# MathSBML: A Mathematica Package For Systems Biology

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# SBM L: A Tool-Neutral Model D efinition Form at

SBM L — the Systems Biology Markup Language — is a computer-readable format for representing models of biochemical reaction networks, applicable to:

• m e ta b o lic n e tw o rks,

• cell-signaling pathways,

• genom ic regulatory networks, and • other modeling problems in systems biology.

SBML is based on XML, a standard medium for representing and transporting data that is widely An Example supported on the Internet as well as in computational The following example illustrates a growing cell with a mitotic biology and bioinform atics.

Because SBM L is tool-independent, it enables

- use of multiple simulation and analysis tools in a single research project without rewriting models for each tool;
- publication of models in peer-re viewed journals— other researchers can download and use your modele ven if they use a different software en vironm ent:
- sur vival of models—they can outlive the software used to create them , making your work still useful e ∨en if a particular sim u lation package is no longer supported;

computational systems biology. SBML is currently with the simulator, at any time. For example, supported by a ver 60 to als including the following.

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BALSA	D B s o I ve	LION Target Engine	SC Ip a th
BASIS	D izzą	M ath S B M L	Sigmoid*
B io C h a ro n	E € EĹL	M esoRD	SigPath
biocyc2SBML	e c e IIJ	M etaboLogica	SigIran
B io G <sup>'</sup> rid	ESS	M M T 2	S im p a th ic a
B io N e tG e n	F lu xA n a ly ze r	M o d e s t o	Sim Wiz
B io Sketch P a d	Gepasi	M o le cu lizer	StochSim
Dashboard	IN SILIC Odisco ∨e ry	M O M A *	STOCKS
B io Spread sheet	Jarn ac	Monod	T re lis
B io U M L	JD esigner	N e t B u ild e r	V irtu a IC e II
BSTLab	Jig C e II	Path Art	V L XS u ite
C A D L IV E	JSIM	P a th S c o u t	W in S C A M P
CeIIDesigner	JWS*	P a V E S y	
C e lle ra to r	Karyote*	P a th w a y B u ild e r	
Cellw are	KEGG2SBML	ProcessDB*	*under
COPASI	K in so Ive r*	PySCeS*	d e ∨e lo p m e n t
Cytoscape	lib S B M L	SBW	

# M o d e l S c h e m a t i c



# MathSBML: A Package for Manipulating SBM L Files

</sbml>

Math SBM L is an open-source *Mathematica* package that facilitates working with SBM L models.Features include:

- Import of SBM L models to Mathematica
- Simulation and plotting of SBM L models
- Simulation of models with events
- Sim u lation of differential algebraic systems • Export of models to SBM L, HTM L, Berkeley
- Madonna, XPP, Fortran form ats
- Complete API for creating and modifying models • Tabularm odeldisplay and export to HTM L
- Ab ility to use any M athem atica capability • Open source / freely downloadable (LGPL)

### M odel Interoperability

With MathSBM Linvestigators can explore SBM Lmodels with the full range of *Mathematica* features. Mathematica is one of several platforms widely used by biological modelers and is available in many academic and commercial environments (e.g., over 500 US colleges and universities have site licenses).

Math SBM L provides full model in teroperability with this environment as well as a candidate reference implementation of SBML. Support of other generalpurpose languages, including C/C++, Java, Python, Perl, LISP and MATLAB have been developed separately using libSBML, a platform - independent library that is notpart of Math SBM L.

MathSBM L supports SBM L Level 1, Versions 1 and 2, and SBM L Level 2. The Math SBM L Model Editor supports SBM L Level 2.

Math SBM L will run on any platform that has Mathematica 4.1 or higher installed. The solution of differential-algebraic systems (SBM L models that have algebraic rules) requires Mathematica 5.0 or higher; purely differential systems (SBM L without algebraic rules) can be solved on *Mathematica* 4.1.

### The Model Builder: An SBM L API

MathSBM L contains a simple model editor, allowing users to create SBM L m odels compatible w ith other simulators, as well as a *Mathematica* text-command based API that can be used to produce arbitrarily complex SBML files. The model editor contains a suite of commands to add, modify, or remove single SBM Lobjects (such as a reaction, chemical species, or equation) from the current model. The model may be either created de-novo or read from a file. A fter building the model, the user can test it by running simulations, continue to modify it, or w rite the results as an SBM L file, in any order.

oscillator [Goldbeter, 1991] in which cell division is initiated when a variable passes a threshold. Cell division is indicated by defining a variable "Mass" that divides in half when both of the following tests are true at the same time: M > O.7 and Mass>0.6. The API commands to build and save the model to a file are shown in the box to the right. To read this file into the sim u lator, one could enter

s = SBMLRead["gmo.xml"]; A file on disk can be translated to htm I via

SBMLWrite[inputfile->"gmo.xml", outputfile->

"gmo.html", format-> "HTML"]; The output is illustrated in the large figure below. Other output form ats include XPP, Berkeley Madonna and Fortran. SBML is well on its way to be coming the *lingua franca* of When building a model, the user can save it to a file, or test it

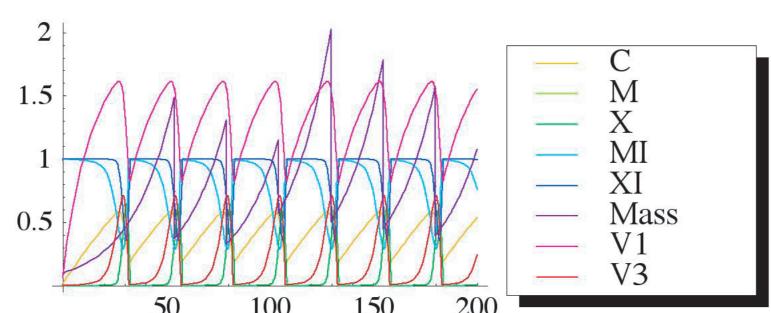
s = loadSimulator[];

returns a data structure (called s, in this case) that is compatible with the simulator; experienced Mathematica users can manipulate this data structure directly.

To run a simulation for, say, 200 time units, and plot all model variables, one would enter

n = SBMLNDSolve[s, 200];plt = SBMLPlot[n];

The resulting screen plot is shown below.



reaction3 reaction3 False MI → M

reaction4 reaction4 False M → MI

reaction5 reaction5 False XI → X

reaction6 reaction6 False X → XI

VARIABLE

Mass

# APICom m and s to Build the Model

<<mathsbml.m; newModel["GMO"]; addCompartment["cell"]; addFunction[id->mitosis,arguments->{m,mpf},math-> ((m>0.6)&&(mpf>0.7)); addSpecies[C,initialConcentration->0.01]; addSpecies[M,initialConcentration->0.01]; addSpecies[X,initialConcentration->0.01]; addSpecies[MI,initialConcentration->0.99]; addSpecies[XI,initialConcentration->0.99]; addParameter[Mass,value->0.1,constant->False]; addParameter[mu,value->0.05]; addParameter[V1,constant->False]; addParameter[V3,constant->False]; addParameter[VM1,value->3]; addParameter[VM3,value->1]; addParameter[Kc, value->0.5]; addRule[type->"RateRule", variable->Mass, math->mu\*Mass]; addRule[type->"AssignmentRule", variable->V1,

math-> C\*VM1/(Kc+C)]; addRule[type->"AlgebraicRule", math->M\*VM3-V3]; addReaction[products->{C},kineticLaw->(vi-kd\*C), parameters->{vi->0.025,kd>0.01},

reversible-> False]; addReaction[reactants->{C},modifiers->{X}, kineticLaw ->vd\*X\*C/(Kd+C),parameters->{vd->0.25, Kd-> .02},reversible-> False];

addReaction[MI->M,kineticLaw-> (V1\*MI/(K1+MI)),reversible-> False,parameters->{ K1-> .005}];

addReaction[M->MI,kineticLaw->V2\*M/(K2+M), parameters->{V2-> 1.5, K2->.005}, reversible->False]; addReaction[XI->X,kineticLaw->V3\*XI/(K3+XI),

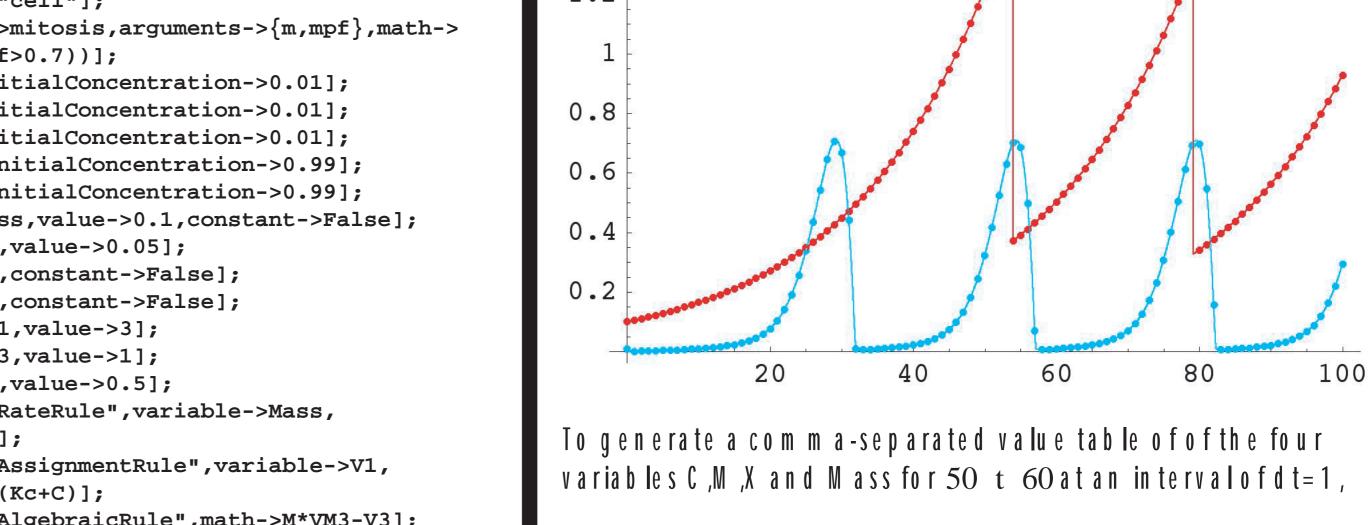
parameters->{K3->.005 }, reversible->False]; addReaction[X->XI,kineticLaw->V4\*X/(K4+X), parameters->{K4->.005, V4->.5},reversible->False]; add Event["CellDivision", trigger->mitosis[Mass,M], eventAssignment->{Mass->(Mass/2)}];

createModel["gmo.xml"];

Plots can be exported at any resolution and into any standard graphics form at; other options allow one to plot specific variables, om it the lines in favor of interpolated points, or generate a table of data. For example, to plot values of model variables M and Mass at an interval of dt=1 and then draw a smooth line show ing the complete plot:

p1 = SBMLListPlot[{GMO`M, GMO`Mass}, {t, 0, 100, 1}, n, PlotJoined -> False, PlotStyle -> {PointSize[0.01]} ]; p2 = SBMLListPlot[{GMO`M, GMO`Mass}, {t, 0, 100, .01}, n,

PlotJoined-> True];  $p3 = Show[{p1, p2}];$ 



dataTable[{GMO`C, GMO`M, GMO`X, GMO`Mass}, {t, 50,

60, 1}, n, format -> "CSV", file -> "data.csv"];

The contents of data.csv are illustrated:

# Availability and Documentation

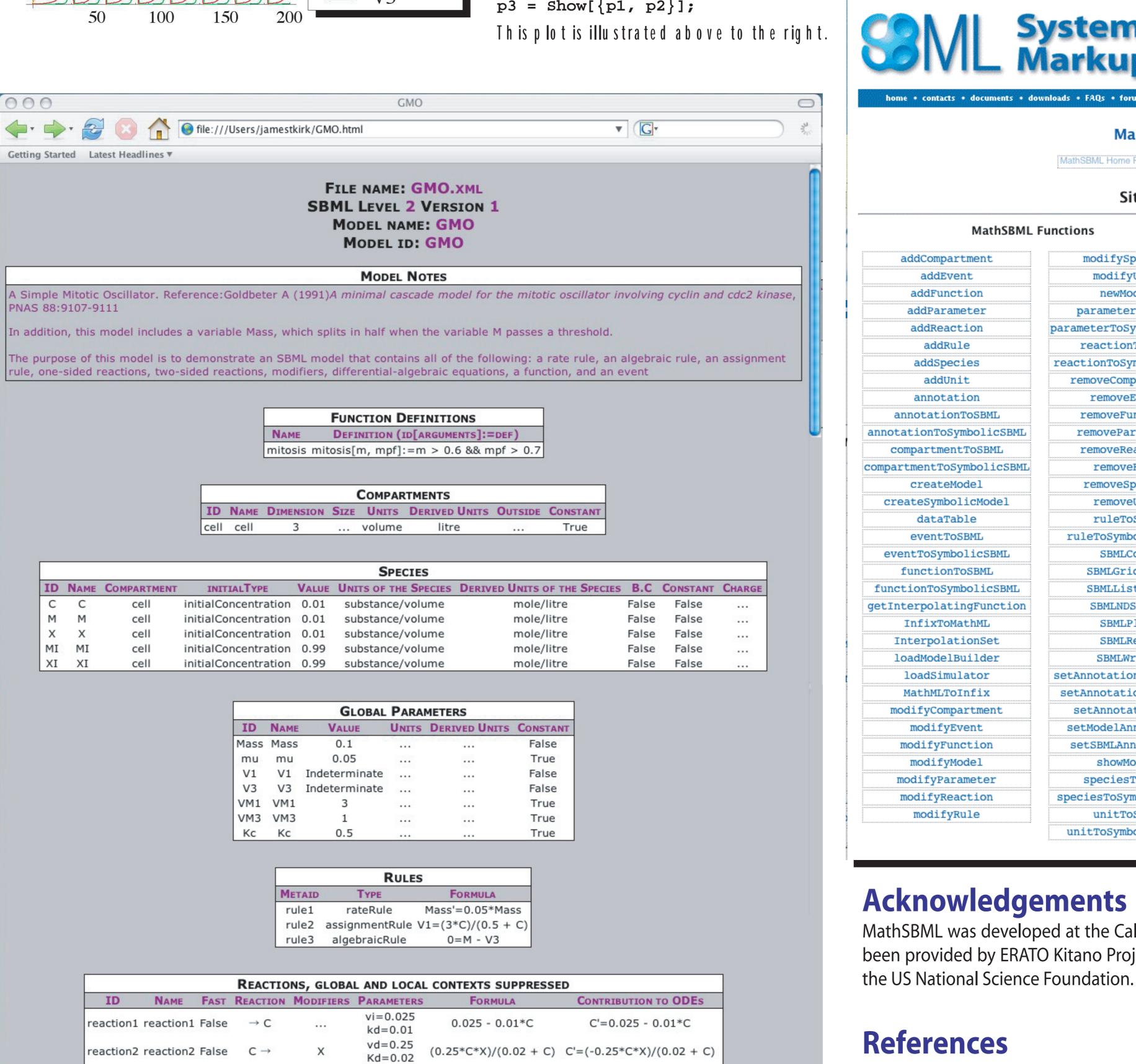
MathSBML is available free of charge from SourceForge under an LGPL license. It is open source and may be downloaded with a single click from our download site at:

# http://sf.net/projects/sbm l

Extensive documentation is included with the download, and is also available on line at the SBM L web site:

http://www.sbml.org/software/mathsbml/

For e ≫ample, the site map contains links to documentation on all API function points, as illustrated in the figure below.



(MI\*V1)/(0.005 + MI) MI'=-((MI\*V1)/(0.005 + MI))

(1.5\*M)/(0.005 + M)

(0.5\*X)/(0.005 + X)

DELAY TIMEUNITS

DIFFERENTIAL EQUATIONS, GLOBAL CONTEXT SUPPRESSED

EVENTS

TRIGGER

CellDivision CellDivision mitosis[Mass, M] 0

enerated by jamestkirk with MathSBML 2.4.0 (15-September-2004) on Slartibartifast at 20-September-2004 11:20:23.403293 using PowerPC/PowerMac/MacOSX

C'=0.025 - 0.01\*C - (0.25\*C\*X)/(0.02 + C)

M'=(-1.5\*M)/(0.005 + M) + (MI\*V1)/(0.005 + MI)

Mass'=0.05\*Mass

MI'=(1.5\*M)/(0.005 + M) - (MI\*V1)/(0.005 + MI)

X'=(-0.5\*X)/(0.005 + X) + (V3\*XI)/(0.005 + XI)

XI'=(0.5\*X)/(0.005 + X) - (V3\*XI)/(0.005 + XI)

MI'=(1.5\*M)/(0.005 + M)

M'=(-1.5\*M)/(0.005 + M)

X'=(V3\*XI)/(0.005 + XI)

XI' = -((V3\*XI)/(0.005 + XI))

XI'=(0.5\*X)/(0.005 + X)

X'=(-0.5\*X)/(0.005 + X)

### Systems Biology Markup Language MathSBML Home Page | MathSBML Site Map Site Map Other Pages Download Site (@sf.net) modifySpecies Abstracts, Publications, Posters modifyUnit Annotations in the Model Builder newModel Array Support in MathML (Modified Partial Implementation of Level 3 Proposal) parameterToSBML Bugs and Known Issues parameterToSymbolicSBML Examples reactionToSBMI FORTRAN Conversion (SBMLWrite) reactionToSymbolicSBML HTML Conversion (SBMLWrite) removeCompartment Mathematica v5 (@wri.com) removeEvent Mathematica v4 (@wri.com) MathSBML Home Page removeFunction MathSBML Installation Instructions removeParameter Model Builder Overview removeReaction Model Construction removeRule SBML Home Page removeSpecies Variable Scoping (Contexts) removeUnit XPP Conversion (SBMLWrite) ruleToSBML ruleToSymbolicSBML SBMLCopy SBMLGridPlot SBMLListPlot SBMLNDSolve SBMLPlot SBMLRead SBMLWrite setAnnotationNamespac setAnnotationPackage setAnnotationURL setModelAnnotation setSBMLAnnotation showMode] speciesToSBML speciesToSymbolicSBMI unitToSBML unitToSymbolicSBML

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http://sbml.org

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