



ENGINEERING CHEMISTRY

Department of Science and Humanities

Class Content:

- *Vibrational spectroscopy*
- *Expression for vibrational energy levels
(Harmonic oscillator)*
- *Vibrational spectrum(Harmonic oscillator)*

Vibrational Spectroscopy

- When a molecule undergoes vibrational changes it absorbs **IR radiation**
- For a molecule to be vibrationally active (IR active) the vibration of a molecule must be associated with **change in dipole moment**
- Vibrations of molecules can result in changes in electric dipoles that can interact with the **electrical component** of the electromagnetic radiation.

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Module I- Molecular Spectroscopy

- When the frequencies match, **resonance occurs** and the molecule absorbs energy and goes to the higher **vibrational levels** and exhibits **vibrational spectrum**
- Molecules such as **HCl ,CO and H₂O** will show vibrational spectra while **H₂, Cl₂** will not
- **CO₂** molecule does not possess permanent dipole moment but **is IR active** as when it vibrates asymmetrically or in bending mode ,there is change in dipole moment

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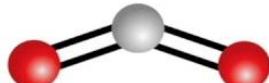
Module I- Molecular Spectroscopy

CO_2 molecule although does not possess permanent dipole moment is IR active because some of its vibrational modes are IR active:

CO_2 **symmetric stretch** is IR inactive as there is no change in dipole moment when molecule vibrates in this mode.

CO_2 **asymmetric stretch** is IR active

CO_2 **bending** mode is IR active



Symmetrical stretching

No change in dipole moment therefore IR inactive

Asymmetrical stretching

Change in dipole moment therefore IR active

In plane bending

Change in dipole moment therefore IR active

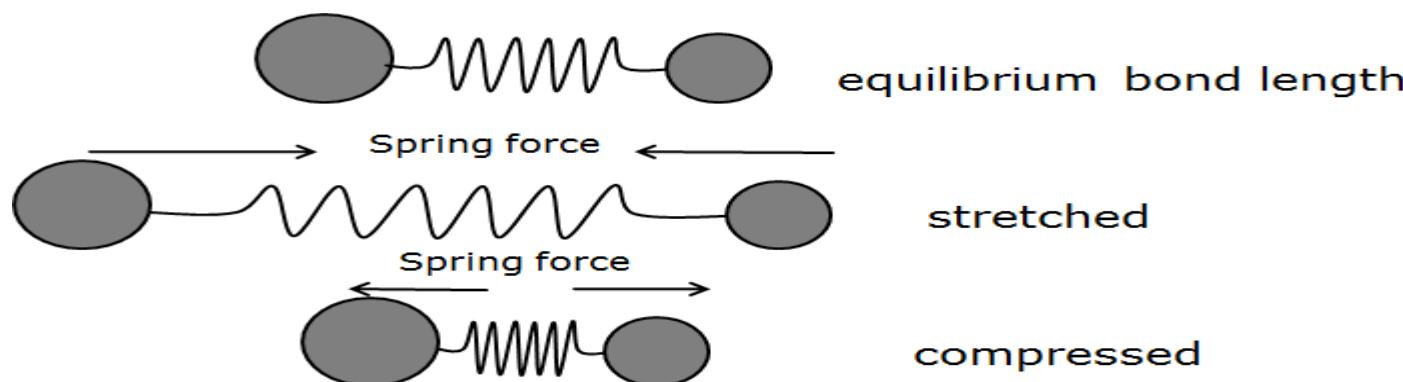
Source: <http://cepekmedia.co.nf>

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Module I- Molecular Spectroscopy

Vibrational spectroscopy of diatomic molecule: simple harmonic oscillator (SHO) model

- Every type of bond in a molecule has a unique natural **vibrational frequency**
- Therefore the IR spectrum of every molecule is **unique** as much as the finger print of human beings
- Bonds are not static but **vibrating in different ways**
- A vibrating bond can therefore be considered a spring with its ends tethered to two atoms as in the figure and obeys **Hooke's law**



Source : Ramasahayam, Swathi & Roy Chowdhury, Shubhajit. (2016). Non Invasive Estimation of Blood Urea Concentration using Near Infrared Spectroscopy. International Journal on Smart Sensing and Intelligent Systems. 9. 10.21307/ijssis-2017-878.

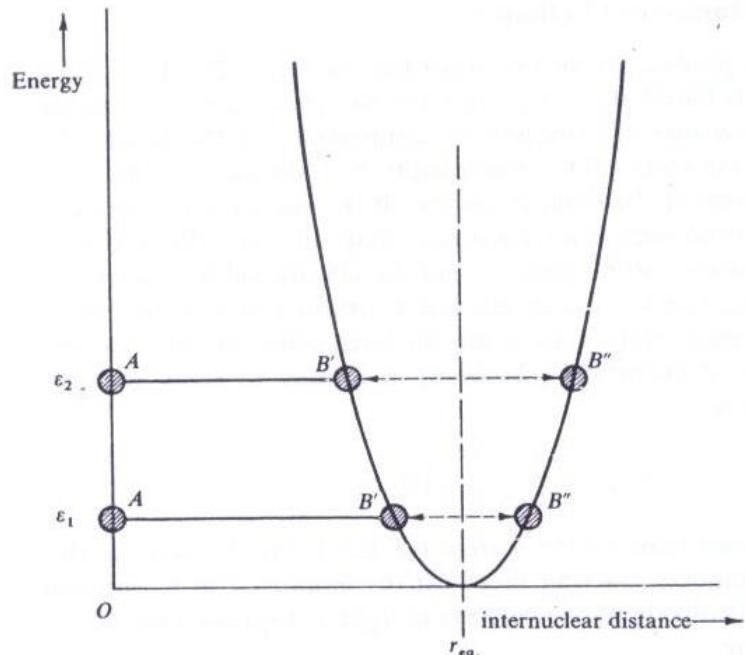
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The vibrating bond obeys Hooke's law, $F=-k(r-r_{eq})$

where k is a force constant, r is the inter nuclear distance, r_{eq} is equilibrium inter nuclear distance or bond length.

Energy is given by $E = \frac{1}{2} k(r - r_{eq})^2$ Hence the energy curve is **parabolic**



Source: Fundamentals of Molecular Spectroscopy: C. N. Banwell and Elaine M McCash,
Fifth Edition, MCGRAW-HILL Education (India) Private Ltd.

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Module I- Molecular Spectroscopy

The **oscillation frequency** is given by,

$$\nu_{osc} = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}} \text{Hz}$$

where μ is **reduced mass**

Expressing frequency of oscillation in terms of wave number

$$\bar{\nu}_{osc} = \frac{1}{2\pi c} \sqrt{\frac{k}{\mu}} \text{cm}^{-1}$$

Solving **Schrodinger equation for harmonic oscillator** shows vibrational energy levels are quantised and are given by the expression

$$E_v = \left(v + \frac{1}{2}\right) h \nu_{osc} \text{Joules}$$

where **v= vibrational quantum number** which can take up values zero upwards;
v=0,1,2,3....

Vibrational energy expressed in terms of wave number is given by,

$$\varepsilon_v = \left(v + \frac{1}{2}\right) \bar{\nu}_{osc} \text{cm}^{-1}$$

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The energy levels will appear at,

v	ϵ_v
0	$\epsilon_0 = \frac{1}{2} \bar{\nu}_{osc} cm^{-1}$
1	$\epsilon_1 = \frac{3}{2} \bar{\nu}_{osc} cm^{-1}$
2	$\epsilon_2 = \frac{5}{2} \bar{\nu}_{osc} cm^{-1}$

ϵ_0 is called **zero point energy**

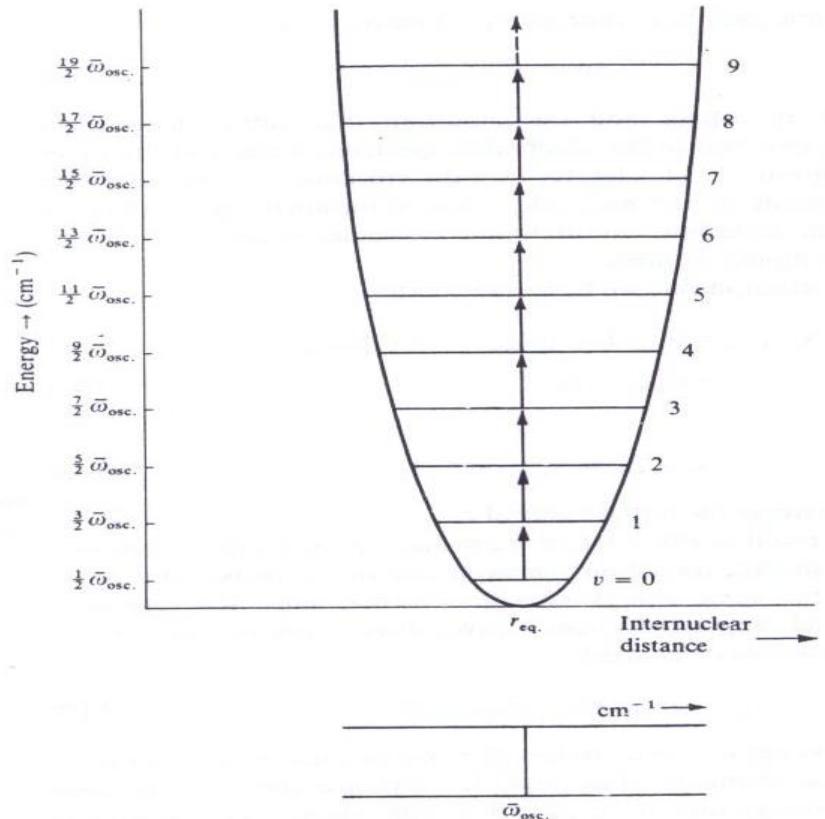
The **difference between any two consecutive energy levels** is equal to
Hence the energy levels are equally spaced.

The **selection rules** for vibrational transitions are

- **Gross selection rule** : When the molecule vibrates there should be a change in the dipole moment
- **$\Delta v = \pm 1$**

Therefore transition between any two consecutive vibrational levels are allowed and only **one line** is observed in the vibrational spectrum at $\bar{\nu}_{osc} cm^{-1}$

Vibrational energy levels and resulting spectrum for a diatomic molecule executing simple harmonic motion



Source: Fundamentals of Molecular Spectroscopy: C. N. Banwell and Elaine M McCash, Fifth Edition, McGRAW-HILL Education (India) Private Ltd.

From the spectrum $\bar{\nu}_{\text{osc}}$ can be obtained and using the expression

$$\bar{\nu}_{\text{osc}} = \frac{1}{2\pi c} \sqrt{\frac{k}{\mu}} \text{ cm}^{-1}$$

k can be determined which is the **bond strength (force constant)** of the molecule



THANK YOU

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