Application of the chiral forces to elctroweak processes

Vitalii Urbanevych

Ph.D. thesis written under the supervision of dr. hab Roman Skibiński at the Jagiellonian University, Faculty of Physics, Astronomy and Applied Computer Science, Kraków,

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CHAPTER 1

PLAN

- Why we study few nucleon systems
 - Strong interactions (2N and 3N force investigation; QCD, relativistic effects)
 - Electro-magnetic processes (electrons-, photons-induced reactions) (Arenhovel did ...)
 - Weak interactions (neutrons)
- Nuclear forces used in the thesis
 - AV18
 - Chiral (scs, sms; difference between chiral models; regularization problem)
- Currents used in the thesis (regularization of currents to be done)
- Formalism & numerical methods
 - Lippman-Schwinger eq
 - Schrodinger eq for deuteron; wave functions (sms) for deuteron figures, binding energy
 - Three body: Fadeev eq. for bound (He3, H3) and scattering states
 - Siegert theorem?
 - Partial wave decomposition, states $(pq\alpha)$, Jakobi momenta; operators in PW decomp. (current); Mathematica for PW
 - Theoretical uncertainties: truncation error, cut-off dependency, chiral order dependency
- Results (find everything what I have calculated: all processes and energies
 - H2 photodisintegration
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 - Pion capture

- Summary
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Why we study few nucleon systems

The study of light nuclei and their reactions for the decades has been serving as an easiest way to investigate NN systems and forces inside the atoms. Convenient way to proceed may be an interaction of nucleus with other nucleus, particles or electromagnetic probes in elastic or inelastic scattering. It is possible to perform such an experiments and check if theory works. People take into account that interactions may be caused by different forces and therefore should be described in different ways. It can be either strong, weak or electromagnetic interaction. It depends on the type of particle being scattered and the target which reaction it is.

In order to proper describe the nuclear reactions many components should be taken into account. First of all, different forces may act on the participants.

The strong nuclear force appear inside the nuclei and among others bound neutrons and protons together. The description of strong interactions is extremely difficult as it deals not only with nucleon, but with their constituents: quarks and gluons. Quantum chromodynamics (QCD) is a modern theory describing strong interactions, but it has also its limitations and, at the moment, it is not useful at low energies ($Q^2 \lesssim 1 GeV^2$). So other approaches are coming into the scene such as chiral effective theory, lattice calculation and others [1].

Starting the study of three- (and more) nucleon systems it was found that strong 2N force is not enough to describe the system and 3N force was introduced. The first applications of such a force showed that it brings sufficient contribution and cannot be ignored [2]. Whereas the first applications included only early "realistic" potential, the latter investigations only proved this statements [3, 4]. It was also used to construct four-nucleon (4N) bound state [5].

Electromagnetic force appears between charged particles like protons, electrons or pions. Also, the force is transferred between charged particles with a photon, so in photon-and electron- scatterings on the nuclei an electromagnetic force is playing an important role. Arenhövel [6] studied electromagnetic process - deuteron photodisintegration, applying different approaches and comparing the results with experimental data.

The weak force...

...

Nuclear forces used in the thesis

In order to construct a potential people often use phenomenological or semi-phenomenological approaches. It allows to combine theoretical knowledge about processes and experimental data.

One of such potentials, which was used in current thesis is Argonne V18 (AV18) [7] In order to construct NN force, authors combine analytical electromagnetic and one-pion-exchange parts with phenomenological one, fitting parameters to the Nijmegen partial-wave analysis of pp and np data [8]. Authors showed, that AV18 potential delivers good results in the description of nucleon scattering data as well as deuteron properties.

In the early 1990-ies Weinberg [9,10] introduced an idea of using a most general Lagrangian satisfying assumed symmetry principles and in particular spontaneously broken

chiral symmetry to describe nuclear interactions at low energies. This idea together with effective field theory (EFT) of QCD led to the development of the Chiral Effective Field Theory (χ EFT) which nowadays has become one of the most advanced approach to describing nuclear reactions at low energies.

For the EFT it is very important to define a quantity, which powers will determine a perturbation order. In the χ EFT there are two natural scales: so-called soft scale - the mass of Pion $Q \sim M_{\pi}$ and hard scale - $\Lambda_{\chi} \sim 1~GeV$ (chiral symmetry breaking scale). The ratio between these two scales $(Q/\Lambda_{\chi})^{\nu}$ is being used as an expansion parameter in χ EFT with power ν .

Considering so-called irreducible (the diagrams that cannot be split by cutting nucleon lines), Weinberg [9, 10] came to the identity for the powers of such diagrams

$$\nu_W = 4 - A - 2C + 2L + \sum_i \Delta_i, \tag{1.1}$$

where

$$\Delta_i \equiv d_i + \frac{n_i}{2} - 2 \tag{1.2}$$

In Eq. (1.1), C is a number of pieces which are connected, L - the number of loops in the graph. In Eq. (1.2), n_i is a number of nucleon field operators, d_i - the number of insertions (or derivatives) of M_{π} .

The further analysis of Eq. (1.1) revealed some problems which occur for particular values of parameters in the equation, namely negative values of ν_W are possible. In order to deal with that, Eq. (1.1) was slightly modified adding 3A - 6 to it [11,12]:

$$\nu = \nu_W + 3A - 6 = -2 + 2A - 2C + 2L + \sum_i \Delta_i \tag{1.3}$$

In χ EFT the first order is called "leading order" (LO, $\nu=0$) and it is followed by next-to-leading order (NLO, $\nu=2$) ¹, next-to-next-to-leading order (N²LO, $\nu=3$) and so on. At each chiral order, particular interaction diagrams are described. At LO there is a diagram which consists of 2 contact terms and the diagram implying one-pion exchange. Both diagrams reflect only 2NF as well as diagrams at NLO, where more contact terms are introduced together with two-pion exchange diagrams. Each subsequent order includes more and more sophisticated diagrams describing nucleons interaction, 3NF appears at N²LO while 4NF contributions are firstly described at N³LO. So there is a systematic way to include all the forces from simplest diagrams at LO and gradually adding more and more terms. It is also beneficial in the way that one can obtain results using chiral potential at different orders and track which one gives larger or smaller contribution (changes in the final results). The highest order for which there is a derived term in potential is N⁴LO at the moment. Nevertheless leading F-wave contact interactions from N⁵LO are included in the N⁴LO+ potential, which is regarded as a best possible potential within my work.

There are a number of another approaches within χ EFT utilized. The group of Piarulli is using quite similar approach, including the same chiral potentials with minor differences [13, 14].

Machleidt, Ekstrim, pion-less EFT, Lattice EFT(Mesissner)

¹The $\nu=1$ order is completely vanished due to parity and time-reversal invariance, so next-to-leading order stands for the second order of expansion.

The χEFT may be applied both in coordinate and momentum spaces. Nevertheless in both cases it requires regularization which is cutting low coordinate values in order to avoid infinities (or high momentum values - in momentum space). The semilocal momentum-space regularized (SMS) potential is being regularized using the Gaussian form factor $F(\bar{l}^2)$:

$$F(\vec{l}^2) = e^{-\frac{\vec{l}^2 + M_\pi^2}{\Lambda^2}},\tag{1.4}$$

where M_{π} is an effective pion mass and Λ - is a cutoff parameter.

The form factor from Eq. (1.4), being used together with Feynman propagator, ensures that long-range part of the forces has no singularities.

The value at which the cut is applied (cut-off value) is not fixed and usually calculations are being performed for different cut-off values. The comparison of such results may reveal stronger or weaker dependance and in perfect case one will come up with such a potential, were the cut will not affect results much. On the Fif. 1.1 I show values of the 2N potential $\langle \vec{p}|V|\vec{p}'\rangle$ as a function on the momentum $|\vec{p}|$ with fixed value $|\vec{p}'|=0.054[\text{fm}]$.

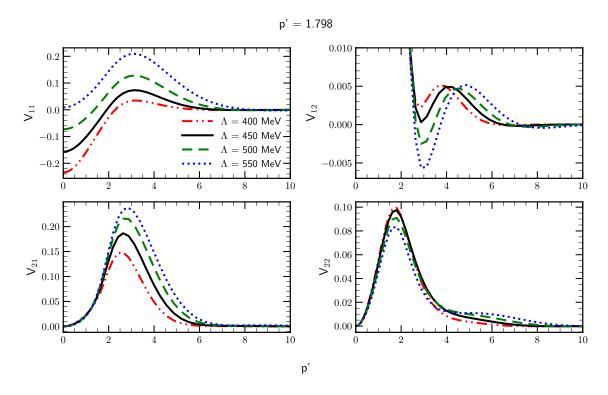


Figure 1.1: Potential components as a function on the momentum p with fixed value of the momentum p'=1.798 [fm?].

The potential may be transformed from coordinate to momentum space (or vice versa), but it is important at which frame the regularization was performed and what was a regularization function. That's why there are different versions of chiral potential. One is semilocal coordinate-space regularized (SCS) potential [15] and another one is similar, but with regularization applied in momentum space (SMS potential) [16].

Currents

CHAPTER 2

FORMALISM & NUMERICAL METHODS

Despite the deuteron problem was solved long time ago, I will describe it briefly in order to introduce the notation and formalism. For 3N case only extension will be needed.

In order to calculate any observable for the deuteron photodisintegration, one has to find a nuclear matrix elements:

$$N^{\mu} = \langle \Psi_f \vec{P}_f \mid \frac{1}{e} J^{\mu}(0) \mid \Psi_i \vec{P}_i \rangle = \langle p'(l's')j'm'_j t'm'_t \vec{P}_f \mid J^{\mu} \mid \phi_d m_d \vec{P}_i \rangle, \tag{2.1}$$

where J^{μ} is a four-vector current operator which acts between initial and final two-nucleon states.

2.1 Deuteron bound state

Let's find a deuteron bound state wave function ϕ_d . The time-independent Schrödinger equation for two particles in such case will be:

$$(H_0 + V) \mid \psi_{12} \rangle = E_d \mid \psi_{12} \rangle, \tag{2.2}$$

with a kinetic energy H_0 and potential V. The kinetic energy H_0 can be represented in terms of relative and total momenta of the particles:

$$H_0 = \frac{\vec{p}_1^2}{2m_1} + \frac{\vec{p}_2^2}{2m_2} = \frac{\vec{p}^2}{2\mu} + \frac{\vec{\mathcal{P}}^2}{2M},\tag{2.3}$$

where relative and total momenta are defined as follows:

$$\vec{p} = \frac{(m_1 \vec{p}_1 - m_2 \vec{p}_2)}{m_1 + m_2} \tag{2.4}$$

$$\vec{\mathcal{P}} = \vec{p_1} + \vec{p_2} \tag{2.5}$$

and $M = m_1 + m_2$ is a total mass, $\mu = \frac{m_1 m_2}{M}$ is a relative mass of two nucleons, $\vec{p_i}$ is a momentum of i-th particle.

Potential V is assumed to depend on the relative degrees of freedom, so Eq. (2.2) may be decomposed into two separated equations:

$$\frac{\vec{p}^2}{2u} \langle \vec{p} \mid \Psi_{int} \rangle + \int d\vec{p}' \langle \vec{p} \mid V \mid \vec{p}' \rangle \langle \vec{p}' \mid \Psi_{int} \rangle = (E_d - E_{c.m.}) \langle \vec{p} \mid \Psi_{int} \rangle \tag{2.6}$$

$$\frac{\vec{\mathcal{P}}^2}{2M} \langle \mathcal{P} \mid \Psi_{c.m.} \rangle = E_{c.m.} \langle \mathcal{P} \mid \Psi_{c.m.} \rangle, \tag{2.7}$$

with $\langle \vec{p}, \vec{\mathcal{P}} | H_0 | \Psi_{12} \rangle = \frac{\vec{p}^2}{2\mu} \langle \vec{p} | \Psi_{int} \rangle + \frac{\vec{\mathcal{P}}^2}{2M} \langle \mathcal{P} | \Psi_{c.m.} \rangle$. So $\Psi_{c.m.}$ is a component of total wave function, which reflects a deuteron as a single object with momentum $\vec{\mathcal{P}}$ while Ψ_{int} is an internal wave function describing interaction between nucleons. Basis state $|\vec{p}\rangle$ obeys a completeness equation:

$$\int d^3 \vec{p} \, |\vec{p}\rangle \, \langle \vec{p}| = 1 \tag{2.8}$$

Eq.(2.6) is basically a Schrödinger equation for one particle with mass μ and Eq.(2.7) can be regarded as a Schrödinger equation for particle with mass M in a free motion. Assuming that deuteron is at rest $(E_{c.m.} = 0)$ we can stick to the Eq.(2.6) only. So that:

$$\frac{\vec{p}^2}{2\mu} \langle \vec{p} \mid \Psi_{int} \rangle + \int d\vec{p}' \langle \vec{p} \mid V \mid \vec{p}' \rangle \langle \vec{p}' \mid \Psi_{int} \rangle = E_d \langle \vec{p} \mid \Psi_{int} \rangle$$
 (2.9)

Working in 3 dimensional space is difficult (especially numerically) so i introduce the partial-wave representation (PWD) of the momentum state in the following form:

$$|\vec{p}\rangle = |p\alpha\rangle \equiv |p(ls)jm_j\rangle |tm_t\rangle,$$
 (2.10)

where we introduce quantum numbers l, s ,j ,t as orbital angular momentum, total spin, total angular momentum and total isospin respectively. m_j and m_t are isospin and spin projections.

Yet one can introduce simpler states than it is in (2.10).

$$|p(ls)jm_j\rangle = \sum_{m_l} c(lsj; m_l, m_j - m_l, m_j) |plm_l\rangle |s m_j - m_l\rangle$$
 (2.11)

Also we can decompose spin and isospin states as follows:

$$|sm_s\rangle = \sum_{m_1} c(\frac{1}{2}\frac{1}{2}s; m_1, m_s - m_1, m_s) |\frac{1}{2}m_1\rangle |\frac{1}{2}m_s - m_1\rangle$$
 (2.12)

$$|tm_t\rangle = \sum_{\nu_1} c(\frac{1}{2}\frac{1}{2}t; \nu_1, m_t - \nu_1, m_t) |\frac{1}{2}\nu_1\rangle |\frac{1}{2}m_t - \nu_1\rangle$$
 (2.13)

In Eqs.(2.11) -(2.13), c(...) are Clebsh-Gordon coefficients. Nucleons are spin $\frac{1}{2}$ particles, and also we treat proton and neutron as the same particle in different isospin states, so that isospin is $\nu_1 = \frac{1}{2}$ for proton and $\nu_1 = -\frac{1}{2}$ for neutron.

The states $|plm_l\rangle$ from Eq.(2.11) are orthogonal, so that

$$\langle p'l'm'_l \mid plm_l \rangle = \frac{\delta(p-p')}{p^2} \delta_{ll'} \delta_{m_l m'_l}$$
 (2.14)

and also satisfy the completeness relation:

$$\sum_{l=0}^{\infty} \sum_{m_l=-l}^{l} \int dp p^2 \mid p l m_l \rangle \langle p l m_l \mid = 1$$
 (2.15)

These states also fulfill a relation

$$\langle \vec{p}' \mid plm_l \rangle = \frac{\delta(|\vec{p}'| - p)}{p^2} Y_{lm_l}(\hat{p}'), \qquad (2.16)$$

where $Y_{lm}(\hat{p}')$ is a spherical harmonic and 'hat' means a unit vector in direction of \vec{p} :

$$\vec{p} \equiv |\vec{p}|\hat{p} \equiv p\hat{p} \tag{2.17}$$

Nucleons are fermions so exchanging leads to antisymmetry of the wave function. In PWD it leads to the requirement which can be expressed as:

$$(-1)^{l+s+t} = -1 (2.18)$$

Taking into account Eq.(2.18), one can find only one possible PWD state combination for the deuteron bound state(under ... experimental evidence): 2 coupled channels for l=0,2; s=1; j=1 and $t=m_t=0$. These 2 channels are usually denoted as 3S_1 and 3D_1 and corresponding wave functions are $\phi_0(p)$ and $\phi_2(p)$:

$$\phi_l(p) = \langle pl | \Psi_{int} \rangle = \langle p(l1) 1 m_d | \langle 00 | \Psi_{int} \rangle; l = 0, 2. \tag{2.19}$$

So with a new basis Eq.(2.9) takes a form:

$$\frac{\vec{p}^2}{2\mu}\phi_l(p) + \sum_{l'=0,2} \int dp' p'^2 \langle plm_l \mid V \mid p'l'm_l' \rangle \phi_{l'}(p) = E_d \phi_l(p), \tag{2.20}$$

for l=0,2. In case one does not have a matrix elements for the potential $\langle plm_l | V | p'l'm'_l \rangle$ in analytical form, but only values for some grid of points, there is still one complication in the Eq.(2.20) - integration. In order to get rid of the integral I use a Gaussian quadrature method of numerical integration [17]. It allows to replace an integral by the weighted sum: $\int_a^b f(x)dx = \sum_{i=1}^n \omega_i f(x_i)$ In current work I used 72 points in the interval from 0 to 50fm. Using this method, Eq.(2.9) becomes

$$\frac{\vec{p}^2}{2\mu}\phi_l(p) + \sum_{l'=0} \sum_{j=0}^{N} \omega_j p_j'^2 \langle p_j l m_l \mid V \mid p_j' l' m_l' \rangle \phi_{l'}(p) = E_d \phi_l(p), \tag{2.21}$$

I solve this equation as an eigenvalue problem $M\Psi = E_n\Psi$ and in that way find simultaneously wave function values and binding energy E_n . The binding energy E_n calculated with potentials of different chiral orders is presented on the Fig. 2.1.

2.2 2N scattering state

2.2.1 The Lippmann-Schwinger equation

Let us start from the time-independent formulation of the scattering process. In such a case Hamiltonian will be:

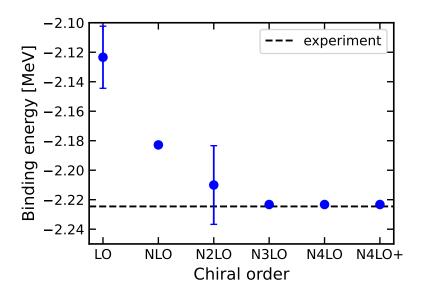


Figure 2.1: Deuteron binding energy calculated using chiral potential with different chiral orders. Error bands represent a standard deviation of the calculated binding energy with respect to the cutoff parameter Λ . Experimental data is taken from [18]

$$H = H_0 + V, \tag{2.22}$$

where H_0 is a kinetic energy operator $H_0 = \frac{\vec{p}^2}{2m}$ and V is a nucleon-nucleon interaction. For a free particle motion, V will be absent and we will denote an energy eigenstate as $|\vec{p}\rangle$ - a free particle state. In the case of the scattering process, the eigenstate will differ from $|\phi\rangle$, but in case of elastic scattering (which we re interested in) the energy eigenvalue E should be the same.

So these two states fulfill Schrödinger equations for such scattering process:

$$\begin{cases} H_0 \mid \vec{p} \rangle &= E \mid \vec{p} \rangle \\ (H_0 + V) \mid \psi \rangle &= E \mid \psi \rangle \end{cases}$$
 (2.23)

We are interested in solution for Eq. (2.23), so that $|\psi\rangle \rightarrow |\vec{p}\rangle$ as $V \rightarrow 0$ and both $|\psi\rangle$ and $|\vec{p}\rangle$ have the same energy eigenvalues E. As we have scattering process, the energy spectra for both operators H_0 and $H_0 + V$ are continuous.

From Eq. (2.23) follows that

$$|\psi\rangle = \frac{1}{E - H_0} V |\psi\rangle + |\vec{p}\rangle, \qquad (2.24)$$

where $|\vec{p}\rangle$ is a solution to the free-particle Schrödinger equation

$$H_0 |\vec{p}\rangle = E |\vec{p}\rangle, \tag{2.25}$$

with same energy eigenvalue [19]. In addition, it guarantees that application of the operator $(E - H_0)$ to the (2.24) results in the second equation from the system (2.23).

In order to deal with a singular operator $\frac{1}{E-H_0}$ in eq.(2.24), the well-known technique is to make such an operator complex by adding small imaginary number to the denominator so Eq.(2.24) becomes

$$|\psi\rangle = G_0(E \pm i\epsilon)V |\psi\rangle + |\vec{p}\rangle,$$
 (2.26)

where G_0 is a free propagator:

$$G_0(z) = \frac{1}{z - H_0} \tag{2.27}$$

Solution with $G_0(E-i\epsilon)$ corresponds to the incoming spherical wave, while $G_0(E+i\epsilon)$ - to the outgoing one. Since we are interested in the scattering process, only the (+) sign survives.

Eq. (2.26) is known as a Lippmann-Schwinger equation (LSE) and using the definition of the transition operator t:

$$t \left| \vec{p} \right\rangle = V \left| \psi \right\rangle \tag{2.28}$$

we can rewrite it as

$$|\psi\rangle = (1 + G_0(E + i\epsilon)Vt)|\vec{p}\rangle \tag{2.29}$$

With substitution of Eq. (2.26) into Eq. (2.28) we can find an explicit form of the t operator:

$$t | \vec{p} \rangle = V G_0(E + i\epsilon) V | \psi \rangle + V | \vec{p} \rangle =$$

$$= V G_0(E + i\epsilon) t | \vec{p} \rangle + V | \vec{p} \rangle$$
(2.30)

Getting rid of the initial state $|\vec{p}\rangle$ in the Eq. (2.30) we can get a LSE for the transition operator in the iterative form:

$$t = V + VG_0Vt = = V + VG_0V + VG_0VG_0V + \dots$$
 (2.31)

In the partial-wave representation, LSE Eq. (2.30) may be written as:

$$\langle p'(l's')jt|t(E)|p(ls)jt\rangle = \langle p'(l's)jt|V|p(ls)jt\rangle +$$

$$+ \sum_{l''} \int_{0}^{\infty} dp''p''^{2} \langle p'(l's)jt|V|p''(l''s)jt\rangle$$

$$\times \frac{1}{E+i\epsilon-p''^{2}/m} \langle p''(l''s)jt|t(E)|p''(ls)jt\rangle \quad (2.32)$$

Using Eq. (2.29) we can write Eq. (2.1) as

$$N^{\mu} = \langle \phi m_p m_n | \left(1 + G_0(E + i\epsilon)Vt \right) \frac{1}{e} J^{\mu}(0) | \Psi_i \vec{P}_i \rangle$$
 (2.33)

2.3 3N bound state

The 3N bound state is derived from a general Schrödinger for 3N system and its total wave function obeys the following equation:

$$|\Psi_i\rangle = G_0(E + i\epsilon) \sum_{j=1}^{3} (V_j + V_4^j) |\Psi_i\rangle,$$
 (2.34)

where G_0 is a free propagator from Eq. (2.27), V_i - is a two-body potential acting between nucleons k and l (j, k and l - are the numbers of each nucleon) and $V_4^{\mathfrak{I}}$ is a component of three-body potential $V_4 = \sum_{j=1}^3 V_4^j$. E - is a binding energy.

Eq. (2.34) can be split into 3 independent equations for so-called Faddeev components $|\psi_j\rangle$

$$|\Psi_i\rangle = \sum_{j=1}^3 |\psi_j\rangle. \tag{2.35}$$

Using Eq. (2.35) one can decompose Eq. (2.34) into separate equations for each Faddeev component:

$$|\psi_i\rangle = G_0(E + i\epsilon)(V_i + V_4^j)|\Psi_i\rangle, \qquad (2.36)$$

Next I introduce a permutation operator P, which is a combination of operators P_{ik} :

$$P = P_{12}P_{23} + P_{13}P_{32}. (2.37)$$

The operator component P_{jk} acting on the state interchange the momenta and quantum numbers of the nucleon number j and k.

Using Eq. (2.37) and Eq. (2.35), one can rewrite Eq. (2.36) in the following form:

$$|\psi_j\rangle = G_0(E+i\epsilon)t_jP|\psi_i\rangle + (1+G_0(E+i\epsilon)t_j)G_0(E+i\epsilon)V_4^j(1+P)|\psi_i\rangle, \qquad (2.38)$$

where t_j is a two-body t-operator which obeys Eq. (2.30) for corresponding two-body potential V_i .

2.4Photodisintegration transition amplitude for Nd state

Analogously to the bound state, one can express a nucleon-deuteron scattering state using a permutation operator Eq. (2.37)

$$\left|\Psi^{(-)}\right\rangle^{Nd} = \frac{1}{\sqrt{3}}(1+P)\left|\Psi_1^{(-)}\right\rangle^{Nd}$$
 (2.39)

A scattering state $|\Psi_1^{(-)}\rangle^{Nd}$ can be expressed in terms of asymptotic state $|\Phi_1^{Nd}\rangle$, where particles 2 and 3 form a deuteron and the third particle (number 1) is a nucleon which propagates freely with relative momentum \vec{q}_0 with respect to the deuteron:

$$\left|\Psi_{1}^{(-)}\right\rangle^{Nd} \equiv \lim_{\epsilon \to 0} i\epsilon G(E_{Nd} - i\epsilon) \left|\Phi_{1}^{Nd}\right\rangle$$

$$\left|\Phi_{1}^{Nd}\right\rangle \equiv \left|\Phi_{d(2,3)}\right\rangle \left|\vec{q}_{0}\right\rangle,$$
(2.40)

$$\left|\Phi_{1}^{Nd}\right\rangle \equiv \left|\Phi_{d(2.3)}\right\rangle \left|\vec{q}_{0}\right\rangle, \tag{2.41}$$

where $|\Phi_{d(2,3)}\rangle$ is a deuteron wave function and $|\vec{q}_0\rangle$ - a free particle state. E_{Nd} is a total energy of the 3N system:

$$E_{Nd} = E_d + \frac{3|\vec{q}_0|^2}{4m},\tag{2.42}$$

where E_d is a deuteron binding energy and m - nucleon mass.

The full propagator $G(E_{Nd})$ in this case takes a form:

$$G(z) = \frac{1}{z - (H_0 + \sum_{i=1}^4 V_i)}$$
 (2.43)

2.5 3N scattering state

As in Sec. 2.4, one can write an equation for the 3-nucleone scattering state:

$$\left|\Psi^{(-)}\right\rangle^{3N} = \frac{1}{\sqrt{3}} \left|\Psi_j^{(-)}\right\rangle^{3N} \tag{2.44}$$

with a set of corresponding equations for $\left|\Psi_{j}^{(-)}\right\rangle^{3N}$

$$\left|\Psi_{j}^{(-)}\right\rangle^{3N} \equiv \lim_{\epsilon \to 0} i\epsilon G(E_{3N} - i\epsilon) \left|\Phi_{j}^{3N}\right\rangle$$
 (2.45)

$$\left|\Phi_{j}^{3N}\right\rangle \equiv \frac{1}{\sqrt{2}}(1-P_{kl})\left|\vec{p}(kl)\vec{q}(j)\right\rangle$$
 (2.46)

$$E_{3N} = \frac{|\vec{p}|^2}{m} + \frac{3|\vec{q}|^2}{4m}, \tag{2.47}$$

2.6 Nuclear electromagnetic current

2.7 Theoretical uncertainties

Truncation error

As it was mention above, each subsequent order of chiral expansion provides us with more and more sophisticated potential which is expected to increase accuracy of data description. Starting from the leading order (LO) and coming next to N2LO, N3LO and so on, we take into account more Feynmann diagrams and in result potential is expected to provide us with more precise predictions for the regarded process and observable. But the chiral expansion (as any expansion) in principle can be continued up to the infinity, improving the resulting series. In practice we are limited by a finite, rather small, number of terms and we would like to find out the uncertainty appearing from cutting off remaining part of the expansion. This theoretical uncertainty is called a truncation error. Various ways of estimation its value have been proposed [20–24]. Such estimation is based on predictions at lower orders. It is worth adding that Bayesian analysis is also used for truncation error estimation

We use method proposed in [22]. Let's regard some observable $X^{i}(p)$ which is calculated at *i*-s order of chiral expansion with expansion parameter Q $(i = 0, 2, 3...)^{1}$. Here

 $^{^{1}}$ We do not have a first order of expansion because this term in chiral expansion is always vanished

p specifies a momentum scale of the current reaction in the center of mass frame (in the case of deuteron photodisintegration it would be a photon's momentum).

If I define a difference between observable at each subsequent orders as:

$$\Delta X^{(2)} = |X^{(2)} - X^{(0)}|, \Delta X^{(i>2)} = |X^{(i)} - X^{(i-1)}|, \tag{2.48}$$

then chiral expansion for X can be written as:

$$X = X^{(0)} + \Delta X^{(2)} + \Delta X^{(3)} + \dots + \Delta X^{(i)}.$$
 (2.49)

The truncation error at order i - $\delta X^{(i)}$ - is estimated using actual and expected values of the observable at higher orders as following:

$$\delta X^{(0)} = Q^2 |X^{(0)}|, (2.50)$$

$$\delta X^{(0)} = Q^{2} |X^{(0)}|, \qquad (2.50)$$

$$\delta X^{(i)} = \max_{2 \le j \le i} (Q^{i+1} |X^{(0)}|, Q^{i+1-j} |\Delta X^{(j)}|.) \qquad (2.51)$$

Additionally, following the [22] I use the actual high-order predictions in order to specify uncertainties so that:

$$\delta X^{(i)} \ge \max_{j,k} (|X^{j \ge i} - X^{k \ge i}|) \tag{2.52}$$

and to be conservative I use additional restriction:

$$\delta X^{(i)} \ge Q \delta X^{(i-1)}. \tag{2.53}$$

All the conditions above assume that we use the whole available information at hand.

Cutoff dependency

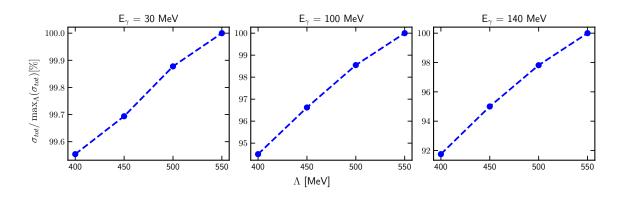


Figure 2.2: Total cross section of the deuteron photodisintegration process (normalized to the maximal cross section among all Λ) as a dependence on the cutoff parameter Λ for three photon energy E_{γ} values: 30, 100 and 140 MeV.

Another theoretical uncertainty comes from the choice of the cutoff parameter's value which was mentioned already.

and NLO corresponds to the quadratic term (number 2)

According to [16], where the SMS potential was presented, four values of the cutoff parameter Λ are recommended: 400, 450, 500 and 550 MeV. Using each of them one obtains different predictions which off course can further differ from actual (experimental) value. Therefore the choice of Λ value may affect a quality of the prediction.

Comparison of predictions obtained with different values of the cutoff parameter Λ is presented on the Fig. 2.2. Each subfigure shows a predictions for the total cross section as a function of the cutoff parameter for the photons energies 30, 100 and 140 MeV normalized to the maximum value among all cross sections obtained with various Λ (at the chiral order N⁴LO+). As we can see, there is almost linear dependance with positive linearity coefficient value: with higher Λ the cross section value increases as well. The noticeable is also the fact, that with higher photon's energy, the cutoff dependance becomes stronger: for $E_{\gamma} = 30$ MeV the maximal difference between predictions is around 0.5% while for 140 MeV it increases to more than 8%. This results are generally within our expectations that our model works better at smaller energies.

Other uncertainies

There are a plenty possibilities were uncertainties may appear. Taking into account that all the results include calculations, we can come up with a lot of places were numerical methods with limited precision come into the scene. First of all we have a potential which is being defined on some grid of points. So the choice of grid affect a final results' precision. The same grid is also used for numerical integration (e.g. in Eq. (2.21)) where the final integral is also dependant on the points. Usually, we use a grid ...values

In addition our approach is based on the partial wave decomposition which supposes that limited numer of partial waves are included (usually for 2N scattering we use $J^{max} = 4$ which corresponds to 18 partial waves).

Finally every computer calculations include limited machine precision which can be noticeable for a complex calculations.

CHAPTER 3

RESULTS

3.1 Deuteron photodisintegraion

3.1.1 Cross section

In this section I will show the results of my calculation starting from the deuteron photodisintegration process. One of the most studying observable is obviously the cross section. There is a number of papers which present measurement results for both differential and total cross section [25–33] and it seems interesting to compare our predictions with experimental results.

In Fig. 3.1 and Fig. 3.2 I present predictions for the total cross section σ_{tot} [μ b] which I obtained using the chiral potential at the order N⁴LO+ and with the cutoff parameter $\Lambda=450$ MeV (my best predictions). From Fig. 3.1, we see that at low photon energies (below 50 MeV) predictions which include 2N contributions via the Siegert approach, describe experimental results quite well. We can suppose that the difference with experimental data may come from the statistical uncertainty of the data itself, as my predictions are often in between the data from different sources. Moreover even at such low energies the 1N current is clearly not enough to describe this observable as dashed pink line has much lower values and the difference becomes even larger with larger photon's energies. At 5 MeV the difference between 1N predictions and 1N + Siegert is 297.54 μ b (10.8%), increasing energy to 10 MeV it is 304.28 μ b (20.4%) and at 20 MeV it is 229.50 μ b (39.2%). Even with energy increasing from 5 MeV to 20 MeV - the difference between predictions has changed from 10.8% to 39.2% and from Fig. 3.1 we see that the gap continues increasing even more with larger energies.

Here and later the relative difference between set of predictions $(x_1, x_2, ..., x_N)$ is calculated using the formula:

$$\Delta = \frac{\max(x) - \min(x)}{\frac{1}{N} \sum_{i=1}^{N} x_i} \cdot 100\%$$
 (3.1)

Having look at the higher energies (above 50 MeV, Fig. 3.2) we can notice that the discrepancy with experimental data is not only quantitative, but also qualitative. There is a peak around 300 MeV in the experimental data from [30] which is not reflected in my predictions. The reason of such discrepancy is most likely coming from the relativistic effects which I do not take into account. At higher energies their contribution becomes

larger and here we observe a clear justification of such a lack. It is also confirmed by the calculations in [6] where authors discuss different potentials applying to the Deuteron photodisintegration. Despite authors use a simpler potentials that ours, their predictions obtained with and without including relativistic effects show, that such a peak appears in the latter case.

Nevertheless my main goal is to describe deuteron photodisintegration at low energies and predictions seem to be well describing experimental data at $E_{\gamma} \lesssim 50$ MeV. The higher energies region is presented in order to investigate how far the predictions are from experimental results and what can be improved in the future (e.g. include relativistic part).

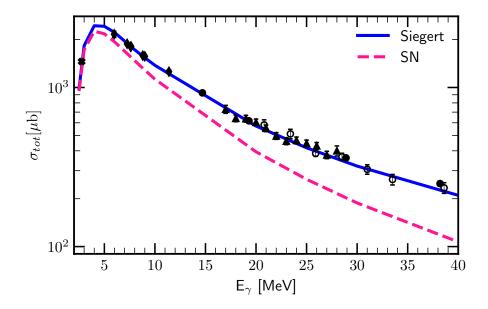


Figure 3.1: Total cross section as a function of the photon's energy E_{γ} . Solid blue line presents results obtained with SN+Siegert and dashed pink line - with only SN current. The experimental data are from [30] (black filled circles), [25] (empty circles), [26] (squares), [27] (triangles), [28] (cross "X") and [29] (dimonds).

In Fig. 3.3 I present an example of such a procedure being applied to the total cross-section for the deuteron photodisintegration at three photon energie values: 30, 100 and 140 MeV as a function of the chiral order. Error bands show truncation errors calculated using Eq. 2.50 - 2.53. One can see that truncation errors are being reduced with each consecutive chiral order: for LO it is the biggest while for N4LO+ it is hardly visible at presented scale. In each case the prediction is within the uncertainty range of lower orders.

Figures 3.4a - 3.5 show my predictions for the differential cross section $\frac{d\sigma}{d\Omega}$, where each subfigure presents results obtained using different values of the photon energy: 30, 100 and 140 MeV with 2N current's contributions taken into account via Siegert theorem. Fig. 3.4a shows the predictions obtained using different chiral orders (from LO to N⁴LO+) and with $\Lambda = 450$ MeV. Comparing the best predictions (N⁴LO+, $\Lambda = 450$ MeV) for each subfigure, we can conclude that the higher photon's energy is, the larger is difference between the theoretical predictions and experimental measurements. At $E_{\gamma} = 30$ MeV (top panel) my predictions almost perfectly match the data and the difference is almost always within the experimental uncertainties. Going to the energy 100 MeV (middle

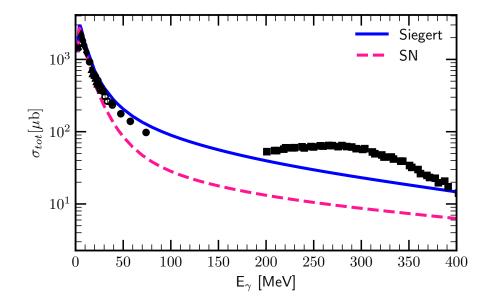


Figure 3.2: The same as on the Fig. 3.2 but for the energy range 2.5 - 400 MeV.

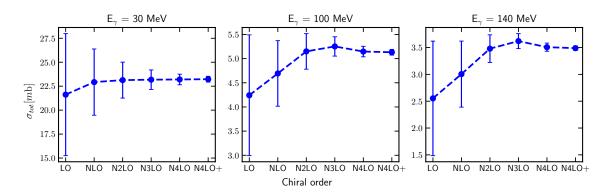


Figure 3.3: Total cross section of the deuteron photonisintegration process as a dependance on the chiral order for three photon energy E_{γ} values: 30, 100 and 140 MeV. Error bands show an estimated truncation error at each order.

subfigure) the descriptions seems not to be such good: theoretical predictions match the data qualitatively, but the gap in the angles range ($60^{\circ} < \theta_p < 130^{\circ}$) is around 30% (check the value!). Looking at the bottom figure, it is even hard to say about good qualitative description: the general trend of the angular dependance is presented, but still the predictions are far from the? experimental values.

Figures for each energy confirm the convergence of the predictions with respect to the chiral order. We see that the curves at LO are far from both experimental data and the best potential's predictions (N⁴LO+) and the higher is photon's energy, the larger is this difference. With each subsequent chiral order, the curves are more closer to each other and the difference between N⁴LO and N⁴LO+ is hardly visible at current scale. The relative difference at 30 MeV around the point of maximum ($\theta_p = 80^{\circ}$) is 0.05% which is 0.02 $\frac{\text{nb}}{\text{sr}}$; at 100 MeV and $\theta_p = 107^{\circ}$ it is 0.79% (0.025 $\frac{\text{nb}}{\text{sr}}$); and at 140 MeV (same angle) it is 1.80% - 0.043 $\frac{\text{nb}}{\text{sr}}$. Having such a small differences between predictions from two highest chiral orders, I can conclude that predictions are converged and further chiral orders would rather not bring large contribution to the cross section values. The difference

with experimental data is rather systematic and is independent on the chiral order. The relative difference between experimental data and predictions obtained with N^4LO+ and $\Lambda=450\,\mathrm{MeV}$ at 30 MeV is less then 13 % and absulute difference is $<3.07\,\frac{\mu\mathrm{b}}{\mathrm{sr}}$. At 100 MeV descripancy is larger and relative difference reaches 46% with absolute difference up to $1.39\,\frac{\mu\mathrm{b}}{\mathrm{sr}}$. Coming to 140 MeV the relative difference increases up to 48.6% and absolute - $1.93\,\frac{\mu\mathrm{b}}{\mathrm{sr}}$. What may be helpful for a better data description is a 2N current and relativistic correction, mentioned earlier.

Predictions obtained with Argonne V18 (AV18) potential (dashed-dotted purple line on the Fig. 3.4a) show that it is very similar at lower energies (relative difference at 30 MeV is 0.06 % at the point of maximum - 80°) and with increasing energy to 140 MeV it growes to 3.1 %] at same angle. It can be connected with our potential's quality loss, but AV18 can be struggling with high energies as well.

The Fig. 3.5a presents theoretical truncation uncertainties and it once more confirms that for the regarded nuclear reaction chiral order N⁴LO+ is able to produce converged predictions: the black band is hardly visible for the $E_{\gamma} = 30 \,\text{MeV}$ (the relative error for N⁴LO+ at 80° is only 0.12%) and is also quite narrow for larger energies (at 140 MeV the error at the same angle is 1.42%).

Fig. 3.5b presents a cutoff dependency of predictions. The ideal case is when the dependency is so weak that the choice of the parameter Λ would not make large changes. In practice the choice of this parameter can be important as it makes a noticeable difference in predictions.

On the top of Fig. 3.5b (when $E_{\gamma}=30\,\mathrm{MeV}$) the cutoff dependance is so weak, that, in fact, all the lines (for different Λ values) overlap each other and we cannot distinguish them with the naked eye: the relative difference ar maximum is $0.08\,\%$. Nevertheless, with increasing photon's energy to $100\,\mathrm{MeV}$ and $140\,\mathrm{MeV}$ (middle and bottom rows of Fig. 3.5b) the spread becomes larger: the cutoff error is $3.35\,\%$ at $100\,\mathrm{MeV}$ and $5.56\,\%$ at $140\,\mathrm{MeV}$ (the same θ_p).

On the Fig. 2.2 we saw that the total cross section for the same energies has the cutoff spread around $4.5\,\%$ for $100\,\text{MeV}$ and $8\,\%$ for $140\,\text{MeV}$. For $30\,\text{MeV}$ it is below $1\,\%$.

In Fig. 3.4b I show different components of the best prediction (N⁴LO+, $\Lambda=450\,\mathrm{MeV}$) for three values of photon's energy. Prediction with plane-wave component only (without rescattering part) has relatively small deviation from the full predictions, but the difference increases at larger energies. With $E_{\gamma}=30\,\mathrm{MeV}$ the relative difference is $10\,\%$ (4.03 $\frac{\mu b}{\mathrm{sr}}$) at $\theta_p=80^\circ$. Difference at 100 MeV and the same angle is $4\,\%$ (0.21 $\frac{\mu b}{\mathrm{sr}}$) and at 140 MeV it is $7\,\%$ (0.21 $\frac{\mu b}{\mathrm{sr}}$). In contrast, predictions without Siegert component (1NC) have much larger gap with full prediction: the difference is $46.5\,\%$ (13.67 $\frac{\mu b}{\mathrm{sr}}$) at $30\,\mathrm{MeV}$, $78.6\,\%$ (2.88 $\frac{\mu b}{\mathrm{sr}}$) at $100\,\mathrm{MeV}$ and $77.8\,\%$ (1.68 $\frac{\mu b}{\mathrm{sr}}$) at $140\,\mathrm{MeV}$. Obviously 2NC contributions are extremely important in this case, the difference connected with 2NC contributions is much higher then theoretical errors or even rescattering contribution.

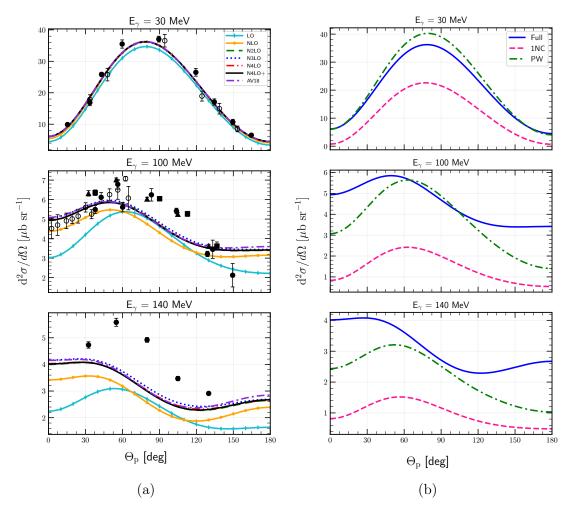


Figure 3.4: Differential cross section as a function of the outgoing proton angle in the center of mass frame for the photon's energy 30 MeV (top), 100 MeV (middle) and 140 MeV (bottom). (a) Results obtained using SMS potential at different chiral orders (from LO to N⁴LO+) with the cutoff parameter $\Lambda=450$ MeV and 2NC contributions taking via Siegert theorem. For the sake of comparison, predictions obtained with the AV18 potential are on both figures as well. Data points (filled and empty circles) are from [32] for $E_{\gamma}=30$ and 100 MeV and [33] for $E_{\gamma}=140$ MeV. (b) Predictions obtained with chiral N⁴LO+ potential and $\Lambda=450$ MeV. Blue solid line is a best predictions we have (planewave plus rescattering parts, 1NC + Siegert), pink dashed line shows predictions obtained with single-nucleon current only (without Siegert contributions) and green dashed-dotted line is a prediction with plane-wave part only - without rescattering.

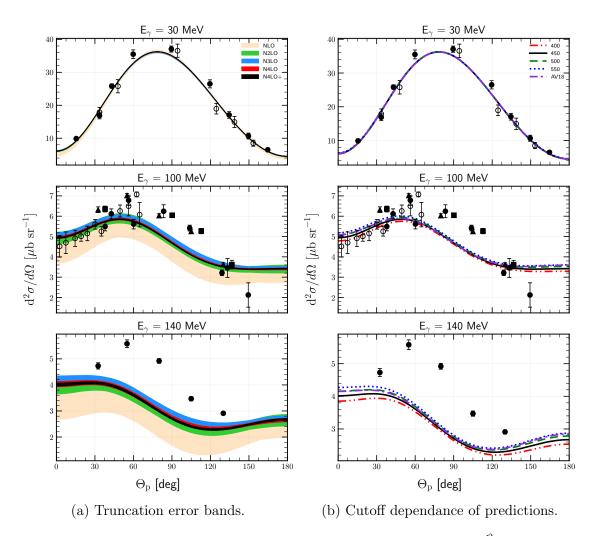


Figure 3.5: Theoretical uncertainies for the differential cross section $\frac{d^2\sigma}{d\Omega}$ as a function of the outgoing proton's momentum polar angle θ_p in the center of mass frame for the photon's energy is 30 MeV (top row), 100 MeV (middle row) and 140 MeV (bottom row). (a) The truncation error bands for each energy in a corresponding row. Results are obtained using potential with different chiral orders (from NLO to N⁴LO+) with cutoff parameter $\Lambda = 450 \,\text{MeV}$ and 2NC contributions taking via Siegert approach. (b) Predictions obtained using different values of the cutoff parameter Λ (double-dotted-dashed red line presents results obtaining with a cutoff values $\Lambda = 400 \,\text{MeV}$, solid black line - $450 \,\text{MeV}$, dashed green line - $500 \,\text{MeV}$ and dotted blues line - $550 \,\text{MeV}$) and the chiral potential N⁴LO+. Data points are the same as in Fig. 3.4a

3.1.2 Polarisation observables

In this subsection I will present my predictions for selected polarisation observables. I start with deuteron analyzing power T_{20} , T_{21} and T_{22} , which according to [6] are defined as:

$$T_{2i}(\theta) = \frac{(2 - \delta_{i0}) \operatorname{Re} V_{2i}}{V_{00}}, i = 0, 1, 2$$
 (3.2)

On the Figures 3.6 (a, b) and 3.7(a,b) I show my predictions for the T_{20} , T_{21} , and iT_{11} respectively as a functions of the outgoing proton angle θ in the CM frame. Each of them is prepared with photon's energy 30 MeV and is organized in the similar way: the top pane shows a dependance of the predictions on the chiral order of the potentia. The middle subfigure is showing a correspondent truncation error for each of the predictions from a top one (without LO, because its uncertainty is too large and will make the readability worse). The last (bottom) pane shows the cutoff dependance for each observable at the chiral order N⁴LO+.

All the polarisation observables presented here, show a good convergence upon a chiral order as it is hard to distinguish the predictions from each subsequent order starting from the N²LO. The relative width of N⁴LO+ truncation band for T₂₀, T₂₁ and T₂₂ are 0.06 %, 0.05 % and 0.19 % respectively (at $\theta_p = 90^{\circ}$, 60° and 90° respectively). The slowest convergence is observed for iT_{11} (Fig. 3.7b) where we can stll recognize N²LO band. Still it has only a 0.2 % width of N⁴LO+ truncation band at $\theta_p = 20^{\circ}$ (maximum point). The cutoff dependency for all regarded observables is weak and predictions for each value of the Λ are hardly separable with the naked eye. The relative spread of cutoff predictions at the same angles as above are 0.87 %, 0.94 %, 3.42 % and 0.68 % respectively for T₂₀, T₂₁, T₂₂ and iT_{11} respectively.

Predictions for the photon's energy $E_{\gamma} = 100$ MeV (Figs. 3.8 and 3.9) preserve similar trends for each obserable. Generally, predictions are being converged starting even from the N²LO while for iT_{11} we can see that truncation error's bands are noticeably wide even at N⁴LO and N⁴LO+ Cutoff dependance at this energy is a bit stronger, especially for T_{22} and iT_{11} components (Fig. 3.7), where one can see slightly stronger discrepancy at the stationary points.

Looking at the predictions for the deuteron tensor analyzing power, we can conclude that cutoff dependence is generally weak and the choice of Λ does not affect predictions much: the relative spread among all cutoffs for T_{20} is 2.28 % around the point of maximum $(\theta_p = 90^\circ)$. For other components of the tensor analyzing power spread is: T_{21} - 0.5 % at $\theta_p = 60^\circ$; T_{22} - 4.1 % at $\theta_p = 90^\circ$; iT_{11} - 11.4 % at $\theta_p = 20^\circ$. We see that iT_{11} has much larger spread in the maximum point and is more sensitive to the cutoff choice.

In the case of the chiral order convergence, we can also see that predictions are mostly converged after N²LO or N³LO. The relative width of N⁴LO+ truncation band for T₂₀, T₂₁ and T₂₂ are 0.7%, 0.7% and 0.04% respectively (at the same angles as the spread was shown above). One exception here is also a iT₁₁ for which this width is much larger - 6.8% at $\theta_p = 20^{\circ}$. The truncation uncertainty is much lower then one, connected to the choice of cutoff parameter. iT₁₁ seem to be more sensitive both to the choice of cutoff parameter and to the chiral order. Even for this observable cutoff spread is almost twice larger than truncation error's band. Standing out of other tensor components, iT₁₁ can be usefull for the investigation of global convergence with respect to the chiral order and cutoff dependance of the model. Of course, we can also confirm once more that our model is less accurate at higher energies which is reflected in a stronger cutoff dependance and

slower chiral convergence.

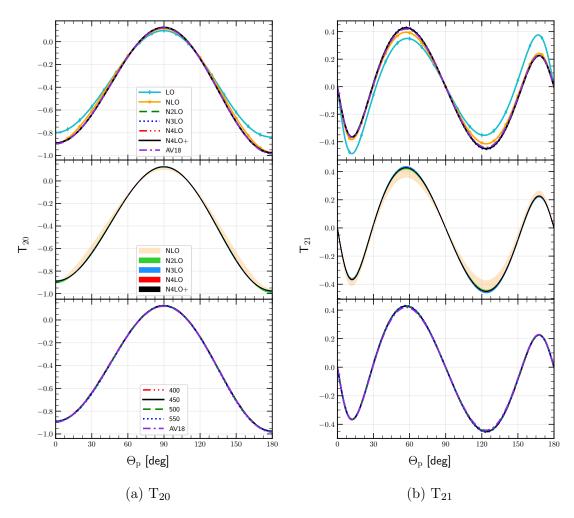


Figure 3.6: Tensor analyzing power T_{20} (a) and T_{21} (b) as a function of the outgoing proton angle in the center of mass frame for the photon's energy 30 MeV. Top row presents results obtained using potential with different chiral orders (from LO to N^4LO+) with cutoff parameter $\Lambda=450$ MeV. The middle row shows truncation errors for each chiral order starting from NLO and bottom row presents a cutoff dependency (chiral potential N^4LO+). For the sake of comparison, predictions obtained with AV18 potential are on figures as well.

In Fig. 3.10 together with best prediction at $E_{\gamma} = 30 \,\mathrm{MeV}$ (N⁴LO+, $\Lambda = 450 \,\mathrm{MeV}$, Siegert theorem), I show predictions obtained with 1NC only and with plane-wave contribution without rescattering part. In case of deuteron's tensor analyzing power components, the contribution of rescattering part is not that big for T_{20} , T_{21} and T_{22} (up to 20% in extremum points). Nevertheless, for iT_{11} we see that PW part equals to zero. It may be connected with some features of this particular components, such that plane-wave part cancels out. The 2NC component taken into account via Siegert theorem has a dominant contribution here. We see that 1NC predictions are absolutely away from the Full predictions and in case of iT_{11} does not even reflect total prediction qualitatively.

Fig. 3.11 presents similar results but for $E_{\gamma}=30\,\mathrm{MeV}$ and it is intersting that difference between Full and 1NC prediction becomes smaller and it is especially visible for T_{22} . At this energy the relative difference at $\theta_p=90^\circ$ is 43.6% comparing to 122.8% at $E_{\gamma}=30\,\mathrm{MeV}$. Similarly, the difference for T_{20} at $E_{\gamma}=30\,\mathrm{MeV}(\theta_p=90^\circ)$ is 91.4% and

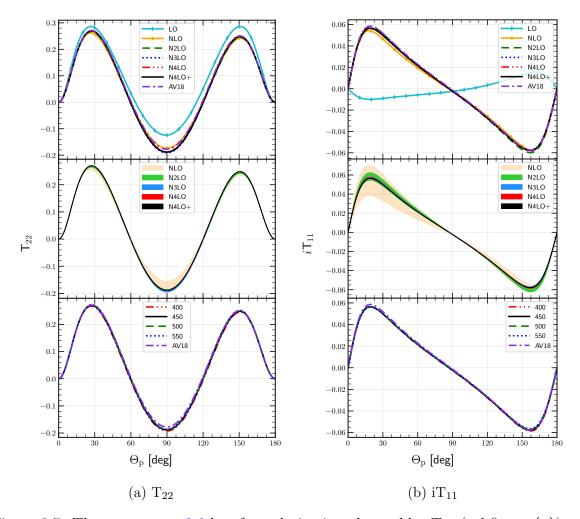


Figure 3.7: The same as on 3.6 but for polarisation observables T_{22} (subfigure (a)) and iT_{11} (subfigure (b)).

at $E_{\gamma}=100\,\mathrm{MeV}$ it drops down to 28.8 %. This trend is noticeable looking on Figures (3.12 - 3.18). With

On the next figures, I show the predictions in a similar way as it was done in [31] in order to compare my predictions with the experimental data. On the Figures 3.12 - 3.18 I show an angular dependance of the T_{2i} (i = 0, 1, 2) for a specific energy bands. Solid blue line shows an average value of the observable in the specified energy range obtained at N⁴LO+ with $\Lambda = 450$ MeV, while the pink dashed line is a prediction obtained with a same setup but without using a contributions from Siegert approach (single nucleon current only). Bands for each of prediction specify the spread of predictions in regarded energy band.

One can see that the data description is better for the predictions with Siegert contributions and SN current is not able to describe experiment properly. With increasing energy (more than $100 \,\mathrm{MeV}$), the difference between predicted values and experimental data becomes larger (especially for T_{22}), but the model I use is not meant to be used for high energies and figures are presented out of the curiosity.

On the Figure 3.19 the energy dependance of T_{20} and T_{22} (integrated over all angles) is presented for the energy range 0-400 MeV. I also demonstrate the experimental data from [31] and [34] as well as theoretical calculations from [35] on the figure. For T_{20} the model is able to describe experimental data well even for high energies. On the

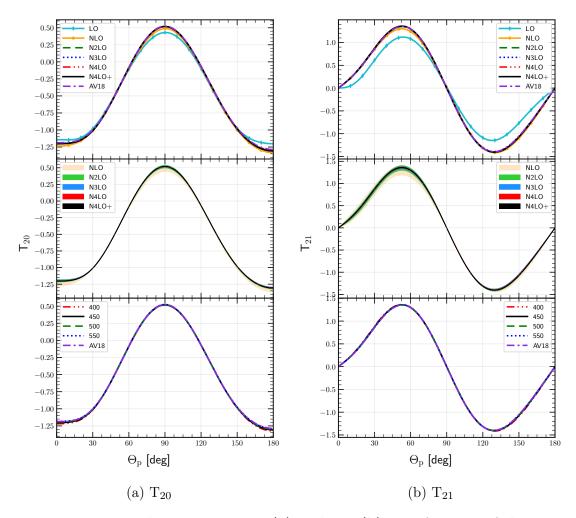


Figure 3.8: Tensor analyzing power T_{20} (a) and T_{21} (b) as a function of the outgoing proton angle in the center of mass frame for the photon's energy 100 MeV. Top row presents results obtained using potential with different chiral orders (from LO to N^4LO+) with cutoff parameter $\Lambda=450$ MeV. The middle row shows truncation errors for each chiral order starting from NLO and bottom row presents a cutoff dependency (chiral potential N^4LO+). For the sake of comparison, predictions obtained with AV18 potential are on figures as well.

other hand, T_{22} is not so well described: for the low energies the prediction curve is somehow within uncertainties of experimental data, but further the difference with the data becomes larger. Also it is not reflect the qualitative nature of the data as we can see that after around 150 MeV data points start ascending which is not represented in my predictions. Theoretical predictions from [35] (brown dashed curve) are also not able to describe data quantitatively for T_{22} , but the growth is presented there.

Similar situation is on the Figures 3.20 and 3.21 where I show an energy dependance of Deuteron analyzing power components for specific angular ranges (following the data from [31]). Predictions for T_{20} are able to reflect the experimental results, while for T_{21} and T_{22} predictions are reasonable (quantitative-wise) only for lower energies and difference with data becomes larger when energy increases. Predictions for T_{22} once more confirm an insufficiency of SN and an importance of 2-nucleon current contributions.

On the Fig. 3.22 I demonstrate predictions for the photon asymmetry Σ_{γ} for the deuteron photodisintegration with $E_{\gamma} = 20 \text{ MeV}$ (a) and 60 MeV(b) as well as experimental

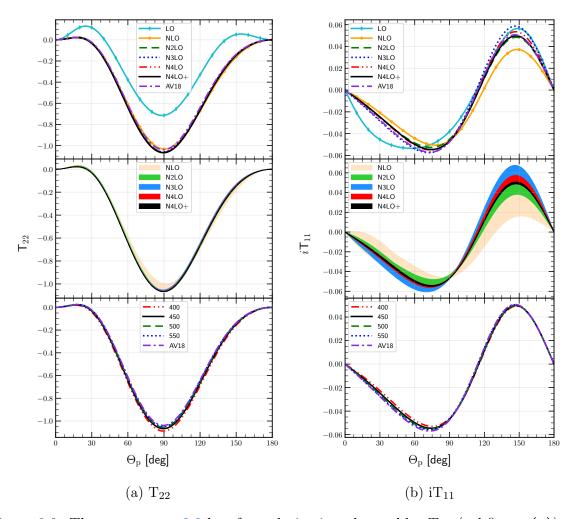


Figure 3.9: The same as on 3.8 but for polarisation observables T_{22} (subfigure (a)) and iT_{11} (subfigure (b)).

data. Both (a) and (b) figures are organized similarly to the figures I showed earlier for the tensor analyzing power (e.g. Fig. 3.7). That is the top pane is aimed to demonstrate predictions obtained with chiral potential at different orders, the middle one is showing a truncation error bands and the bottom - shows the cutoff dependance. What we can see here is good convergence with respect to the chiral order. For both regarded energies predictions at different orders are very close to each other except for LO and NLO curves. Nevertheless, at 60 MeV we can see that truncation error bands reveal some uncertainty connected with the chiral order and I can assume that even some higher chiral orders would still contribute to the predictions at this energy.

Cutoff dependance is also stronger at 60 MeV. We can clearly see that predictions are different for each value of the Λ . The standard deviation with respect to the cutoff parameter at 20 MeV does not exceed 0.7% of the mean value while at the photon's energy 60 MeV the maximum value is around 2.5% (at $\theta = 115^{\circ}$).

Regarding the correspondace to experimental data, we can clearly see that for the lower energy predictions are almost perfectly overlaping with exparimental point (and error bars). Few points are laying outside the predictions but it can be caused by experimental issues. For 60 MeV, experimental data points are constantly below prediction curves (especially in the middle of angles range). It seems that some systematic uncertainty is presented in predictions and multiplication by some factor (presumably less than 1)

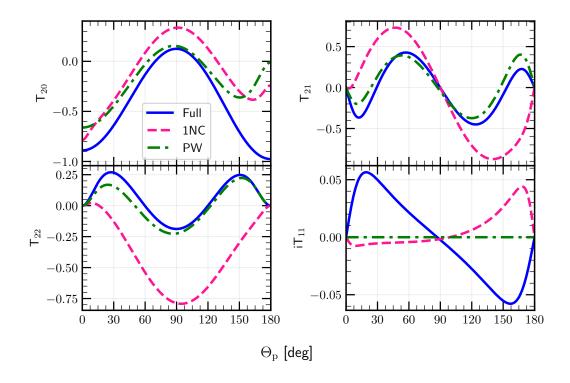


Figure 3.10: Tensor analyzing power components T_{20} , T_{21} , T_{22} and iT_{11} as a functions of the outgoing proton angle θ_p (in the center of mass frame) at $E_{\gamma} = 30 \,\mathrm{MeV}$. Similarly to Fig. 3.4b predictions obtained with chiral N⁴LO+ potential and $\Lambda = 450 \,\mathrm{MeV}$ are presented for each component. Blue solid line is a best predictions we have (plane-wave plus rescattering parts, 1NC + Siegert), pink dashed line shows predictions obtained with single-nucleon current only (without Siegert contributions) and green dashed-dotted line is a prediction with plane-wave part only - without rescattering.

could help predictions be more similar to experimental data.

On the Fig. 3.23 I present dependance of the asymmetry Σ_{γ} on the photon's energy with fixed value of the outgoing proton's angle $\theta_p = 90^{\circ}$ (following the data given at [36] and [37]). It is noticeable that with increasing energy, the prediction curve becomes more and more above the experimental data. This trend was also observed in angular dependance of the asymmetry at 60 MeV so I can assume that within our framework, Σ_{γ} is sensitive to the initial photon's energy and some contributions are missing in order to prepare good predictions at higher energies. From the Fig. 3.23 we can say that large descripancy with data starts appearing after 35 MeV.

The proton polarization is demonstrated on the Fig. 3.24 for the photon's energy 30 MeV(a) and 100 MeV(b). In this case even higher energy such as 100 MeV does not reveal neither slower convergence with respect to the chiral order no stronger cutoff dependence. Figures for both energies show that only next-to-leading order brings relatively high contribution while taking into account each subsequent order does not change predictions largely. In the case of cutoff dependence, we see that curves for each value of Λ are very close to each other. The standard deviation of the predictions with respect to the cutoff parameter has maximal value 1.94% at $E_{\gamma}=30 \text{MeV}$ and 3.2% at 100 MeV. The dependence is slightly stronger for higher energy, but these values are comparable.

Predictions for the neuteron polarization at energy 2.75 MeV are on the Fig. 3.25a. The choice of energy is conditioned by the availability of experimental data. We can



Figure 3.11: The same as on Fig. 3.10 but for $E_{\gamma} = 100 \,\mathrm{MeV}$

see that predictions reflect the behavior of experimental data points qualitatively, having more o less constant offset of the values. Similar offset was obtained also in predictions at [6], where various approaches were presented. Interesting is that predictions clearly show symmetrical form of the curve, while in the experimental data have some deviations from symmetrical form. It can be a sign that some problem with data can be in this case (taking into account also that experiment had been done in 196) as well as inaccuracy in theoretical models.



Figure 3.12: Tensor analyzing powers T_{20} , T_{21} and T_{22} as a functions of the outgoing proton angle θ_p (in the center of mass frame). Solid blue line is a mean value of my predictions obtained with a SMS potential at N⁴LO+ chiral order and with $\Lambda=450~\text{MeV}$ at energy values from 25 to 45 MeV and where SN current was used together with Siegert approach. Pink dashed line is similar prediction but with SN only. The corresponding bands show the deviation of predictions in the regarded energy region. Filled circles are experimental data from [31] for the analogous energy span.

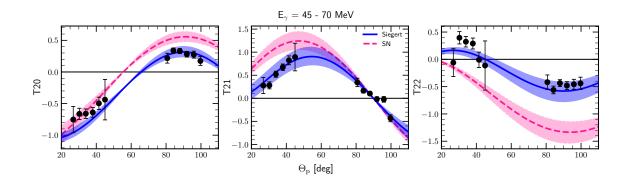


Figure 3.13: The same as on the Fig. 3.12 but for energy bin $45 - 70 \,\mathrm{MeV}$



Figure 3.14: The same as on the Fig. 3.12 but for energy bin $70 - 100 \,\mathrm{MeV}$



Figure 3.15: The same as on the Fig. 3.12 but for energy bin $100-140\,\mathrm{MeV}$



Figure 3.16: The same as on the Fig. 3.12 but for energy bin $140-180\,\mathrm{MeV}$



Figure 3.17: The same as on the Fig. 3.12 but for energy bin $180 - 230 \,\mathrm{MeV}$

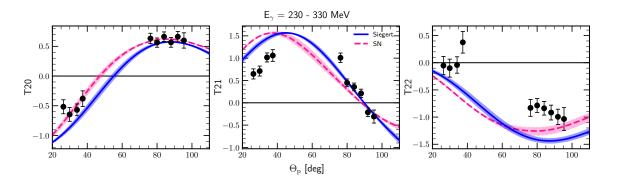


Figure 3.18: The same as on the Fig. 3.12 but for energy bin $230-330\,\mathrm{MeV}$

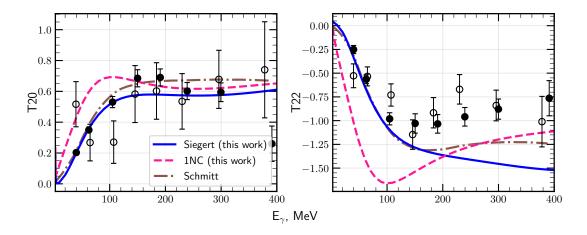


Figure 3.19: Tensor analyzing powers T_{20} and T_{22} as a functions of the photon energy E_{γ} with fixed outgoing proton angle $\theta_p = 88^{\circ}$ (in the center of mass frame). My predictions (blue solid line) are obtained with SMS potential at chiral order N^4LO+ and with cutoff parameter $\Lambda = 450\,\text{MeV}$ with 2NC contributions included via Siegert theorem, dashed pink line show prediction obtained without 2NC contributions. Dashed-dotted brown line presents calculations from [35]. Experimental data is taken from [31] (filled circles) and [34] (empty circles).

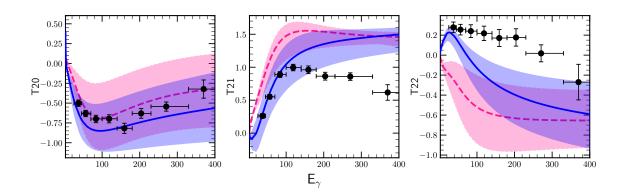


Figure 3.20: Tensor analyzing powers T_{20} , T_{21} and T_{22} as a functions of the photon's energy within the outgoing proton's angle range $24^{\circ} - 48^{\circ}$ (in the center of mass frame). Solid blue line is a mean value of my predictions obtained with SMS potential at N^4LO+ chiral order and with $\Lambda=450$ MeV at energy values from 25 to 45 MeV within a given angles range and where SN current was used together with Siegert approach. Pink dashed line is similar prediction but with SN only. The corresponding bands show the deviation of predictions in the regarded energy region. Filled circles are experimental data from [31] for the analogous energy span.



Figure 3.21: The same as on the Fig. 3.20 but for the angles' range $70^{\circ} - 102^{\circ}$.

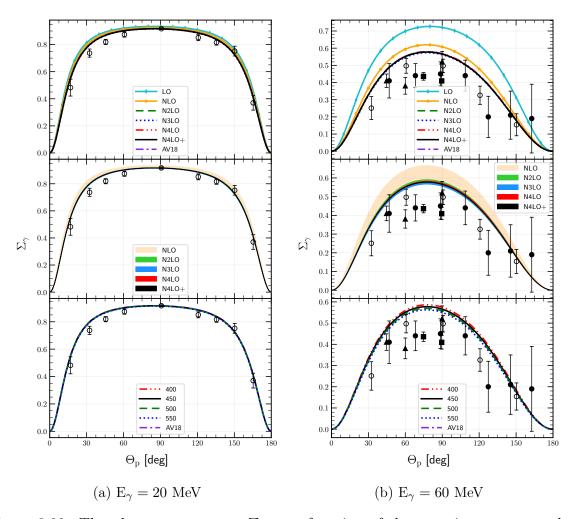


Figure 3.22: The photon asymmetry Σ_{γ} as a function of the outgoing proton angle in the center of mass frame for the photon's energy 30 MeV(a) and 100 MeV(b). Top row presents results obtained using potential with different chiral orders (from LO to N⁴LO+) with cutoff parameter $\Lambda=450$ MeV. The middle row shows truncation errors for each chiral order starting from NLO and bottom presents a cutoff dependency (chiral potential N⁴LO+). Filled circles are experimental data from [38], empty circles - from [37], filled squares - from [39] and triangles are from [40]. For the sake of comparison, predictions obtained with AV18 potential are on figures as well.

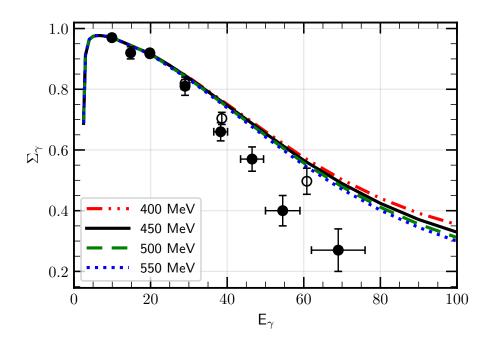


Figure 3.23: The photon asymmetry Σ_{γ} as a function of the photon energy with fixed outgoing proton angle $\theta_p = 90^{\circ}$. Each curve corresponds to the particular value of the cutoff parameter and chiral potential used here is N⁴LO+. Filled circles are experimental data from [36], empty circles - from [37].



Figure 3.24: Proton polarisation $P_y(p)$ as a function of the outgoing proton angle in the center of mass frame for the photon's energy 30 MeV (a) and 100 MeV (b). Top figure presents results obtained using potential with different chiral orders (from LO to N⁴LO+) with cutoff parameter $\Lambda = 450$ MeV. The middle pane shows truncation errors for each chiral order starting from NLO and bottom figure presents a cutoff dependency (chiral potential N⁴LO+). For the sake of comparison, predictions obtained with AV18 potential are on figures as well.

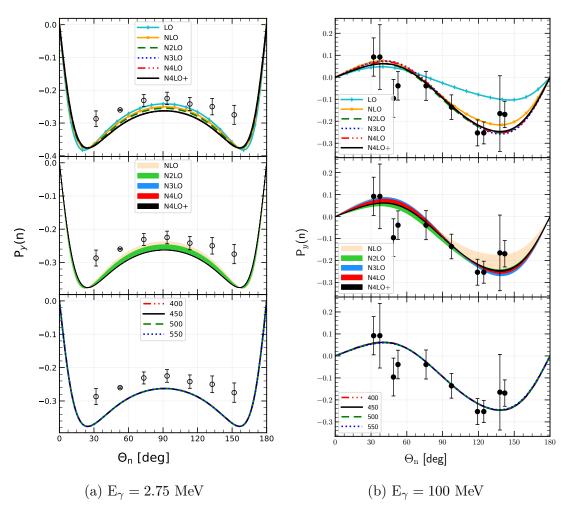


Figure 3.25: Neuteron polarisation $P_y(n)$ as a function of the outgoing neuteron angle in the center of mass frame for the photon's energy 2.75 MeV(a) and 100 MeV(b). Top row presents results obtained using potential with different chiral orders (from LO to N⁴LO+) with cutoff parameter $\Lambda=450$ MeV. The middle pane shows truncation errors for each chiral order starting from NLO and bottom figure presents a cutoff dependency (chiral potential N⁴LO+). Experimental data is from [41] (empty circles) and [42] (filled circles).

3.2 Helium photodisintegration

3.2.1 3N photodisintegration

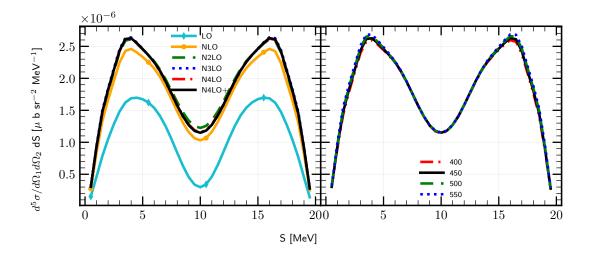


Figure 3.26: The five-fold differential cross section for the photon energy $E_{\gamma}=30$ MeV for the kinematic configuration $\theta_1=15^{\circ},\ \phi_1=0^{\circ},\ \theta_2=15^{\circ},\ \phi_2=180^{\circ}.$ The left figure presents results obtained using potential with different chiral orders (from LO to N⁴LO+) with cutoff parameter $\Lambda=450$ MeV. The right figure presents a cutoff dependency (chiral potential N⁴LO+).

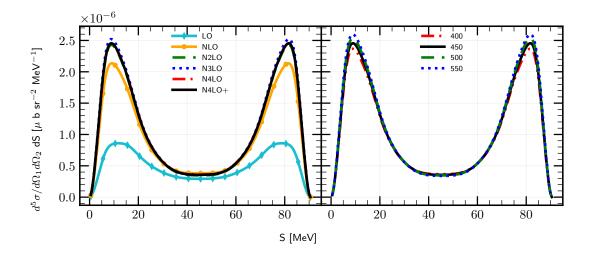


Figure 3.27: The same as on Fig. 3.26 but for the photon energy $E_{\gamma} = 100 \text{ MeV}$

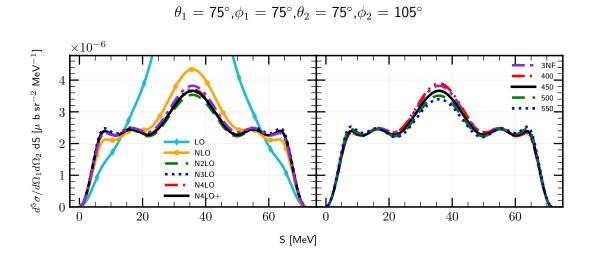


Figure 3.28: The five-fold differential cross section for the photon energy $E_{\gamma} = 100$ MeV. The left figure presents results obtained using potential with different chiral orders (from LO to N⁴LO+) with cutoff parameter $\Lambda = 450$ MeV. The right figure presents a cutoff dependency (chiral potential N⁴LO+).

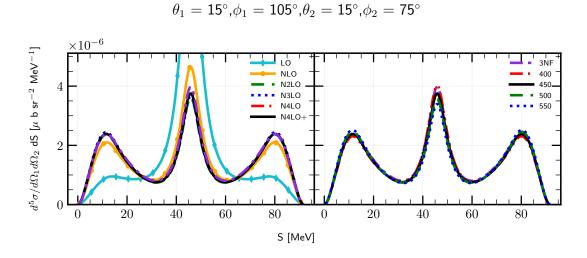


Figure 3.29: The five-fold differential cross section for the photon energy $E_{\gamma}=100$ MeV. The left figure presents results obtained using potential with different chiral orders (from LO to N⁴LO+) with cutoff parameter $\Lambda=450$ MeV. The right figure presents a cutoff dependency (chiral potential N⁴LO+).

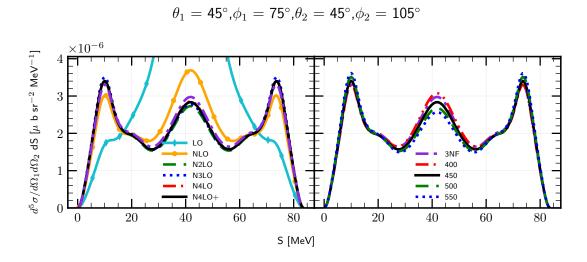


Figure 3.30: The five-fold differential cross section for the photon energy $E_{\gamma} = 100$ MeV. The left figure presents results obtained using potential with different chiral orders (from LO to N⁴LO+) with cutoff parameter $\Lambda = 450$ MeV. The right figure presents a cutoff dependency (chiral potential N⁴LO+).

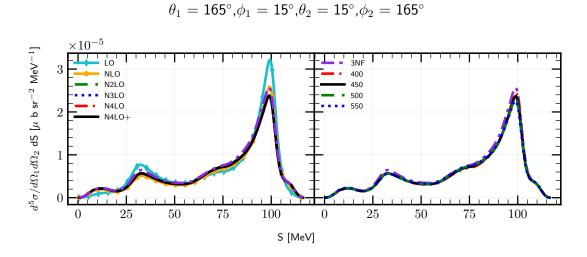


Figure 3.31: The five-fold differential cross section for the photon energy $E_{\gamma} = 100$ MeV. The left figure presents results obtained using potential with different chiral orders (from LO to N⁴LO+) with cutoff parameter $\Lambda = 450$ MeV. The right figure presents a cutoff dependency (chiral potential N⁴LO+).

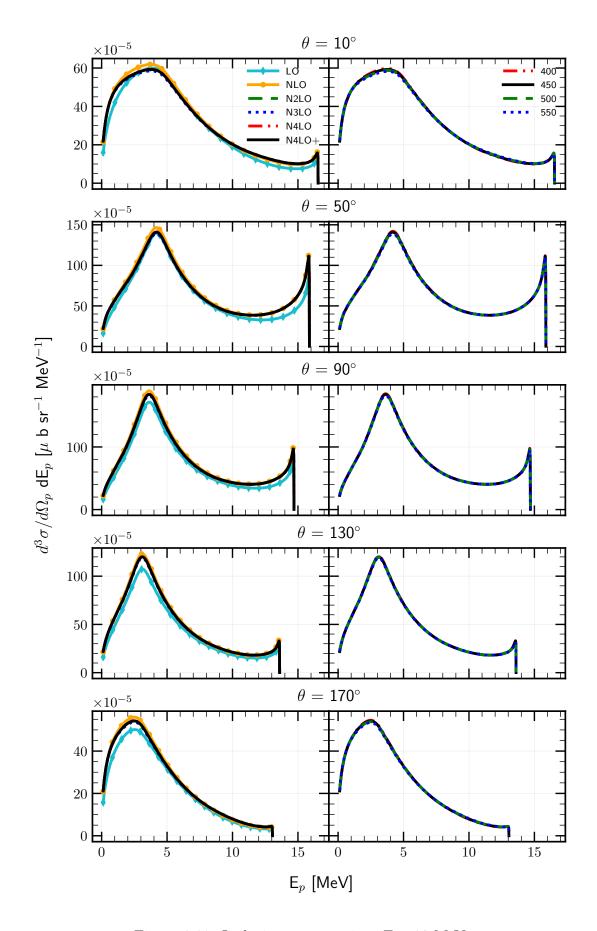


Figure 3.32: Inclusive cross section. E_{γ} =30 MeV

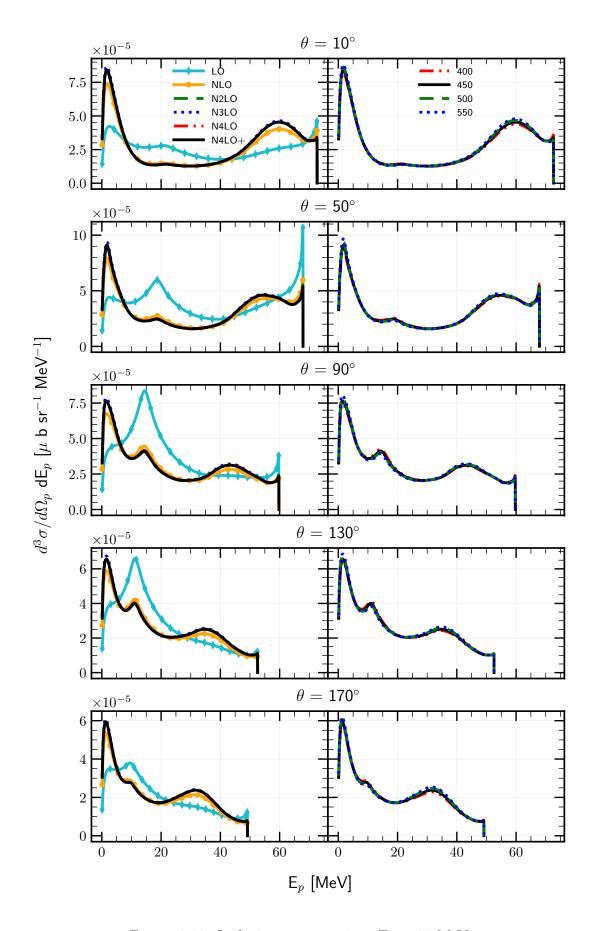


Figure 3.33: Inclusive cross section. $E_{\gamma}{=}100~\mathrm{MeV}$

3.2.2 Nd photodisintegration

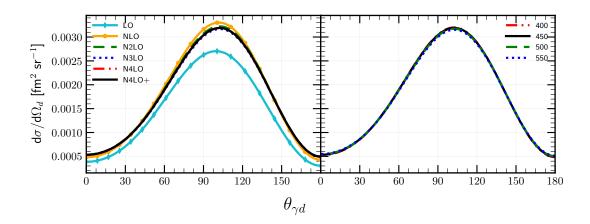


Figure 3.34: Differential cross section for the d- γ two-body photodisintegraion of ³He as a function of the d γ angle. The initial photon energy $E_{\gamma}=30$ MeV.

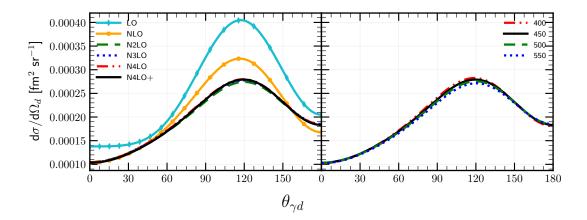


Figure 3.35: The same as on Fig. 3.34 but for the photon energy $E_{\gamma} = 100 \text{ MeV}$

3.3 Pion absorption from the lowes atomic orbital

3.3.1 Pion absorption in ³He

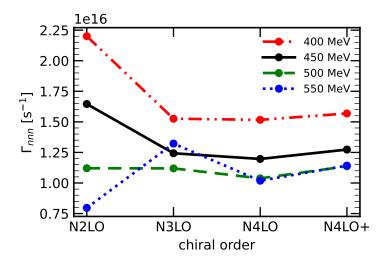


Figure 3.36

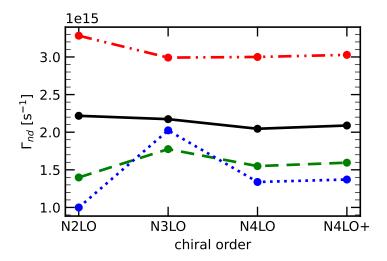


Figure 3.37

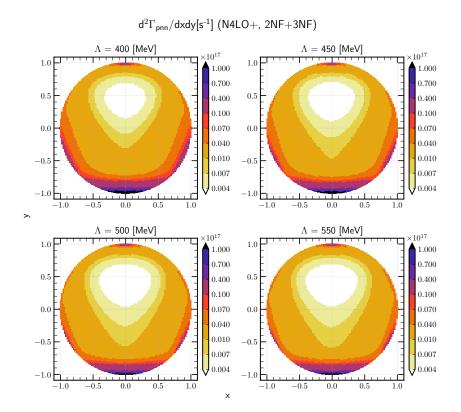


Figure 3.38

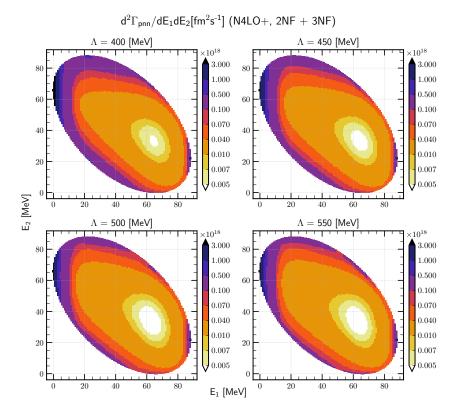


Figure 3.39

$d^2\Gamma_{pnn}/dxdy[s^{-1}]$ (N4LO+, 2NF+3NF, PWIAS) $\Lambda = 400 \, [MeV]$ $\Lambda = 450 \, [MeV]$ 1e17 1.0 1.000 0.700 0.700 0.5 0.400 0.5 0.400 0.100 0.100 0.0 0.070 0.0 0.070 0.040 0.040 0.010 0.010 -0.5-0.50.007 0.007 -1.0 0.004 0.004 -0.5 0.0 0.5 -0.50.0 0.5 $\Lambda = 500 [MeV]$ $\Lambda = 550 [MeV]$ 1e17 1e17 ____ 1.0 11111 1.0 1.000 1.000 0.700 0.700 0.5 0.400 0.5 0.400 0.100 0.100 0.0 0.070 0.0 0.070 0.040 0.040 -0.5 0.010 0.010 0.007 0.007 -1.0 -1.0 0.004 0.004 -0.5 -0.5 0.0 0.0 0.5 0.5 -1.0

Figure 3.40

х

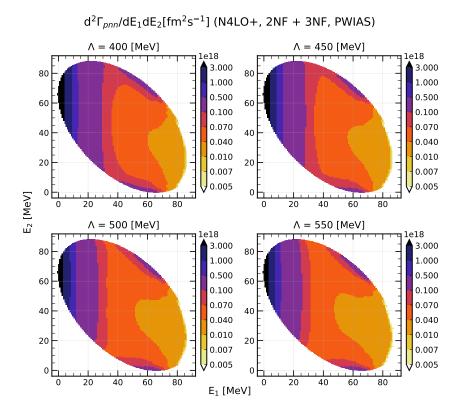


Figure 3.41

$d^2\Gamma_{pnn}/dxdy[s^{-1}]$ (N4LO+, 2NF+3NF, 1NC) $\Lambda = 400 [MeV]$ $\Lambda = 450 [MeV]$ 1.00 1.00 0.5 0.5 0.80 0.80 0.60 0.60 0.0 0.40 0.0 0.40 0.20 0.20 0.10 0.10 -0.5 -0.5 0.08 0.08 0.06 0.06 -1.0 0.0 $\Lambda = 500 [MeV]$ $\Lambda = 550 [MeV]$ 1e15 1.0 1.0 4.00 4.00 1.00 1.00 0.5 0.80 0.5 0.80 0.60 0.60 0.0 0.40 0.0 0.40 0.20 0.20 0.10 0.10 -0.5 -0.50.08 0.08 0.06 0.06 -0.5 0.0 0.5 1.0 0.0 1.0 -0.5 Х

Figure 3.42

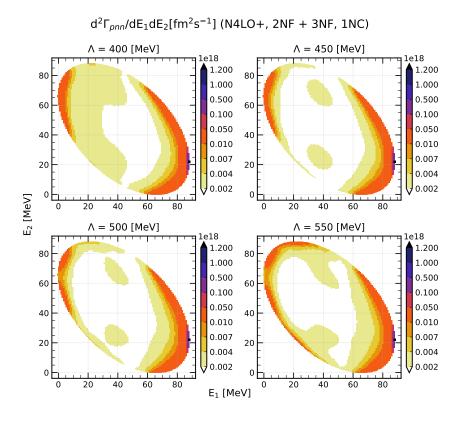


Figure 3.43

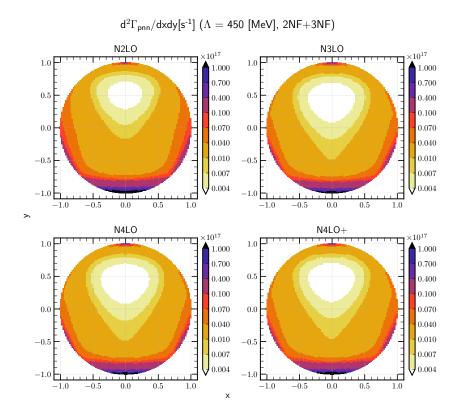


Figure 3.44

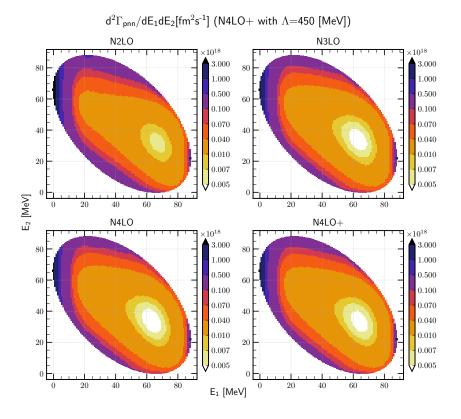


Figure 3.45

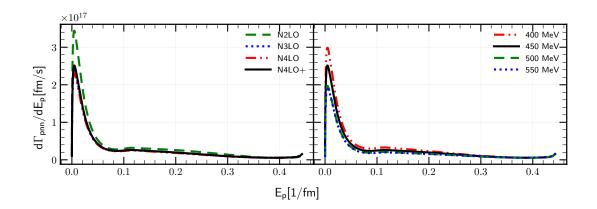


Figure 3.46

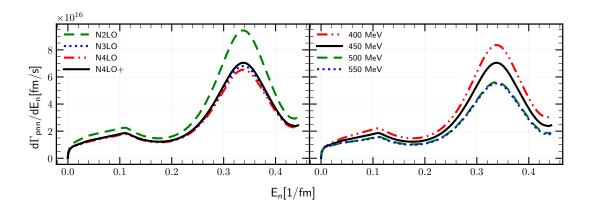


Figure 3.47

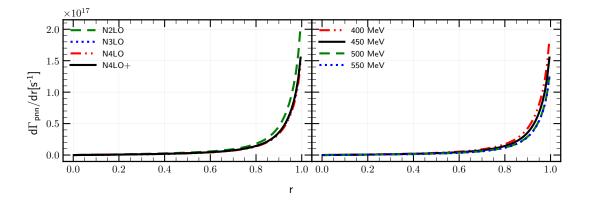


Figure 3.48

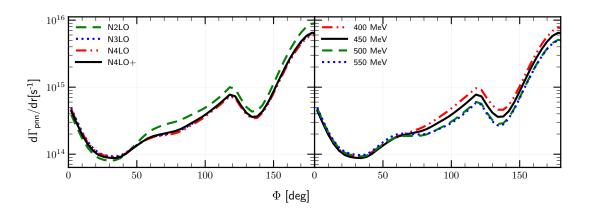


Figure 3.49

3.3.2 $\pi^- + {}^3H \rightarrow n + n + n$

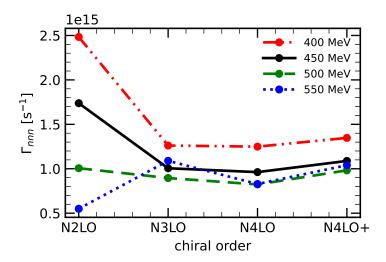


Figure 3.50

$d^2\Gamma_{nnn}/dxdy[s^{-1}]$ (N4LO+, 2NF+3NF) $\Lambda = 400 [MeV]$ $\Lambda = 450 [MeV]$ 1e16 1e16 1.0000 1.0000 0.4000 0.4000 0.2000 0.2000 0.5 0.5 0.1000 0.1000 0.0500 0.0500 0.0 0.0 0.0100 0.0100 0.0050 0.0050 -0.50.0020 0.0020 0.0013 0.0013 1.0 -0.5 0.0 0.5 -1.0 -0.5 0.0 $\Lambda = 500 [MeV]$ $\Lambda = 550 [MeV]$ 1e16 1e16 1.0000 1.0000 1.0 0.4000 0.4000 0.5 0.2000 0.5 0.2000 0.1000 0.1000 0.0 0.0500 0.0 0.0500 0.0100 0.0100 0.0050 0.0050 -0.5-0.50.0020 0.0020 0.0013 0.0013 -1.0-0.50.0 0.5 1.0 -1.0 -0.50.0 0.5 Х

Figure 3.51

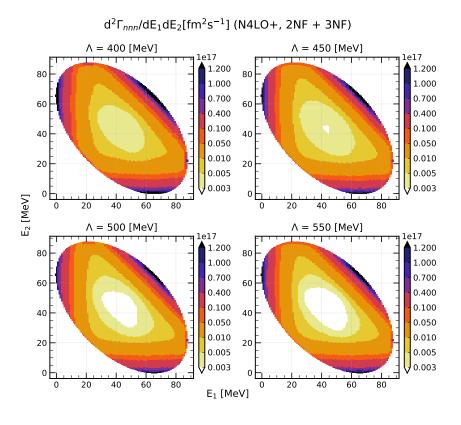


Figure 3.52

$d^2\Gamma_{nnn}/dxdy[s^{-1}] (\Lambda = 450 [MeV], 2NF+3NF)$ N2LO N3LO 1e16 1e16 1.0000 1.0000 1.0 0.4000 0.4000 0.2000 0.2000 0.5 0.5 0.1000 0.1000 0.0500 0.0500 0.0 0.0 0.0100 0.0100 0.0050 0.0050 -0.5 -0.50.0020 0.0020 0.0013 0.0013 1.0 -0.5 0.0 0.5 1.0 -1.0 -0.5 0.0 0.5 N4LO N4LO+ 1e16 1e16 1.0000 1.0000 1.0 0.4000 0.4000 0.2000 0.2000 0.5 0.5 0.1000 0.1000 0.0500 0.0500 0.0 0.0 0.0100 0.0100 0.0050 0.0050 -0.5 0.0020 0.0020 0.0013 0.0013 -0.5 -1.0-0.5 0.0 0.5 1.0 0.0 0.5 -1.0 1.0

Figure 3.53

Х

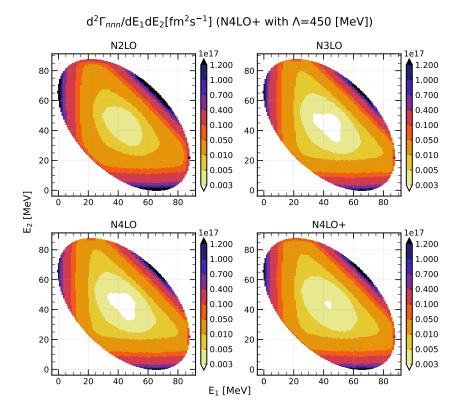


Figure 3.54

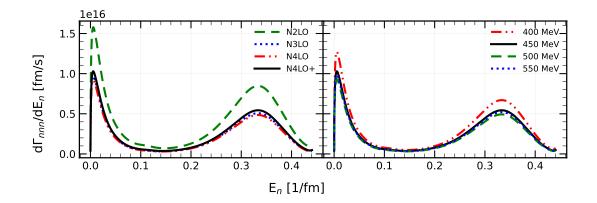


Figure 3.55

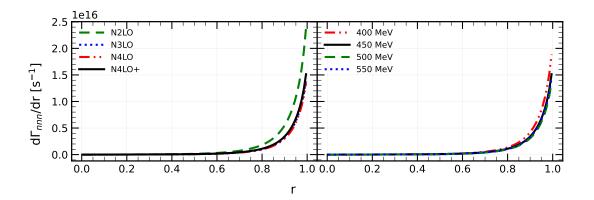


Figure 3.56

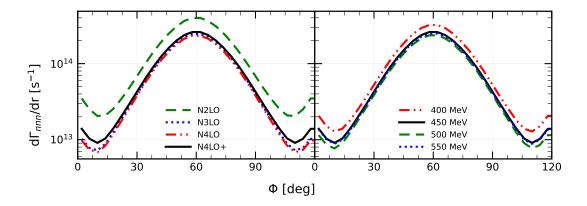


Figure 3.57

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