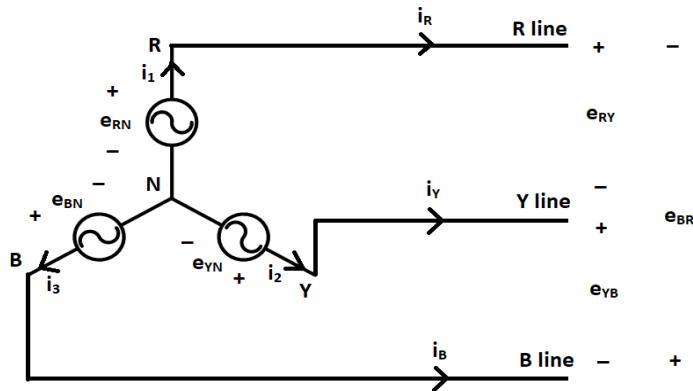


## NOTES-Class 41

### Balanced Star (or) WYE Connected Three Phase System

To make a star connected three phase system, similar terminals such as R', Y' and B' are connected together to make 'Neutral' point (N) of the three phase system. And lines are run from the other three terminals i.e., R, Y and B.



#### Phase Voltage:

The voltage across the terminals of a phase is called the Phase Voltage.

Here,  $e_{RN}$ ,  $e_{YN}$  &  $e_{BN}$  represent phase voltages.

#### Line Voltage:

The voltage across any two lines is called the Line Voltage. Here,  $e_{RY}$ ,  $e_{YB}$  &  $e_{BR}$  represent Line (or) Line to line voltages.

#### Phase Current:

The current flowing through a phase is called the Phase Current. Here,  $i_1$ ,  $i_2$  &  $i_3$  represent phase currents.

#### Line Current:

The current flowing through a line is called the Line Current. Here,  $i_R$ ,  $i_Y$  &  $i_B$  represent line currents.

### **Relation between Line & Phase currents – Balanced Star System:**

In a balanced star connected three phase system, it can be observed that

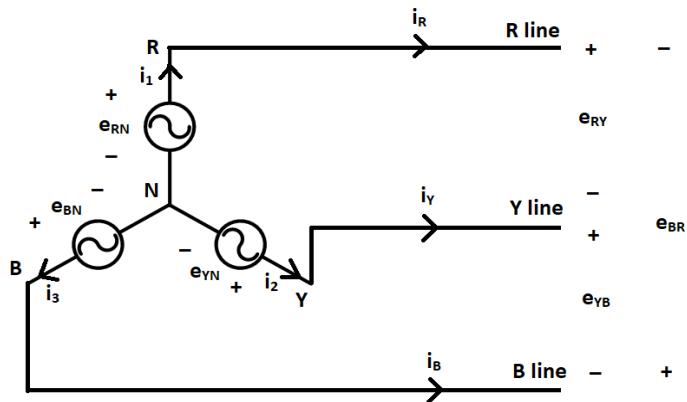
Line current = Phase current

$$\text{i.e., } i_1 = i_R$$

$$i_2 = i_Y$$

$$i_3 = i_B$$

### **Relation between Line & Phase voltages – Balanced Star System:**



By KVL in the path RYNR,  $-e_{RY} - e_{YN} + e_{RN} = 0$

Hence,  $e_{RY} = e_{RN} - e_{YN}$

$$\overline{E_{RY}} = \overline{E_{RN}} - \overline{E_{YN}}$$

$$\overline{E_{RN}} = \frac{E_m}{\sqrt{2}} \angle 0^\circ = E_{ph} \angle 0^\circ$$

where,  $E_{ph}$  is the RMS value of phase voltage.

$$\overline{E_{YN}} = \frac{E_m}{\sqrt{2}} \angle -120^\circ = E_{ph} \angle -120^\circ$$

$$\overline{E_{BN}} = \frac{E_m}{\sqrt{2}} \angle -240^\circ = E_{ph} \angle -240^\circ$$

$$\overline{E_{RY}} = E_{ph} \angle 0^\circ - E_{ph} \angle -120^\circ$$

$$= E_{ph} (1 - (\cos 120^\circ - j \sin 120^\circ))$$

$$= E_{ph} \left( \frac{3}{2} + j \frac{\sqrt{3}}{2} \right)$$

$$= \sqrt{3} E_{ph} (\cos 30^\circ + j \sin 30^\circ)$$

$$= \sqrt{3} E_{ph} \angle 30^\circ$$

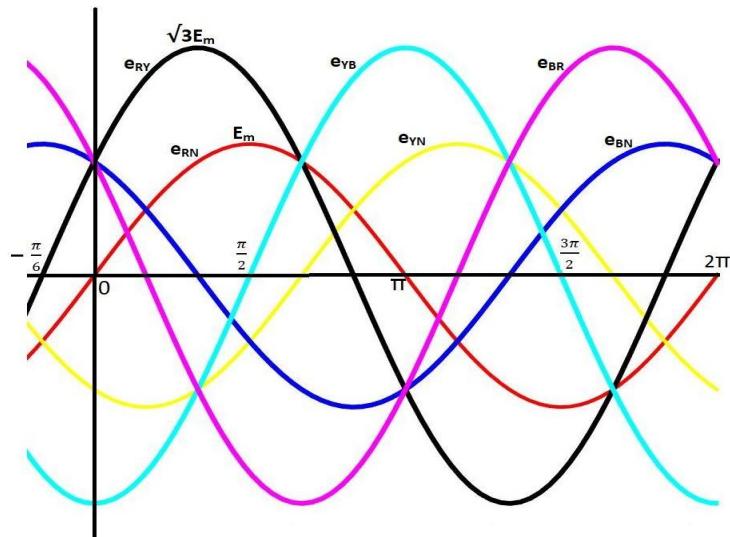
$$\overline{E_{YB}} = \overline{E_{YN}} - \overline{E_{BN}} = \sqrt{3} E_{ph} \angle -90^\circ$$

$$\overline{E_{BR}} = \overline{E_{BN}} - \overline{E_{RN}} = \sqrt{3} E_{ph} \angle -210^\circ$$

Thus, in a balanced star connected three phase system,

- (i)      Magnitude (RMS value) of Line Voltage =  $\sqrt{3} \times$  (Magnitude of Phase Voltage)
- (ii)     Each line voltage leads the corresponding phase voltage by  $30^\circ$

**Balanced Star System – Line and Phase Voltage Waveforms:**



**Balanced Star System – Phasor diagram:**

$$\overline{E_{RY}} = \overline{E_{RN}} - \overline{E_{YN}}$$

