate keys

$R_2(C B C)$

$$\begin{aligned} B^+ &= ABCDEF \\ C^+ &= CDEF \end{aligned}$$

candidate key

$$\begin{array}{ccc} A & \xrightarrow{\quad} & B \\ B & \xrightarrow{\quad} & A \end{array}$$

$$B \rightarrow C$$

$R_3(CDDE)$

$$C^+ = \cancel{CD}E$$

$$D^+ = \cancel{D}E$$

$$E^+ = \cancel{E}$$

$$DE^+ = \cancel{DE}$$

$$C \rightarrow DE$$

$$D \rightarrow E$$

$F_1 \cup F_2 \cup F_3$

$$= \{ A \rightarrow B, B \rightarrow A, \\ B \rightarrow C, C \rightarrow DE, \\ D \rightarrow E \}$$

G covers F
✓

Given decomposition is
dependency preserving.

$R(ABCD)$

$F : \{ C \} \{ A \rightarrow B, C \rightarrow D \}$

$R_1(AC)$

$$A^+ = AB$$

$$C^+ = \cancel{C}D$$

$$AC^+ = ABCD$$

no functional dependency

$R_2(BD)$

$$B^+ = B$$

$$D^+ = D$$

$$BD^+ = BD$$

no functional dependency

no functional dependency

$$F_1 = \emptyset$$

dependency

$$F_2 = \emptyset$$

[only trivial FDs are present]

$$F_1 \cup F_2 = \emptyset$$

$$\text{but } F: \{ A \rightarrow B, C \rightarrow D \}$$

G does not cover F.

so given decomposition is
not dependency preserving.

$R(A B C D E)$

$$F: \{ A \rightarrow B C D E, BC \rightarrow A E D, D \rightarrow E \}$$

$R_1(A B)$

$$A^+ = A B C D E$$

$$B^+ = B$$

A B

$R_2(C B C)$

$$B^+ = B$$

$$C^+ = C$$

$$BC^+ = A B C D E$$

$$\phi$$

$R_3(C D E)$

$$C^+ = C$$

$$D^+ = D E$$

$$E^+ = E$$

$$C D^+ = C D E$$

$$C E^+ = C E$$

$$D E^+ = D E$$

$$C D E^+ = C D E$$

$$D \rightarrow E$$

performing union

$$G = \{ A \rightarrow B, D \rightarrow E \}$$

$$F = \{ A \rightarrow B C D E, BC \rightarrow A D E, D \rightarrow E \}$$

$$F = \{ A \rightarrow BC\bar{D} \cup \bar{D} \bar{E}, \bar{D} \rightarrow E \}$$

$$A^+ = AB \quad BC^+ = BC \quad \underline{\underline{D}}^+ = \underline{\underline{DE}}$$

clearly G does not cover F
 \therefore The given decomposition is
 not dependency preserving.

$R(CABCD)$

$$F = \{ A \rightarrow B, B \rightarrow C, C \rightarrow D, D \rightarrow A \}$$

$R_1(AB)$

$$A^+ = A\cancel{BCD}$$

$$B^+ = A\cancel{BCD}$$

$$\begin{array}{l} A \rightarrow B \\ B \rightarrow A \end{array}$$

$R_2(CB)$

$$\begin{array}{l} B^+ = A\cancel{BCD} \\ C^+ = A\cancel{BCD} \end{array}$$

$$\begin{array}{l} B \rightarrow C \\ C \rightarrow B \end{array}$$

$R_3(CD)$

$$\begin{array}{l} C^+ = A\cancel{BCD} \\ D^+ = A\cancel{BCD} \end{array}$$

$$\begin{array}{l} C \rightarrow D \\ D \rightarrow C \end{array}$$

$G = \{$

$$\begin{array}{l} A \rightarrow B \\ B \rightarrow A \end{array}$$

$$\begin{array}{l} B \rightarrow C \\ C \rightarrow B \end{array} \quad \begin{array}{l} C \rightarrow D \\ D \rightarrow C \end{array}$$

$$\underline{\underline{A}}^+ = \underline{\underline{ABC}}D$$

$$\underline{\underline{B}}^+ = \underline{\underline{BC}}DA$$

$$\underline{\underline{C}}^+ = \underline{\underline{CD}}AB$$

$$\underline{\underline{D}}^+ = \underline{\underline{DA}}BC$$

G covers F .

G covers F .
so, the decomposition is
dependency preserving

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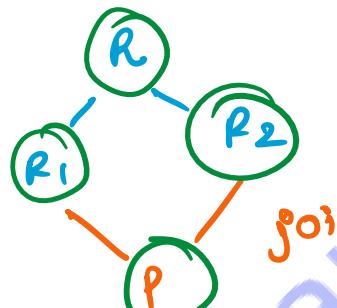
LOSSLESS JOIN DECOMPOSITION | ADDITIVE JOIN DECOMPOSITION PROPERTY

11 October 2023 22:16

lossless join → mandatory property for decomposition.

$R(ABC)$

1	1	1
2	1	2
3	2	1
4	3	2



IS $R = P$?
If yes → lossless join decomposition

$R_1(AB)$

1	1
2	1
3	2
4	3

$R_2(BC)$

1	1	1
1	2	2
2	2	1
3	2	2

$R_1(AB)$

1	1
2	1
3	2

$R_2(BC)$

1	1
1	2
2	1

cartesian product $R_1 \times R_2$

A	B	B	C
1	1	1	1
1	1	2	1

$3 \times 3 = 9$ rows
also named

A	B	C	D	E
1	1	1	1	1
1	1	1	2	
			2	
				2

$3 \times 3 = 7$ rows
are formed

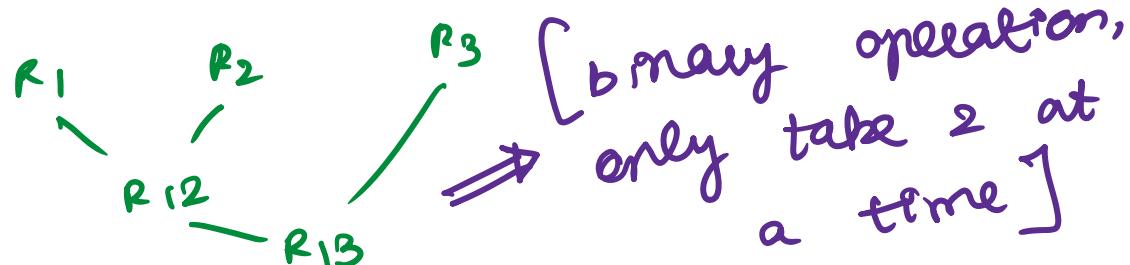
Natural join $R_1 \bowtie R_2$

consider only these rows where
 $R_1 \cdot B = R_2 \cdot B$ while joining

A	B	C
1	1	1
1	1	2
2	1	1
2	1	2
3	2	1

only 5 rows
in natural
join

Note: If no common attributes are present between the relations, the result of natural join will be the same as that of the cartesian product.



$R(ABC)$

$R_1(A,B)$

$R_2(B,C)$

$R(A, B, C)$

1	1	1
2	1	2
3	2	1
4	3	2

1	1
2	1
3	2
4	3

1	1
1	2
2	1
3	2

Now $R_1 \bowtie R_2$:

$\left(\begin{matrix} 4 \\ 4+2 \end{matrix} \right) + 6$ tuples
extra
not allowed

A	B	C
1	1	1
1	1	2
2	1	1
2	1	2
3	1	2
3	2	1
4	1	2
4	2	2

Lossless decom position must be reformed.
→ EXACTLY SAME → not lossless.
Given decomposition is [lossy]

$R(A, B, C)$		
1	1	1
2	1	2
3	2	1
4	2	2

$R_1(A, B)$

$R_2(B, C)$

this decomposition is lossless (C missing)
C is lost while joining

for a lossless join decomposition:

① $\text{att}(R_1) \cup \text{att}(R_2) = \text{att}(R)$

② $\text{att}(R_1) \cap \text{att}(R_2) \neq \emptyset$

③ $\text{att}(R_1) \cap \text{att}(R_2)$ must be a one - ...

- (3) $\text{att}(R_1) \cap \text{att}(R_2)$ must be
candidate of at least one
key sub-relation
- $\text{att}(R_1) \cap \text{att}(R_2) \rightarrow \text{att}(R_1)$
- (OR)
- $\text{att}(R_1) \cap \text{att}(R_2) \rightarrow \text{att}(R_2)$
-

$R(ABC)$	$R_1(AB)$	$R_2(CAC)$
1 1 1	1 1	1 1
2 1 2	2 1	2 2
3 2 1	3 2	3 1
4 2 2	4 2	4 2

$R_1 \bowtie R_2 :$

	A	B	C
1	1	1	1
2	2	1	2
3	3	2	1
4	4	2	2

super key $A \rightarrow B$

super key $A \rightarrow C$

\therefore This decomposition is lossless

$R(ABC)$	$R_1(AB)$	$R_2(BC)$
1 1 3	1 1	1 3
2 1 3	2 1	2 3
3 2 6	3 2	3 6
4 3 7	4 3	7

① $AB \cup BC = ABC$

$\sim \cap \cap BC = B$

∴ ~~3~~ 3 is a duplicate

- ① "D
 $AB \cap BC = B$ ✓
 ② checking if B is ck of R₁: No
 ③ checking if B is ck of R₂: Yes
 ✓

↳ all properties are satisfied.
 So the decomposition lossless
is lossless.

performing \bowtie and checking

$R_1 \bowtie R_2$

A	B	C	D	E
1	1	3		
2	1	3		
3	2	6		
		7		
F	3			

exactly same as R



$R(A B C D E)$

A	B	C	D	E
1	1	2	1	3
2	2	2	1	3
3	1	6	3	6
4	2	8	5	7
5	3	9	5	7

① $R_1(A B C)$ $R_2(D E)$

↳ no common attribute

☒ lossy

↪ no common attribute

② $R_1(ABC)$ $R_2(CDE)$

↪ common attribute : C

For R_1

$C \rightarrow B$ \times
 $C \rightarrow A$ \times (OK)

For R_2

$C \rightarrow D$ ✓
 $C \rightarrow E$ ✓
✓

✓ lossless

③ $R_1(ABC)$ $R_2(CABDE)$

↪ common attributes : AB

For R_1 $AB \rightarrow C$ ✓ For R_2

AB → DE ✓

✓ lossless

④ $R_1(AB)$ $R_2(BCDE)$

attributes : B

↪ common
For R_1 $B \rightarrow A$ \times

R_2 :

$B \rightarrow C$ \times
 $B \rightarrow D$ \times
 $B \rightarrow E$ \times

✗ lossy

⑤ $R_1(AB)$

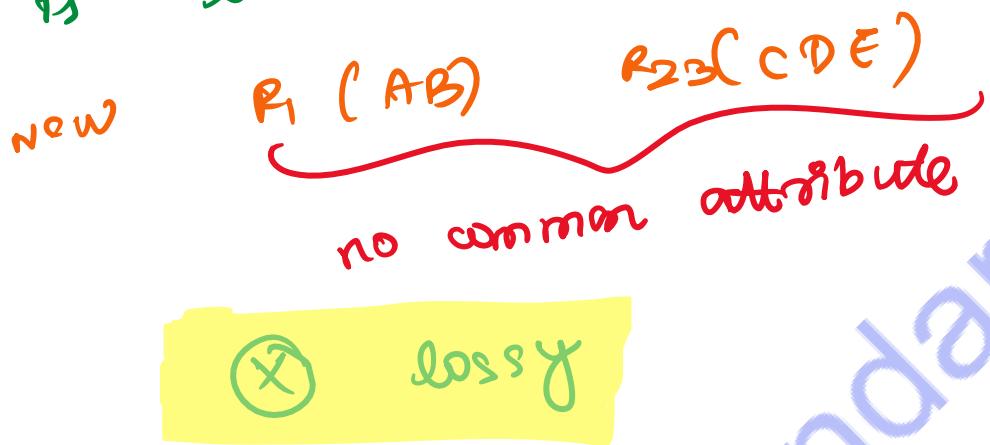
$R_2(CD)$

$R_3(DE)$

common attribute D

$$R_2 : \begin{matrix} D \rightarrow C \\ \text{X} \end{matrix} \text{ (cor)} \quad R_3 : \begin{matrix} D \rightarrow E \\ \text{X} \end{matrix} \quad \checkmark$$

decomposition into R_2 and R_3
is lossless



$R(CABCD)$

$$F : \{ A \rightarrow B, B \rightarrow C, C \rightarrow A \}$$

$R_1(ABC)$ $R_2(CD)$

common attribute: C
 $C^+ = ABC$ \rightarrow candidate key of R_1

✓ lossless

$R(ABCDEF)$

$$F : \{ AB \rightarrow C, C \rightarrow D, D \rightarrow EF, F \rightarrow A, D \rightarrow B \}$$

$$D : \{ \underbrace{ABC}_{R_1}, \underbrace{CDE}_{R_2}, \underbrace{EF}_{R_3} \}$$

[another form of representation]

$\overbrace{R_1 \quad R_2 \quad R_3}^{\text{union of all attributes}} = ABCDE$ ✓

representation]

Taking $R_1 \bowtie R_3 \rightarrow$ no common attribute

Taking $R_1 \bowtie R_2 \rightarrow$ C is common attribute

$C^+ = CDEFAB$ ↪ consolidate key for both R_1 & R_2

$R_1 \quad R_2$ is lossless, now join them

$R_{12} (ABCDEF)$ $R_3 (CFG)$

↪ common attribute: E

$E^+ = E$ ↪ candidate key of
not a R_{12} (or) R_3 ✗

∴ this decomposition is lossy.

Updating previous Qn

adding another FD : $E \rightarrow F$

$E^+ = EF \rightarrow E$ is a candidate key of R_3

key \Leftrightarrow

\hookleftarrow lossless

\downarrow

thus decomposition is lossless

check if it is dependency preserving:

$R(C A B C D E)$

$F : \{ AB \rightarrow C, C \rightarrow D, D \rightarrow EF, F \rightarrow A, D \rightarrow B \}$

$D : \{ ABC, CDE, EF \}$

$R_1(A B C)$

$$A^+ = A$$

$$B^+ = B$$

$$C^+ = CDEF / AB$$

$$AB^+ = ABCD / EF$$

$$C \rightarrow AB$$

$$AB \rightarrow C$$

$R_2(C D E)$

$$E^+ = E$$

$$F^+ = FA$$

$$\emptyset$$

$R_2(C D E)$

$$C^+ = CDEF / AB$$

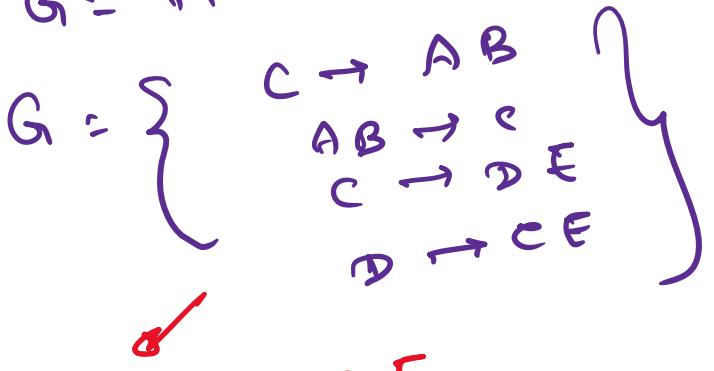
$$D^+ = DEF / ABC$$

$$EF^+ = E$$

$$C \rightarrow DE$$

$$D \rightarrow CE$$

$$G = F_1 \cup F_2 \cup F_3$$



$$\begin{array}{l}
 \text{D} \rightarrow F \\
 F \rightarrow A
 \end{array}
 \quad \text{are lost}
 \quad
 \begin{array}{l}
 \cancel{\overline{AB}}^+ = ABCDE \\
 \cancel{\overline{C}}^+ = \cancel{C}^D E A B \\
 \cancel{\overline{D}}^+ = \cancel{D}^C E A B \\
 \cancel{\overline{F}}^+ = F
 \end{array}$$

G does not cover F .

∴ The decomposition is
not dependency preserving.

CANONICAL COVER | MINIMAL COVER | IRREDUCIBLE SET OF FUNCTIONAL DEPENDENCIES

12 October 2023 07:16

F' is said to be a canonical cover of F if F' does not have

- (i) extraneous / redundant attributes
- (ii) redundant functional dependencies

STEPS :

- ① splitting rule so that in every functional dependency, right hand side has single attribute.
- ② Remove extraneous attribute.
- ③ Remove redundant functional dependencies

eg

$$AB \rightarrow C, A \rightarrow C$$

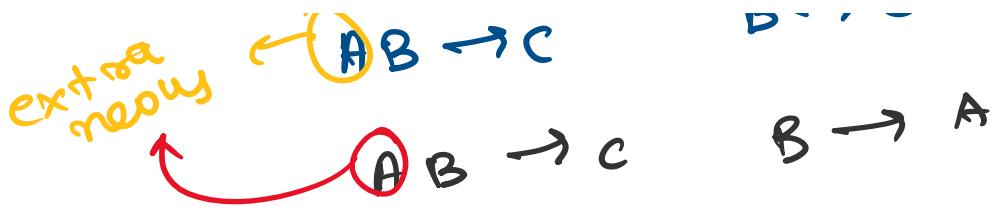
extraneous attribute

$$A B \rightarrow C \quad A \rightarrow B$$

here also B is extraneous

extraneous $\leftarrow AB \rightarrow C$

$$B \rightarrow C$$



Redundant functional dependency

even after removing the functional dependency, it indirectly still exists

Eg: $F: \{ AB \rightarrow C, C \rightarrow AB, B \rightarrow C, ABC \rightarrow AC, A \rightarrow C, AC \rightarrow B \}$

① split

$$F: \{ AB \rightarrow C, C \rightarrow A, C \rightarrow B, B \rightarrow C, ABC \rightarrow A, ABC \rightarrow C, A \rightarrow C, AC \rightarrow B \}$$

$\underbrace{ABC \rightarrow A, ABC \rightarrow C}_{\text{trivial FD}}$ $\underbrace{A \rightarrow C}_{\text{trivial FD}}$

②

extraordinary

$F: \{ AB \rightarrow C, C \rightarrow A, C \rightarrow B, B \rightarrow C, A \rightarrow C, AC \rightarrow B \}$

Note: also

$$AB \rightarrow C \quad A \rightarrow C$$

canonical cover is not necessarily unique. more than one canonical cover may exist.

cover may exist.

$$F = \{ B \rightarrow C, C \rightarrow A, C \rightarrow B, A \rightarrow C, \cancel{A \rightarrow C}, \cancel{\{AC \rightarrow B\}} \}$$

extraneously

$$F = \{ B \rightarrow C, C \rightarrow A, C \rightarrow B, A \rightarrow C, A \rightarrow B \}$$

③ redundant FD's

To check if a FD is redundant or not, temporarily remove it and find $(LHS)^+$. If RHS is still formed, it means that the FD is redundant.

Checking $C \rightarrow A$:

$$C^+ = CB$$

$C \rightarrow A$ is not redundant

$$C \rightarrow B :$$

$$C^+ = CA\underline{B}$$

exists

$C \rightarrow B$ is redundant

$$F = \{ C \rightarrow A, B \rightarrow C, A \rightarrow C, A \rightarrow B \}$$

Checking $A \rightarrow C$:

$$\underline{A}^+ = ABC$$

$A \rightarrow C$ is redundant

$$F = \{ C \rightarrow A, B \rightarrow C, A \rightarrow B \}$$

$F : \{ c \rightarrow A, B \rightarrow c, A \rightarrow 'd' \}$

checking $A \rightarrow B$: $A^+ = A$ \times $A \rightarrow B$ is essential

Finally

$F' = \{ A \rightarrow B, B \rightarrow c, c \rightarrow A \}$

→ minimal cover / canonical cover / irreducible set of FDs

2NF DECOMPOSITION

12 October 2023 07:34

$R(A B C D)$
 $F: \{ A \rightarrow B, B \rightarrow C \}$

candidate key : AD

2NF:

$\begin{matrix} A \rightarrow B \\ \text{proper subset of } AD \end{matrix} \Rightarrow \begin{matrix} \text{partial dependency} \\ \text{non prime attribute} \end{matrix}$

$\textcircled{X} \text{ not in 2NF}$

[$B \rightarrow C$ is not a partial dependency]

$A \rightarrow B$ is a partial dependency.

LHS = A

Finding $A^+ = ABC$ put these in one relation

In the other relation

put remaining attributes + LHS

$R_1(A B C)$

$R_2(A D)$

This is a

lossless join

decomposition.

$$A^+ = ABC$$

$$A^+ = A / BC$$

$$B^+ = BC$$

$$D^+ = \emptyset$$

$$C^+ = \emptyset$$

$$\emptyset$$

$$BC^+ = BC$$

... non null only

$$BC' = DY$$

$\cap \neq BC$

B → C

As there are only
2 attributes, P₂
P₃ in BCNF

Now $P_1(DBC)$ with

$$\begin{array}{ccc} A & \rightarrow & BC \\ B & \rightarrow & C \end{array}$$

candidate key : A

As the candidate key is single
and primary in 2NF.

valued, it is in 2. checking for dependency preserving:

$$G = f_1 \cup f_2 =$$

$$\underline{A^+} = \underline{ABC}$$

$$\underline{B}^T = \underline{B}C$$

G covers F

$$R_1(ABC) \rightarrow R_2(AD)$$

lossless &
dependency
preserving

R (A B C D)

$F: \{A \rightarrow B, C \rightarrow D\}$

$F : \{ A \rightarrow B, C \rightarrow D \}$
candidate key : $AC \rightarrow$ only candidate key

2NF :

A → B

em

non

C → D
PC NPA

$A \leftarrow$
 proper subset of AC
 \nwarrow non prime
 \downarrow PS
 \downarrow NPA

Both are partial dependencies

Lossless ✓

$$A^+ = AB$$

$$R_1(AB)$$

$$A \rightarrow B$$

$$C^+ = CD$$

$$R_2(CD)$$

$$C \rightarrow D$$

Remaining + LHS
into R_3
 $R_3 \subset AC^c$

$G = F_1 \cup F_2 \cup F_3 = \{ A \rightarrow B, C \rightarrow D \} = F$
 ↳ dependency preserving relation ✓

all subrelations have only two attributes → BCNF ✓

CON checking rule by rule

$$R_1(AB)$$

CK: A

$A \rightarrow B$
 single prime
 $A \rightarrow B$
 prime not transitive

2NF ✓

$A \rightarrow B$
 superkey
 $B \rightarrow D$
 single

3NF ✓

BCNF ✓

$$R_2 \subset CD$$

CK: C

$C \rightarrow D$
 single

2NF ✓

CK: C

single

$C \rightarrow D$
prime → not transitive \rightarrow 3NF ✓

$C \rightarrow D$
super key → BCNF ✓

$R_3(C A^e)$ → Functional dependencies $\Rightarrow \phi$ \rightarrow BCNF ✓

∴ Decomposition is
 $R_1(A B)$ $R_2(C D)$ $R_3(A C)$
It is in BCNF. It is lossless
and dependency preserving.

2NF TO 3NF

15 October 2023 09:28

$R(ABCD)$

$f : \{ A \rightarrow B, B \rightarrow C, C \rightarrow D \}$

candidate

key : A

$B \rightarrow C$
non prime
non prime

$C \rightarrow D$
non prime
non prime

$B^+ = BCD$

$C^+ = CD$

CK $R_1(BCD)$

$B^+ = BCD$

$C^+ = CD$

$D^+ = D$

CK $R_2(CD)$

$C^+ = CD$

$C \rightarrow D$

2 transitive dependencies

(to ensure lossless)
Remaining LHS

$R_3(ABC)$

CK $A^+ = ABC$
 $B^+ = BC$
 $C^+ = C$

$B \rightarrow CD$
 $C \rightarrow D$

BCNF

$A \rightarrow BC$
 $B \rightarrow C$

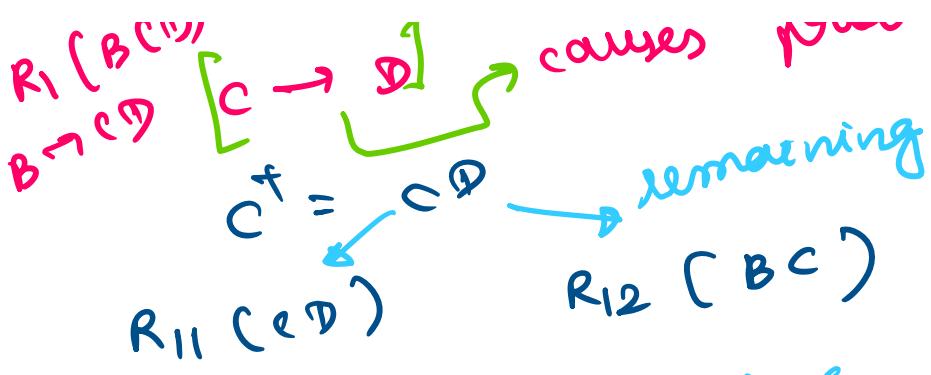
transitive dependency
converted into 2NF. But it is
not necessary that they should be
in 3NF.

$R_1 \rightarrow 2NF$

$R_2, R_3 \rightarrow BCNF$

again apply the same steps
for decomposition

$R_1(BCD)$
in $[C \rightarrow D]$ causes problem



union { $B \rightarrow C$ } $B \rightarrow C$ dependency
 $\{ B \rightarrow C \}$ $B \rightarrow CD$ preserving
 $C \rightarrow D$ $C \rightarrow D$
 clearly G covers F

Now $R_{11} \{ cD \} \rightarrow BCNF$
 $R_{12} \{ BC \} \rightarrow BCNF$

$R_{11} \{ cD \}$ $R_{12} \{ BC \}$
 \Downarrow duplicate
 $R_2 \{ CD \}$ $R_3 \{ ABC \}$

Renaming:

$R_1 \{ ABC \}$ $R_2 \{ BC \}$ $R_3 \{ CD \}$
 relation gets converted to $BCNF$

Here it is lossless and dependency preserving. But sometimes while converting it into $BCNF$ it may not be dependency preserving.

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NORMALIZING A TABLE

15 October 2023 09:46

Normalize a relation from :
 1NF \rightarrow BCNF

$R(ABCDEF)$

$F = \{ A \rightarrow BD, B \rightarrow C, E \rightarrow FG, AE \rightarrow H \}$

candidate key : $AE \rightarrow$ only candidate key

$A \rightarrow BD$
 partial dependency

$A^+ = ABCD$

$E \rightarrow FG$
 partial dependency
 $E^+ = EFG$

$D = \{ ABCD, EFG, AEH \}$

$C \in ABCD$
 $A^+ = BCD$
 $B^+ = BC$
 $C^+ = C$
 $D^+ = \emptyset$
 $A \rightarrow BCD$

$E^+ = EFG$
 $F^+ = F$
 $G^+ = G$
 $E \rightarrow FG$

BCNF

AEH
 $A^+ = ABD$

$E^+ = EFG$

$F^+ = F$

$AE^+ = ABD$
 $C \in K$

$AE \rightarrow H$

BCNF

$B \rightarrow C$
 partial dependency

partial dependency

2NF

⇒ till now: $\{ABCD, EFG, AEH\}$
requires further decomposition

$ABCD = F : \{A \rightarrow BCD, B \rightarrow C\}$

Candidate key: A

$A \rightarrow BCD$

$B \rightarrow C$
transitive dependency

$B^+ = BC$

b

⇒ $\{BC, ABD\}$

BC :
 $B^+ = BC$
 $c^+ = C$

$B \rightarrow C$

BCNF

ABD :

$A^+ = ABCD$

$B^+ = BC$

$D^+ = D$

$A \rightarrow BD$

BCNF

Q. decomposition for BCNF:

∴ final decomposition for BCNF :

{ BC, ABD, EFG, AEH }

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