

ALA

QNo

Solutions

Mistakes

Q2) b)

$$a) p = \frac{(a - \frac{1}{n} \sum a_i)^T (b - \frac{1}{n} \sum b_i)}{\|a - \frac{1}{n} \sum a_i\| \|b - \frac{1}{n} \sum b_i\|}$$

I applied the concept of broadcasting which is not there in ~~numpy~~ numpy.

Q3)

~~Trace~~

$x v_i$ represents the the moment of vector x along the direction v_i

I have written it as the dot product vector vector multiplication

Q5)

$$\text{std}(c) = \frac{1}{2} \text{std}(a+b)$$

$$= \frac{1}{2} (0.159) \approx 0.08$$

I have calculated $\text{std}(a+b)$ using the formula

$$\text{std}(a+b) = \sqrt{a^2 + b^2 + 2 \cdot a \cdot b}$$

but not the other one i.e., $\text{std}(c) = \frac{1}{2} (a+b)$

Q2)

$$\text{Max}(a^T b, b^T c, a^T c)$$

I used the right approach, i.e., convert it to word vector but failed to apply the formula

$$\text{max}(a^T b, b^T c, a^T c)$$

Q3]

$$\|x\|^2 = \beta_1^2 a^T a + \beta_2^2 b^T b + \beta_3^2 c^T c$$

$$a^T a = \|a\|^2 = \|a_1\|^2 + \|a_2\|^2 + \|a_3\|^2$$

$$= 100 + 400 + 900 = 1400$$

$$\|b\|^2 = 25 + 49 + 64 = 138$$

$$\|c\|^2 = 4 + 16 + 25 = 50$$

$$\|x\| = \sqrt{\beta_1^2 \|a\|^2 + \beta_2^2 \|b\|^2 + \beta_3^2 \|c\|^2}$$

$$= \sqrt{(0.2)^2 \times 1400 + (0.3)^2 \times 138 + (0.5)^2 \times 50}$$

Q4]

$$x_4^T x_i$$

$$Q5) 1) q_k = \frac{a}{\|a\|} = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

I calculated

the $\|a\|^2$, $\|b\|^2$ & $\|c\|^2$

values correctly

but calculation

of $\|x\|^2$ I messed up. Did not use the β values in the formulaI have written this wrongly as $x^k x_i$

due to confusion in the concept and lack of time

$$q_b = b - (q_b^T b) q_a$$

$$= \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} - \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}^T \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} - \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$$

I had not read this particular slide and decided to skip it due to time constraint. ~~But~~ I tried to answer it in fluke but the answers ~~were~~ were not related to the concept.

$$2) q_c = (- (q_a^T c) q_a - (q_b^T c) q_b)$$

$$= \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} - \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}^T \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} -$$

$$\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}^T \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} - \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} - \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$$

$$= \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

3] Let q_i be a vector
then q_i

(10)

$$q_i = q_i - (q_1^T q_i) q_1 - (q_2^T q_i) q_2 - \dots - (q_{i-1}^T q_i) q_{i-1}$$

which is of the form

$$\bar{q}_i = q_i^T \begin{pmatrix} -B_1 \\ -B_2 \\ \vdots \\ -B_{i-1} \end{pmatrix} \begin{pmatrix} q_1 \\ q_2 \\ \vdots \\ q_{i-1} \end{pmatrix}$$

if $\bar{q}_i = 0$ then
 q_1, q_2, \dots, q_{i-1}
are linear
independent,

then q_i is ~~also~~ linearly
independent on q_1, q_2, \dots, q_{i-1}

\therefore If $q_i \neq 0$ it
is linear

dependent

4] No, changing the order
will represent 3 different
orthogonal components
will be generated because

choice of first vector
from the dist is AS 15, the
rest of them are normal to the
first selected vector