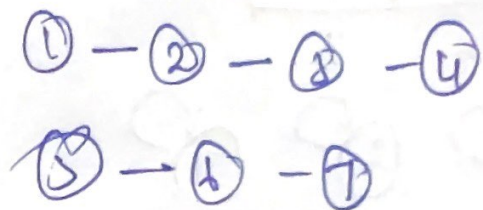


function in all smartphones names can since  
it is being declared in abstract base class.

### Disjoint set



Whether 4 and 7 belongs  
to same graph?

We can make  
it to constant  
time

We can do DFS and  
say No. But it will take  
almost  $O(N)$ .



- 1) union by rank
- 2) union by size

### union by Rank ds 1, 2, 3

Step 1: Find ultimate parent of u and v.

Step 2: Compare rank of ultimate parent  
of u and v.

Step 3: attach smaller rank component  
to larger one and increase the rank by 1.

edges:

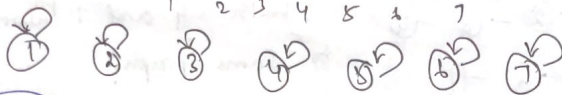
$\{1,2\}$   $\{2,3\}$   $\{4,1\}$   $\{4,7\}$   $\{5,4\}$   $\{3,7\}$

Initially rank = 

0	0	0	0	0	0	0
1	2	3	4	5	6	7

parent = 

1	2	3	4	5	6	7
1	2	3	4	5	6	7



$\{1,2\}$

$p[1] = 1$   
 $= up-u$   
 $p[2] = 2$   
 $= up-v$

$rank[up-u] = 0$      $rank[up-v] = 0$



$\{4,3\}$

$p[2] = 1 = up-u$   
 $p[3] = 3 = up-v$

$r[up-u] = 1$   
 $r[up-v] = 0$

$p[3] = 1$   
 $rank[1] += 1$

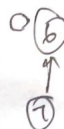


$p[2] = 1$   
 $r[1] += 1$

$\{4,5\}$



$\{6,7\}$



$\{5,6\}$

$up-u = 4$   
 $up-v = 6$



Now ultimate parent of 7 : 4

up of 5 : 4

So 7, 5 belongs to same tree. but it will take logn time. so we do path compression here.

When 6 is attached to 4, all of its children will get attached to 4.



$\{3,7\}$

$up-u = 1$   
 $up-v = 4$

$rank[1] = 1$      $r[4] = 2$

how do we achieve it?



While finding ultimate

parent of u and v, we just update the value of parent using recursion