

CL47_Q1. Obtain the expression for orbital magnetic moment of the electron and Explain Bohr magneton.

Ans:

The basic atomic model of orbiting electrons around the nucleus constitutes tiny current loops at atomic levels. If the electrons are assumed to move in an orbit of radius r with a constant speed v , the period of rotation T , then the current

$$I = \frac{e}{T} = \frac{e\omega}{2\pi}$$

The magnetic moment associated with the electron's moment in the orbit

$$\mu_m = I \cdot A$$

$$= -\frac{e\omega}{2\pi} * \pi r^2 = -\frac{em\omega r^2}{2m}$$

$$\mu_m = -\frac{e}{2m} L, \text{ where } L \text{ is called orbital angular momentum}$$

Thus the magnetic moment of the electron is proportional to its angular momentum. The ratio of the magnetic moment to the angular momentum $\gamma = \frac{\mu_{\text{orb}}}{L} = \left(\frac{e}{2m_e}\right)$ is known as the gyro magnetic ratio. Due to the negative charge of the electron, the vectors $\vec{\mu}$ and \vec{L} point in opposite directions and perpendicular to the plane of the orbit.

The smallest non zero value of the spin magnetic moment due to electrons) is obtained as $\mu_s = \frac{e\hbar}{m}$. The magnetic moment being quantized; the smallest unit of magnetic moment $\mu_B = \frac{e\hbar}{2m} = 9.27 \times 10^{-24} \text{ J/T}$ is called the Bohr magneton

CL47_Q2. Estimate the magnetic moment of an electron that revolves around a nucleus in an orbit of 0.53A^0 radius. If the frequency of revolution $6.6 \times 10^{15} \text{ Hz}$.

Ans:

The magnetic moment associated with the electron's moment in the orbit $\mu e = I \cdot A$

$$\frac{e\omega}{2\pi} * \pi r^2 = \frac{e\omega r^2}{2}$$

$$\mu e = ef \cdot \pi r^2$$

$$= 9.314 \times 10^{-24} \text{ Am}$$

CL47_Q3. Why does a magnetic dipole due to orbital motion of the electron precess in a magnetic field?

Ans:

When a magnetic moment μ is placed in a magnetic field B , it experiences a torque which is given by $\tau = \mu \times B$. The torque then produces a change in angular momentum which is perpendicular to that angular momentum , causing the magnetic moment to precess around the direction of the magnetic field.

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