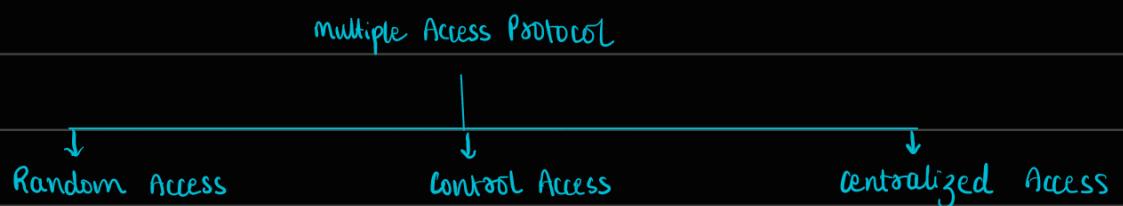


## Multiple Access Control

- Introduction :



- ALOHA
- CSMA
- CSMA/CD
- CSMA/CA
- Reservation
- Polling
- Token Passing
- FDMA
- TDMA
- CDMA



- Even in full-duplex, There is no problem of collision
- Collisions are a problem. So, medium access control helps here



Reason why  $\text{Timeout} = 2 * \text{Pd}$  : Consider the stations at 2 extremes :



Data sent from A to D takes ' $\text{Pd}$ ' time

Ack sent from D to A takes ' $\text{Pd}$ ' time

$$\Rightarrow \text{Timeout} = \text{Pd} + \text{Pd} = 2 * \text{Pd}$$

- After timeout, station will again send data but if it immediately tries to send data packet then collision will occur because timeout is same for all stations. Hence, no station can effectively send data
- So, station MUST NOT send frame immediately after timeout
- It must wait for random amount of time called back-off time.

Backoff time or  
Waiting time

NOTE: Collision no. is  
not the data packet  
NOT station

$k \rightarrow$  Any random no. in b/w 0 to  $2^N - 1$

$N \rightarrow$  Collision number.

Slot time can be either of these : { RTT,  $2 * \text{Pd}$ ,  $\text{Pd}$ ,  $\text{Td}$  }  
(will be given in question)

- Max. no. of attempts for a station = 15
- Binary Exponential Back off Algorithm : Collision prob. decreases exponentially

Eg.-



Collision occurs at time t = :

$$\textcircled{A} : N=1 \quad \text{and} \quad \textcircled{B} : N=1$$

$$F = \{0, 1\} \quad F = \{0, 1\}$$

$$P(A) = 25\%$$

$$\text{So, } 4 \text{ possibilities: } \{ (0,0), (0,1), (1,0), (1,1) \}$$

$\uparrow \qquad \qquad \uparrow$   
Collision (50%)

$$P(B) = 25\%$$

Say we take (0,1). This means A does not wait and sends the frame immediately and B waits for (1 slot time). So, A now sends pkt 2 and B is still trying to send pkt 1.

Say collision occurs now as well (t<sub>1</sub>):

$$P(A) = \frac{\# \{x > y\}}{\text{Total}}$$

$$\textcircled{A} : N=2$$

$$\textcircled{B} : N=1$$

$$= 5/8 = 62.5\%$$

$$F = \{0, 1, 2, 3\}$$

$$F = \{0, 1\}$$

$$P(B) = \frac{\# \{y > x\}}{\text{Total}}$$

$$\text{So, } 8 \text{ possibilities: } \{ (0,0), (1,1), \dots \}$$

$\downarrow$   
Collision (25%)

$$= 1/8 = 12.5\%$$

Now, say we take any non-collision case: (1,0)

$$\textcircled{A} N=3 \quad \text{and} \quad \textcircled{B} = 1$$

$$P(A) = 13/16 = 81.25\%$$

$$F = \{0, 1, \dots, 7\} \quad F = \{0, 1\}$$

$$P(B) = 1/16 = 6.25\%$$

$$\text{So, } 16 \text{ possibilities: } \{ (0,0), (1,1), \dots \}$$

Collision (12.5%)

- Disadvantages: The algorithm suffers from CAPTURE EFFECT. If any station wins the 1<sup>st</sup> collision then it has more probability of winning in the next collision. So, here:

$$P(A)_{t_0} < P(A)_{t_1} < P(A)_{t_2} \dots \quad CP: \text{Collision Prob.}$$

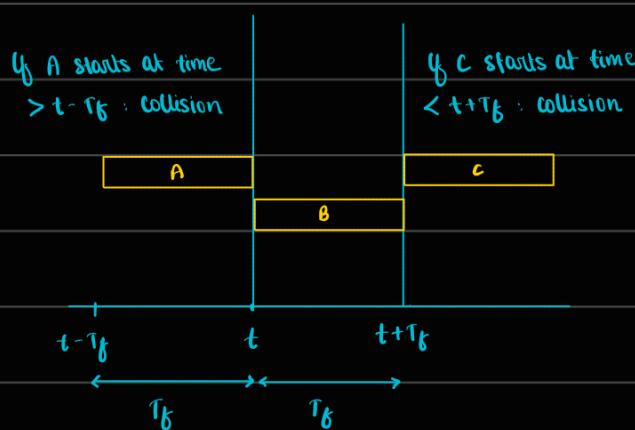
$$P(B)_{t_0} > P(B)_{t_1} > P(B)_{t_2} \dots$$

$$CP_{t_0} > CP_{t_1} > CP_{t_2} > CP_{t_3} \dots$$

- Throughput of pure ALOHA:  $S = G e^{-2G}$  where  $G = \text{no. of frames generated by network in one transmission time}$

for maximum throughput,  $dS/dG = 0 \Rightarrow G = 1/2 \Rightarrow \text{max. throughput} = 18.4\%$

Also,  $G = 1/2$  implies 1 frame should be generated in 2 frames' transmission time meaning, if we do this, collisions won't occur. This is called the Vulnerable time :



So, time range at which collisions can occur :

$(t - Tf, t + Tf)$   $\Rightarrow$  Vulnerable time = max. - min. of this range

$$Vt = 2Tf$$

- Eg. ① Pure ALOHA ; 200 bits frames ; shared channel of B = 200 kbps ; What is the throughput if the system (all stations together) produces 1000 frames generated by network in 1 sec. (Throughput here is defined as average no. of frames successfully transmitted per second)

$$L = 200 \text{ bits}, B = 200 \times 10^3 \text{ bps}, T_f = L/B = 1 \text{ ms}$$

1s  $\longrightarrow$  1000 frames

1ms  $\longrightarrow$  1 frame = 61

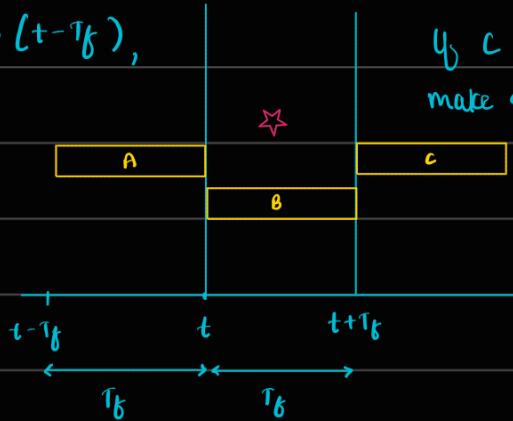
$$S = 61e^{-26} = e^{-2} = 0.135 = 13.5\%$$

Throughput (as defined here) =  $1000 \times 0.135 = 135$  frames per second

- Slotted ALOHA :
  - It divides the time of shared channel in discrete intervals called time slots (time slots = transmission time for one frame)
  - Any station can transmit its data at any time slots. Only condition is that station must start its transmission from the BEGINNING OF THE TIME SLOT.
  - If the beginning of the slot is missed, then station has to wait until the beginning of the next time slot
  - A collision may occur if 2 or more stations try to transmit data at the beginning of the same time slot

If A starts at time  $> (t - T_f)$ ,  
make start time as

$$(t - T_f + T_f) = t$$



If C starts at time  $< (t + T_f)$ ,  
make start time as  $(t + T_f + T_f) = t + 2T_f$

$$\text{Vulnerable Time} = T_f \quad (V_f)$$

$\star$  Collision will occur at cases like this : (say  $T_f = 2 \text{ secs}$ )

A wants to send at  $T_f + (T_f/10)$   $\rightarrow$  A will send at  $2T_f$

B wants to send at  $T_f + (T_f/20)$   $\rightarrow$  B " "

C want to send at  $T_f + (T_f/3)$   $\rightarrow$  C "

⇒ Collision

- Throughput of slotted ALOHA:  $S = 6t e^{-6t}$  where  $6t$  = no. of frames generated by network in one transmission time

for max. throughput,  $\frac{dS}{dt} = 0 \Rightarrow 6t = 1$ . Meaning, generate 1 frame

per transmission time to avoid collision and maximize throughput

$$\text{Max. Throughput} = e^{-1} = 0.368 = 36.8\%$$

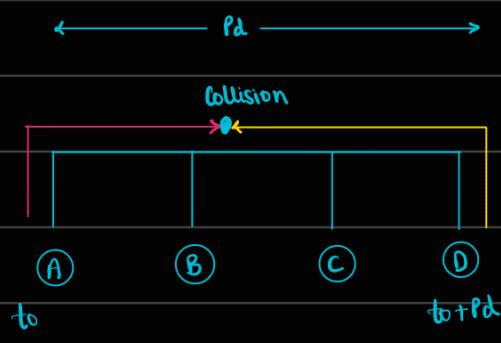
- CSMA (Carrier Sense Multiple Access)

- Was developed to minimize the chance of collision. Chances of collision can be reduced if the station senses the medium or carrier before trying to use it
- CSMA requires each station to sense the carrier before transmitting the data
- Each station can sense the carrier ONLY at its point of contact with carrier
- It is not possible for any station to sense the whole carrier. So, there is huge possibility that the station might sense the carrier free when it is actually not

- Vulnerable time of CSMA :

$$\text{So, Collision range} = t_0 + P_d - t_0 = P_d$$

$$\Rightarrow \text{Vulnerable Time (VR)} = P_d$$



Medium is IDLE TILL the 1st bit of data reaches ALL THE STATIONS

So, the possibility of collision exists because of prop. delay as when a frame is sent, it might take a small amount of time for the 1st bit to reach every station.

(due to which the carrier is sensed as idle by other stations)

So, initially B senses as IDLE then as soon as the 1st bit reaches B's point to contact,



that station's data that was collided.

But there can be a case where the station sends the entire frame BEFORE receiving the JAM signal. In this case, the station won't think the collision is because of its data transmission.

SOLUTION : Station has to be sending frames when a JAM signal is received by it  
⇒ These should a minimum frame size

Min. frame size to avoid collision in CSMA/CD (Ethernet)

$$Td(f_{\text{frame}}) \geq 2pd + Td(\text{js})$$

$$\geq R\pi + Td(\text{js})$$

Eg. ① CSMA/CD ; B = 1Gbps ; d = 1km ; signal speed = 200,000 km/s ; No repeaters ;

Min. frame size in bits = ?

o (not given)

$$T_d(f_{\text{frame}}) = \frac{f_{\text{frame}}}{\beta} \geq 2P_d + T_d(\vec{s})$$

$$\Rightarrow L_{frame} \geq B(2d/v) \geq 10^4 \text{ bits}$$

$$\Rightarrow \text{Min. frame size} = 10^4 \text{ bits}$$

$$② CSMA/CD ; B = 20 \times 10^6 \text{ bps} ; P_d = 4 \mu\text{s} ; \text{Min. } L_{frame} \text{ in Bytes} = ?$$

$$\text{Min. } L_{frame} = B(2P_d + T_d(ss)) = 1600 \text{ bits} = 200 \text{ Bytes}$$

$$③ CSMA/CD ; B = 10 \text{ Mbps} ; P_d = 4 \mu\text{s} ; L_{ss} = 48 \text{ bits} ; \text{Min. } L_{frame} = ?$$

$$L_{frame} = (2P_d + T_d(ss)) \times B = (2P_d + L_{ss}/B) \times B = (4 \mu\text{s} + 8) \times 10^7 = 512 \text{ bits}$$

- Few Formulae:

- Efficiency in Ethernet  $= \frac{1}{1 + 6.4 \alpha}$  where  $\alpha = \frac{P_d}{T_d}$   
 $(CSMA/CD)$   $= \frac{T_d}{\text{Collision time} + T_d + P_d}$  where collision time = slot duration  $\times$  slot size

- Throughput of host = Prob. of success for a single station  
 $= p(1-p)^{N-1}$  where  $p$  = prob. that a specific host successfully transmits and  $N$  = total no. of hosts in the network

- Throughput of channel = Prob. of success for ANY station among all stations  
 $= Np(1-p)^{N-1}$

