

**Условие**

$$\varphi = -x_1 - 6x_2 + 6x_3 + 2x_4 + x_5 \rightarrow \max$$

$$\begin{cases} x_1 + 2x_2 = 4 \\ -2x_2 + 3x_3 = 6 \\ -x_1 + 2x_4 + 3x_5 = 2 \end{cases}$$
$$\begin{cases} 2 \leq x_1 \leq 4 \\ -1 \leq x_2 \leq 3 \\ 1 \leq x_3 \leq 4 \\ 2 \leq x_4 \leq 5 \\ 0 \leq x_5 \leq 4 \end{cases}$$

**Решение** Возьмём как начальный базис  $J_B = \{2, 3, 5\}$

$$\left[ \begin{array}{ccc|c} 2 & -2 & 0 & -6 \\ 0 & 3 & 0 & 6 \\ 0 & 0 & 3 & 1 \end{array} \right] \Rightarrow u = \begin{pmatrix} -1 \\ 2 \\ \frac{1}{3} \end{pmatrix}$$

$$\delta_1 = \frac{1}{3}$$

$$\delta_4 = \frac{4}{3}$$

$$\mathfrak{x}_1 = 4$$

$$\mathfrak{x}_4 = 5$$

$$\left[ \begin{array}{cccc|c} 2 & 0 & 0 & 0 & 0 \\ -2 & 3 & 0 & 0 & 6 \\ 0 & 0 & 3 & 0 & -4 \end{array} \right] \Rightarrow \begin{array}{l} \mathfrak{x}_2 = 0 \\ \mathfrak{x}_3 = 2 \\ \mathfrak{x}_5 = -\frac{4}{3} \end{array}$$

$$j_* = 5$$

$$\left[ \begin{array}{ccc|c} 2 & -2 & 0 & 0 \\ 0 & 3 & 0 & 6 \\ 0 & 0 & 3 & -4 \end{array} \right] \Rightarrow p_u = \begin{pmatrix} 0 \\ 0 \\ \frac{1}{3} \end{pmatrix}$$

$$p_{\delta_1} = \frac{1}{3}$$

$$p_{\delta_4} = \frac{-2}{3}$$

$$\begin{array}{l} \sigma_1 = \infty \\ \sigma_5 = 2 \end{array} \implies \begin{array}{l} \sigma = 2 \\ j_0 = 5 \end{array}$$

$$J_{\text{B}} = \{2, 3, 4\}$$

$$\left[ \begin{array}{ccc|c} 2 & -2 & 0 & -6 \\ 0 & 3 & 0 & 6 \\ 0 & 0 & 2 & 2 \end{array} \right] \implies u = \begin{pmatrix} -1 \\ 2 \\ 1 \end{pmatrix}$$

$$\delta_1 = 1$$

$$\delta_5 = -4$$

$$\mathfrak{x}_1 = 4$$

$$\mathfrak{x}_5 = 0$$

$$\left[ \begin{array}{cccc|c} 2 & 0 & 0 & 0 & 0 \\ -2 & 3 & 0 & 6 & 6 \\ 0 & 0 & 2 & 6 & 6 \end{array} \right] \implies \begin{array}{l} \mathfrak{x}_2 = 0 \\ \mathfrak{x}_3 = 2 \\ \mathfrak{x}_5 = 3 \end{array}$$

Критерий оптимальности выполняется

**Ответ:**  $x = (4, 0, 2, 3, 0)$