

1.  
a) Forecast Rain, i.e.,  
~~when she said rain and actual happened~~  
~~& when she said no rain & no rain happened~~

i.e.,  ~~$P(\text{Forecast}) = P(\text{forecast rain, and actual rain})$~~   
 ~~$+ P(\text{forecast no rain, and no rain})$~~   
 $P(\text{forecast rain}) = P(\text{forecast rain, and actual rain})$   
 $+ P(\text{forecast rain, and no rain})$   
 $= 0.4 + 0.2$   
 $= 0.6 \text{ or } 60\%$

- b) Mistake

$$P(\text{Mistake}) = P(\text{forecast rain, and no rain}) + P(\text{forecast no rain, and actual rain})$$
$$= 0.2 + 0.15$$
$$= 0.35$$

c)  $P(\text{actual rain} / \text{forecast rain}) = \frac{P(\text{forecast rain, and actual rain})}{P(\text{forecast rain})}$

$$= \frac{0.4}{0.6} = 0.667$$

$$= 66.7\%$$

$$c) P(\text{forecast rain} | \text{actual rain}) = \frac{P(\text{forecast rain, and actual rain})}{P(\text{actual rain})}$$

$$P(\text{actual rain}) = P(\text{forecast rain, and actual rain}) + P(\text{forecast rain, and no rain})$$

$$= 0.4 + 0.15 = 0.55$$

$$P(\text{forecast rain} | \text{actual rain}) = \frac{0.4}{0.55}$$

$$= 0.7272$$

$$= 72.72\%$$

$$2] a) P(\text{ectopic pregnancy} | \text{smoker}) = 2 \times$$

$$P(\text{ectopic pregnancy} | \text{non smoker})$$

$$b) P(\text{smoker}) = 32\% \text{ or } 0.32$$

$$c) P(\text{non smoker}) = 1 - P(\text{smoker})$$

$$= 1 - 0.32$$

$$= 0.68 \text{ or } 68\%$$



$$d) P(\text{smoker} | \text{ectopic pregnancies})$$

$$= \frac{P(\text{smoker and ectopic pregnancies})}{P(\text{ectopic pregnancies})}$$

$$= \frac{P(\text{smoker and ectopic pregnancies})}{P(\text{ectopic pregnancies})}$$

$$= \frac{P(\text{ectopic pregnancy and smoker})}{P(\text{ectopic pregnancy})}$$

$$= \frac{P(\text{ectopic pregnancy and smoker})}{P(\text{ectopic pregnancy and smoker}) + P(\text{ectopic pregnancy and non smoker})}$$

$$= \frac{P(\text{ep/smoker}) \cdot P(\text{smoker})}{P(\text{ep/smoker}) \cdot P(\text{smoker}) + P(\text{ep/non smoker}) \cdot P(\text{non smoker})}$$

$$= \frac{P(\text{ep/smoker}) \cdot P(\text{smoker})}{P(\text{ep/smoker}) \cdot P(\text{smoker}) + P(\text{ep/non smoker}) \cdot P(\text{non smoker})}$$

$$= \frac{P(\text{ep/smoker}) \cdot P(\text{smoker})}{P(\text{ep/smoker}) \cdot P(\text{smoker}) + P(\text{ep/non smoker}) \cdot P(\text{non smoker})} = A$$

$$= B$$

$$= \frac{2 \cdot P(\text{ep/non smoker}) \cdot A}{A + B}$$

$$\therefore \text{as we know } A = 2 \cdot B$$

$$= \frac{2B \cdot \cancel{\text{Smoker}}}{2B + 15}$$

$$= \frac{\cancel{2B} \cdot 2B \cdot P(\text{Smoker})}{2B \cdot P(\text{Smoker}) + B \cdot P(\text{non-smoker})}$$

$$= \frac{2B \cdot 0.32}{2B \cdot 0.32 + B \cdot 0.68}$$

$$= \frac{0.32 \times 2B}{B(2 \times 0.32 + 0.68)}$$

$$= \frac{0.64}{0.64 + 0.68} = \frac{0.64}{1.32}$$

$$= 0.4848 \text{ or } 48.48\%$$

$$3] \quad P(F) = 0.52 \quad P(CS) = 0.05$$

$$P(F \cap CS) = 0.02$$

$$a) \quad P(F|CS) = \frac{P(F \cap CS)}{P(CS)} = \frac{0.02}{0.05}$$

$$b) \quad P(CS|F) = \frac{P(CS \cap F)}{P(F)} = \frac{0.02}{0.52}$$

$$4] \quad P(\text{str}) = 0.002 \quad P(\text{Eng}) = 0.002$$

$$P(CS) = 0.01$$

$$P(HE) = 0.003$$

$$P(\text{Crash}|\text{str}) = 0.25$$

$$P(\text{Crash}|\text{Eng}) = 0.3$$

$$P(\text{Crash}|CS) = 0.9$$

$$P(\text{Crash}|HE) = 0.1$$



$$P(CS | \text{Crash}) = \frac{P(\text{Crash} | CS) \times P(CS)}{P(\text{Crash})}$$

$$P(\text{Crash}) = P(\text{Crash} \cap CS) + P(\text{Crash} \cap \text{str}) + P(\text{Crash} \cap \text{Eng}) + P(\text{Crash} \cap \text{HE})$$

$$= P(\text{Crash} | CS) \cdot P(CS) + P(\text{Crash} | \text{str}) \cdot P(\text{str}) + P(\text{Crash} | \text{Eng}) \cdot P(\text{Eng}) + P(\text{Crash} | \text{HE}) \cdot P(\text{HE})$$

$$= 0.9 \times 0.01 + 0.25 \times 0.0001 + 0.3 \times 0.0001$$

$$P(CS | \text{Crash}) = \frac{0.9 \times 0.001}{0.0155}$$

$$5) \quad P(L_1) = 0.8$$

$$P(L_2) = 0.2$$

$$P(WD | \text{No window}) = 0.2 \Rightarrow P(WD | L_1)$$

$$P(WD | \text{window}) = 0.9 = P(WD | L_2)$$

$$P(L_1 | WD) = \frac{P(L_1 \cap WD)}{P(WD)}$$

$$= \frac{P(WD | L_1) \cdot P(L_1)}{P(WD)}$$

$$= \frac{P(WD | L_1) \cdot P(L_1)}{P(WD | \text{No window}) \cdot P(\text{No window}) + P(WD | \text{window}) \cdot P(\text{window})}$$

$$= \frac{0.2 \times 0.8}{0.2 \times 0.8 + 0.9 \times 0.2}$$

$$P(L_2 | WD) = \frac{P(WD | L_2) \times P(L_2)}{P(WD)}$$

$$= \frac{0.9 \times 0.2}{0.9 \times 0.2 + 0.2 \times 0.8}$$

$$= 0.5294 = 52.94\%$$



6) a) Probability that random person will be able to donate without any knowledge about donors blood type

From above chart,

following is possible only to  $O^-$

Probability that random person can donate to another person without any information about blood types of both = Population percentage of  $O^-$

$$= 6.6 \% \text{ or } 0.066$$

b) According to above information Blood transfusion policy should be that

They should collect and maintain  $O^-$  blood more as it can be given to any person

c) Perform blood typing on all the three soldiers, if the wounded soldier's blood type matches with any one of other two ~~then~~ ~~do~~ According to chart then do blood transfusion otherwise wait till the required

blood type is arranged by keeping the wounded soldier alive by doing other activities

1.