

Question Answers: Spin magnetic moment and Larmor precession

2A.

Torque on a magnetic dipole: When a magnetic dipole with moment

$$\vec{\tau} = \vec{\mu} \times \vec{B}$$

The magnitude of this torque is

$$\tau = \mu B \sin(\theta)$$

This torque tries to align the magnetic moment with the field.

Work done in rotation:

$$dW = \tau d\theta = \mu B \sin(\theta) d\theta$$

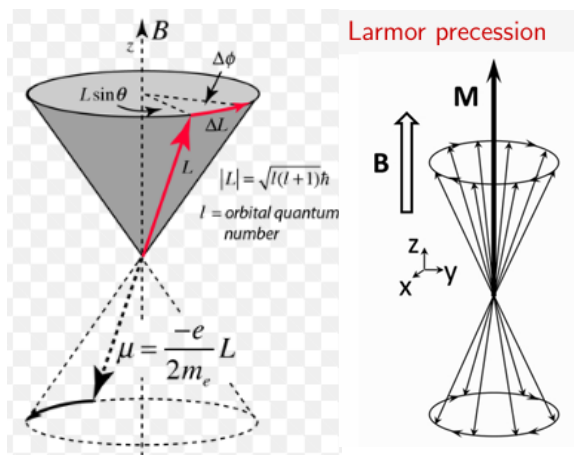
Total work done: The total work done to rotate the dipole is found by integrating the infinitesimal work:

$$W = \int_{\theta_1}^{\theta_2} \mu B \sin(\theta) d\theta$$

$$W = -\mu B \{ \cos(\theta_2) - \cos(\theta_1) \}$$

Magnetic Energy = $-\mu B \cos \theta$ (If $\theta_2 = \theta, \theta_1 = 90^\circ$)

3A.



Torque, $\vec{\tau} = \vec{\mu} \times \vec{B}$

The magnitude of this torque is

$$\tau = \mu B \sin(\theta) \dots (1)$$

$$\tau = \frac{\Delta L}{\Delta t}$$

$$\tau = \frac{\Delta \phi}{\Delta t} L \sin \theta (\Delta L = \Delta \phi L \sin \theta, \text{ see figure})$$

$$\tau = \omega L \sin \theta \dots (2)$$

From (1) and (2)

$$\omega = \frac{\mu B}{L}, \mu = \frac{eL}{2m_e}$$

$$\text{hence, } \omega = \frac{eB}{2m_e} \text{ or } \omega = \gamma B,$$

γ is gyromagnetic ratio