

1. An electron is confined in a 3D cubic infinite well of side 1nm, compute the energy difference between the ground state and the second excited state.

Answer: Energy eigen value is given as

$$E_n = \frac{\hbar^2}{8ma^2} (n_x^2 + n_y^2 + n_z^2)$$

Ground state: (1, 1, 1) $\Rightarrow E_{111} = 3 \frac{\hbar^2}{8ma^2}$

Second excited state: (1, 2, 2) $\Rightarrow E_{122} = 9 \frac{\hbar^2}{8ma^2}$

Energy difference: $\Delta E = E_{122} - E_{111} = 6 \frac{\hbar^2}{8ma^2}$

For an electron in a cubic box of side 1 nm; $\Delta E = 3.61 \times 10^{-19} \text{ J}$

2. List first six possible distinct eigen states of 3d infinite well.

Answer: The first six energy eigen states ordered in the increasing order of the energy

State No.	(n_x, n_y, n_z)	$n_x^2 + n_y^2 + n_z^2$	Degeneracy
1	(1, 1, 1)	3	1
2	(1, 1, 2) or (2, 1, 1) or (1, 2, 1)	6	3
3	(1, 2, 2) or (2, 2, 1) or (2, 1, 2)	9	3
4	(1, 1, 3) or (3, 1, 1) or (1, 3, 1)	11	3
5	(2, 2, 2)	12	1
6	(1, 2, 3) or (1, 3, 2) or (2, 3, 1) or (2, 1, 3) or (3, 1, 2) or (3, 2, 1)	14	6