

# ThesisProgress

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## 1 08.02.2017 Step 1

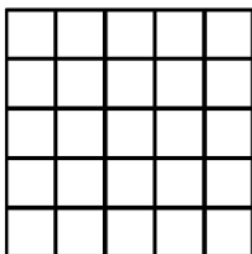


Figure 1: Map of the room.

Let's assume that we have rectangle room with is divided into cells so we have  $n$  cells in the row and  $m$  cells in the column (for example, as it is shown at Fig. 1). A WiFi access point is placed somewhere in this room (we do not care about its position now).

**Task:** receiving signal strength  $x$  from the user decide in which cell the user is located.

**Prior information:**

- $(i, j) \forall i = \overline{1, n}; j = \overline{1, m}$  - cells in the room. For further simplicity let's assume that  $(i, j) = k$ .
- $p(k)$  - the probability of that when user is in the room he will stand at cell  $k$ .
- $\mu_k$  - the signal strength that can be observed at cell  $k$  (at this step we suppose that there is no noise in signal and that we can only observe some particular signal strength in each cell).

**Input:**  $x$  - received signal strength.

**Output:**  $\hat{k}$  - the cell where the user is standing.

**Comment:** The prior information about cells probability  $p(k)$  on this step is gotten by this expression [1]:

$$P_{received}(d) = P_{received}(d_0) - 10 * \alpha * \log(\frac{d}{d_0})$$

where  $\alpha = 3, d_0 = 4, P_{received}(d_0) = -53$ .

**Solution:**

$$\hat{k} = \operatorname{argmax}_k p(x, k) = \operatorname{argmax}_k p(k|x)p(x) = \operatorname{argmax}_k p(k|x)$$

where  $p(k|x)$  can be found as  $p(k|x) = \frac{p(x|k)p(k)}{p(x)}$ .

## 2 10.02.2017 Step 2

We should define  $p(x|k)$  to find the distribution of signal inside each cell. For beginning, let's take normal distribution  $N(\mu_k, \sigma_k^2)$  for each cell  $k$ . So,  $p(x|k) \sim N(\mu_k, \sigma_k^2)$ .

Also, for the simplification we will assume that  $\mu_k = P_{received}(d)$  and  $\forall k \sigma_k^2 = 1$ .

**Next step:** define the way to calculate variance for each cell (obviously, they cannot be equal to 1 and be also equal to each other in common case).

## 3 12.02.2017 Step 3

Idea - apply particle filtering for  $p(x|k)$  approximation.

## 4 14.02.2017

**Particle filter. Key idea:** we have some region of start points - our assumptions about start position of the user, defined in some probabilistic approach. Then we have motion activity. We apply this motion to all this points and among them define that have the biggest weights. And only these points will stay in the model. After that just continue to that moment when we will be able exactly define user's position.[5]

**In context of the idea current issues:** how define start points; what about the motion - how to define or predict it; generally how to apply it to the task.

**Other issues:** is it the best model? Can be other models found that will be more suitable?

## 5 15.02.2017

According to "Prioritized Online Positioning Algorithm" described in [3]:

1. Define feasible region.
2. Find possible locations in the feasible region.
3. Apply particle filter to reduce the number of particles on step  $t + 1$ .

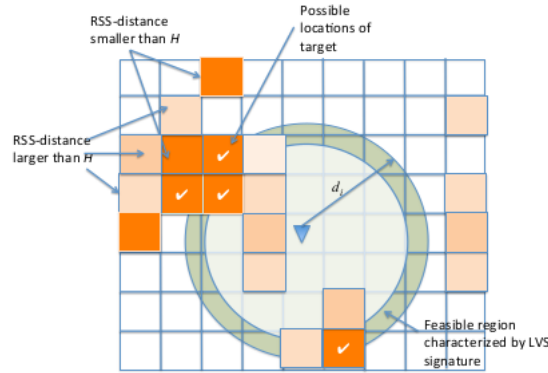


Figure 2: The idea of "Prioritized Online Positioning Algorithm" [3]

### Issues:

- Feasible region is defined from some target  $v$ . How to define the target? How define start points?
- What is the purpose of feasible region? Does it correlate with motion?
- Test radio-map - how to get it? What information it should bring?

## 6 16.02.2017 Step 3. Continue.

- $t_0$ : suppose we start from the single user's position  $(x(t_0); y(t_0))$  somewhere in the room. Also we have some value of the velocity of the user  $v_0$ .
- $t_1$ : after some  $\Delta t$  we get our  $RSSI(t_1)$ . According to this RSSI we can calculate the probability of user's presence in cell  $k$  having such RSSI -  $p(k|RSSI(t_1))$ .  
Further, we can make an assumption about acceleration of the user - for example, we have  $\vec{a}_1 \sim N(0, \sigma)$  - the model of person's motion. We

can make  $k$  hypothesis about the supposing value of the acceleration and generate  $k$  samples. For each  $\vec{a_1(i)}$  we calculate  $\Delta s$ . Also, we calculate the probability of each hypothesis  $p(k|\vec{a_1(i)})$ .

- Using all previous information we calculate the new possible position of the user  $(x_i(t_1), y_i(t_1))$ . Among them we can choose only with the highest probabilities (particle filtering).
- Apply these three steps further until the error will not change.

Next:

- Look throw the code from [3].
- Python libs for visualization.
- Look for some model of person's motion.

## 7 22.02.2017

- The calibration data is then often used to estimate the parameters of locally Gaussian models, which have proven to be very effective for localization[2].
- How to distinguish fingerprint twins - generate and use user-motion database for the location [4]. (Can be useful for further development.)
- For practical positioning systems with limited computational power, e.g., slow processors, particle filter is the best choice. If the density functions are transferred between different nodes, Fourier-based filter should be used because fewer components require smaller bandwidth and communication time [6].

## 8 27.02.2017.Location Tracking Model.Version 1.

As basic information (at time  $t_0$ ) we have:

1. Signal propagation map: in each cell  $\{c_{ij}\}_{i=\overline{1,n};j=\overline{1,m}}$  signal has propagation with distribution  $N(\mu_{ij}, \sigma_{ij}^2)$ . (Suppose we work in discrete space.)
2. Start point  $s^{t_0} = (x^0; y^0)$ .
3. Start velocity  $v^0$ .

After some  $\Delta t$  at time  $t_1$  we got  $RSSI^{t_1}$ . After that:

1. We can calculate for each cell  $c_{ij}$  conditional probability  $p(c_{ij}|RSSI^{t_1})$  - the probability of staying at cell  $c_{ij}$  under condition of getting such signal strength.
2. **Person's motion model.** We make assumption about person's acceleration to predict his possible position. We suppose that acceleration has distribution  $N(0; \sigma_a^2)$ . Generate  $K$  samples  $\vec{a}_k$ ,  $k = \overline{1, K}$ .
3. Calculate new possible position according to the generated accelerations:  $s_k^{t_1} = s^{t_0} + v^0 \Delta t + \frac{a_k \Delta t^2}{2}$ .
4. For every cell  $c_{ij}$  calculate:  $p(RSSI^{t_1}, s_{ij}^{t_1}) = p(RSSI^{t_1})p(s_{ij}^{t_1})$ .
5. Leave particles with max probability with some threshold.
6. Continue.

For this approach put:  $n = 100$ ,  $m = 100$ ,  $v^0 = 0$ ,  $K = 100$ .

Points to think about / rebuild in model:

- Person's motion model. What parameters of normal distribution should we put? What other description of this model can be (other distribution, etc.)?
- Discrete space or continuous space?
- At point 4 the probability can be decomposed not in such way - the random variables can be dependent.
- Further model improvements - person's rotation element, dependence of current point of time of not one but some previous ones, ... .

## 9 Current approaches. 15.03.2017

For all:

**Input:** sequence of RSSI measurements:  $RSSI_1 \dots RSSI_n$ .

**Output:** path estimation  $(x_1, y_1) \dots (x_n, y_n)$ .

1. Simple Bayes approach  
Each step does not depend on any previous step and motion of the user. We get as input RSSI and at each approach the position as:

$$(x, y) = \operatorname{argmax}_{x, y} p(RSSI_i | (x, y))$$

2. Bayes approach with motion

Here we also add a model of user's motion:  $a \sim N(0, 1)$ . At each step we generate K samples of possible  $a$  and move previous position. Again does not depend on previous step. Position and acceleration will be chosen as:

$$(x, y, a) = \operatorname{argmax}_{x, y, a_k} p(RSSI_i | (x, y)) p(a_k)$$

3. Viterbi algorithm

**Parameters:** Let's suppose  $s = (x, y)$ . So, there should be provided information:  $p(s_i | s_{i-1} \dots s_{i-k})$ ,  $k = 1, \dots$ .

## References

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