

Cloud Computing

Spring 2017

Project 8\*

Harp Mini-Batch Kmeans

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\* *NOTE: We are using the free one time late submission for this project*

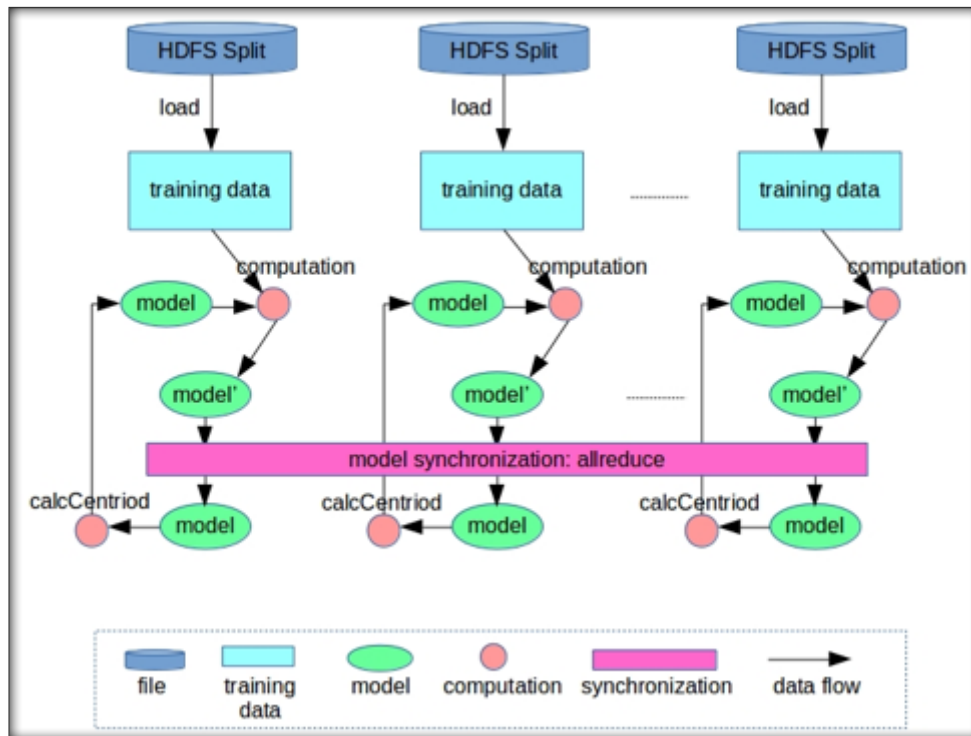
**Goal:** The goal for this project is to implement Harp[1] Mini-Batch Kmeans (mbkmeans) from scratch.

## Working Of the Program

The K-Means algorithm reiterates the following set of steps until there is no change in the partition assignments. In that, it has clarified which data point is assigned to which partition.

1. Choose K points as the initial set of centroids.
2. Assign each data point in the data set to the closest centroid (this is done by calculating the distance between the data point and each centroid).
3. Calculate the new centroids based on the clusters that were generated in step 2. Normally this is done by calculating the mean of each cluster.
4. Repeat step 2 and 3 until data points do not change cluster assignments, which means that their centroids are set. [1]

## DATAFLOW



The program includes the following tasks:

1. The Main Method - Configures and runs the job iteratively.
2. The mapCollective function

Reads data from context and then call runKmeans function to actually run kmeans Mapper task

```
protected void mapCollective( KeyValReader reader, Context context) throws IOException, InterruptedException
```

3. The runKmeans function – We have used the AllReduce collective communication to do synchronization.

```
private void runKmeans(List<String> fileNames, Configuration conf, Context context) throws IOException
```

4. Computing local centroids

```
private void computation(Table<DoubleArray> cenTable, Table<DoubleArray> previousCenTable, ArrayList<DoubleArray> dataPoints)
```

5. Calculate new centroids

This function calculates the new centroids and prints the same.

```
private void calculateCentroids ( Table<DoubleArray> cenTable, Table<DoubleArray> previouscentable)
```

## Algorithm:

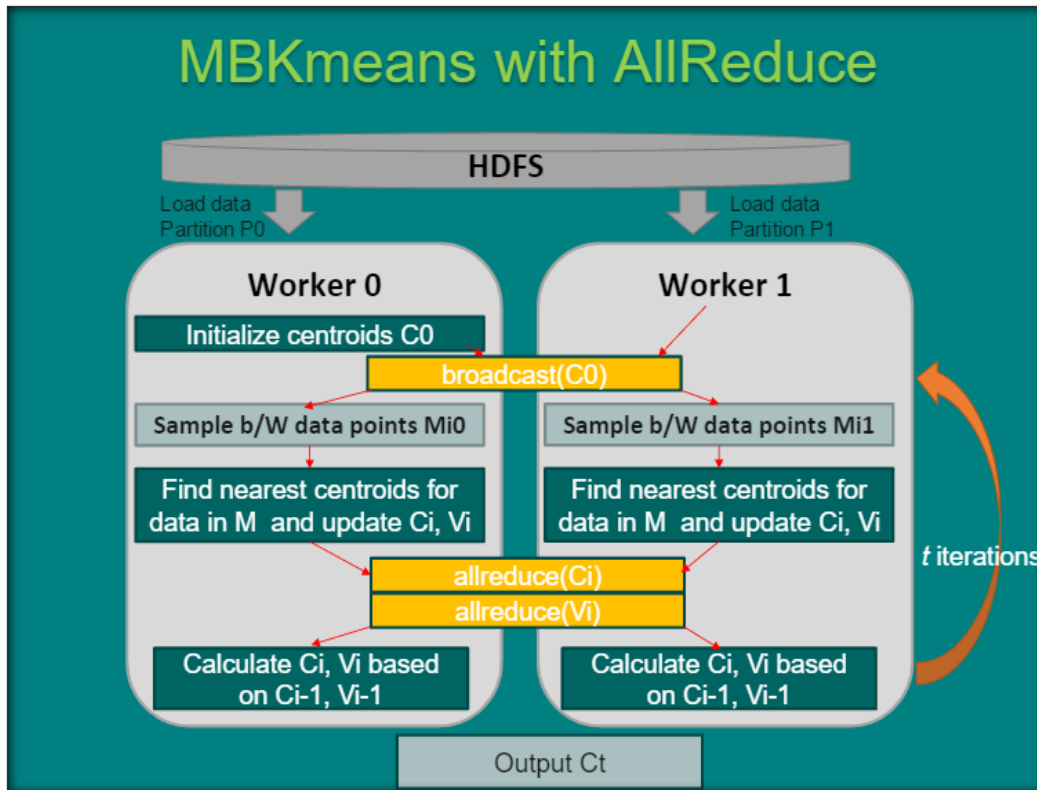
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**Algorithm 1** Mini-batch  $k$ -Means.

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```
1: Given:  $k$ , mini-batch size  $b$ , iterations  $t$ , data set  $X$ 
2: Initialize each  $\mathbf{c} \in C$  with an  $\mathbf{x}$  picked randomly from  $X$ 
3:  $\mathbf{v} \leftarrow 0$ 
4: for  $i = 1$  to  $t$  do
5:    $M \leftarrow b$  examples picked randomly from  $X$ 
6:   for  $\mathbf{x} \in M$  do
7:      $\mathbf{d}[\mathbf{x}] \leftarrow f(C, \mathbf{x})$  // Cache the center nearest to  $\mathbf{x}$ 
8:   end for
9:   for  $\mathbf{x} \in M$  do
10:     $\mathbf{c} \leftarrow \mathbf{d}[\mathbf{x}]$  // Get cached center for this  $\mathbf{x}$ 
11:     $\mathbf{v}[\mathbf{c}] \leftarrow \mathbf{v}[\mathbf{c}] + 1$  // Update per-center counts
12:     $\eta \leftarrow \frac{1}{\mathbf{v}[\mathbf{c}]}$  // Get per-center learning rate
13:     $\mathbf{c} \leftarrow (1 - \eta)\mathbf{c} + \eta\mathbf{x}$  // Take gradient step
14:   end for
15: end for
```

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### Compiling the code:

```
cd $HARP_ROOT_DIR
mvn clean package
cd $HARP_ROOT_DIR/harp-tutorial-app
cp target/harp-tutorial-app-1.0-SNAPSHOT.jar $HADOOP_HOME
cd $HADOOP_HOME
```

### Run Harp K-Means:

```
hadoop jar harp-tutorial-app-1.0-SNAPSHOT.jar edu.iu.mbkmeans.common.MBKmeansMapCollective <numOfDataPoints> <num of Centroids> <size of vector> <number of map tasks> <number of iteration> <workDir> <localDir> <communication operation>
```

Here,

**<workDir>**: This is the root directory running in HDFS.

**<localDir>**: This argument is the local directory where mbkmeans stores the data points that it generates.

**<communication operation>**: set this to "allreduce"

## **Output and Experimentations:**

Below are the screen shots of our output. For **Bonus Credits**, we experimented with the input size, dimensions or the vector size and the number of Centroids.

### **Example command to Run MBKmeans:**

```
hadoop jar harp-tutorial-app-1.0-SNAPSHOT.jar  
edu.iu.mbkmeans.common.MBKmeansMapCollective 100 5 10 100 2 10  
/mbkmeans /tmp/minibatchkmeans allreduce
```

### **1. VARYING THE INPUT SIZE:**

1. Data-Points: 1000

```
6.124391173137189 2.75258105173362 2.2004755465820667  
5.791558346375341 7.294164964669375 4.89699489040294  
7.280705874781242 5.255530801554653 2.566855808559354  
7.184701954168311  
5.649812870845929 3.2437651741349436 0.12365797832135983  
8.892137111903772 7.504458300973682 0.8292970390751153  
3.6010701209646276 0.5518463889241765 2.0424928400030975  
1.0629250989725858  
7.275432835151969 7.623022383457695 1.314759526479392  
0.9022649616494138 8.868327695622293 3.7516639368386775  
0.4259342237130659 3.3299462596796325 6.4160097693011044  
4.685119088767387  
1.6652795569467416 2.683718181316536 4.8745677145556225  
7.899908148146702 4.5329434386872265 1.621618714522448  
0.17352099335004367 2.3083710319427753 5.824711801342804  
3.8582579669548656  
3.2840706194708567 7.028811258997408 3.9478771626048594  
2.8336513606954172 4.534251146087951 8.13546700855315  
9.463163202662036 2.813931298545592 8.88173153235201  
7.548762197351985  
9.482399969386124 5.573657863216964 6.146037000856523  
8.782945543829811 6.998919053542179 2.772337112469898
```

6.305478583931561 0.13735570368125338 7.4873976260873345  
1.4131485129001342  
8.880090250547969 7.099200630407887 4.182147104486775  
7.3597717739172435 7.15039111854776 2.2198695512872035  
0.32761239137783393 9.787595550106632 2.502805732468343  
2.5334483747842573  
1.3921032254608257 7.658478575025294 1.5460879803366578  
1.7052368721035316 2.7455589442070294 7.8336305875493935  
8.809117493531106 6.529719267293171 8.624398832716428  
3.2770599851488225  
0.8089421158682764 5.1415721374212096 6.341285867010578  
8.952439955219061 3.0689655805335816 7.359935612247467  
5.644895992399404 2.4791203576045504 0.2706895375066498  
5.955317724888321  
6.894543174709414 6.388418016309765 1.1384354344405234  
1.3101395035991914 3.2867900402647443 8.909195807632509  
3.8849901492018866 0.9380686526547366 1.755921335391294  
0.6121409244582887

```
VirtualBox: ~/Documents/hadoop-2.6.0
Total megabyte-seconds taken by all map tasks=35914752
Map-Reduce Framework
  Map input records=2
  Map output records=1
  Input split bytes=176
  Spilled Records=0
  Failed Shuffles=0
  Merged Map outputs=0
  GC time elapsed (ms)=208
  CPU time spent (ms)=2490
  Physical memory (bytes) snapshot=356237312
  Virtual memory (bytes) snapshot=3885727744
  Total committed heap usage (bytes)=519045120
File Input Format Counters
  Bytes Read=0
File Output Format Counters
  Bytes Written=1829
end Job#0 19:05:27.199
| Job#0 Finished in 40254 milliseconds |
Total Mini-Batch K-means Execution Time: 40254
Harp Mini-Batch Kmeans Completed
cc@cc-VirtualBox:~/Documents/hadoop-2.6.0$ hdfs dfs -cat /mbkmeans/centroids/*
6.124391173137189 2.75258105173362 2.2004755465820667 5.791558346375341 7.294164964669375 4.89699489040294 7.280705874781242 5.255530801554653 2.566855
808559354 7.184701954168311
5.649812870845929 3.2437651741349436 0.12365797832135983 8.892137111903772 7.504458300973682 0.8292970390751153 3.6010701209646276 0.5518463889241765 2
.0424928400030975 1.0629250989725858
7.275432835151969 7.623022383457695 1.314759526479392 0.9022649616494138 8.868327695622293 3.7516639368386775 0.4259342237130659 3.3299462596796325 6.4
160097693011044 4.685119088767387
1.6652795569467416 2.683718181316536 4.8745677145556225 7.899908148146702 4.5329434386872265 1.621618714522448 0.17352099335004367 2.3083710319427753 5
.824711801342804 3.8582579669548656
3.2840706194708567 7.028811258997408 3.9478771626048594 2.8336513606954172 4.534251146087951 8.13546700855315 9.463163202662036 2.813931298545592 8.881
73153235201 7.548762197351985
9.482399969386124 5.573657863216964 6.146037000856523 8.782945543829811 6.998919053542179 2.772337112469898 6.305478583931561 0.13735570368125338 7.487
3976260873345 1.4131485129001342
8.880090250547969 7.099200630407887 4.182147104486775 7.3597717739172435 7.15039111854776 2.2198695512872035 0.32761239137783393 9.787595550106632 2.50
2805732468343 2.5334483747842573
1.3921032254608257 7.658478575025294 1.5460879803366578 1.7052368721035316 2.7455589442070294 7.8336305875493935 8.809117493531106 6.529719267293171 8.
624398832716428 3.2770599851488225
0.8089421158682764 5.1415721374212096 6.341285867010578 8.952439955219061 3.0689655805335816 7.359935612247467 5.644895992399404 2.4791203576045504 0.2
706895375066498 5.955317724888321
6.894543174709414 6.388418016309765 1.1384354344405234 1.3101395035991914 3.2867900402647443 8.909195807632509 3.8849901492018866 0.9380686526547366 1.
755921335391294 0.6121409244582887
```

## 2. Input Size: 10,000

```
Harp Mini-Batch Kmeans Completed
cc@cc-VirtualBox:~/Documents/hadoop-2.6.0$ hdfs dfs -cat /mbkmeans/centroids/*
4.143574220383406 8.610731260783353 2.6652193632989265 4.97926360317535 1.251522862751846 0.5373793205447008 1.9902743254682231 0.8423113063584642 3.92
23563921571314 3.5188083855507104
3.1596980426467525 4.849131060024971 1.0656607339513402 3.6880788547361822 2.0797798831192593 3.517698388308622 7.229264862281316 0.6551520123664722 4.
250686322400288 4.544438940292568
4.619092816282063 7.286153145128676 8.376931641027308 5.583357957548294 1.356359299212847 2.006371914247169 5.73682964268194 0.7114138612547105 3.57251
42281884747 8.70054471563247
6.3146516028376105 9.502315009438156 8.952101953107558 5.30936335310799 0.36522652363712216 3.562560157418452 7.1559716684248444 8.559030607507921 4.55
9239972717421 0.6276844741090171
8.192036534976666 8.911088808999866 5.148501228967567 6.873313378342537 3.248050029691499 6.782626432003854 6.693963044344588 3.96476611188909 3.760625
206843841 8.362367119224004
3.8152979321828253 8.550592392498718 3.566999711174815 6.936028448700931 5.149345352812066 8.399568393111682 5.870803466351347 3.5347353288586003 3.245
7621760490363 1.187312390536004
1.4503616753509896 8.933159362250224 1.481728545792661 9.057828517169918 7.047819899074035 7.549444568171796 9.243566810293437 4.516924247807394 3.1996
592525955836 2.6368787990784712
9.601658871514674 0.9585853321252191 8.903917527251561 1.3076496705202056 9.496051550804959 4.1820393357722345 6.466713664453106 7.391921698058669 1.05
36667084682116 9.626371341160699
3.630425590842764 9.910861222281858 4.074034462976492 3.7312036775118465 1.6581487673357276 5.030124757153612 3.949000559334018 6.8260861451216375 7.4
33818266095173 9.760715809615139
6.322857583389178 9.257886124907003 4.8346477244524575 6.387009310931624 9.652876898594084 2.084612366533597 5.642307443900022 7.627131886993896 9.4962
31315477825 8.595737374663337
```

4.143574220383406 8.610731260783353 2.6652193632989265  
4.97926360317535 1.251522862751846 0.5373793205447008  
1.9902743254682231 0.8423113063584642 3.9223563921571314  
3.5188083855507104  
3.1596980426467525 4.849131060024971 1.0656607339513402  
3.6880788547361822 2.0797798831192593 3.517698388308622  
7.229264862281316 0.6551520123664722 4.250686322400288  
4.544438940292568  
4.619092816282063 7.286153145128676 8.376931641027308  
5.583357957548294 1.356359299212847 2.006371914247169  
5.73682964268194 0.7114138612547105 3.5725142281884747  
8.70054471563247  
6.3146516028376105 9.502315009438156 8.952101953107558  
5.30936335310799 0.36522652363712216 3.562560157418452  
7.1559716684248444 8.559030607507921 4.559239972717421  
0.6276844741090171  
8.192036534976666 8.911088808999866 5.148501228967567  
6.873313378342537 3.248050029691499 6.782626432003854  
6.693963044344588 3.96476611188909 3.760625206843841  
8.362367119224004  
3.8152979321828253 8.550592392498718 3.566999711174815  
6.936028448700931 5.149345352812066 8.399568393111682  
5.870803466351347 3.5347353288586003 3.2457621760490363



1.187312390536004  
1.4503616753509896 8.933159362250224 1.481728545792661  
9.057828517169918 7.047819899074035 7.549444568171796  
9.243566810293437 4.516924247807394 3.1996592525955836  
2.6368787990784712  
9.601658871514674 0.9585853321252191 8.903917527251561  
1.3076496705202056 9.496051550804959 4.1820393357722345  
6.466713664453106 7.391921698058669 1.0536667084682116  
9.626371341160699  
3.630425590842764 9.910861222281858 4.074034462976492  
3.7312036775118465 1.6581487673357276 5.030124757153612  
3.9490005559334818 6.8260861451216375 7.433818266095173  
9.760715809615139  
6.322857583389178 9.257886124907003 4.8346477244524575  
6.387009310931624 9.652876898594084 2.084612366533597  
5.642307443900022 7.627131886993896 9.496231315477825  
8.595737374663337

### 3. Input Size: 100000

```
Total Mini-Batch K-means Execution Time: 33369
Harp Mini-Batch Kmeans Completed
cc@cc-VirtualBox:~/Documents/hadoop-2.6.0$ hdfs dfs -cat /mbkmeans/centroids/*
6.000799340689287 2.379972125239851 0.7460327832177449 1.5164982148108908 5.357883291504578 6.805983242054731 1.1996669265044302 8.214491739984311 0.75
01252792324453 6.471380435529658
8.610714380492025 0.7533278751364636 1.9239927280989855 4.139746924462495 6.215410456030649 4.616577256238705 7.355740758908224 4.781621712201555 7.827
246221265231 3.1881090347235364
8.546623393584587 1.690352916524428 0.9662822095568013 6.743831279257501 7.388299109537321 4.660532682264452 6.759365394377312 5.909117814793371 4.5784
69486095184 7.039615789544486
6.881335686587291 9.346628594034131 2.037494699825919 5.387161727709744 9.809252143661475 0.6443116877320054 3.8099385935855787 1.4624634735840547 2.22
61262812735403 8.640953927283476
8.030687805988649 1.3101530758773738 6.537603953909686 8.756722645749747 7.1935033427169435 0.32470723666721435 2.154486583724633 0.28872014330045603 5
.18056085172047 6.3486018358062015
6.445939731669293 6.086653363984011 7.294737847474684 5.095187533243866 1.0826885619505777 6.541293828892767 3.882114450219867 3.4861975360212174 0.866
4492264089274 9.398486497724862
9.040351281149663 6.855114886105796 5.081307490579606 0.5540420019722836 3.3793160375554434 5.391464766754691 5.904697212403541 6.689921761043868 3.833
5307835548074 3.687416211518615
4.480096122244516 8.379712225526365 4.121715414037029 4.79691582533896 2.8804985454522303 2.121450851999811 6.606906846671787 6.828895395457584 9.38118
6873505902 1.6484566578039261
0.031337524191746846 5.7699265754711835 5.212272795214038 2.823885691265734 7.8834534651056245 2.968027396901196 3.2759289565853678 6.442316865291673 9
.000167462558423 9.508147811384537
3.1901944927751735 9.341750113856659 5.415633586838695 2.5711922273789387 2.460678005259128 6.371975235449608 2.438537812383376 0.7922669884106792 0.58
34488118039205 3.970348171122493
```

6.000799340689287 2.379972125239851 0.7460327832177449  
1.5164982148108908 5.357883291504578 6.805983242054731  
1.1996669265044302 8.214491739984311 0.7501252792324453  
6.471380435529658  
8.610714380492025 0.7533278751364636 1.9239927280989855  
4.139746924462495 6.215410456030649 4.616577256238705  
7.355740758908224 4.781621712201555 7.827246221265231



3.1881090347235364  
8.546623393584587 1.690352916524428 0.9662822095568013  
6.743831279257501 7.388299109537321 4.660532682264452  
6.759365394377312 5.909117814793371 4.578469486095184  
7.039615789544486  
6.881335686587291 9.346628594034131 2.037494699825919  
5.387161727709744 9.809252143661475 0.6443116877320054  
3.8099385935855787 1.4624634735840547 2.2261262812735403  
8.640953927283476  
8.030687805988649 1.3101530758773738 6.537603953909686  
8.756722645749747 7.1935033427169435 0.32470723666721435  
2.154486583724633 0.28872014330045603 5.18056085172047  
6.3486018358062015  
6.445939731669293 6.086653363984011 7.294737847474684  
5.095187533243866 1.0826885619505777 6.541293828892767  
3.882114450219867 3.4861975360212174 0.8664492264089274  
9.398486497724862  
9.040351281149663 6.855114886105796 5.081307490579606  
0.5540420019722836 3.3793160375554434 5.391464766754691  
5.904697212403541 8.689921761043868 3.8335307835548074  
3.687416211518615  
4.480096122244516 8.379712225526365 4.121715414037029  
4.79691582533896 2.8804985454522303 2.121450851999811  
6.606906846671787 6.828895395457584 9.381186873505902  
1.6484566578039261  
0.031337524191746846 5.7699265754711835 5.212272795214838  
2.823885691265734 7.8834534651056245 2.968027396901196  
3.2759289565853678 6.442316865291673 9.000167462558423  
9.508147811384537  
3.1901944927751735 9.341750113856659 5.415633586838695  
2.5711922273789387 2.460678005259128 6.371975235449608  
2.438537812383376 0.7922669884106792 0.5834488118039205  
3.970348171122493

#### 4. Input Size= 1000000

0.2261403562707387 1.8332989625414586 3.8188590061971883 8.86862232408929 7.484332541749809 2.245451439018098 8.082753138810098 6.633151342058072 6.826392036876242 3.7165133001214965  
1.4720812372728875 1.3122020447868166 7.649703864140792 3.3844855314543842 7.713783424086809 7.55818580467411 5.630729546656465 1.0920677791686495 9.865565373372823 3.913242106779885  
9.815686409393328 7.919896185256289 8.268243706145235 7.689258892162122 4.7512893351573195 6.48996151892908 6.032207106686562 8.25885187043156 7.82187729602508 6.284144300028768  
9.807316932596654 0.7180597730770466 7.203389533955056 2.857564901994658 0.23597050617346738 5.1725208979880355 6.401281108383362 3.273713897248286 3.4519336571491577 3.0024201204593637  
7.208640700164398 1.348095802516971 2.262944748659599 0.37750620657764133 4.1023733125787 5.35937880590153 3.242981435193241 1.0219965798024588 9.589485888916442 7.7718169591862285  
3.8604706276806966 4.770202018095839 1.822134034994044 1.2099698956688731 1.981615302139711 5.807219481305685 2.9192355705452124 7.4365144626880095 8.613401135777554 4.655057833708217  
8.864099954821846 6.406206645788121 3.5887343193949195 0.9430725251844574 9.591655792917326 0.6038212389056608 3.0465588140752944 9.792609058828598 0.955057836235792 5.8211538947547625  
7.022684292728108 3.249261649550684 8.474177414323671 3.287948701330974 5.242451706161311 9.612176693078498 6.997574552979601 9.643866590418762 9.294252616491356 7.738339821291661  
3.308783540768808 0.6233862071200014 9.763309790529494 0.44080649506699765 4.383018990134772 1.5227870364185891 7.618013634813377 0.9533479711174697 2.5246418754899382 2.528134843017922  
0.16650678334354296 9.100002422863676 4.0948195905109985 9.805453952739677 3.2390905477334697 9.286534268350833 8.626541424221145 3.889034207014314 2.902426876107025 0.7218228973585428

0.2261403562707387 1.8332989625414586 3.8188590061971883  
8.86862232408929 7.484332541749809 2.245451439018098  
8.082753138810098 6.633151342058072 6.826392036876242  
3.7165133001214965  
1.4720812372728875 1.3122020447868166 7.649703864140792  
3.3844855314543842 7.713783424086809 7.55818580467411  
5.630729546656465 1.0920677791686495 9.865565373372823  
3.913242106779885  
9.815686409393328 7.919896185256289 8.268243706145235  
7.689258892162122 4.7512893351573195 6.48996151892908  
6.032207106686562 8.25885187043156 7.821877729602508  
6.284144300028768  
9.807316932596654 0.7180597730770466 7.203389533955056  
2.857564901994658 0.23597050617346738 5.1725208979880355  
6.401281108383362 3.273713897248286 3.4519336571491577  
3.0024201204593637  
7.208640700164398 1.348095802516971 2.262944748659599  
0.37750620657764133 4.1023733125787 5.35937880590153  
3.242981435193241 1.0219965798024588 9.589485888916442  
7.7718169591862285  
3.8604706276806966 4.770202018095839 1.822134034994044  
1.2099698956688731 1.981615302139711 5.807219481305685  
2.9192355705452124 7.4365144626880095 8.613401135777554

4.655057833708217  
8.864099954821846 6.406206645788121 3.5887343193949195  
0.9430725251844574 9.591655792917326 0.6038212389056608  
3.0465588140752944 9.792609058828598 0.9355057836235792  
5.8211538947547625  
7.022684292728108 3.249261649550684 8.474177414323671  
3.287948701330974 5.242451706161311 9.612176693078498  
6.997574552979601 9.643866590418762 9.294252616491356  
7.738339821291661  
8.308783540768808 0.6233862071200014 9.763309790529494  
0.44080649506699765 4.383018990134772 1.5227870364185891  
7.618013634813377 0.9533479711174697 2.5246418754899382  
2.528134843017922  
0.16650678334354296 9.100002422863676 4.0948195905109985  
9.805453952739677 3.2390905477334697 9.286534268350833  
8.626541424221145 3.889034207014314 2.902426876107025  
0.7218228973585428

## ***2. VARYING THE VECTOR SIZE OR DIMENSION***

dimension/vector size=2

datapoints=10,000

### ***OUTPUT:***

8.392628304575984 9.471987035173404  
3.1224825151944033 6.375810627068318  
2.4895374825214214 9.280271498366771  
1.69386427200945 9.901851428995727  
5.816333942252282 6.326596059490721  
3.0684838481646217 5.054957750535985  
5.300759279064402 0.05626807739536388  
0.10043666904612003 6.760730164464502  
7.324669358508197 9.09265121200024  
1.4727927792438955 6.565293806149462

## ***3. VARYING THE NUMBER OF CENTROIDS***

NUMBER OF CENTROIDS =5

INPUT\_SIZE=100

```
7.401696309505682 8.78299579069802 7.176346064804422 8.364304193028051 4.167538487326659 9.368255139616009 5.354386491259746 5.313458705799824 2.189257
008612262 7.944924142555387
9.4438749957018 0.7541741779297373 4.808389826254135 2.5831916311926397 2.8425946995718943 8.149091427169955 8.600629819891948 1.8430543401615196 8.095
32859583909 7.617662196272272
0.2925158532356864 9.628622455083812 0.4919197191761471 6.643466114103006 8.62907575390577 4.330916042617533 0.49705408008891117 7.3162618044224095 1.3
196791714599176 1.4025273471781385
2.0970262589609314 2.3429701872495654 1.1835014328573257 2.892281561162524 9.549152689380174 4.102796750510123 4.922635362653475 9.665303457298267 0.73
23706675474106 5.875212870577807
2.570034151093105 2.04365568553895 1.3229704023564048 2.035539195766373 5.5911035773255 2.4249829577858986 0.35728144331031664 4.49138059977419 6.86190
57477266026 9.071362552685018
```

## ***OUTPUT:***

```
7.401696309505682 8.78299579069802 7.176346064804422 8.364304193028051
4.167538487326659 9.368255139616009 5.354386491259746
5.313458705799824 2.189257008612262 7.944924142555387
9.4438749957018 0.7541741779297373 4.808389826254135
2.5831916311926397 2.8425946995718943 8.149091427169955
8.600629819891948 1.8430543401615196 8.09532859583909
7.617662196272272
0.2925158532356864 9.628622455083812 0.4919197191761471
6.643466114103006 8.62907575390577 4.330916042617533
0.49705408008891117 7.3162618044224095 1.3196791714599176
1.4025273471781385
2.0970262589609314 2.3429701872495654 1.1835014328573257
2.892281561162524 9.549152689380174 4.102796750510123
4.922635362653475 9.665303457298267 0.7323706675474106
5.875212870577807
2.570034151093105 2.04365568553895 1.3229704023564048
2.035539195766373 5.5911035773255 2.4249829577858986
0.35728144331031664 4.49138059977419 6.8619057477266026
9.071362552685018
```

## **REFERENCES:**

[1] <https://dsc-spidal.github.io/harp/docs/examples/kmeans/>