

Lecture 42

2. It is observed that second phase current in a balanced delta system is  $10\sin(\omega t - 60^\circ)\text{A}$ . Express all the three phase currents and all the three line currents in both time form and phasor form.

Solution:

Let Phase currents be  $i_1, i_2, \& i_3$

Line currents be  $i_R, i_Y, i_B$

Given that 2<sup>nd</sup> phase current is

$$i_2(t) = 10 \sin(\omega t - 60^\circ) \text{A}$$

Other phase currents are

$$\begin{aligned} i_1(t) &= 10 \sin(\omega t - 60^\circ + 120^\circ) \\ &= 10 \sin(\omega t + 60^\circ) \text{A} \end{aligned}$$

(1<sup>st</sup> phase current leads 2<sup>nd</sup> phase current by  $120^\circ$ )

$$\begin{aligned} i_3(t) &= 10 \sin(\omega t - 60^\circ - 120^\circ) \\ &= 10 \sin(\omega t - 180^\circ) \end{aligned}$$

(3<sup>rd</sup> phase current lags 2<sup>nd</sup> phase current by  $120^\circ$ )

## Line currents

$$\begin{aligned} i_R(t) &= \sqrt{3} \times 10 \sin(\omega t + 60^\circ - 30^\circ) \\ &= 17.3 \sin(\omega t + 30^\circ) \text{ A} \end{aligned}$$

1<sup>st</sup> line current is  $\sqrt{3} I_{ph}$  & lags  
1<sup>st</sup> phase current by  $30^\circ$

Similarly

$$\begin{aligned} i_Y(t) &= \sqrt{3} \times 10 \sin(\omega t - 60^\circ - 30^\circ) \\ &= 17.3 \sin(\omega t - 90^\circ) \text{ A} \end{aligned}$$

2<sup>nd</sup> line current lags 2<sup>nd</sup> phase current  
by  $30^\circ$

$$\begin{aligned} i_B(t) &= \sqrt{3} \times 10 \sin(\omega t - 180^\circ - 30^\circ) \\ &= 17.3 \sin(\omega t - 210^\circ) \text{ A} \end{aligned}$$

## Phasor forms of currents

### Phase Currents

$$\vec{I}_1 = \frac{10}{\sqrt{2}} \angle 60^\circ$$

$$\vec{I}_2 = \frac{10}{\sqrt{2}} \angle -60^\circ$$

$$\vec{I}_3 = \frac{10}{\sqrt{2}} \angle -180^\circ$$

### Phase voltages

$$\vec{I}_R = \frac{17.3}{\sqrt{2}} \angle 30^\circ$$

$$\vec{I}_Y = \frac{17.3}{\sqrt{2}} \angle -90^\circ$$

$$\vec{I}_B = \frac{17.3}{\sqrt{2}} \angle -210^\circ$$

### Unit III: Assessment: Q & A (Selected)

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