

```
#include <iostream>
#include <iomanip>
#include <cmath>
#include <ctime> //Random Number Generator
```

```
// Goal to match Average Case with Monte Carlo
using namespace std;
```

```
int insertionA10(int A[], int n); // in practise they have
to be sorted
```

```
int main()
{
    double MonteCarlo;
    double average_calculation;
    int reapeation = 10000;
    int bound = 10000;
    int n[] = {100, 500, 1000, 2500, 3000, 3500}; // values
for n
```

```
    srand(time(NULL)); // Utilizes the computer's internal
clock to determine the seed, which constantly changes as
time progresses. It's crucial to note that if the seed
remains constant, the sequence of numbers will reapeation
with each execution of the program.
```

```
cout << setw(5) << "Size Input" << setw(27) << "Average  
Calculated" << setw(22) << "Monte Carlo" << endl;
```

```
cout <<  
"===== "  
===== " << endl;
```

```
for (int i = 0; i < sizeof(n); i++) {  
    long long int total_steps = 0;  
    int size_input = n[i];  
    int *arr = new int[size_input];
```

```
    // Generate ten thousand random sequences  
    for (int j = 0; j < reapeation; j++) {  
        for (int k = 0; k < size_input; k++) {  
            arr[k] = rand() % bound;}  
            int insertion = insertionA10(arr, size_input); //  
calling insertionA10  
            total_steps += insertion; } // update total_steps
```

```
    // Monte Carlo  
    MonteCarlo = static_cast<double>(total_steps) /  
reapeation;  
    // The average calculated value  $A_i(n) = n^2/4 + 3n/4$ 
```

```

    average_calculation = (pow(size_input, 2) / 4) + (3 *
size_input / 4);

    cout << setprecision(1) << fixed << setw(7) <<
size_input << setw(25) << average_calculation << setw(26)
<< MonteCarlo << endl;}

    return 0;
}

```

```

int insertionA10(int A[], int n)
{
    int steps = 0;

    A[0] = -32768; // The smallest attainable integer using a
2-byte

    int i, j, temp;
    for (i = 1; i <= n; i++) {
        j = i;

        while (A[j] < A[j - 1]) { //introducing temporary
variable

            temp = A[j]; // assigning first value to temporary
            A[j] = A[j - 1]; // assigning value of second to
first

            A[j - 1] = temp; // assigning temporary variable to
second

            j--;

            steps++; } // need to add counter in while loop
    }
}

```

```
    steps++;} // need to add another counter for edge cases  
because it is not count first or last comparison because  
they might not need comparison  
    return steps;  
}
```

// In summary, the fact that the real average values closely match the calculated averages across various input sizes indicates that the Monte Carlo simulation effectively approximates the practical performance of algorithm A10. This serves as strong validation for the accuracy of the simulation approach.