

# Energy Dissipation in Particle-based Impact Damper Systems: Investigation based on Elasto-plastic impact model

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ME701L Nonlinear Dynamical Systems

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# Outline

1 Overview

2 System Characteristics

3 Results

- Phase portraits of the system
- Energy dissipation characteristics

4 Conclusion and perspectives

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## Overview of particle-based dampers

- Particle-based dampers usually involve macroscopic particle(s) held within cavities as depicted in the figure.
- In systems involving particle-based dampers, the energy of the system is dissipated due to inter-particle, wall-particle collision and frictional contact between surfaces.

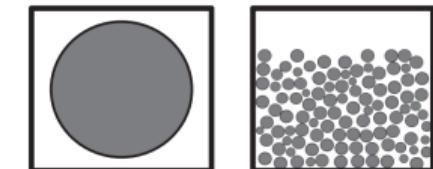


Figure: Image credit:-  
Prasad,et al. 2022

### Energy dissipation

Studies are limited due to the non-linear nature of the interaction between the constituents of the system. The below assumptions are popularly employed to simplify the system,

- contacts with a **constant coefficient of restitution**,
- **instantaneous contacts**.

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# Description of System

EoM for primary system

$$m_{PS}\ddot{z} + C\dot{z} + Kz = F(t) + F_d(t)$$

EoM for  $i^{th}$  particle

$$\begin{aligned} m_i \ddot{\mathbf{u}}_i &= \sum_j (\mathbf{N}_{ij} + \mathbf{f}_{ij}) + \sum_k (\mathbf{N}_{ik} + \mathbf{f}_{ik}) \\ I_i \ddot{\theta}_i &= R_i \sum_j (\mathbf{n}_{ij} \times \mathbf{f}_{ij}) + R_i \sum_k (\mathbf{n}_{ik} \times \mathbf{f}_{ik}) \end{aligned}$$

Non-linearity involved within the system

$$\begin{aligned} \mathbf{N}_{ij} &= -(A_{ij} \delta_{n,ij}^{3/2} + \gamma_{ij} \dot{\delta}_{n,ij}) \mathbf{n}_{ij} \\ \mathbf{f}_{ij} &= -\mu |\mathbf{N}_{ij}| \tanh(k_s \dot{\delta}_{t,ij}) \mathbf{t}_{ij} \end{aligned}$$

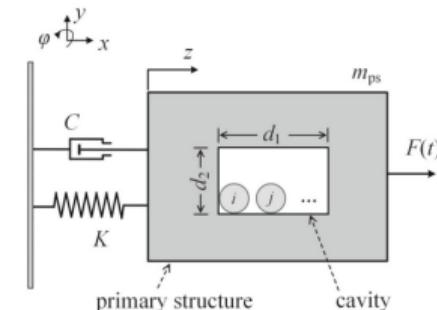


Figure: Schematic of system, Image credit-Li. et al. 2024

Impulse load

$$F(t) = \begin{cases} F_0 \sin(\pi \frac{t}{t_0}) & \text{if } t \leq t_0 \\ 0 & \text{if } t > t_0. \end{cases}$$

# Elasto-plastic impact model

Jackson, Green, and Marghitu 2010

$$e = \begin{cases} 1 & \text{if } 1 > V_1^* > 0 \\ 1 - 0.1/n(V_1^*) \left( \frac{V_1^* - 1}{59} \right)^{0.156} & \text{if } 60 > V_1^* \geq 1 \\ 1 - 0.1/n(60) - 0.11/n \left( \frac{V_1^*}{60} \right) (V_1^* - 60)^{2.36\epsilon_y} & \text{if } 1000 > V_1^* \geq 60. \end{cases}$$

$$V_1^* = \frac{V_1}{V_c}, \quad V_c = \sqrt{\frac{4\omega_c P_c}{5m^*}}, \quad \omega_c = \left( \frac{\pi \dot{C}_k S_{y,k}}{2E^*} \right)^2 R^*,$$

$$P_c = \frac{4}{3} \left( \frac{R^*}{E^*} \right)^2 \left( \frac{\pi}{2} C_k S_{y,k} \right)^3, \quad C_k = 1.295 e^{0.736\nu_k},$$

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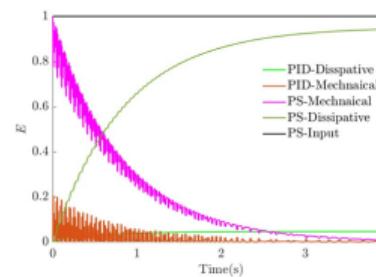
2 System Characteristics

3 Results

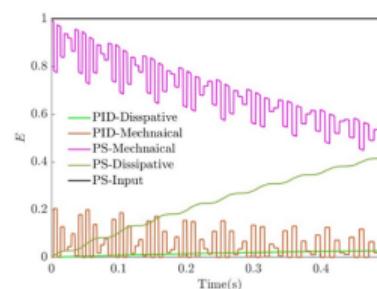
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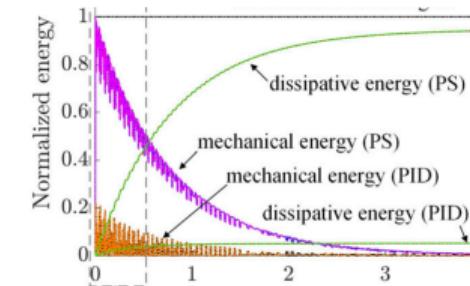
# Benchmark Validation



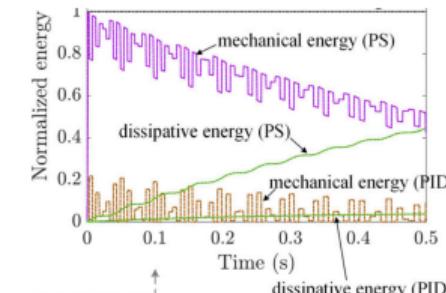
(a) Current work



(c) Current work



(b) Li et al. (2024)



(d) Li et al. (2024)

# Elasto-plastic impact model

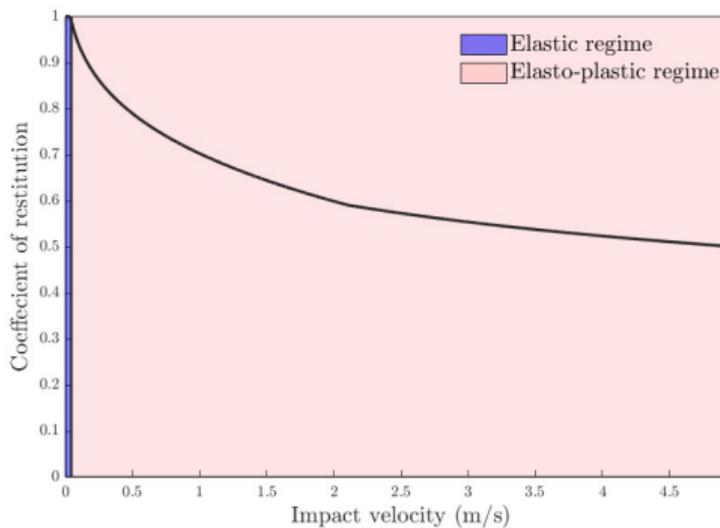


Figure: Variation of  $e$  with the impact velocity

S.no	Property	Value
1	Material	Steel
2	Modulus of elasticity	200 GPa
3	Poisson ratio	0.3
4	Yield stress	1030 MPa
5	Density	7850 kg/m <sup>3</sup>
6	Diameter of particle	33.17 mm
7	Length of cavity	67.14 mm
8	$M_{PS}$	20 Kg
9	$k$	80000 N/m
10	$\Delta t_1$	$5 \times 10^{-6}$ s
11	$\Delta t_2$	$3 \times 10^{-8}$ s

Table: Parameters employed in this study

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## Phase portrait $F_0 = 0N$

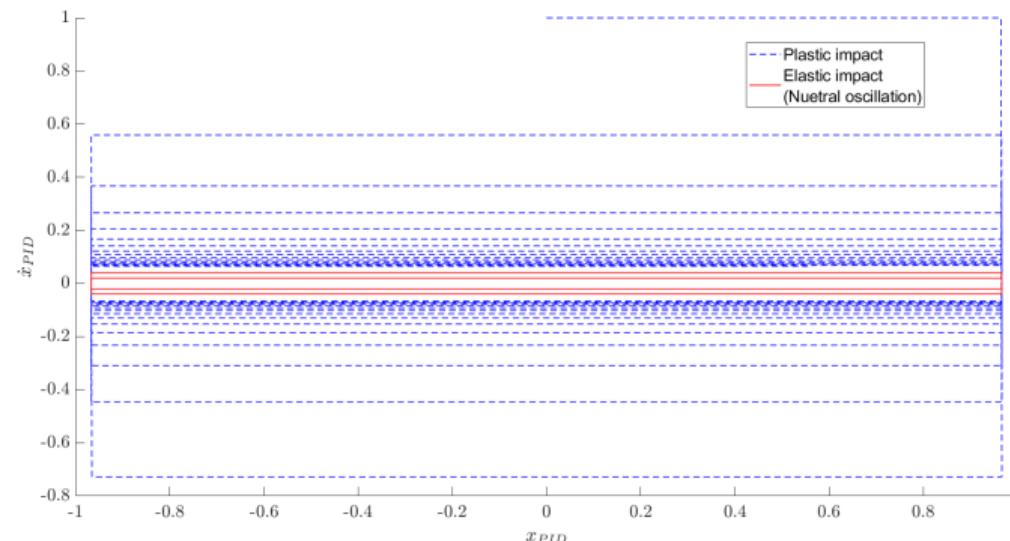
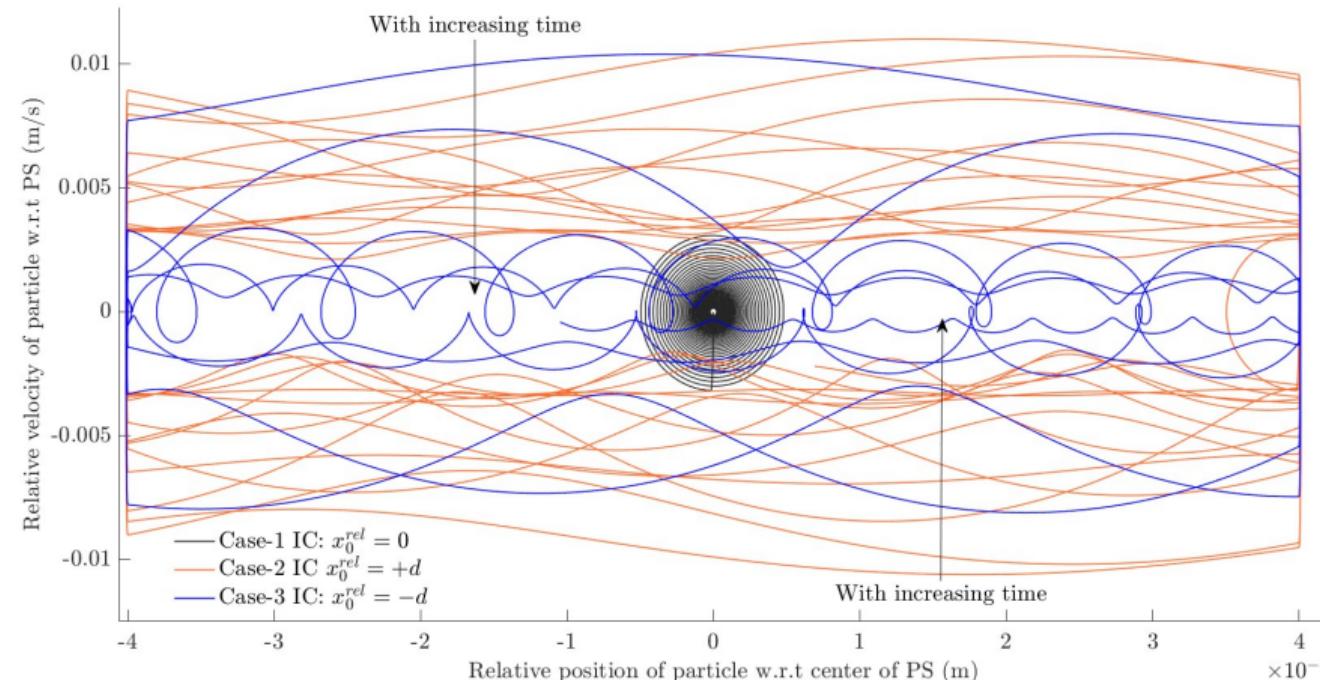
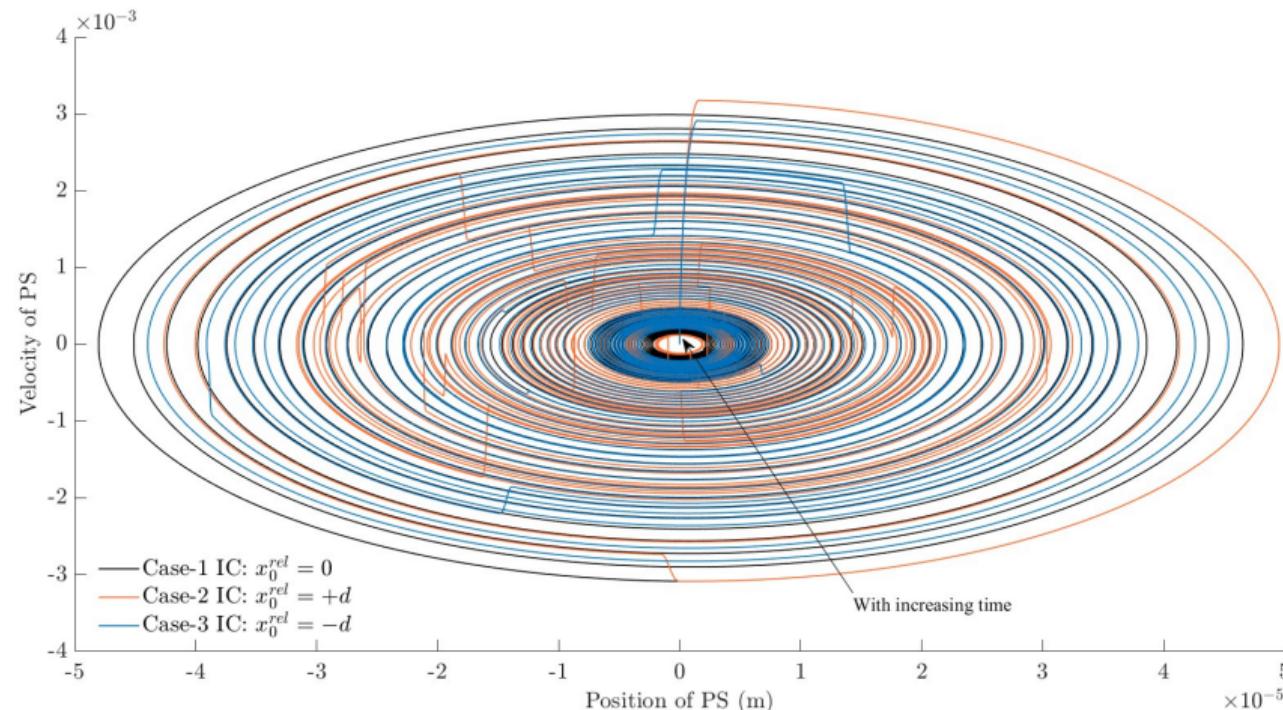


Figure: Phase portrait of the system; the PS is assumed to be fixed.

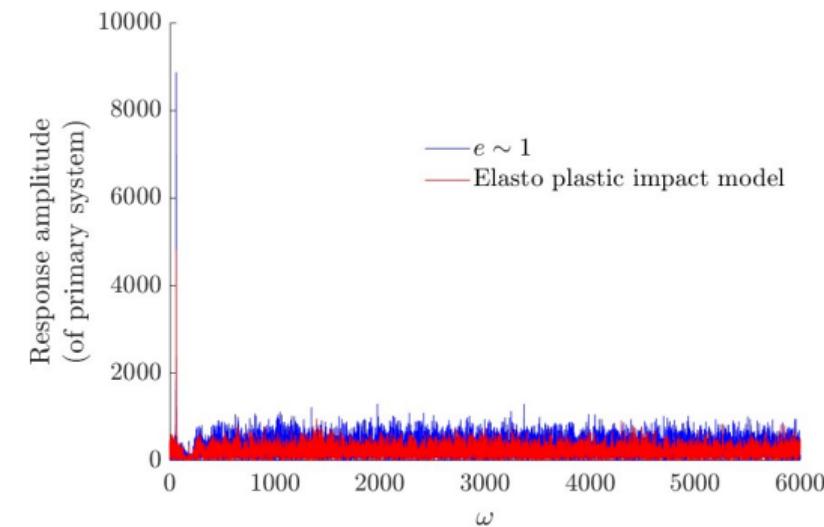
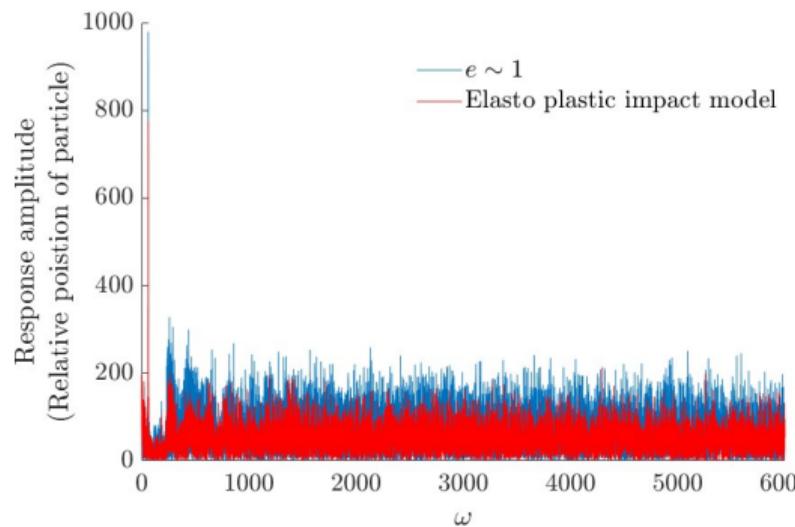
## Phase portrait $F_0 = 100\text{N}$ , $t_f = 0.001\text{s}$



## Phase portrait $F_0 = 100\text{N}$ , $t_f = 0.001\text{s}$



## Amplitude response in frequency domain



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## Energy dissipation characteristics

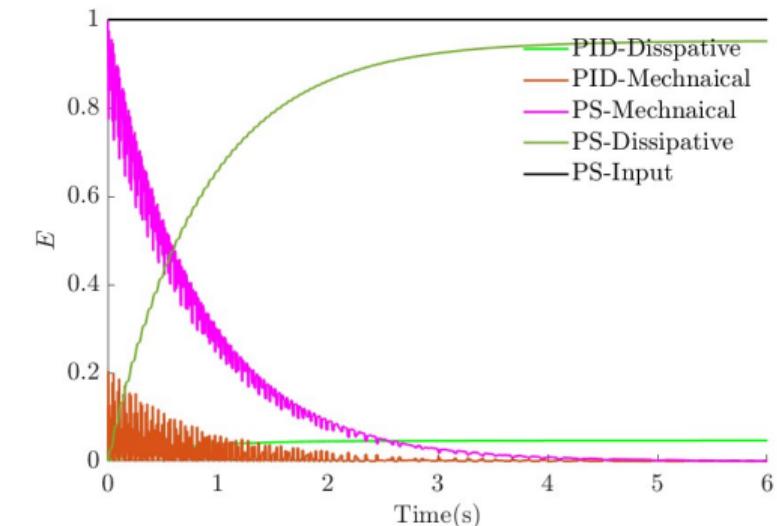
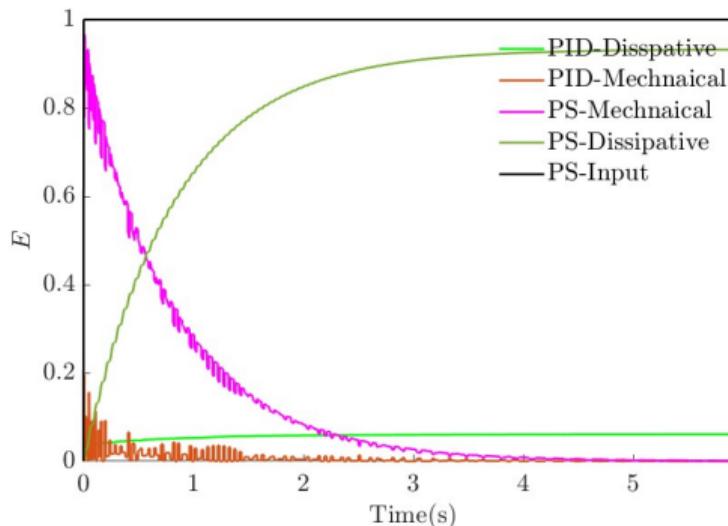


Figure: Energy dissipation characteristics (a) Elasto-plastic impact (b)  $e \sim 1$

## Energy dissipation characteristics (contd..)

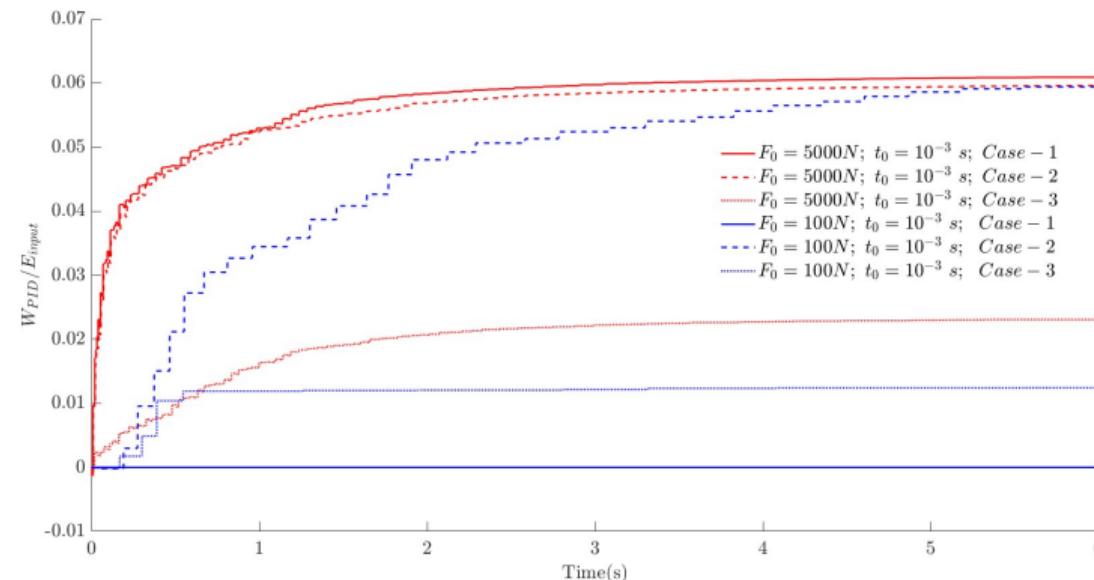
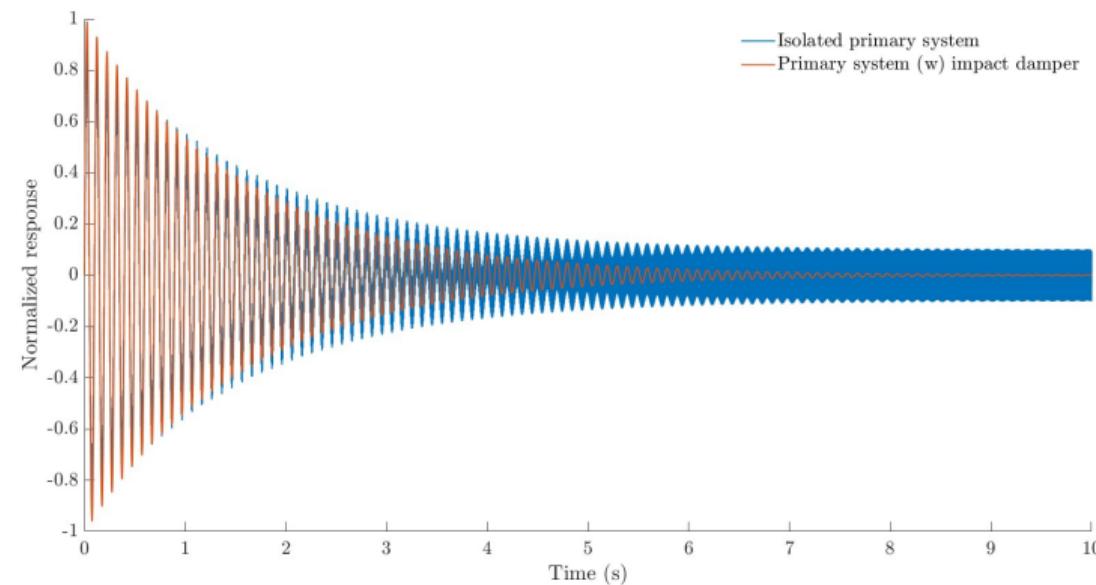


Figure: Sensitivity of energy dissipation characteristics on initial condition

## Energy dissipation characteristics (contd..)



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## Conclusion and perspectives

- ① The energy dissipation in the work of Li et al. 2024<sup>1</sup> is observed to be an underestimation as they assumed a constant coefficient of restitution.
- ② Similar to observations made in Li et al. 2024<sup>1</sup>, the energy dissipation is observed to be sensitive to the initial topology of the system. The chaotic behaviour is confirmed from the phase portraits.

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<sup>1</sup>Li, X., Mojahed, A., Wang, C. et al. Irreversible energy transfers in systems with particle impact dampers. Nonlinear Dynamics 112, 35–58 (2024)

# Thank You!