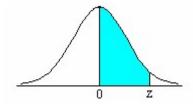
TABLE 1 Normal Curve Areas

The entries in the body of the table correspond to the area shaded under the normal curve.



z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.0000	0.0040	0.0080	0.0120	0.0160	0.0199	0.0239	0.0279	0.0319	0.0359
0.1	0.0398	0.0438	0.0478	0.0517	0.0557	0.0596	0.0636	0.0675	0.0714	0.0753
0.2	0.0793	0.0832	0.0871	0.0910	0.0948	0.0987	0.1026	0.1064	0.1103	0.1141
0.3	0.1179	0.1217	0.1255	0.1293	0.1331	0.1368	0.1406	0.1443	0.1480	0.1517
0.4	0.1554	0.1591	0.1628	0.1664	0.1700	0.1736	0.1772	0.1808	0.1844	0.1879
0.5	0.1915	0.1950	0.1985	0.2019	0.2054	0.2088	0.2123	0.2157	0.2190	0.2224
0.6	0.2257	0.2291	0.2324	0.2357	0.2389	0.2422	0.2454	0.2486	0.2517	0.2549
0.7	0.2580	0.2611	0.2642	0.2673	0.2703	0.2734	0.2764	0.2794	0.2823	0.2852
8.0	0.2881	0.2910	0.2939	0.2967	0.2995	0.3023	0.3051	0.3078	0.3106	0.3133
0.9	0.3159	0.3186	0.3212	0.3238	0.3264	0.3289	0.3315	0.3340	0.3365	0.3389
1.0	0.3413	0.3438	0.3461	0.3485	0.3508	0.3531	0.3554	0.3577	0.3599	0.3621
1.1	0.3643	0.3665	0.3686	0.3708	0.3729	0.3749	0.3770	0.3790	0.3810	0.3830
1.2	0.3849	0.3869	0.3888	0.3907	0.3925	0.3944	0.3962	0.3980	0.3997	0.4015
1.3	0.4032	0.4049	0.4066	0.4082	0.4099	0.4115	0.4131	0.4147	0.4162	0.4177
1.4	0.4192	0.4207	0.4222	0.4236	0.4251	0.4265	0.4279	0.4292	0.4306	0.4319
1.5	0.4332	0.4345	0.4357	0.4370	0.4382	0.4394	0.4406	0.4418	0.4429	0.4441
1.6	0.4452	0.4463	0.4474	0.4484	0.4495	0.4505	0.4515	0.4525	0.4535	0.4545
1.7	0.4554	0.4564	0.4573	0.4582	0.4591	0.4599	0.4608	0.4616	0.4625	0.4633
1.8	0.4641	0.4649	0.4656	0.4664	0.4671	0.4678	0.4686	0.4693	0.4699	0.4706
1.9	0.4713	0.4719	0.4726	0.4732	0.4738	0.4744	0.4750	0.4756	0.4761	0.4767
2.0	0.4772	0.4778	0.4783	0.4788	0.4793	0.4798	0.4803	0.4808	0.4812	0.4817
2.1	0.4821	0.4826	0.4830	0.4834	0.4838	0.4842	0.4846	0.4850	0.4854	0.4857
2.2	0.4861	0.4864	0.4868	0.4871	0.4875	0.4878	0.4881	0.4884	0.4887	0.4890
2.3	0.4893	0.4896	0.4898	0.4901	0.4904	0.4906	0.4909	0.4911	0.4913	0.4916
2.4	0.4918	0.4920	0.4922	0.4925	0.4927	0.4929	0.4931	0.4932	0.4934	0.4936
2.5	0.4938	0.4940	0.4941	0.4943	0.4945	0.4946	0.4948	0.4949	0.4951	0.4952
2.6	0.4953	0.4955	0.4956	0.4957	0.4959	0.4960	0.4961	0.4962	0.4963	0.4964
2.7	0.4965	0.4966	0.4967	0.4968	0.4969	0.4970	0.4971	0.4972	0.4973	0.4974
2.8	0.4974	0.4975	0.4976	0.4977	0.4977	0.4978	0.4979	0.4979	0.4980	0.4981
2.9	0.4981	0.4982	0.4982	0.4983	0.4984	0.4984	0.4985	0.4985	0.4986	0.4986
3.0	0.4987	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990
3.1	0.4990	0.4991	0.4991	0.4991	0.4992	0.4992	0.4992	0.4992	0.4993	0.4993
3.2	0.4993	0.4993	0.4994	0.4994	0.4994	0.4994	0.4994	0.4995	0.4995	0.4995
3.3	0.4995	0.4995	0.4995	0.4996	0.4996	0.4996	0.4996	0.4996	0.4996	0.4997
3.4	0.4997	0.4997	0.4997	0.4997	0.4997	0.4997	0.4997	0.4997	0.4997	0.4998
3.5	0.4998	0.4998	0.4998	0.4998	0.4998	0.4998	0.4998	0.4998	0.4998	0.4998
3.6	0.4998	0.4998	0.4999	0.4999	0.4999	0.4999	0.4999	0.4999	0.4999	0.4999
3.7	0.4999	0.4999	0.4999	0.4999	0.4999	0.4999	0.4999	0.4999	0.4999	0.4999
3.8	0.4999	0.4999	0.4999	0.4999	0.4999	0.4999	0.4999	0.4999	0.4999	0.4999
3.9	0.5000	0.5000	0.5000	0.5000	0.5000	0.5000	0.5000	0.5000	0.5000	0.5000

TABLE A.2

t Distribution: Critical Values of t

		Significance level						
Degrees of	Two-tailed test:	10%	5%	2%	1%	0.2%	0.1%	
freedom	One-tailed test:	5%	2.5%	1%	0.5%	0.1%	0.05%	
1		6.314	12.706	31.821	63.657	318.309	636.619	
2 3		2.920 2.353	4.303 3.182	6.965 4.541	9.925 5.841	22.327 10.215	31.599 12.924	
4		2.333	2.776	3.747	4.604	7.173	8.610	
5		2.015	2.571	3.365	4.032	5.893	6.869	
6		1.943	2.447	3.143	3.707	5.208	5.959	
7		1.894	2.365	2.998	3.499	4.785	5.408	
8		1.860	2.306	2.896	3.355	4.501	5.041	
9 10		1.833 1.812	2.262 2.228	2.821 2.764	3.250 3.169	4.297 4.144	4.781 4.587	
11 12		1.796 1.782	2.201 2.179	2.718 2.681	3.106 3.055	4.025 3.930	4.437 4.318	
13		1.771	2.160	2.650	3.033	3.852	4.221	
14		1.761	2.145	2.624	2.977	3.787	4.140	
15		1.753	2.131	2.602	2.947	3.733	4.073	
16		1.746	2.120	2.583	2.921	3.686	4.015	
17		1.740	2.110	2.567	2.898	3.646	3.965	
18		1.734	2.101	2.552	2.878	3.610	3.922	
19 20		1.729 1.725	2.093 2.086	2.539 2.528	2.861 2.845	3.579 3.552	3.883 3.850	
21			2.080					
21		1.721 1.717	2.080	2.518 2.508	2.831 2.819	3.527 3.505	3.819 3.792	
23		1.714	2.069	2.500	2.807	3.485	3.768	
24		1.711	2.064	2.492	2.797	3.467	3.745	
25		1.708	2.060	2.485	2.787	3.450	3.725	
26		1.706	2.056	2.479	2.779	3.435	3.707	
27		1.703	2.052	2.473	2.771	3.421	3.690	
28 29		1.701 1.699	2.048 2.045	2.467 2.462	2.763 2.756	3.408 3.396	3.674 3.659	
30		1.697	2.043	2.457	2.750	3.385	3.646	
32		1.694	2.037	2.449	2.738	3.365	3.622	
34		1.691	2.032	2.441	2.728	3.348	3.601	
36		1.688	2.028	2.434	2.719	3.333	3.582	
38		1.686	2.024	2.429	2.712	3.319	3.566	
40		1.684	2.021	2.423	2.704	3.307	3.551	
42		1.682	2.018	2.418	2.698	3.296	3.538	
44 46		1.680 1.679	2.015 2.013	2.414 2.410	2.692 2.687	3.286 3.277	3.526 3.515	
48		1.677	2.013	2.410	2.682	3.269	3.505	
50		1.676	2.009	2.403	2.678	3.261	3.496	
60		1.671	2.000	2.390	2.660	3.232	3.460	
70		1.667	1.994	2.381	2.648	3.211	3.435	
80		1.664	1.990	2.374	2.639	3.195	3.416	
90 100		1.662 1.660	1.987 1.984	2.368 2.364	2.632 2.626	3.183 3.174	3.402 3.390	
120 150		1.658 1.655	1.980 1.976	2.358 2.351	2.617 2.609	3.160 3.145	3.373 3.357	
200		1.653	1.970	2.345	2.601	3.131	3.340	
300		1.650	1.968	2.339	2.592	3.118	3.323	
400		1.649	1.966	2.336	2.588	3.111	3.315	
500		1.648	1.965	2.334	2.586	3.107	3.310	
600		1.647	1.964	2.333	2.584	3.104	3.307	
∞		1.645	1.960	2.326	2.576	3.090	3.291	

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TABLE A.3

F Distribution: Critical Values of F (5% significance level)

v_1	1	2	3	4	5	6	7	8	9	10	12	14	16	18	20
v ₂ 1 2 3 4 5	161.45 18.51 10.13 7.71 6.61	199.50 19.00 9.55 6.94 5.79			230.16 19.30 9.01 6.26 5.05	233.99 19.33 8.94 6.16 4.95	236.77 19.35 8.89 6.09 4.88	238.88 19.37 8.85 6.04 4.82		241.88 19.40 8.79 5.96 4.74		245.36 19.42 8.71 5.87 4.64	246.46 19.43 8.69 5.84 4.60		
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	4.06	4.00	3.96	3.92	3.90	3.87
7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68	3.64	3.57	3.53	3.49	3.47	3.44
8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39	3.35	3.28	3.24	3.20	3.17	3.15
9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	3.14	3.07	3.03	2.99	2.96	2.94
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02	2.98	2.91	2.86	2.83	2.80	2.77
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90	2.85	2.79	2.74	2.70	2.67	2.65
12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80	2.75	2.69	2.64	2.60	2.57	2.54
13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71	2.67	2.60	2.55	2.51	2.48	2.46
14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65	2.60	2.53	2.48	2.44	2.41	2.39
15	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.59	2.54	2.48	2.42	2.38	2.35	2.33
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54	2.49	2.42	2.37	2.33	2.30	2.28
17	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.49	2.45	2.38	2.33	2.29	2.26	2.23
18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46	2.41	2.34	2.29	2.25	2.22	2.19
19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42	2.38	2.31	2.26	2.21	2.18	2.16
20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39	2.35	2.28	2.22	2.18	2.15	2.12
21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37	2.32	2.25	2.20	2.16	2.12	2.10
22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34	2.30	2.23	2.17	2.13	2.10	2.07
23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32	2.27	2.20	2.15	2.11	2.08	2.05
24	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30	2.25	2.18	2.13	2.09	2.05	2.03
25	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.28	2.24	2.16	2.11	2.07	2.04	2.01
26	4.22	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.27	2.22	2.15	2.09	2.05	2.02	1.99
27	4.21	3.35	2.96	2.73	2.57	2.46	2.37	2.31	2.25	2.20	2.13	2.08	2.04	2.00	1.97
28	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.24	2.19	2.12	2.06	2.02	1.99	1.96
29	4.18	3.33	2.93	2.70	2.55	2.43	2.35	2.28	2.22	2.18	2.10	2.05	2.01	1.97	1.94
30	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21	2.16	2.09	2.04	1.99	1.96	1.93
35	4.12	3.27	2.87	2.64	2.49	2.37	2.29	2.22	2.16	2.11	2.04	1.99	1.94	1.91	1.88
40	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12	2.08	2.00	1.95	1.90	1.87	1.84
50	4.03	3.18	2.79	2.56	2.40	2.29	2.20	2.13	2.07	2.03	1.95	1.89	1.85	1.81	1.78
60	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04	1.99	1.92	1.86	1.82	1.78	1.75
70	3.98	3.13	2.74	2.50	2.35	2.23	2.14	2.07	2.02	1.97	1.89	1.84	1.79	1.75	1.72
80	3.96	3.11	2.72	2.49	2.33	2.21	2.13	2.06	2.00	1.95	1.88	1.82	1.77	1.73	1.70
90	3.95	3.10	2.71	2.47	2.32	2.20	2.11	2.04	1.99	1.94	1.86	1.80	1.76	1.72	1.69
100	3.94	3.09	2.70	2.46	2.31	2.19	2.10	2.03	1.97	1.93	1.85	1.79	1.75	1.71	1.68
120	3.92	3.07	2.68	2.45	2.29	2.18	2.09	2.02	1.96	1.91	1.83	1.78	1.73	1.69	1.66
150	3.90	3.06	2.66	2.43	2.27	2.16	2.07	2.00	1.94	1.89	1.82	1.76	1.71	1.67	1.64
200	3.89	3.04	2.65	2.42	2.26	2.14	2.06	1.98	1.93	1.88	1.80	1.74	1.69	1.66	1.62
250	3.88	3.03	2.64	2.41	2.25	2.13	2.05	1.98	1.92	1.87	1.79	1.73	1.68	1.65	1.61
300	3.87	3.03	2.63	2.40	2.24	2.13	2.04	1.97	1.91	1.86	1.78	1.72	1.68	1.64	1.61
400	3.86	3.02	2.63	2.39	2.24	2.12	2.03	1.96	1.90	1.85	1.78	1.72	1.67	1.63	1.60
500	3.86	3.01	2.62	2.39	2.23	2.12	2.03	1.96	1.90	1.85	1.77	1.71	1.66	1.62	1.59
600	3.86	3.01	2.62	2.39	2.23	2.11	2.02	1.95	1.90	1.85	1.77	1.71	1.66	1.62	1.59
750	3.85	3.01	2.62	2.38	2.23	2.11	2.02	1.95	1.89	1.84	1.77	1.70	1.66	1.62	1.58
1000	3.85	3.00	2.61	2.38	2.22	2.11	2.02	1.95	1.89	1.84	1.76	1.70	1.65	1.61	1.58

TRIAL MODE - Click here for more information

Table A.3 (continued)

F Distribution: Critical Values of F (5% significance level)

v_1	25	30	35	40	50	60	75	100	150	200
v ₂ 1 2 3 4 5	249.26 19.46 8.63 5.77 4.52	250.10 19.46 8.62 5.75 4.50	250.69 19.47 8.60 5.73 4.48	251.14 19.47 8.59 5.72 4.46	19.48 8.58 5.70	19.48 8.57 5.69	19.48 8.56 5.68	19.49 8.55 5.66	8.54	19.49 8.54 5.65
6 7 8 9 10	3.83 3.40 3.11 2.89 2.73	3.81 3.38 3.08 2.86 2.70	3.79 3.36 3.06 2.84 2.68	3.77 3.34 3.04 2.83 2.66	3.02 2.80	3.74 3.30 3.01 2.79 2.62	2.99	2.97		3.69 3.25 2.95 2.73 2.56
11 12 13 14 15	2.60 2.50 2.41 2.34 2.28	2.57 2.47 2.38 2.31 2.25	2.55 2.44 2.36 2.28 2.22	2.53 2.43 2.34 2.27 2.20	2.24	2.30 2.22	2.37 2.28 2.21	2.26 2.19	2.44 2.33 2.24 2.17 2.10	2.43 2.32 2.23 2.16 2.10
16 17 18 19 20	2.23 2.18 2.14 2.11 2.07	2.19 2.15 2.11 2.07 2.04	2.17 2.12 2.08 2.05 2.01	2.15 2.10 2.06 2.03 1.99	2.04		2.00	1.98	2.05 2.00 1.96 1.92 1.89	2.04 1.99 1.95 1.91 1.88
21 22 23 24 25	2.05 2.02 2.00 1.97 1.96	2.01 1.98 1.96 1.94 1.92	1.98 1.96 1.93 1.91 1.89	1.96 1.94 1.91 1.89 1.87	1.94 1.91 1.88 1.86 1.84	1.92 1.89 1.86 1.84 1.82	1.84	1.82 1.80	1.86 1.83 1.80 1.78 1.76	1.84 1.82 1.79 1.77 1.75
26 27 28 29 30	1.94 1.92 1.91 1.89 1.88	1.90 1.88 1.87 1.85 1.84	1.87 1.86 1.84 1.83 1.81	1.85 1.84 1.82 1.81 1.79	1.82 1.81 1.79 1.77 1.76		1.76 1.75 1.73	1.76 1.74 1.73 1.71 1.70	1.74 1.72 1.70 1.69 1.67	1.73 1.71 1.69 1.67 1.66
35 40 50 60 70	1.82 1.78 1.73 1.69 1.66	1.79 1.74 1.69 1.65 1.62	1.76 1.72 1.66 1.62 1.59	1.74 1.69 1.63 1.59 1.57	1.56	1.58	1.55 1.51	1.63 1.59 1.52 1.48 1.45	1.61 1.56 1.50 1.45 1.42	1.60 1.55 1.48 1.44 1.40
80 90 100 120 150	1.64 1.63 1.62 1.60 1.58	1.60 1.59 1.57 1.55 1.54	1.57 1.55 1.54 1.52 1.50	1.54 1.53 1.52 1.50 1.48	1.49 1.48 1.46	1.45 1.43	1.44 1.42 1.40	1.39 1.37	1.39 1.38 1.36 1.33 1.31	1.36 1.34 1.32
200 250 300 400 500	1.56 1.55 1.54 1.53 1.53	1.52 1.50 1.50 1.49 1.48	1.48 1.47 1.46 1.45 1.45	1.46 1.44 1.43 1.42 1.42	1.41 1.40 1.39 1.38 1.38	1.39 1.37 1.36 1.35 1.35	1.34	1.32 1.31 1.30 1.28 1.28	1.28 1.27 1.26 1.24 1.23	1.26 1.25 1.23 1.22 1.21
600 750 1000	1.52 1.52 1.52	1.48 1.47 1.47	1.44 1.44 1.43	1.41 1.41 1.41	1.37 1.37 1.36	1.34 1.34 1.33	1.31 1.30 1.30	1.27 1.26 1.26	1.23 1.22 1.22	1.20 1.20 1.19

TABLE A.3 (continued)

F Distribution: Critical Values of F (1% significance level)

<i>v</i> ₁	1	2	3	4	5	6	7	8	9	10	12	14	16	18	20
v_2	4052.18	4999.50	5403.35	5624.58	5763.65		5928.36	5981.07			6106.32	6142.67	6170.10	6191.53	6208.73
2	98.50	99.00	99.17		99.30										
3	34.12	30.82			28.24		27.67					26.92			
4	21.20	18.00	16.69		15.52		14.98	14.80							
5	16.26	13.27	12.06	11.39	10.97	10.67	10.46	10.29	10.16	10.05	9.89	9.77	9.68	9.61	9.55
6	13.75	10.92	9.78	9.15	8.75	8.47	8.26	8.10	7.98	7.87	7.72	7.60	7.52	7.45	7.40
7	12.25	9.55	8.45	7.85	7.46	7.19	6.99	6.84			6.47	6.36			6.16
8	11.26	8.65	7.59	7.01	6.63	6.37	6.18	6.03	5.91	5.81	5.67	5.56			5.36
9	10.56	8.02	6.99	6.42	6.06	5.80	5.61	5.47				5.01	4.92		
10	10.04	7.56	6.55	5.99	5.64	5.39	5.20	5.06	4.94	4.85	4.71	4.60	4.52	4.46	4.41
11	9.65	7.21	6.22	5.67	5.32	5.07	4.89	4.74			4.40	4.29	4.21	4.15	4.10
12	9.33	6.93	5.95	5.41	5.06	4.82	4.64	4.50				4.05	3.97		3.86
13	9.07	6.70	5.74	5.21	4.86	4.62	4.44	4.30				3.86			
14	8.86	6.51	5.56	5.04	4.69	4.46		4.14		3.94		3.70			
15	8.68	6.36	5.42	4.89	4.56	4.32	4.14	4.00	3.89	3.80	3.67	3.56	3.49	3.42	3.37
16	8.53	6.23	5.29	4.77	4.44	4.20	4.03	3.89	3.78	3.69	3.55	3.45	3.37	3.31	3.26
17	8.40	6.11	5.18	4.67	4.34	4.10	3.93	3.79	3.68			3.35	3.27		3.16
18	8.29	6.01	5.09	4.58	4.25	4.01	3.84	3.71	3.60		3.37	3.27			3.08
19	8.18	5.93	5.01	4.50		3.94	3.77	3.63	3.52		3.30	3.19			3.00
20	8.10	5.85	4.94	4.43	4.10	3.87	3.70	3.56	3.46	3.37	3.23	3.13	3.05	2.99	2.94
21	8.02	5.78	4.87	4.37	4.04	3.81	3.64	3.51	3.40	3.31	3.17	3.07	2.99	2.93	2.88
22	7.95	5.72	4.82	4.31	3.99	3.76	3.59	3.45	3.35	3.26	3.12	3.02	2.94	2.88	2.83
23	7.88	5.66	4.76	4.26		3.71	3.54	3.41	3.30		3.07	2.97			
24	7.82	5.61	4.72	4.22	3.90	3.67	3.50	3.36				2.93	2.85		
25	7.77	5.57	4.68	4.18	3.85	3.63	3.46	3.32	3.22	3.13	2.99	2.89	2.81	2.75	2.70
26	7.72	5.53	4.64	4.14	3.82	3.59	3.42	3.29	3.18			2.86			
27	7.68	5.49	4.60	4.11	3.78	3.56	3.39	3.26				2.82			
28	7.64	5.45	4.57	4.07	3.75	3.53	3.36	3.23	3.12		2.90	2.79			
29	7.60	5.42	4.54	4.04	3.73	3.50	3.33	3.20	3.09			2.77			2.57
30	7.56	5.39	4.51	4.02	3.70	3.47	3.30	3.17	3.07	2.98	2.84	2.74	2.66	2.60	2.55
35	7.42	5.27	4.40	3.91	3.59	3.37	3.20	3.07	2.96	2.88	2.74	2.64			
40	7.31	5.18	4.31	3.83	3.51	3.29	3.12	2.99				2.56			
50	7.17	5.06	4.20	3.72	3.41	3.19		2.89	2.78	2.70		2.46			
60	7.08	4.98	4.13	3.65	3.34	3.12	2.95	2.82	2.72	2.63	2.50			2.25	
70	7.01	4.92	4.07	3.60	3.29	3.07	2.91	2.78	2.67	2.59	2.45	2.35	2.27	2.20	2.15
80	6.96	4.88	4.04	3.56	3.26	3.04	2.87	2.74				2.31	2.23		2.12
90	6.93	4.85	4.01	3.53	3.23	3.01	2.84	2.72		2.52	2.39	2.29	2.21		
100	6.90	4.82	3.98	3.51	3.21	2.99		2.69	2.59			2.27	2.19		
120	6.85	4.79	3.95	3.48	3.17	2.96	2.79	2.66							
150	6.81	4.75	3.91	3.45	3.14	2.92	2.76	2.63	2.53	2.44	2.31	2.20	2.12	2.06	2.00
200	6.76	4.71	3.88	3.41	3.11	2.89	2.73	2.60	2.50		2.27	2.17	2.09	2.03	1.97
250	6.74	4.69	3.86	3.40		2.87	2.71	2.58		2.39		2.15			1.95
300	6.72	4.68	3.85	3.38	3.08	2.86	2.70	2.57			2.24	2.14			
400	6.70	4.66	3.83	3.37		2.85	2.68	2.56				2.13			
500	6.69	4.65	3.82	3.36	3.05	2.84	2.68	2.55	2.44	2.36	2.22	2.12	2.04	1.97	1.92
600	6.68	4.64	3.81	3.35	3.05	2.83	2.67	2.54				2.11	2.03		
750	6.67	4.63	3.81	3.34		2.83	2.66					2.11	2.02		
1000	6.66	4.63	3.80	3.34	3.04	2.82	2.66	2.53	2.43	2.34	2.20	2.10	2.02	1.95	1.90

Table A.3 (continued)

F Distribution: Critical Values of F (1% significance level)

<i>v</i> ₁	25	30	35	40	50	60	75	100	150	200
v_2 1 2 3 4 5	6239.83 99.46 26.58 13.91 9.45	6260.65 99.47 26.50 13.84 9.38	6275.57 99.47 26.45 13.79 9.33	99.47 26.41	6302.52 99.48 26.35 13.69 9.24	99.48 26.32	99.49 26.28	6334.11 99.49 26.24 13.58 9.13	99.49	6349.97 99.49 26.18 13.52 9.08
6	7.30	7.23	7.18	7.14	7.09	7.06	7.02	6.99	6.95	6.93
7	6.06	5.99	5.94	5.91	5.86	5.82	5.79	5.75	5.72	5.70
8	5.26	5.20	5.15	5.12	5.07	5.03	5.00	4.96	4.93	4.91
9	4.71	4.65	4.60	4.57	4.52	4.48	4.45	4.41	4.38	4.36
10	4.31	4.25	4.20	4.17	4.12	4.08	4.05	4.01	3.98	3.96
11	4.01	3.94	3.89	3.86	3.81	3.78	3.74	3.71	3.67	3.66
12	3.76	3.70	3.65	3.62	3.57	3.54	3.50	3.47	3.43	3.41
13	3.57	3.51	3.46	3.43	3.38	3.34	3.31	3.27	3.24	3.22
14	3.41	3.35	3.30	3.27	3.22	3.18	3.15	3.11	3.08	3.06
15	3.28	3.21	3.17	3.13	3.08	3.05	3.01	2.98	2.94	2.92
16	3.16	3.10	3.05	3.02	2.97	2.93	2.90	2.86	2.83	2.81
17	3.07	3.00	2.96	2.92	2.87	2.83	2.80	2.76	2.73	2.71
18	2.98	2.92	2.87	2.84	2.78	2.75	2.71	2.68	2.64	2.62
19	2.91	2.84	2.80	2.76	2.71	2.67	2.64	2.60	2.57	2.55
20	2.84	2.78	2.73	2.69	2.64	2.61	2.57	2.54	2.50	2.48
21 22 23 24 25	2.79 2.73 2.69 2.64 2.60	2.72 2.67 2.62 2.58 2.54	2.67 2.62 2.57 2.53 2.49	2.64 2.58 2.54 2.49 2.45			2.51 2.46 2.41 2.37 2.33	2.48 2.42 2.37 2.33 2.29	2.44 2.38 2.34 2.29 2.25	2.42 2.36 2.32 2.27 2.23
26	2.57	2.50	2.45	2.42	2.36	2.33	2.29	2.25	2.21	2.19
27	2.54	2.47	2.42	2.38	2.33	2.29	2.26	2.22	2.18	2.16
28	2.51	2.44	2.39	2.35	2.30	2.26	2.23	2.19	2.15	2.13
29	2.48	2.41	2.36	2.33	2.27	2.23	2.20	2.16	2.12	2.10
30	2.45	2.39	2.34	2.30	2.25	2.21	2.17	2.13	2.09	2.07
35	2.35	2.28	2.23	2.19	2.14	2.10	2.06	2.02	1.98	1.96
40	2.27	2.20	2.15	2.11	2.06	2.02	1.98	1.94	1.90	1.87
50	2.17	2.10	2.05	2.01	1.95	1.91	1.87	1.82	1.78	1.76
60	2.10	2.03	1.98	1.94	1.88	1.84	1.79	1.75	1.70	1.68
70	2.05	1.98	1.93	1.89	1.83	1.78	1.74	1.70	1.65	1.62
80	2.01	1.94	1.89	1.85	1.79		1.70	1.65	1.61	1.58
90	1.99	1.92	1.86	1.82	1.76		1.67	1.62	1.57	1.55
100	1.97	1.89	1.84	1.80	1.74		1.65	1.60	1.55	1.52
120	1.93	1.86	1.81	1.76	1.70		1.61	1.56	1.51	1.48
150	1.90	1.83	1.77	1.73	1.66		1.57	1.52	1.46	1.43
200	1.87	1.79	1.74	1.69		1.58	1.53	1.48	1.42	1.39
250	1.85	1.77	1.72	1.67		1.56	1.51	1.46	1.40	1.36
300	1.84	1.76	1.70	1.66		1.55	1.50	1.44	1.38	1.35
400	1.82	1.75	1.69	1.64		1.53	1.48	1.42	1.36	1.32
500	1.81	1.74	1.68	1.63		1.52	1.47	1.41	1.34	1.31
600	1.80	1.73	1.67	1.63	1.56	1.51	1.46	1.40	1.34	1.30
750	1.80	1.72	1.66	1.62	1.55	1.50	1.45	1.39	1.33	1.29
1000	1.79	1.72	1.66	1.61	1.54	1.50	1.44	1.38	1.32	1.28

TABLE A.3 (continued)

F Distribution: Critical Values of F (0.1% significance level)

v_1	1 1	2	3	4	5	6	7	8	9	10	12	14	16	18	20
	4.05e05 998.50 167.03 74.14 47.18	999.00		999.25	999.30	999.33	999.36	999.37	999.39	999.40 129.25	999.42	999.43	999.44	999.44	999.45
6	35.51	27.00	23.70	21.92	20.80	20.03	19.46	19.03	18.69	18.41	17.99	17.68	17.45	17.27	17.12
7	29.25	21.69	18.77	17.20	16.21	15.52	15.02	14.63	14.33	14.08	13.71	13.43	13.23	13.06	12.93
8	25.41	18.49	15.83	14.39	13.48	12.86	12.40	12.05	11.77	11.54	11.19	10.94	10.75	10.60	10.48
9	22.86	16.39	13.90	12.56	11.71	11.13	10.70	10.37	10.11	9.89	9.57	9.33	9.15	9.01	8.90
10	21.04	14.91	12.55	11.28	10.48	9.93	9.52	9.20	8.96	8.75	8.45	8.22	8.05	7.91	7.80
11	19.69	13.81	11.56	10.35	9.58	9.05	8.66	8.35	8.12	7.92	7.63	7.41	7.24	7.11	7.01
12	18.64	12.97	10.80	9.63	8.89	8.38	8.00	7.71	7.48	7.29	7.00	6.79	6.63	6.51	6.40
13	17.82	12.31	10.21	9.07	8.35	7.86	7.49	7.21	6.98	6.80	6.52	6.31	6.16	6.03	5.93
14	17.14	11.78	9.73	8.62	7.92	7.44	7.08	6.80	6.58	6.40	6.13	5.93	5.78	5.66	5.56
15	16.59	11.34	9.34	8.25	7.57	7.09	6.74	6.47	6.26	6.08	5.81	5.62	5.46	5.35	5.25
16	16.12	10.97	9.01	7.94	7.27	6.80	6.46	6.19	5.98	5.81	5.55	5.35	5.20	5.09	4.99
17	15.72	10.66	8.73	7.68	7.02	6.56	6.22	5.96	5.75	5.58	5.32	5.13	4.99	4.87	4.78
18	15.38	10.39	8.49	7.46	6.81	6.35	6.02	5.76	5.56	5.39	5.13	4.94	4.80	4.68	4.59
19	15.08	10.16	8.28	7.27	6.62	6.18	5.85	5.59	5.39	5.22	4.97	4.78	4.64	4.52	4.43
20	14.82	9.95	8.10	7.10	6.46	6.02	5.69	5.44	5.24	5.08	4.82	4.64	4.49	4.38	4.29
21	14.59	9.77	7.94	6.95	6.32	5.88	5.56	5.31	5.11	4.95	4.70	4.51	4.37	4.26	4.17
22	14.38	9.61	7.80	6.81	6.19	5.76	5.44	5.19	4.99	4.83	4.58	4.40	4.26	4.15	4.06
23	14.20	9.47	7.67	6.70	6.08	5.65	5.33	5.09	4.89	4.73	4.48	4.30	4.16	4.05	3.96
24	14.03	9.34	7.55	6.59	5.98	5.55	5.23	4.99	4.80	4.64	4.39	4.21	4.07	3.96	3.87
25	13.88	9.22	7.45	6.49	5.89	5.46	5.15	4.91	4.71	4.56	4.31	4.13	3.99	3.88	3.79
26	13.74	9.12	7.36	6.41	5.80	5.38	5.07	4.83	4.64	4.48	4.24	4.06	3.92	3.81	3.72
27	13.61	9.02	7.27	6.33	5.73	5.31	5.00	4.76	4.57	4.41	4.17	3.99	3.86	3.75	3.66
28	13.50	8.93	7.19	6.25	5.66	5.24	4.93	4.69	4.50	4.35	4.11	3.93	3.80	3.69	3.60
29	13.39	8.85	7.12	6.19	5.59	5.18	4.87	4.64	4.45	4.29	4.05	3.88	3.74	3.63	3.54
30	13.29	8.77	7.05	6.12	5.53	5.12	4.82	4.58	4.39	4.24	4.00	3.82	3.69	3.58	3.49
35	12.90	8.47	6.79	5.88	5.30	4.89	4.59	4.36	4.18	4.03	3.79	3.62	3.48	3.38	3.29
40	12.61	8.25	6.59	5.70	5.13	4.73	4.44	4.21	4.02	3.87	3.64	3.47	3.34	3.23	3.14
50	12.22	7.96	6.34	5.46	4.90	4.51	4.22	4.00	3.82	3.67	3.44	3.27	3.41	3.04	2.95
60	11.97	7.77	6.17	5.31	4.76	4.37	4.09	3.86	3.69	3.54	3.32	3.15	3.02	2.91	2.83
70	11.80	7.64	6.06	5.20	4.66	4.28	3.99	3.77	3.60	3.45	3.23	3.06	2.93	2.83	2.74
80	11.67	7.54	5.97	5.12	4.58	4.20	3.92	3.70	3.53	3.39	3.16	3.00	2.87	2.76	2.68
90	11.57	7.47	5.91	5.06	4.53	4.15	3.87	3.65	3.48	3.34	3.11	2.95	2.82	2.71	2.63
100	11.50	7.41	5.86	5.02	4.48	4.11	3.83	3.61	3.44	3.30	3.07	2.91	2.78	2.68	2.59
120	11.38	7.32	5.78	4.95	4.42	4.04	3.77	3.55	3.38	3.24	3.02	2.85	2.72	2.62	2.53
150	11.27	7.24	5.71	4.88	4.35	3.98	3.71	3.49	3.32	3.18	2.96	2.80	2.67	2.56	2.48
200	11.15	7.15	5.63	4.81	4.29	3.92	3.65	3.43	3.26	3.12	2.90	2.74	2.61	2.51	2.42
250	11.09	7.10	5.59	4.77	4.25	3.88	3.61	3.40	3.23	3.09	2.87	2.71	2.58	2.48	2.39
300	11.04	7.07	5.56	4.75	4.22	3.86	3.59	3.38	3.21	3.07	2.85	2.69	2.56	2.46	2.37
400	10.99	7.03	5.53	4.71	4.19	3.83	3.56	3.35	3.18	3.04	2.82	2.66	2.53	2.43	2.34
500	10.96	7.00	5.51	4.69	4.18	3.81	3.54	3.33	3.16	3.02	2.81	2.64	2.52	2.41	2.33
600	10.94	6.99	5.49	4.68	4.16	3.80	3.53	3.32	3.15	3.01	2.80	2.63	2.51	2.40	2.32
750	10.91	6.97	5.48	4.67	4.15	3.79	3.52	3.31	3.14	3.00	2.78	2.62	2.49	2.39	2.31
1000	10.89	6.96	5.46	4.65	4.14	3.78	3.51	3.30	3.13	2.99	2.77	2.61	2.48	2.38	2.30

Table A.3 (continued)

F Distribution: Critical Values of F (0.1% significance level)

	25	30	35	40	50	60	75	100	150	200
v ₂ 1 2 3 4 5	999.46	999.47	6.28e05 999.47 125.17 45.23 24.72	999.47	999.48	999.48	999.49	999.49	999.49	999.49
6	16.85	16.67	16.54	16.44	16.31	16.21	16.12	16.03	15.93	15.89
7	12.69	12.53	12.41	12.33	12.20	12.12	12.04	11.95	11.87	11.82
8	10.26	10.11	10.00	9.92	9.80	9.73	9.65	9.57	9.49	9.45
9	8.69	8.55	8.46	8.37	8.26	8.19	8.11	8.04	7.96	7.93
10	7.60	7.47	7.37	7.30	7.19	7.12	7.05	6.98	6.91	6.87
11	6.81	6.68	6.59	6.52	6.42	6.35	6.28	6.21	6.14	6.10
12	6.22	6.09	6.00	5.93	5.83	5.76	5.70	5.63	5.56	5.52
13	5.75	5.63	5.54	5.47	5.37	5.30	5.24	5.17	5.10	5.07
14	5.38	5.25	5.17	5.10	5.00	4.94	4.87	4.81	4.74	4.71
15	5.07	4.95	4.86	4.80	4.70	4.64	4.57	4.51	4.44	4.41
16	4.82	4.70	4.61	4.54	4.45	4.39	4.32	4.26	4.19	4.16
17	4.60	4.48	4.40	4.33	4.24	4.18	4.11	4.05	3.98	3.95
18	4.42	4.30	4.22	4.15	4.06	4.00	3.93	3.87	3.80	3.77
19	4.26	4.14	4.06	3.99	3.90	3.84	3.78	3.71	3.65	3.61
20	4.12	4.00	3.92	3.86	3.77	3.70	3.64	3.58	3.51	3.48
21	4.00	3.88	3.80	3.74	3.64	3.58	3.52	3.46	3.39	3.36
22	3.89	3.78	3.70	3.63	3.54	3.48	3.41	3.35	3.28	3.25
23	3.79	3.68	3.60	3.53	3.44	3.38	3.32	3.25	3.19	3.16
24	3.71	3.59	3.51	3.45	3.36	3.29	3.23	3.17	3.10	3.07
25	3.63	3.52	3.43	3.37	3.28	3.22	3.15	3.09	3.03	2.99
26	3.56	3.44	3.36	3.30	3.21	3.15	3.08	3.02	2.95	2.92
27	3.49	3.38	3.30	3.23	3.14	3.08	3.02	2.96	2.89	2.86
28	3.43	3.32	3.24	3.18	3.09	3.02	2.96	2.90	2.83	2.80
29	3.38	3.27	3.18	3.12	3.03	2.97	2.91	2.84	2.78	2.74
30	3.33	3.22	3.13	3.07	2.98	2.92	2.86	2.79	2.73	2.69
35	3.13	3.02	2.93	2.87	2.78	2.72	2.66	2.59	2.52	2.49
40	2.98	2.87	2.79	2.73	2.64	2.57	2.51	2.44	2.38	2.34
50	2.79	2.68	2.60	2.53	2.44	2.38	2.31	2.25	2.18	2.14
60	2.67	2.55	2.47	2.41	2.32	2.25	2.19	2.12	2.05	2.01
70	2.58	2.47	2.39	2.32	2.23	2.16	2.10	2.03	1.95	1.92
80	2.52	2.41	2.32	2.26	2.16	2.10	2.03	1.96	1.89	1.85
90	2.47	2.36	2.27	2.21	2.11	2.05	1.98	1.91	1.83	1.79
100	2.43	2.32	2.24	2.17	2.08	2.01	1.94	1.87	1.79	1.75
120	2.37	2.26	2.18	2.11	2.02	1.95	1.88	1.81	1.73	1.68
150	2.32	2.21	2.12	2.06	1.96	1.89	1.82	1.74	1.66	1.62
200	2.26	2.15	2.07	2.00	1.90	1.83	1.76	1.68	1.60	1.55
250	2.23	2.12	2.03	1.97	1.87	1.80	1.72	1.65	1.56	1.51
300	2.21	2.10	2.01	1.94	1.85	1.78	1.70	1.62	1.53	1.48
400	2.18	2.07	1.98	1.92	1.82	1.75	1.67	1.59	1.50	1.45
500	2.17	2.05	1.97	1.90	1.80	1.73	1.65	1.57	1.48	1.43
600	2.16	2.04	1.96	1.89	1.79	1.72	1.64	1.56	1.46	1.41
750	2.15	2.03	1.95	1.88	1.78	1.71	1.63	1.55	1.45	1.40
1000	2.14	2.02	1.94	1.87	1.77	1.69	1.62	1.53	1.44	1.38

Critical values of chi-square (right tail)

Significance level (α)

Degrees of					,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	•		
freedom	00	075	0.5	0	4	05	025	01
(<i>df</i>)	.99	.975	.95	.9	.1	.05	.025	.01
1		0.001	0.004	0.016	2.706	3.841	5.024	6.635
2	0.020	0.051	0.103	0.211	4.605	5.991	7.378	9.210
3	0.115	0.216	0.352	0.584	6.251	7.815	9.348	11.345
4	0.297	0.484	0.711	1.064	7.779	9.488	11.143	13.277
5	0.554	0.831	1.145	1.610	9.236	11.070	12.833	15.086
6	0.872	1.237	1.635	2.204	10.645	12.592	14.449	16.812
7	1.239	1.690	2.167	2.833	12.017	14.067	16.013	18.475
8	1.646	2.180	2.733	3.490	13.362	15.507	17.535	20.090
9	2.088	2.700	3.325	4.168	14.684	16.919	19.023	21.666
10	2.558	3.247	3.940	4.865	15.987	18.307	20.483	23.209
11	3.053	3.816	4.575	5.578	17.275	19.675	21.920	24.725
12	3.571	4.404	5.226	6.304	18.549	21.026	23.337	26.217
13	4.107	5.009	5.892	7.042	19.812	22.362	24.736	27.688
14	4.660	5.629	6.571	7.790	21.064	23.685	26.119	29.141
15	5.229	6.262	7.261	8.547	22.307	24.996	27.488	30.578
16	5.812	6.908	7.962	9.312	23.542	26.296	28.845	32.000
17	6.408	7.564	8.672	10.085	24.769	27.587	30.191	33.409
18	7.015	8.231	9.390	10.865	25.989	28.869	31.526	34.805
19	7.633	8.907	10.117	11.651	27.204	30.144	32.852	36.191
20	8.260	9.591	10.851	12.443	28.412	31.410	34.170	37.566
21	8.897	10.283	11.591	13.240	29.615	32.671	35.479	38.932
22	9.542	10.982	12.338	14.041	30.813	33.924	36.781	40.289
23	10.196	11.689	13.091	14.848	32.007	35.172	38.076	41.638
24	10.856	12.401	13.848	15.659	33.196	36.415	39.364	42.980
25	11.524	13.120	14.611	16.473	34.382	37.652	40.646	44.314
26	12.198	13.844	15.379	17.292	35.563	38.885	41.923	45.642
27	12.879	14.573	16.151	18.114	36.741	40.113	43.195	46.963
28	13.565	15.308	16.928	18.939	37.916	41.337	44.461	48.278
29	14.256	16.047	17.708	19.768	39.087	42.557	45.722	49.588
30	14.953	16.791	18.493	20.599	40.256	43.773	46.979	50.892
40 50	22.164 29.707	24.433	26.509	29.051	51.805	55.758	59.342	63.691
50		32.357	34.764	37.689	63.167	67.505	71.420	76.154
60 70	37.485	40.482	43.188	46.459	74.397	79.082	83.298	88.379
70 80	45.442	48.758	51.739	55.329	85.527	90.531	95.023	100.425
80 100	53.540	57.153	60.391	64.278	96.578	101.879	106.629	112.329
100	61.754	65.647	69.126	73.291	107.565	113.145	118.136	124.116
1000	70.065	74.222	77.929	82.358	118.498	124.342	129.561	135.807