Module 2

Chapter 1: The Relational Data Model

Introduction

The relational data model was first introduced by Ted Codd of IBM Research in 1970 in a classic paper (Codd 1970), and it attracted immediate attention due to its simplicity and mathematical foundation. The model uses the concept of a mathematical relation—which looks somewhat like a table of values—as its basic building block, and has its theoretical basis in set theory and first-order predicate logic.

The first commercial implementations of the relational model became available in the early 1980s, such as the SQL/DS system on the MVS operating system by IBM and the Oracle DBMS. Since then, the model has been implemented in a large number of commercial systems. Current popular relational DBMSs (RDBMSs) include DB2 and Informix Dynamic Server (from IBM), Oracle and Rdb (from Oracle), Sybase DBMS (from Sybase) and SQLServer and Access (from Microsoft). In addition, several open source systems, such as MySQL and PostgreSQL, are available.

1.1 Relational Model Concepts

The relational model represents the database as a collection of relations. Informally, each relation resembles a table of values or, to some extent, a flat file of records. It is called a **flat file** because each record has a simple linear or flat structure.

When a relation is thought of as a **table** of values, each row in the table represents a collection of related data values. A row represents a fact that typically corresponds to a real-world entity or relationship. The table name and column names are used to help to interpret the meaning of the values in each row.

For example, in STUDENT relation because each row represents facts about a particular student entity. The column names—Name, Student_number, Class, and Major—specify how to interpret the data values in each row, based on the column each value is in. All values in a column are of the same data type.

In the formal relational model terminology, a row is called a tuple, a column header is called an attribute, and the table is called a relation. The data type describing the types of values that can appear in each column is represented by a domain of possible values.

1.1.1 Domains, Attributes, Tuples, and Relations

Domain

A **domain** D is a set of atomic values. By **atomic** we mean that each value in the domain is indivisible as far as the formal relational model is concerned. A common method of specifying a domain is to specify a data type from which the data values forming the domain are drawn. It is also useful to specify a name for the domain, to help in interpreting its values.

Some examples of domains follow:

- Usa_phone_numbers: The set of ten-digit phone numbers valid in the United States.
- Social_security_numbers: The set of valid nine-digit Social Security numbers.
- Names: The set of character strings that represent names of persons.
- Employee_ages. Possible ages of employees in a company; each must be an integer value between 15 and 80.

The preceding are called logical definitions of domains. A **data type** or **format** is also specified for each domain. For example, the data type for the domain Usa_phone_numbers can be declared as a character string of the form (ddd)ddddddd, where each d is a numeric (decimal) digit and the first three digits form a valid telephone area code. The data type for Employee_ages is an integer number between 15 and 80.

Attribute

An attribute A_i is the name of a role played by some domain D in the relation schema R. D is called the **domain** of A_i and is denoted by $\mathbf{dom}(A_i)$.

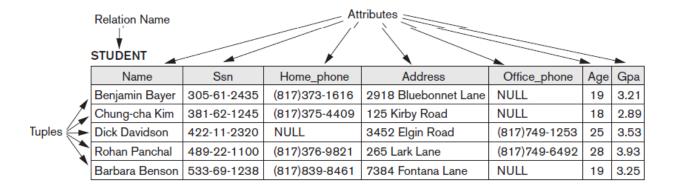
Tuple

Mapping from attributes to values drawn from the respective domains of those attributes. Tuples are intended to describe some entity (or relationship between entities) in the miniworld

Example: a tuple for a PERSON entity might be

Relation

A named set of tuples all of the same form i.e., having the same set of attributes.



Relation schema

A **relation schema** R, denoted by $R(A_1, A_2, ..., A_n)$, is made up of a relation name R and a list of attributes $A_1, A_2, ..., A_n$. Each **attribute** A_i is the name of a role played by some domain D in the relation schema R. D is called the **domain** of A_i and is denoted by **dom** (A_i) . A relation schema is used to *describe* a relation; R is called the **name** of this relation.

The **degree** (or arity) of a relation is the number of attributes n of its relation schema. A relation of degree seven, which stores information about university students, would contain seven attributes describing each student. as follows:

STUDENT(Name, Ssn, Home_phone, Address, Office_phone, Age, Gpa)

Using the data type of each attribute, the definition is sometimes written as:

STUDENT(Name: string, Ssn: string, Home_phone: string, Address: string,

Office_phone: string, Age: integer, Gpa: real)

Domains for some of the attributes of the STUDENT relation: dom(Name) = Names; dom(Ssn) = Social_security_numbers;

dom(HomePhone)=USA_phone_numbers,dom(Office_phone)= USA_phone_numbers,

Relation (or relation state)

A relation (or relation state) r of the relation schema by $R(A_1, A_2, ..., A_n)$, also denoted by r(R), is a set of n-tuples $r = \{t_1, t_2, ..., t_m\}$. Each n-tuple t is an ordered list of n values $t = < v_1, v_2, ..., v_n >$, where each value vi, $1 \le i < \le n$, is an element of dom (A_i) or is a special NULL value. The i^{th} value in tuple t, which corresponds to the attribute A_i , is referred to as $t[A_i]$ or t. A_i .

The terms **relation intension** for the schema R and **relation extension** for a relation state r(R) are also commonly used.

1.1.2 Characteristics of Relations

1. Ordering of Tuples in a Relation

A relation is defined as a *set* of tuples. Mathematically, elements of a set have *no order* among them; hence, tuples in a relation do not have any particular order. Tuple ordering is not part of a relation definition because a relation attempts to represent facts at a logical or abstract level. Many tuple orders can be specified on the same relation.

2. Ordering of Values within a Tuple and an Alternative Definition of a Relation

The order of attributes and their values is *not* that important as long as the correspondence between attributes and values is maintained. An alternative definition of a relation can be given, making the ordering of values in a tuple unnecessary. In this definition A **relation** schema $R(A_1, A_2, ..., A_n)$, set of attributes and a **relation state** r(R) is a finite set of mappings $r = \{t1, t2, ..., tm\}$, where each tuple ti is a **mapping** from R to D.

According to this definition of tuple as a mapping, a **tuple** can be considered as a set of (\langle attribute \rangle , \langle value \rangle) pairs, where each pair gives the value of the mapping from an attribute A_i to a value vi from $dom(A_i)$. The ordering of attributes is not important, because the attribute name appears with its value.

3. Values and NULLs in the Tuples

Each value in a tuple is atomic. NULL values are used to represent the values of attributes that may be unknown or may not apply to a tuple. For example some STUDENT tuples have NULL for their office phones because they do not have an office .Another student has a NULL for home phone In general, we can have several meanings for NULL values, such as value unknown, value exists but is not available, or attribute does not apply to this tuple (also known as value undefined).

4. Interpretation (Meaning) of a Relation

The relation schema can be interpreted as a declaration or a type of **assertion**. For example, the schema of the STUDENT relation of asserts that, in general, a student entity has a Name, Ssn, Home_phone, Address, Office_phone, Age, and Gpa. Each tuple in the relation can then be interpreted as a particular instance of the assertion. For example, the first tuple asserts the fact that there is a STUDENT whose Name is Benjamin Bayer, Ssn is 305-61-2435, Age is 19, and so on.

An alternative interpretation of a relation schema is as a **predicate**; in this case, the values in each tuple are interpreted as values that *satisfy* the predicate.

1.1.3 Relational Model Notation

- Relation schema R of degree n is denoted by By $R(A_1, A_2, ..., A_n)$
- Uppercase letters Q, R, S denote relation names
- Lowercase letters q, r, s denote relation states
- Letters t, u, v denote tuples
- In general, the name of a relation schema such as STUDENT also indicates the current set of tuples in that relation
- An attribute A can be qualified with the relation name R to which it belongs by using the dot notation R.A—for example, STUDENT.Name or STUDENT.Age.
- An *n*-tuple t in a relation r(R) is denoted by $t = \langle v_1, v_2, ..., v_n \rangle$, where v_i is the value corresponding to attribute A_i . The following notation refers to **component values** of tuples:
- Both $t[A_i]$ and $t.A_i$ (and sometimes t[i]) refer to the value v_i in t for attribute A_i .
- Both $t[A_u, A_w, ..., A_z]$ and $t.(A_u, A_w, ..., A_z)$, where $A_u, A_w, ..., A_z$ is a list of attributes from R, refer to the subtuple of values $\langle v_u, v_w, ..., v_z \rangle$ from t corresponding to the attributes specified in the list.

1.2 Relational Model Constraints and Relational Database Schemas

Constraints are restrictions on the actual values in a database state. These constraints are derived from the rules in the miniworld that the database represents. Constraints on databases can generally be divided into three main categories:

- 1. Inherent model-based constraints or implicit constraints
 - Constraints that are inherent in the data model.
 - The characteristics of relations are the inherent constraints of the relational model and belong to the first category. For example, the constraint that a relation cannot have duplicate tuples is an inherent constraint.
- 2. Schema-based constraints or explicit constraints
 - Constraints that can be directly expressed in schemas of the data model, typically by specifying them in the DDL.
 - The schema-based constraints include domain constraints, key constraints, constraints on NULLs, entity integrity constraints, and referential integrity constraints.
- 3. Application-based or semantic constraints or business rules
 - Constraints that *cannot* be directly expressed in the schemas of the data model, and hence must be expressed and enforced by the application programs.

• Examples of such constraints are the salary of an employee should not exceed the salary of the employee's supervisor and the maximum number of hours an employee can work on all projects per week is 56.

1.2.1 Domain Constraints

Domain Constraints specify that within each tuple, the value of each attribute A must be an atomic value from the domain dom(A). The data types associated with domains typically include standard numeric data types for integers (such as short integer, integer, and long integer) and real numbers (float and doubleprecision float). Characters, Booleans, fixed-length strings, and variable-length strings are also available, as are date, time, timestamp, and money, or other special data types.

1.2.2 Key Constraints and Constraints on NULL Values

All tuples in a relation must also be distinct. This means that no two tuples can have the same combination of values for *all* their attributes. There are other **subsets of attributes** of a relation schema R with the property that no two tuples in any relation state r of R should have the same combination of values for these attributes.

Suppose that we denote one such subset of attributes by SK; then for any two *distinct* tuples t1 and t2 in a relation state r of R, we have the constraint that: $t_1[SK] \neq t_2[SK]$. such set of attributes SK is called a **superkey** of the relation schema R

superkey

A superkey SK specifies a *uniqueness constraint* that no two distinct tuples in any state *r* of *R* can have the same value for SK. Every relation has at least one default superkey—the set of all its attributes.

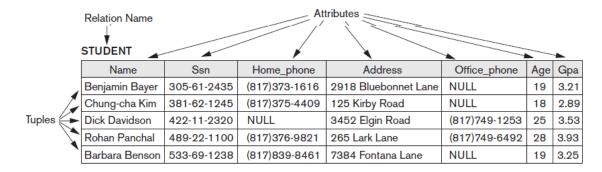
Kev

A key K of a relation schema R is a superkey of R with the additional property that removing any attribute A from K leaves a set of attributes K, that is not a superkey of R anymore. Hence, a key satisfies two properties:

1. Two distinct tuples in any state of the relation cannot have identical values for (all) the attributes in the key. This first property also applies to a superkey.

2. It is a minimal superkey—that is, a superkey from which we cannot remove any attributes and still have the uniqueness constraint in condition 1 hold. This property is not required by a superkey.

Example: Consider the STUDENT relation



- The attribute set {Ssn} is a key of STUDENT because no two student tuples can have the same value for Ssn
- Any set of attributes that includes Ssn—for example, {Ssn, Name, Age}—is a superkey
- The superkey {Ssn, Name, Age} is not a key of STUDENT because removing Name or Age or both from the set still leaves us with a superkey

In general, any superkey formed from a single attribute is also a key. A key with multiple attributes must require *all* its attributes together to have the uniqueness property.

Candidate key

A relation schema may have more than one key. In this case, each of the keys is called a **candidate key.** For example, the CAR relation has two candidate keys: License_number and Engine_serial_number

CAR

License_number	Engine_serial_number	Make	Model	Year
Texas ABC-739	A69352	Ford	Mustang	02
Florida TVP-347	B43696	Oldsmobile	Cutlass	05
New York MPO-22	X83554	Oldsmobile	Delta	01
California 432-TFY	C43742	Mercedes	190-D	99
California RSK-629	Y82935	Toyota	Camry	04
Texas RSK-629	U028365	Jaguar	XJS	04

Primary key

It is common to designate one of the candidate keys as the **primary key** of the relation. This is the candidate key whose values are used to *identify* tuples in the relation. We use the convention that the attributes that form the primary key of a relation schema are underlined. Other candidate keys are designated as **unique keys** and are not underlined

Another constraint on attributes specifies whether NULL values are or are not permitted. For example, if every STUDENT tuple must have a valid, non-NULL value for the Name attribute, then Name of STUDENT is constrained to be NOT NULL.

1.2.3 Relational Databases and Relational Database Schemas

A Relational database schema S is a set of relation schemas $S = \{R_1, R_2, ..., R_m\}$ and a s et of integrity constraints IC.

Example of relational database schema:

COMPANY = {EMPLOYEE, DEPARTMENT, DEPT_LOCATIONS, PROJECT, WORKS_ON, DEPENDENT}

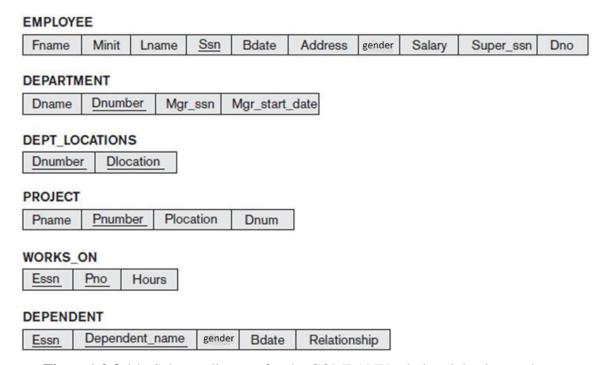


Figure 1.2.3 (a): Schema diagram for the COMPANY relational database schema.

The underlined attributes represent primary keys

A Relational database state is a set of relation states $DB = \{r_1, r_2, ..., r_m\}$. Each r_i is a state of R and such that the r_i relation states satisfy integrity constraints specified in IC.

EMPLOYEE

Fname	Minit	Lname	Ssn	Bdate	Address	gende	Salary	Super_ssn	Dno
John	В	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	М	30000	333445555	5
Franklin	Т	Wong	333445555	1955-12-08	638 Voss, Houston, TX	М	40000	888665555	5
Alicia	J	Zelaya	999887777	1968-01-19	3321 Castle, Spring, TX	F	25000	987654321	4
Jennifer	S	Wallace	987654321	1941-06-20	291 Berry, Bellaire, TX	F	43000	888665555	4
Ramesh	K	Narayan	666884444	1962-09-15	975 Fire Oak, Humble, TX	М	38000	333445555	5
Joyce	Α	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5
Ahmad	V	Jabbar	987987987	1969-03-29	980 Dallas, Houston, TX	М	25000	987654321	4
James	Е	Borg	888665555	1937-11-10	450 Stone, Houston, TX	М	55000	NULL	1

DEPARTMENT

Dname	Dnumber	Mgr_ssn	Mgr_start_date
Research	5	333445555	1988-05-22
Administration	4	987654321	1995-01-01
Headquarters	1	888665555	1981-06-19

WORKS_ON

Essn	Pno	Hours
123456789	1	32.5
123456789	2	7.5
666884444	3	40.0
453453453	1	20.0
453453453	2	20.0
333445555	2	10.0
333445555	3	10.0
333445555	10	10.0
333445555	20	10.0
999887777	30	30.0
999887777	10	10.0
987987987	10	35.0
987987987	30	5.0
987654321	30	20.0
987654321	20	15.0
888665555	20	NULL

DEPT_LOCATIONS

Dnumber	Dlocation
1	Houston
4	Stafford
5	Bellaire
5	Sugarland
5	Houston

PROJECT

Pname	Pnumber	Plocation	Dnum
ProductX	1	Bellaire	5
ProductY	2	Sugarland	5
ProductZ	3	Houston	5
Computerization	10	Stafford	4
Reorganization	20	Houston	1
Newbenefits	30	Stafford	4

DEPENDENT

Essn	Dependent_name	gender	Bdate	Relationship
333445555	Alice	F	1986-04-05	Daughter
333445555	Theodore	M	1983-10-25	Son
333445555	Joy	F	1958-05-03	Spouse
987654321	Abner	М	1942-02-28	Spouse
123456789	Michael	М	1988-01-04	Son
123456789	Alice	F	1988-12-30	Daughter
123456789	Elizabeth	F	1967-05-05	Spouse

Figure 1.2.3(b): One possible database state for the COMPANY relational database schema.

A database state that does not obey all the integrity constraints is called **Invalid state** and a state that satisfies all the constraints in the defined set of integrity constraints IC is called a **Valid state**

Attributes that represent the same real-world concept may or may not have identical names in different relations. For example, the Dnumber attribute in both DEPARTMENT and DEPT_LOCATIONS stands for the same real-world concept—the number given to a department. That same concept is called Dno in EMPLOYEE and Dnum in PROJECT.

Alternatively, attributes that represent different concepts may have the same name in different relations. For example, we could have used the attribute name Name for both Pname of PROJECT and Dname of DEPARTMENT; in this case, we would have two attributes that share the same name but represent different realworld concepts—project names and department names.

1.2.4 Integrity, Referential Integrity, and Foreign Keys

Entity integrity constraint

The entity integrity constraint states that no primary key value can be NULL. This is because the primary key value is used to identify individual tuples in a relation. Having NULL values for the primary key implies that we cannot identify some tuples. For example, if two or more tuples had NULL for their primary keys, we may not be able to distinguish them if we try to reference them from other relations.

Key constraints and entity integrity constraints are specified on individual relations.

Referential integrity constraint

The referential integrity constraint is specified between two relations and is used to maintain the consistency among tuples in the two relations. Informally, the referential integrity constraint states that a tuple in one relation that refers to another relation must refer to an existing tuple in that relation.

For example COMPANY database, the attribute Dno of EMPLOYEE gives the department number for which each employee works; hence, its value in every EMPLOYEE tuple must match the Dnumber value of some tuple in the DEPARTMENT relation.

To define referential integrity more formally, first we define the concept of a *foreign key*. The conditions for a foreign key, given below, specify a referential integrity constraint between the two relation schemas R_1 and R_2 .

A set of attributes FK in relation schema R_1 is a **foreign key** of R_1 that **references** relation R_2 if it satisfies the following rules:

- 1. Attributes in FK have the same domain(s) as the primary key attributes PK of R_2 ; the attributes FK are said to **reference** or **refer to** the relation R_2 .
- 2. A value of FK in a tuple t_1 of the current state $r_1(R_1)$ either occurs as a value of PK for some tuple t_2 in the current state $r_2(R_2)$ or is NULL.

In the former case, we have $t_1[FK] = t_2[PK]$, and we say that the tuple t_1 **references** or **refers to** the tuple t_2 .

In this definition, R_1 is called the **referencing relation** and R_2 is the **referenced relation**. If these two conditions hold, a **referential integrity constraint** from R_1 to R_2 is said to hold.

1.2.5 Other Types of Constraints

Semantic integrity constraints

Semantic integrity constraints can be specified and enforced within the application programs that update the database, or by using a general-purpose constraint specification language. Examples of such constraints are the salary of an employee should not exceed the salary of the employee's supervisor and the maximum number of hours an employee can work on all projects per week is 56. Mechanisms called **triggers** and **assertions** can be used. In SQL, CREATE ASSERTION and CREATE TRIGGER statements can be used for this purpose.

Functional dependency constraint

Functional dependency constraint establishes a functional relationship among two sets of attributes X and Y. This constraint specifies that the value of X determines a unique value of Y in all states of a relation; it is denoted as a functional dependency $X \to Y$. We use functional dependencies and other types of dependencies as tools to analyze the quality of relational designs and to "normalize" relations to improve their quality.

State constraints(static constraints)

Define the constraints that a valid state of the database must satisfy

Transition constraints(dynamic constraints)

Define to deal with state changes in the database

1.3 Update Operations, Transactions, and Dealing with Constraint Violations

The operations of the relational model can be categorized into **retrievals** and **updates**

There are three basic operations that can change the states of relations in the database:

- 1. Insert used to insert one or more new tuples in a relation
- 2. Delete- used to delete tuples
- 3. Update (or Modify)- used to change the values of some attributes in existing tuples

Whenever these operations are applied, the integrity constraints specified on the relational database schema should not be violated.

1.3.1 The Insert Operation

The Insert operation provides a list of attribute values for a new tuple *t* that is to be inserted into a elation *R*. Insert can violate any of the four types of constraints

- **1. Domain constraints :** if an attribute value is given that does not appear in the corresponding domain or is not of the appropriate data type
- **2. Key constraints :** if a key value in the new tuple t already exists in another tuple in the relation r(R)
- **3.** Entity integrity: if any part of the primary key of the new tuple t is NULL
- **4. Referential integrity:** if the value of any foreign key in *t* refers to a tuple that does not exist in the referenced relation

Examples:

1. Operation:

```
Insert < 'Cecilia', 'F', 'Kolonsky', NULL, '1960-04-05', '6357 Windy Lane, Katy, TX', F, 28000, NULL, 4>
```

Result: This insertion violates the entity integrity constraint (NULL for the primary key Ssn), so it is rejected

2. Operation:

```
Insert <'Alicia', 'J', 'Zelaya', '999887777', '1960-04-05', '6357 Windy Lane, Katy, TX', F, 28000, '987654321', 4>
```

Result: This insertion violates the key constraint because another tuple with the same Ssn value already exists in the EMPLOYEE relation, and so it is rejected.

3. Operation:

```
Insert < 'Cecilia', 'F', 'Kolonsky', '677678989', '1960-04-05', '6357 Windswept, Katy, TX', F, 28000, '987654321', 7>
```

Result: This insertion violates the referential integrity constraint specified on Dno in EMPLOYEE because no corresponding referenced tuple exists in DEPARTMENT with Dnumber = 7.

4. Operation:

```
Insert < 'Cecilia', 'F', 'Kolonsky', '677678989', '1960-04-05', '6357 Windy Lane, Katy, TX', F, 28000, NULL, 4>
```

Result: This insertion satisfies all constraints, so it is acceptable.

If an insertion violates one or more constraints, the default option is to reject the insertion. It would be useful if the DBMS could provide a reason to the user as to why the insertion was rejected. Another option is to an attempt to correct the reason for rejecting the insertion

1.3.2 The Delete Operation

The Delete operation can violate only referential integrity. This occurs if the tuple being deleted is referenced by foreign keys from other tuples in the database. To specify deletion, a condition on the attributes of the relation selects the tuple (or tuples) to be deleted.

Examples:

1. Operation:

Delete the WORKS_ON tuple with Essn = '999887777' and Pno =10.

Result: This deletion is acceptable and deletes exactly one tuple.

2. Operation:

Delete the EMPLOYEE tuple with Ssn = '999887777'.

Result: This deletion is not acceptable, because there are tuples in WORKS_ON that refer to this tuple. Hence, if the tuple in EMPLOYEE is deleted, referential integrity violations will result.

3. Operation:

Delete the EMPLOYEE tuple with Ssn = '333445555'

Result: This deletion will result in even worse referential integrity violations, because the tuple involved is referenced by tuples from the EMPLOYEE, DEPARTMENT, WORKS_ON, and DEPENDENT relations.

Several options are available if a deletion operation causes a violation

- 1. restrict is to reject the deletion
- 2. cascade, is to attempt to cascade (or propagate) the deletion by deleting tuples that reference the tuple that is being deleted

3. Set null or set default - is to modify the referencing attribute values that cause the violation; each such value is either set to NULL or changed to reference another default valid tuple.

1.3.3 The Update Operation

The Update (or Modify) operation is used to change the values of one or more attributes in a tuple (or tuples) of some relation *R*. It is necessary to specify a condition on the attributes of the relation to select the tuple (or tuples) to be modified.

Examples:

1. Operation:

Update the salary of the EMPLOYEE tuple with Ssn = '999887777' to 28000.

Result: Acceptable.

2. Operation:

Update the Dno of the EMPLOYEE tuple with Ssn = '999887777' to 7.

Result: Unacceptable, because it violates referential integrity.

3. Operation:

Update the Ssn of the EMPLOYEE tuple with Ssn = '999887777' to '987654321'.

Result: Unacceptable, because it violates primary key constraint by repeating a value that already exists as a primary key in another tuple; it violates referential integrity constraints because there are other relations that refer to the existing value of Ssn

Updating an attribute that is neither part of a primary key nor of a foreign key usually causes no problems; the DBMS need only check to confirm that the new value is of the correct data type and domain.

1.3.4 The Transaction Concept

A **transaction** is an executing program that includes some database operations, such as reading from the database, or applying insertions, deletions, or updates to the database. At the end of the transaction, it must leave the database in a valid or consistent state that satisfies all the constraints specified on the database schema. A single transaction may involve any number of retrieval operations and any number of update operations. These retrievals and updates will together form an atomic unit of work against the database. For example, a transaction to apply a bank withdrawal will typically read the user account record, check if there is a sufficient balance, and then update the record by the withdrawal amount.

Chapter 2: Relational Algebra

2.1 Introduction

Relational algebra is the basic set of operations for the relational model. These operations enable a user to specify basic retrieval requests as relational algebra expressions. The result of an operation is a new relation, which may have been formed from one or more input relations.

The relational algebra is very important for several reasons

- First, it provides a formal foundation for relational model operations.
- Second, and perhaps more important, it is used as a basis for implementing and optimizing queries in the query processing and optimization modules that are integral parts of relational database management systems (RDBMSs)
- Third, some of its concepts are incorporated into the SQL standard query language for RDBMSs

2.2 Unary Relational Operations: SELECT and PROJECT

2.2.1 The SELECT Operation

The SELECT operation denoted by σ (sigma) is used to select a subset of the tuples from a relation based on a selection condition. The selection condition acts as a filter that keeps only those tuples that satisfy a qualifying condition. Alternatively, we can consider the SELECT operation to *restrict* the tuples in a relation to only those tuples that satisfy the condition.

The SELECT operation can also be visualized as a *horizontal partition* of the relation into two sets of tuples—those tuples that satisfy the condition and are selected, and those tuples that do not satisfy the condition and are discarded.

In general, the select operation is denoted by

σ <selection condition>(R)

where,

- the symbol σ is used to denote the select operator
- the selection condition is a Boolean (conditional) expression specified on the attributes of relation R
- tuples that make the condition true are selected
 - appear in the result of the operation
- tuples that make the condition false are filtered out
 - · discarded from the result of the operation

The Boolean expression specified in <selection condition> is made up of a number of clauses of the form:

<attribute name> <comparison op> <constant value>

or

<attribute name> <comparison op> <attribute name>

where

<attribute name> is the name of an attribute of R,

<comparison op> is one of the operators $\{=, <, \leq, >, \geq, \neq\}$, and

<constant value> is a constant value from the attribute domain

Clauses can be connected by the standard Boolean operators *and*, *or*, and *not* to form a general selection condition

Examples:

1. Select the EMPLOYEE tuples whose department number is 4.

$$\sigma_{DNO=4}$$
 (EMPLOYEE)

2. Select the employee tuples whose salary is greater than \$30,000.

$$\sigma_{SALARY > 30.000}$$
 (EMPLOYEE)

3. Select the tuples for all employees who either work in department 4 and make over \$25,000 per year, or work in department 5 and make over \$30,000

The result of a SELECT operation can be determined as follows:

- The <selection condition> is applied independently to each individual tuple t in R
- If the condition evaluates to TRUE, then tuple *t* is selected. All the selected tuples appear in the result of the SELECT operation
- The Boolean conditions AND, OR, and NOT have their normal interpretation, as follows:
 - (cond1 AND cond2) is TRUE if both (cond1) and (cond2) are TRUE; otherwise,it is FALSE.
 - (cond1 OR cond2) is TRUE if either (cond1) or (cond2) or both are TRUE; otherwise, it is FALSE.
 - (NOT cond) is TRUE if cond is FALSE; otherwise, it is FALSE.

The SELECT operator is unary; that is, it is applied to a single relation. The degree of the relation resulting from a SELECT operation is the same as the degree of R.The number of tuples in the resulting relation is always less than or equal to the number of tuples in R. That is,

$$|\sigma_c(R)| \le |R|$$
 for any condition C

The fraction of tuples selected by a selection condition is referred to as the selectivity of the condition.

The SELECT operation is commutative; that is,

$$\sigma_{< cond1>}(\sigma_{< cond2>}(R)) = \sigma_{< cond2>}(\sigma_{< cond1>}(R))$$

Hence, a sequence of SELECTs can be applied in any order.we can always combine a cascade (or sequence) of SELECT operations into a single SELECT operation with a conjunctive (AND) condition; that is,

 $\sigma_{< cond1>}(\sigma < cond2>(...(\sigma_{< condn>}(R))...)) = \sigma_{< cond1>} AND_{< cond2>} AND$... $AND_{< condn>}(R)$ In SQL, the SELECT condition is specified in the WHERE clause of a query. For example, the following operation:

 $\sigma_{Dno=4}$ AND $_{Salary>25000}$ (EMPLOYEE)

would to the following SQL query:

SELECT * FROM EMPLOYEE WHERE Dno=4 AND Salary>25000;

2.2.2 The PROJECT Operation

The PROJECT operation denoted by π (pi) selects certain columns from the table and discards the other columns. Used when we are interested in only certain attributes of a relation. The result of the PROJECT operation can be visualized as a vertical partition of the relation into two relations:

- one has the needed columns (attributes) and contains the result of the operation
- the other contains the discarded columns

The general form of the PROJECT operation is

$$\pi_{\text{}}(R)$$

where

 π (pi) - symbol used to represent the PROJECT operation,

<attributelist> - desired sublist of attributes from the attributes of relation R.

The result of the PROJECT operation has only the attributes specified in <attribute list> in the same order as they appear in the list. Hence, its degree is equal to the number of attributes in <attribute list>

Example:

1. To list each employee's first and last name and salary we can use the PROJECT operation as follows:

π_{Lname}, Fname, Salary (EMPLOYEE)

If the attribute list includes only nonkey attributes of R, duplicate tuples are likely to occur. The result of the PROJECT operation is a set of distinct tuples, and hence a valid relation. This is known as **duplicate elimination**. For example, consider the following PROJECT operation:

 $\pi_{gender, Salary}(EMPLOYEE)$

Lname	Fname	Salary
Smith	John	30000
Wong	Franklin	40000
Zelaya	Alicia	25000
Wallace	Jennifer	43000
Narayan	Ramesh	38000
English	Joyce	25000
Jabbar	Ahmad	25000
Borg	James	55000

The tuple <'F', 25000> appears only once in resulting relation even though this combination of values appears twice in the EMPLOYEE relation.

The number of tuples in a relation resulting from a PROJECT operation is always less than or equal to the number of tuples in *R*. Commutativity does not hold on PROJECT

$$\pi_{\text{}}(\pi_{\text{}}(R)) = \pi_{\text{}}(R)$$

as long as contains the attributes in t); otherwise, the left-hand side is an incorrect expression.

In SQL, the PROJECT attribute list is specified in the SELECT clause of a query. For example, the following operation:

$$\pi_{gender,\;Salary}(EMPLOYEE)$$

would correspond to the following SQL query:

SELECT DISTINCT gender, Salary **FROM** EMPLOYEE

2.2.3 Sequences of Operations and the RENAME Operation

For most queries, we need to apply several relational algebra operations one after the other. Either we can write the operations as a single relational algebra expression by nesting the operations, or we can apply one operation at a time and create intermediate result relations. In the latter case, we must give names to the relations that hold the intermediate results.

For example, to retrieve the first name, last name, and salary of all employees who work in department number 5, we must apply a SELECT and a PROJECT operation. We can write a single relational algebra expression, also known as an **in-line expression**, as follows:

$$\pi_{\text{Fname, Lname, Salary}}(\sigma_{\text{Dno=5}}(\text{EMPLOYEE}))$$

Alternatively, we can explicitly show the sequence of operations, giving a name to each intermediate relation, as follows:

$$\begin{aligned} DEP5_EMPS \leftarrow \sigma_{Dno=5}(EMPLOYEE) \\ RESULT \leftarrow \pi_{Fname,\,Lname,\,Salary}(DEP5_EMPS) \end{aligned}$$

We can also use this technique to **rename** the attributes in the intermediate and result relations. To rename the attributes in a relation, we simply list the new attribute names in parentheses

TEMP
$$\leftarrow \sigma_{Dno=5}(EMPLOYEE)$$

 $R(First_name, Last_name, Salary) \leftarrow \pi_{Fname, Lname, Salary}(TEMP)$

TEMP

Fname	Minit	Lname	Ssn	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	В	Smith	123456789	1965-01-09	731 Fondren, Houston,TX	М	30000	333445555	5
Franklin	T	Wong	333445555	1955-12-08	638 Voss, Houston,TX	М	40000	888665555	5
Ramesh	K	Narayan	666884444	1962-09-15	975 Fire Oak, Humble,TX	М	38000	333445555	5
Joyce	Α	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5

R

First_name	Last_name	Salary
John	Smith	30000
Franklin	Wong	40000
Ramesh	Narayan	38000
Joyce	English	25000

If no renaming is applied, the names of the attributes in the resulting relation of a SELECT operation are the same as those in the original relation and in the same order. For a PROJECT operation with no renaming, the resulting relation has the same attribute names as those in the projection list and in the same order in which they appear in the list.

We can also define a formal RENAME operation—which can rename either the relation name or the attribute names, or both—as a unary operator.

The general RENAME operation when applied to a relation R of degree n is denoted by any of the following three forms:

1. $\rho_{S(B1, B2, ..., Bn)}(R)$

 ρ (rho) – RENAME operator

2. $\rho S(R)$

S – new relation name

3. $\rho_{(B1, B2,Bn)}(R)$

 $B_1, B_2, \dots B_n$ - new attribute names

The first expression renames both the relation and its attributes. Second renames the relation only and the third renames the attributes only. If the attributes of R are $(A_1, A_2, ..., A_n)$ in that order, then each A_i is renamed as B_i .

Renaming in SQL is accomplished by aliasing using AS, as in the following example:

SELECT E.Fname AS First_name,

E.Lname AS Last_name,

E.Salary AS Salary

FROM EMPLOYEE AS E

WHERE E.Dno=5,

2.3 Relational Algebra Operations from Set Theory

2.3.1 The UNION, INTERSECTION, and MINUS Operations

- UNION: The result of this operation, denoted by $R \cup S$, is a relation that includes all tuples that are either in R or in S or in both R and S. Duplicate tuples are eliminated.
- **INTERSECTION:** The result of this operation, denoted by $R \cap S$, is a relation that includes all tuples that are in both R and S.
- **SET DIFFERENCE** (or MINUS): The result of this operation, denoted by R S, is a relation that includes all tuples that are in R but not in S.

Example: Consider the following two relations: STUDENT & INSTRUCTOR

STUDENT

Ln
Yao
Shah
Kohler
Jones
Ford
Wang
Gilbert

INSTRUCTOR

Fname	Lname
John	Smith
Ricardo	Browne
Susan	Yao
Francis	Johnson
Ramesh	Shah

STUDENT UINSTRUCTOR

STUDENT \cap **INSTRUCTOR**

Fn	Ln
Susan	Yao
Ramesh	Shah
Johnny	Kohler
Barbara	Jones
Amy	Ford
Jimmy	Wang
Ernest	Gilbert
John	Smith
Ricardo	Browne
Francis	Johnson

Fn	Ln
Susan	Yao
Ramesh	Shah

STUDENT – INSTRUCTOR

INSTRUCTOR – STUDENT

Fn	Ln
Johnny	Kohler
Barbara	Jones
Amy	Ford
Jimmy	Wang
Ernest	Gilbert

Fname	Lname
John	Smith
Ricardo	Browne
Francis	Johnson

Example: To retrieve the Social Security numbers of all employees who either work in department 5 or directly supervise an employee who works in department 5

DEP5_EMPS $\leftarrow \sigma_{Dno=5}(EMPLOYEE)$

RESULT1 $\leftarrow \pi_{Ssn}(DEP5_EMPS)$

RESULT2(Ssn) $\leftarrow \pi_{Super_ssn}(DEP5_EMPS)$

RESULT ← RESULT1 ∪ RESULT2

EMPLOYEE

Fname	Minit	Lname	Ssn	Bdate	Address	gender	Salary	Super_ssn	Dno
John	В	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	М	30000	333445555	5
Franklin	Т	Wong	333445555	1955-12-08	638 Voss, Houston, TX	M	40000	888665555	5
Alicia	J	Zelaya	999887777	1968-01-19	3321 Castle, Spring, TX	F	25000	987654321	4
Jennifer	S	Wallace	987654321	1941-06-20	20 291 Berry, Bellaire, TX		43000	888665555	4
Ramesh	K	Narayan	666884444	1962-09-15	9-15 975 Fire Oak, Humble, TX		38000	333445555	5
Joyce	Α	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5
Ahmad	V	Jabbar	987987987	1969-03-29	980 Dallas, Houston, TX	М	25000	987654321	4
James	Е	Borg	888665555	1937-11-10	450 Stone, Houston, TX	М	55000	NULL	1

RESULT1	RESULT2	RESULT
Ssn	Ssn	Ssn
123456789	333445555	123456789
333445555	888665555	333445555
666884444		666884444
453453453		453453453
		888665555
666884444	888000000	66688444 45345345

Single relational algebra expression:

$$Result \leftarrow \pi_{Ssn}\left(\sigma_{Dno=5}\left(EMPLOYEE\right)\right) \cup \quad \pi_{Super_ssn}\left(\sigma_{Dno=5}\left(EMPLOYEE\right)\right)$$

UNION, INTERSECTION and SET DIFFERENCE are binary operations; that is, each is applied to two sets (of tuples). When these operations are adapted to relational databases, the two relations on which any of these three operations are applied must have the same type of tuples; this condition has been called **union compatibility or type compatibility.**

Two relations $R(A_1, A_2, ..., A_n)$ and $S(B_1, B_2, ..., B_n)$ are said to be union compatible (or type compatible) if they have the same degree n and if $dom(A_i) = dom(B_i)$ for $1 \le i \le n$. This means that the two relations have the same number of attributes and each corresponding pair of attributes has the same domain.

Both UNION and INTERSECTION are commutative operations; that is,

$$R \cup S = S \cup R$$
 and $R \cap S = S \cap R$

Both UNION and INTERSECTION can be treated as *n*-ary operations applicable to any number of relations because both are also *associative operations*; that is,

$$R \cup (S \cup T) = (R \cup S) \cup T$$
 and $(R \cap S) \cap T = R \cap (S \cap T)$

The MINUS operation is *not commutative*; that is, in general,

$$R - S \neq S - R$$

INTERSECTION can be expressed in terms of union and set difference as follows:

$$R \cap S = ((R \cup S) - (R - S)) - (S - R)$$

In SQL, there are three operations—UNION, INTERSECT, and EXCEPT—that correspond to the set operations

2.3.2 The CARTESIAN PRODUCT (CROSS PRODUCT) Operation

The CARTESIAN PRODUCT operation—also known as CROSS PRODUCT or CROSS JOIN denoted by \times is a binary set operation, but the relations on which it is applied do *not* have to be union compatible. This set operation produces a new element by combining every member (tuple) from one relation (set) with every member (tuple) from the other relation (set)

In general, the result of $R(A_1, A_2, ..., A_n) \times S(B_1, B_2, ..., B_m)$ is a relation Q with degree n + m attributes $Q(A_1, A_2, ..., A_n, B_1, B_2, ..., B_m)$, in that order. The resulting relation Q has one tuple for each combination of tuples—one from R and one from S. Hence, if R has n_R tuples (denoted as $|R| = n_R$), and S has n_S tuples, then $R \times S$ will have $n_R * n_S$ tuples

Example: suppose that we want to retrieve a list of names of each female employee's dependents.

FEMALE_EMPS $\leftarrow \sigma_{gender='F'}(EMPLOYEE) EMPNAMES \leftarrow$

 $\pi_{Fname, Lname, Ssn}(FEMALE_EMPS) EMP DEPENDENTS \leftarrow$

EMPNAMES × DEPENDENT ACTUAL_DEPENDENTS ←

 $\sigma_{Ssn=Essn}(EMP_DEPENDENTS)$ RESULT $\leftarrow \pi_{Fname, Lname}$

Dependent_name (AC TUAL_DEPENDENTS)

FEMALE EMPS

Fname	Minit	Lname	Ssn	Bdate			Salary	Super_ssn	Dno
Alicia	J	Zelaya	999887777	1968-07-19	3321Castle, Spring, TX	F	25000	987654321	4
Jennifer	S	Wallace	987654321	1941-06-20	291Berry, Bellaire, TX	F	43000	888665555	4
Joyce	Α	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5

EMP_DEPENDENTS

Fname	Lname	Ssn	Essn	Dependent_name	Sex	Bdate	
Alicia	Zelaya	999887777	333445555	Alice	F	1986-04-05	
Alicia	Zelaya	999887777	333445555	Theodore	M	1983-10-25	
Alicia	Zelaya	999887777	333445555	Joy	F	1958-05-03	
Alicia	Zelaya	999887777	987654321	Abner	М	1942-02-28	
Alicia	Zelaya	999887777	123456789	Michael	М	1988-01-04	
Alicia	Zelaya	999887777	123456789	Alice	F	1988-12-30	
Alicia	Zelaya	999887777	123456789	Elizabeth	F	1967-05-05	
Jennifer	Wallace	987654321	333445555	Alice	F	1986-04-05	
Jennifer	Wallace	987654321	333445555	Theodore	М	1983-10-25	
Jennifer	Wallace	987654321	333445555	Joy	F	1958-05-03	
Jennifer	Wallace	987654321	987654321	Abner	M	1942-02-28	
Jennifer	Wallace	987654321	123456789	Michael	М	1988-01-04	
Jennifer	Wallace	987654321	123456789	Alice	F	1988-12-30	
Jennifer	Wallace	987654321	123456789	Elizabeth	F	1967-05-05	
Joyce	English	453453453	333445555	Alice	F	1986-04-05	
Joyce	English	453453453	333445555	Theodore	М	1983-10-25	
Joyce	English	453453453	333445555	Joy	F	1958-05-03	
Joyce	English	453453453	987654321	Abner	М	1942-02-28	
Joyce	English	453453453	123456789	Michael	М	1988-01-04	
Joyce	English	453453453	123456789	Alice	F	1988-12-30	
Joyce	English	453453453	123456789	Elizabeth	F	1967-05-05	

EMPNAMES

Fname	Lname	Ssn
Alicia	Zelaya	999887777
Jennifer	Wallace	987654321
Joyce	English	453453453

RESULT

Fname	Lname	Dependent_name				
Jennifer	Wallace	Abner				

ACTUAL DEPENDENTS

Fname	Lname	Ssn	Essn	Dependent_name	Sex	Bdate	
Jennifer	Wallace	987654321	987654321	Abner	М	1942-02-28	

The CARTESIAN PRODUCT creates tuples with the combined attributes of two relations. We can SELECT related tuples only from the two relations by specifying an appropriate selection condition after the Cartesian product.

In SQL, CARTESIAN PRODUCT can be realized by using the CROSS JOIN option in joined tables

2.4 Binary Relational Operations: JOIN and DIVISION

2.4.1 The JOIN Operation

The JOIN operation, denoted by \square , is used to combine related tuples from two relations into single "longer" tuples. It allows us to process relationships among relations. The general form of a JOIN operation on two relations $R(A_1, A_2, ..., A_n)$ and $S(B_1, B_2, ..., B_m)$ is

Example: Retrieve the name of the manager of each department.

To get the manager's name, we need to combine each department tuple with the employee tuple whose Ssn value matches the Mgr_ssn value in the department tuple

$$\begin{array}{l} \mathsf{DEPT_MGR} \leftarrow \mathsf{DEPARTMENT} \bowtie_{\mathsf{Mgr_ssn} = \mathsf{Ssn}} \mathsf{EMPLOYEE} \\ \mathsf{RESULT} \leftarrow \pi_{\mathsf{Dname,\ Lname,\ Fname}}(\mathsf{DEPT_MGR}) \end{array}$$

DEPT_MGR

Dname	Dnumber	Mgr_ssn		Fname	Minit	Lname	Ssn	
Research	5	333445555		Franklin	Т	Wong	333445555	
Administration	4	987654321	• • • •	Jennifer	S	Wallace	987654321	• • • •
Headquarters	1	888665555		James	Е	Borg	888665555	

The result of the JOIN is a relation Q with n + m attributes $Q(A_1, A_2, ..., A_n, B_1, B_2, ..., B_m$ in that order.Q has one tuple for each combination of tuples—one from R and one from S—whenever the combination satisfies the join condition. This is the main difference between CARTESIAN PRODUCT and JOIN. In JOIN, only combinations of tuples satisfying the join condition appear in the result, whereas in the CARTESIAN PRODUCT all combinations of tuples are included in the result. The join condition is specified on attributes from the two relations R and S and is evaluated for each combination of tuples.

Each tuple combination for which the join condition evaluates to TRUE is included in the resulting relation Q as a single combined tuple. A general join condition is of the form

where each <condition> is of the form A_i θ B_j , A_i is an attribute of R, B is an attribute of S, A_i and B_j have the same domain, and θ (theta) is one of the comparison operators $\{=, <, \leq, >, \geq, \neq\}$. A JOIN operation with such a general join condition is called a **THETA JOIN**. Tuples whose join attributes are NULL or for which the join condition is FALSE do not appear in the result.

2.4.2 Variations of JOIN: The EQUIJOIN and NATURAL JOIN

The most common use of JOIN involves join conditions with equality comparisons only. Such a JOIN, where the only comparison operator used is =, is called an **EQUIJOIN.**In the result of an EQUIJOIN we always have one or more pairs of attributes that have identical values in every tuple.

For example the values of the attributes Mgr_ssn and Ssn are identical in every tuple of DEPT_MGR (the EQUIJOIN result) because the equality join condition specified on these two attributes requires the values to be identical in every tuple in the result.

The standard definition of **NATURAL JOIN** requires that the two join attributes (or each pair of join attributes) have the same name in both relations. If this is not the case, a renaming operation is applied first. Suppose we want to combine each PROJECT tuple with the DEPARTMENT tuple that controls the project.first we rename the Dnumber attribute of DEPARTMENT to Dnum—so that it has the same name as the Dnum attribute in PROJECT—and then we apply NATURAL JOIN:

$$PROJ_DEPT \leftarrow PROJECT * \rho_{(Dname,\,Dnum,\,Mgr_ssn,\,\,Mgr_start_date)}(DEPARTMENT)$$

The same query can be done in two steps by creating an intermediate table DEPT as follows:

$$DEPT \leftarrow \rho_{(Dname,\,Dnum,\,Mgr_ssn,Mgr_start_date)}(DEPARTMENT)$$

$PROJ_DEPT \leftarrow PROJECT * DEPT$

The attribute Dnum is called the **join attribute** for the NATURAL JOIN operation, because it is the only attribute with the same name in both relations.

PROJ_DEPT

Pname	Pnumber	Plocation	Dnum	Dname	Mgr_ssn	Mgr_start_date
ProductX	1	Bellaire	5	Research	333445555	1988-05-22
ProductY	2	Sugarland	5	Research	333445555	1988-05-22
ProductZ	3	Houston	5	Research	333445555	1988-05-22
Computerization	10	Stafford	4	Administration	987654321	1995-01-01
Reorganization	20	Houston	1	Headquarters	888665555	1981-06-19
Newbenefits	30	Stafford	4	Administration	987654321	1995-01-01

If the attributes on which the natural join is specified already have the same names in both relations, renaming is unnecessary. For example, to apply a natural join on the Dnumber attributes of DEPARTMENT and DEPT_LOCATIONS, it is sufficient to write

DEPT_LOCS ← **DEPARTMENT** * **DEPT_LOCATIONS**

DEPT_LOCS

Dname	Dnumber	Mgr_ssn	Mgr_start_date	Location
Headquarters	1	888665555	1981-06-19	Houston
Administration	4	987654321	1995-01-01	Stafford
Research	5	333445555	1988-05-22	Bellaire
Research	5	333445555	1988-05-22	Sugarland
Research	5	333445555	1988-05-22	Houston

In general, the join condition for NATURAL JOIN is constructed by equating each pair of join attributes that have the same name in the two relations and combining these conditions with **AND**. If no combination of tuples satisfies the join condition, the result of a JOIN is an empty relation with zero tuples.

A more general, but nonstandard definition for NATURAL JOIN is

$$Q \leftarrow R *_{(\langle list1 \rangle),(\langle list2 \rangle)} S$$

where,

<list1>: list of i attributes from R,

<list2>: list of i attributes from S

The lists are used to form equality comparison conditions between pairs of corresponding attributes and then the conditions are then ANDed together. Only the list corresponding to attributes of the first relation R—list1>— is kept in the result Q.

will have between zero and $n_R * n_S$ tuples. The expected size of the join result divided by the maximum size n_R * n_S leads to a ratio called join selectivity, which is a property of each join condition. If there is no join condition, all combinations of tuples qualify and the JOIN degenerates into a CARTESIAN PRODUCT, also called CROSS PRODUCT or CROSS JOIN.

A single JOIN operation is used to combine data from two relations so that related information can be presented in a single table. These operations are also known as **inner joins**. Informally, an inner join is a type of match and combine operation defined formally as a combination of CARTESIAN PRODUCT and SELECTION. The NATURAL JOIN or EQUIJOIN operation can also be specified among multiple tables, leading to an n-way join. For example, consider the following three-way join:

$$((\mathsf{PROJECT} \bowtie_{\mathsf{Dnum} = \mathsf{Dnumber}} \mathsf{DEPARTMENT}) \bowtie_{\mathsf{Mar ssn} = \mathsf{Ssn}} \mathsf{EMPLOYEE})$$

This combines each project tuple with its controlling department tuple into a single tuple, and then combines that tuple with an employee tuple that is the department manager. The net result is a consolidated relation in which each tuple contains this project-department-manager combined information.

In SQL, JOIN can be realized in several different ways

- The first method is to specify the <join conditions> in the WHERE clause, along with any other selection conditions.
- The second way is to use a nested relation
- Another way is to use the concept of joined tables

2.4.3 A Complete Set of Relational Algebra Operations The set of relational algebra operations $\{\sigma, \pi, \cup, \rho, -, \times\}$ is a complete set; that is, any of the other original relational algebra operations can be expressed as a sequence of operations from this set.

For example, the INTERSECTION operation can be expressed by using UNION and MINUS as follows:

$$R \cap S \equiv (R \cup S) - ((R - S) \cup (S - R))$$

As another example, a JOIN operation can be specified as a CARTESIAN PRODUCT followed by a SELECT operation,

$$R \bowtie_{<\text{condition}>} S \equiv \sigma_{<\text{condition}>}(R \times S)$$

Similarly, a NATURAL JOIN can be specified as a CARTESIAN PRODUCT preceded by RENAME and followed by SELECT and PROJECT operations. Hence, the various JOIN operations are also not strictly necessary for the expressive power of the relational algebra.

2.4.4 The DIVISION Operation

The DIVISION operation, denoted by \div , is useful for a special kind of query that sometimes occurs in database applications. An example is Retrieve the names of employees who work on all the projects that 'John Smith' works on. To express this query using the DIVISION operation, proceed as follows.

• First, retrieve the list of project numbers that 'John Smith' works on in the intermediate relation SMITH_PNOS:

$$SSN_PNOS \leftarrow \pi_{Essn, Pno}(WORKS_ON)$$

• Next, create a relation that includes a tuple <Pno, Essn> whenever the employee whose Ssn is Essn works on the project whose number is Pno in the intermediate relation SSN_PNOS:

$$\begin{array}{l} \text{SMITH} \leftarrow \sigma_{\text{Fname='John'} \, \text{AND} \, \text{Lname='Smith'}} (\text{EMPLOYEE}) \\ \text{SMITH_PNOS} \leftarrow \pi_{\text{Pno}} (\text{WORKS_ON} \bowtie_{\text{Essn=Ssn}} \text{SMITH}) \end{array}$$

• Finally, apply the DIVISION operation to the two relations, which gives the desired employees' Social Security numbers:

$$\begin{aligned} & \mathsf{SSNS}(\mathsf{Ssn}) \leftarrow \mathsf{SSN_PNOS} \div \mathsf{SMITH_PNOS} \\ & \mathsf{RESULT} \leftarrow \pi_{\mathsf{Fname},\,\mathsf{Lname}}(\mathsf{SSNS} * \mathsf{EMPLOYEE}) \end{aligned}$$

(a) SSN PNOS

Pno
1
2
3
1
2
2
3
10
20
30
10
10
30
30
20
20

SSNS

Ssn
123456789
453453453

SMITH PNOS

Pno
1
2

In general, the DIVISION operation is applied to two relations $R(Z) \div S(X)$, where the attributes of R are a subset of the attributes of S; that is, $X \subseteq Z$.Let Y be the set of attributes of R that are not attributes of S; that is, Y = Z - X (and hence $Z = X \cup Y$). The result of DIVISION is a relation T(Y) that includes a tuple t if tuples t_R appear in R with $t_R[Y] = t$, and with $t_R[X] = t_S$ for every tuple t_S in S. This means that, for a tuple t to appear in the result T of t

Figure below illustrates a DIVISION operation where $X = \{A\}$, $Y = \{B\}$, and $Z = \{A, B\}$.

R		S
Α	В	Α
a1	b1	a1
a2	b1	a2
a3	b1	a3
a4	b1	20
a1	b2	т
a3	b2	В
a2	b3	b1
a3	b3	b4
a4	b3	D4
a1	b4	
a2	b4	
a3	b4	

The tuples (values) b1 and b4 appear in R in combination with all three tuples in S; that is why they appear in the resulting relation T. All other values of B in R do not appear with all the tuples in S and are not selected: b2 does not appear with a2, and b3 does not appear with a1.

The DIVISION operation can be expressed as a sequence of π , \times , and – operations as follows:

$$T1 \leftarrow \pi_Y(R)$$

$$T2 \leftarrow \pi_Y((S \times T1) - R)$$

$$T \leftarrow T1 - T2$$

Table 6.1 Operations of Relational Algebra

Table 611 opera	tions of reactional rigosia	
OPERATION	PURPOSE	NOTATION
SELECT	Selects all tuples that satisfy the selection condition from a relation R .	$\sigma_{< selection \ condition>}(R)$
PROJECT	Produces a new relation with only some of the attributes of R , and removes duplicate tuples.	$\pi_{< attribute \ list>}(R)$
THETA JOIN	Produces all combinations of tuples from R_1 and R_2 that satisfy the join condition.	$R_1 \bowtie_{< join \ condition >} R_2$
EQUIJOIN	Produces all the combinations of tuples from R_1 and R_2 that satisfy a join condition with only equality comparisons.	$\begin{array}{c} R_1 \bowtie_{< \text{join condition}>} R_2, \text{ OR} \\ R_1 \bowtie_{(< \text{join attributes 1}>),} \\ (< \text{join attributes 2}>) \end{array} R_2$
NATURAL JOIN	Same as EQUIJOIN except that the join attributes of R_2 are not included in the resulting relation; if the join attributes have the same names, they do not have to be specified at all.	$\begin{array}{c} R_1 *_{< \text{join condition}>} R_2, \\ \text{OR } R_1 *_{(< \text{join attributes 1}>),} \\ \text{OR } R_1 * R_2 \end{array}$
UNION	Produces a relation that includes all the tuples in R_1 or R_2 or both R_1 and R_2 ; R_1 and R_2 must be union compatible.	$R_1 \cup R_2$
INTERSECTION	Produces a relation that includes all the tuples in both R_1 and R_2 ; R_1 and R_2 must be union compatible.	$R_1 \cap R_2$
DIFFERENCE	Produces a relation that includes all the tuples in R_1 that are not in R_2 ; R_1 and R_2 must be union compatible.	$R_1 - R_2$
CARTESIAN PRODUCT	Produces a relation that has the attributes of R_1 and R_2 and includes as tuples all possible combinations of tuples from R_1 and R_2 .	$R_1 \times R_2$
DIVISION	Produces a relation $R(X)$ that includes all tuples $t[X]$ in $R_1(Z)$ that appear in R_1 in combination with every tuple from $R_2(Y)$, where $Z = X \cup Y$.	$R_1(Z) \div R_2(Y)$

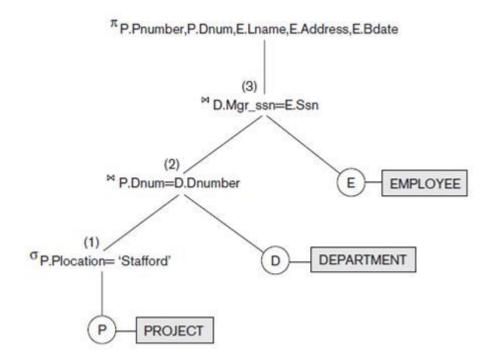
2.4.5 Notation for Query Trees

Query tree (query evaluation tree or query execution tree) is used in relational systems to represent queries internally. A query tree is a tree data structure that corresponds to a relational algebra expression. It represents the input relations of the query as leaf nodes of the tree, and represents the relational algebra operations as internal nodes.

An execution of the query tree consists of executing an internal node operation whenever its operands represented by its child nodes are available, and then replacing that internal node by the relation that results from executing the operation. The execution terminates when the root node is executed and produces the result relation for the query.

Example: For every project located in 'Stafford', list the project number, the controlling department number, and the department manager's last name, address, and birth date.

$$\begin{array}{l} \pi_{\mathsf{Pnumber,\,Dnum,\,Lname,\,Address,\,Bdate}}(((\sigma_{\mathsf{Plocation}=`Stafford'}(\mathsf{PROJECT})) \\ \bowtie_{\,\mathsf{Dnum=Dnumber}}(\mathsf{DEPARTMENT})) \bowtie_{\,\mathsf{Mgr_ssn}=Ssn}(\mathsf{EMPLOYEE})) \end{array}$$



Leaf nodes P, D, and E represent the three relations PROJECT, DEPARTMENT, and EMPLOYEE. The relational algebra operations in the expression are represented by internal tree nodes. The query tree signifies an explicit order of execution in the following sense. The node marked (1) must begin execution before node (2) because some resulting tuples of operation (1) must be available before we can begin to execute operation (2). Similarly, node (2) must begin to execute and produce results before node (3) can start execution, and so on.

A query tree gives a good visual representation and understanding of the query in terms of the relational operations it uses and is recommended as an additional means for expressing queries in relational algebra.

2.5 Additional Relational Operations

2.5.1 Generalized Projection

The generalized projection operation extends the projection operation by allowing functions of attributes to be included in the projection list. The generalized form can be expressed as:

$$\pi_{F1, F2, ..., Fn}(\mathbf{R})$$

where F_1 , F_2 , ..., F_n are functions over the attributes in relation R and may involve arithmetic operations and constant values.

The generalized projection helpful when developing reports where computed values have to be produced in the columns of a query result. For example, consider the relation EMPLOYEE (Ssn, Salary, Deduction, Years_service). A report may be required to show

Net Salary = Salary - Deduction,

Bonus = 2000 * Years_service, and

Tax = 0.25 * Salary.

generalized projection combined with renaming:

REPORT $\leftarrow \rho_{(Ssn, Net_salary, Bonus, Tax)}(\pi_{Ssn, Salary - Deduction, 2000 *}$

Years_service, 0.25 * Salary(EMPLOYEE)).

2.5.2 Aggregate Functions and Grouping

Aggregate functions are used in simple statistical queries that summarize information from the database tuples. Common functions applied to collections of numeric values include SUM, AVERAGE, MAXIMUM, and MINIMUM. The COUNT function is used for counting tuples or values. For example, retrieving the average or total salary of all employees or the total number of employee tuples.

Grouping the tuples in a relation by the value of some of their attributes and then applying an aggregate function independently to each group. For example, group EMPLOYEE tuples by Dno, so that each group includes the tuples for employees working in the same department. We can then list each Dno value along with, say, the average salary of employees within the department, or the number of employees who work in the department.

Aggregate function operation can be defined by using the symbol \Im (script F):

$$\mathfrak{F}$$
 (R)

Where,

<grouping attributes> : list of attributes of the relation specified in R

<function list> : list of (<function> <attribute>) pairs.

<function> - such as SUM, AVERAGE, MAXIMUM, MINIMUM, COUNT

<attribute> is an attribute of the relation specified by R

The resulting relation has the grouping attributes plus one attribute for each element in the function list.

Example: To retrieve each department number, the number of employees in the department, and their average salary, while renaming the resulting attributes

ρ_R(Dno, No of employees, Average sal)(Dno ℑ COUNT Ssn, AVERAGE Salary (EMPLOYEE))

The aggregate function operation.

- a. ρ_{R(Dno, No_of_employees, Average_sal)}(Dno S COUNT Ssn, AVERAGE Salary (EMPLOYEE)).
- b. Dno 3 COUNT San, AVERAGE Salary (EMPLOYEE).
- c. 3 COUNT Ssn, AVERAGE Salary (EMPLOYEE).

R

(a)	Dno	No_of_employees	Average_sal
	5	4	33250
	4	3	31000
	1	1	55000

(b)	Dno	Count_ssn	Average_salary
	5	4	33250
	4	3	31000
	1	1	55000

(c)	Count_ssn	Average_salary	
	8	35125	

2.5.3 Recursive Closure Operations

Recursive closure operation is applied to a recursive relationship between tuples of the same type, such as the relationship between an employee and a supervisor.

Example: Retrieve all supervisees of an employee e at all levels—that is, all employees e' directly supervised by e, all employees e' directly supervised by each employee e', all employees e'' directly supervised by each employee e'' and so on.

$$\begin{array}{l} \mathsf{BORG_SSN} \leftarrow \pi_{\mathsf{Ssn}}(\sigma_{\mathsf{Fname='James'}} \mathsf{AND} \ \mathsf{Lname='Borg'}(\mathsf{EMPLOYEE})) \\ \mathsf{SUPERVISION}(\mathsf{Ssn1}, \mathsf{Ssn2}) \leftarrow \pi_{\mathsf{Ssn},\mathsf{Super_ssn}}(\mathsf{EMPLOYEE}) \\ \mathsf{RESULT1}(\mathsf{Ssn}) \leftarrow \pi_{\mathsf{Ssn1}}(\mathsf{SUPERVISION} \bowtie_{\mathsf{Ssn2=Ssn}} \mathsf{BORG_SSN}) \end{array}$$

SUPERVISION

(Borg's Ssn is 888665555) (Ssn) (Super ssn)

(OSII)	(Ouper_ssii)
Ssn1	Ssn2
12345678	9 333445555
33344555	5 888665555
99988777	7 987654321
98765432	1 888665555
66688444	4 333445555
45345345	3 333445555
98798798	7 987654321
88866555	5 null

RESULT1

Ssn
333445555
987654321

(Supervised by Borg)

•

To retrieve all employees supervised by Borg at level 2—that is, all employees e' supervised by some employee e' who is directly supervised by Borg—we can apply another JOIN to the result of the first query, as follows:

 $\mathsf{RESULT2}(\mathsf{Ssn}) \leftarrow \pi_{\mathsf{Ssn1}}(\mathsf{SUPERVISION} \bowtie {}_{\mathsf{Ssn2}=\mathsf{Ssn}}\mathsf{RESULT1})$

RESULT2

Ssn
123456789
999887777
666884444
453453453
987987987

(Supervised by Borg's subordinates)

To get both sets of employees supervised at levels 1 and 2 by 'James Borg', we can apply the UNION operation to the two results, as follows:

RESULT ← RESULT2 ∪ RESULT1

2.5.4 OUTER JOIN Operations

The JOIN operations match tuples that satisfy the join condition. For example, for a NATURAL JOIN operation R * S, only tuples from R that have matching tuples in S—and vice versa—appear in the result. Hence, tuples without a matching (or related) tuple are eliminated from the

JOIN result. Tuples with NULL values in the join attributes are also eliminated. This type of join, where tuples with no match are eliminated, is known as an inner join.

A set of operations, called **outer joins**, were developed for the case where the user wants to keep all the tuples in R, or all those in S, or all those in both relations in the result of the JOIN, regardless of whether or not they have matching tuples in the other relation.

For example, suppose that we want a list of all employee names as well as the name of the departments they manage if they happen to manage a department; if they do not manage one, we can indicate it with a NULL value. We can apply an operation **LEFT OUTER JOIN**, denoted by

 \bowtie

to retrieve the result as follows:

$$\begin{split} \mathsf{TEMP} \leftarrow (\mathsf{EMPLOYEE} \bowtie_{\mathsf{Ssn=Mgr_ssn}} & \mathsf{DEPARTMENT}) \\ \mathsf{RESULT} \leftarrow & \pi_{\mathsf{Fname.\ Minit.\ Lname.\ Dname}}(\mathsf{TEMP}) \end{split}$$

The LEFT OUTER JOIN operation keeps every tuple in the first, or left, relation R in

 $R \longrightarrow S$; if no matching tuple is found in S, then the attributes of S in the join result are filled or padded with NULL values.

RESULT

Fname	Minit	Lname	Dname
John	В	Smith	NULL
Franklin	Т	Wong	Research
Alicia	J	Zelaya	NULL
Jennifer	S	Wallace	Administration
Ramesh	K	Narayan	NULL
Joyce	Α	English	NULL
Ahmad	V	Jabbar	NULL
James	E	Borg	Headquarters

A similar operation, RIGHT OUTER JOIN, denoted by \searrow keeps every tuple in the *second*, or right, relation S in the result of R \searrow S.

A third operation, **FULL OUTER JOIN**, denoted by , keeps all tuples in both the left and the right relations when no matching tuples are found, padding them with NULL values as needed.

2.5.5 The OUTER UNION Operation

The **OUTER UNION** operation was developed to take the union of tuples from two relations that have some common attributes, but are not union (type) compatible. This operation will take

the UNION of tuples in two relations R(X, Y) and S(X, Z) that are **partially compatible**, meaning that only some of their attributes, say X, are union compatible.

The attributes that are union compatible are represented only once in the result, and those attributes that are not union compatible from either relation are also kept in the result relation T(X, Y, Z). Two tuples t_1 in R and t_2 in S are said to match if $t_1[X] = t_2[X]$. These will be combined (unioned) into a single tuple in t. Tuples in either relation that have no matching tuple in the other relation are padded with NULL values.

For example, an OUTER UNION can be applied to two relations whose schemas are:

```
STUDENT(Name, Ssn, Department, Advisor)
```

INSTRUCTOR(Name, Ssn, Department, Rank)

Tuples from the two relations are matched based on having the same combination of values of the shared attributes—Name, Ssn, Department. All the tuples from both relations are included in the result, but tuples with the same (Name, Ssn, Department) combination will appear only once in the result. Tuples appearing only in STUDENT will have a NULL for the Rank attribute, whereas tuples appearing only in INSTRUCTOR will have a NULL for the Advisor attribute.

A tuple that exists in both relations, which represent a student who is also an instructor, will have values for all its attributes The resulting relation, STUDENT_OR_INSTRUCTOR, will have the following attributes:

STUDENT_OR_INSTRUCTOR(Name, Ssn, Department, Advisor, Rank)

2.6 Examples of Queries in Relational Algebra

Query 1. Retrieve the name and address of all employees who work for the 'Research' department.

```
\begin{split} & \mathsf{RESEARCH\_DEPT} \leftarrow \sigma_{\mathsf{Dname}='\mathsf{Research'}}(\mathsf{DEPARTMENT}) \\ & \mathsf{RESEARCH\_EMPS} \leftarrow (\mathsf{RESEARCH\_DEPT} \bowtie_{\mathsf{Dnumber}=\mathsf{Dno}} \mathsf{EMPLOYEE}) \\ & \mathsf{RESULT} \leftarrow \pi_{\mathsf{Fname},\;\mathsf{Lname},\;\mathsf{Address}}(\mathsf{RESEARCH\_EMPS}) \\ & \mathsf{As}\; a\; single\; in\text{-line}\; expression,\; this\; query\; becomes:} \\ & \pi_{\mathsf{Fname},\;\mathsf{Lname},\;\mathsf{Address}}\left(\sigma_{\mathsf{Dname}='\mathsf{Research'}}(\mathsf{DEPARTMENT} \bowtie_{\mathsf{Dnumber}=\mathsf{Dno}}(\mathsf{EMPLOYEE})) \\ \end{split}
```

Query 2. For every project located in 'Stafford', list the project number, the controlling department number, and the department manager's last name, address, and birth date.

```
\begin{array}{l} \mathsf{STAFFORD\_PROJS} \leftarrow \sigma_{\mathsf{Plocation}=`\mathsf{Stafford}'}(\mathsf{PROJECT}) \\ \mathsf{CONTR\_DEPTS} \leftarrow (\mathsf{STAFFORD\_PROJS} \bowtie_{\mathsf{Dnum}=\mathsf{Dnumber}} \mathsf{DEPARTMENT}) \\ \mathsf{PROJ\_DEPT\_MGRS} \leftarrow (\mathsf{CONTR\_DEPTS} \bowtie_{\mathsf{Mgr\_ssn}=\mathsf{Ssn}} \mathsf{EMPLOYEE}) \\ \mathsf{RESULT} \leftarrow \pi_{\mathsf{Pnumber},\;\mathsf{Dnum},\;\mathsf{Lname},\;\mathsf{Address},\;\mathsf{Bdate}}(\mathsf{PROJ\_DEPT\_MGRS}) \end{array}
```

Query 3. Find the names of employees who work on all the projects controlled by department number 5.

$$\begin{split} & \mathsf{DEPT5_PROJS} \leftarrow \rho_{(\mathsf{Pno})}(\pi_{\mathsf{Pnumber}}(\sigma_{\mathsf{Dnum}=5}(\mathsf{PROJECT}))) \\ & \mathsf{EMP_PROJ} \leftarrow \rho_{(\mathsf{Ssn},\,\mathsf{Pno})}(\pi_{\mathsf{Essn},\,\mathsf{Pno}}(\mathsf{WORKS_ON})) \\ & \mathsf{RESULT_EMP_SSNS} \leftarrow \mathsf{EMP_PROJ} \div \mathsf{DEPT5_PROJS} \\ & \mathsf{RESULT} \leftarrow \pi_{\mathsf{Lname},\,\mathsf{Fname}}(\mathsf{RESULT_EMP_SSNS} * \mathsf{EMPLOYEE}) \end{split}$$

Query 4. Make a list of project numbers for projects that involve an employee whose last name is 'Smith', either as a worker or as a manager of the department that controls the project.

```
\begin{split} & \mathsf{SMITHS}(\mathsf{Essn}) \leftarrow \pi_{\mathsf{Ssn}} \ (\sigma_{\mathsf{Lname} = \mathsf{`Smith'}}(\mathsf{EMPLOYEE})) \\ & \mathsf{SMITH} \_\mathsf{WORKER} \_\mathsf{PROJS} \leftarrow \pi_{\mathsf{Pno}}(\mathsf{WORKS} \_\mathsf{ON} * \mathsf{SMITHS}) \\ & \mathsf{MGRS} \leftarrow \pi_{\mathsf{Lname}, \ \mathsf{Dnumber}}(\mathsf{EMPLOYEE} \ \bowtie \ _{\mathsf{Ssn} = \mathsf{Mgr} \ \mathsf{ssn}} \mathsf{DEPARTMENT}) \\ & \mathsf{SMITH} \_\mathsf{MANAGED} \_\mathsf{DEPTS}(\mathsf{Dnum}) \leftarrow \pi_{\mathsf{Dnumber}} \ (\sigma_{\mathsf{Lname} = \mathsf{`Smith'}}(\mathsf{MGRS})) \\ & \mathsf{SMITH} \_\mathsf{MGR} \_\mathsf{PROJS}(\mathsf{Pno}) \leftarrow \pi_{\mathsf{Pnumber}}(\mathsf{SMITH} \_\mathsf{MANAGED} \_\mathsf{DEPTS} * \mathsf{PROJECT}) \\ & \mathsf{RESULT} \leftarrow (\mathsf{SMITH} \_\mathsf{WORKER} \_\mathsf{PROJS} \cup \mathsf{SMITH} \_\mathsf{MGR} \_\mathsf{PROJS}) \end{split}
```

Query 5. List the names of all employees with two or more dependents.

```
\begin{split} T1(\mathsf{Ssn}, \mathsf{No\_of\_dependents}) &\leftarrow {}_{\mathsf{Essn}} \ \Im_{\ \mathsf{COUNT\ Dependent\_name}}(\mathsf{DEPENDENT}) \\ T2 &\leftarrow \sigma_{\mathsf{No\_of\_dependents} > 2}(T1) \\ \mathsf{RESULT} &\leftarrow \pi_{\mathsf{Lname},\ \mathsf{Fname}}(T2 * \mathsf{EMPLOYEE}) \end{split}
```

Query 6. Retrieve the names of employees who have no dependents.

```
\begin{aligned} & \mathsf{ALL\_EMPS} \leftarrow \pi_{\mathsf{Ssn}}(\mathsf{EMPLOYEE}) \\ & \mathsf{EMPS\_WITH\_DEPS}(\mathsf{Ssn}) \leftarrow \pi_{\mathsf{Essn}}(\mathsf{DEPENDENT}) \\ & \mathsf{EMPS\_WITHOUT\_DEPS} \leftarrow (\mathsf{ALL\_EMPS} - \mathsf{EMPS\_WITH\_DEPS}) \\ & \mathsf{RESULT} \leftarrow \pi_{\mathsf{Lname},\;\mathsf{Fname}}(\mathsf{EMPS\_WITHOUT\_DEPS} * \mathsf{EMPLOYEE}) \end{aligned}
```

Query 7. List the names of mana gers who have at least one dependent.

```
\begin{aligned} &\mathsf{MGRS}(\mathsf{Ssn}) \leftarrow \pi_{\mathsf{Mgr\_ssn}}(\mathsf{DEPARTMENT}) \\ &\mathsf{EMPS\_WITH\_DEPS}(\mathsf{Ssn}) \leftarrow \pi_{\mathsf{Essn}}(\mathsf{DEPENDENT}) \\ &\mathsf{MGRS\_WITH\_DEPS} \leftarrow (\mathsf{MGRS} \cap \mathsf{EMPS\_WITH\_DEPS}) \\ &\mathsf{RESULT} \leftarrow \pi_{\mathsf{Lname},\;\mathsf{Fname}}(\mathsf{MGRS\_WITH\_DEPS} * \mathsf{EMPLOYEE}) \end{aligned}
```

Chapter 3: Mapping Conceptual Design into a Logical Design

3.1 Relational Database Design using ER-to-Relational mapping

Procedure to create a relational schema from an Entity-Relationship (ER)

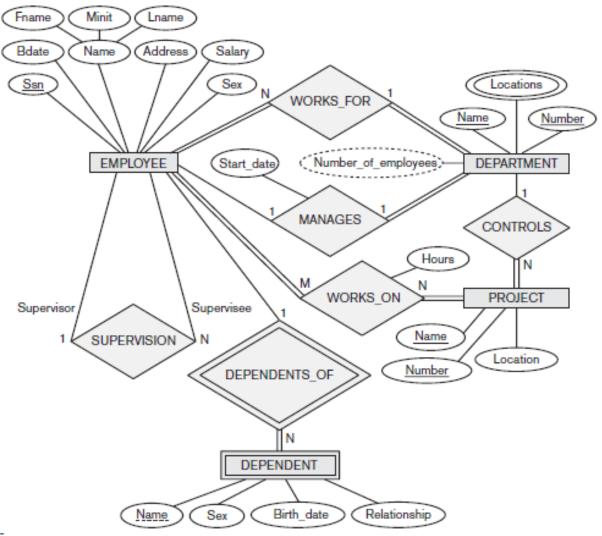


Fig 3.1: ER diagram of company database

Step 1: Mapping of Regular Entity Types

- For each regular entity type, create a relation R that includes all the simple attributes of E
- Include only the simple component attributes of a composite attribute
- Choose one of the key attributes of E as the primary key for R
- If the chosen key of E is a composite, then the set of simple attributes that form it will together form the primary key of R.

- If multiple keys were identified for E during the conceptual design, the information describing the attributes that form each additional key is kept in order to specify secondary (unique) keys of relation R
- In our example-COMPANY database, we create the relations EMPLOYEE, DEPARTMENT, and PROJECT
- we choose Ssn, Dnumber, and Pnumber as primary keys for the relations EMPLOYEE,
 DEPARTMENT, and PROJECT, respectively
- The relations that are created from the mapping of entity types are called entity relations because each tuple represents an entity instance.

EMPLOYEE Minit Fname Lname Ssn Bdate Address Sex Salary DEPARTMENT **Dnumber** Dname **PROJECT** Pname Pnumber Plocation

Step 2: Mapping of Weak Entity Types

- For each weak entity type, create a relation R and include all simple attributes of the entity type as attributes of R
- Include primary key attribute of owner as foreign key attributes of R
- In our example, we create the relation DEPENDENT in this step to correspond to the weak entity type DEPENDENT
- We include the primary key Ssn of the EMPLOYEE relation—which corresponds to the owner entity type—as a foreign key attribute of DEPENDENT; we rename it as Essn
- The primary key of the DEPENDENT relation is the combination {Essn,Dependent_name},
 because Dependent_name is the partial key of DEPENDENT
- It is common to choose the propagate (CASCADE) option for the referential triggered action on the foreign key in the relation corresponding to the weak entity type, since a weak entity has an existence dependency on its owner entity.
- This can be used for both ON UPDATE and ON DELETE.

DEPENDENT

Essn	Dependent_name	Sex	Bdate	Relationship

Step 3: Mapping of Binary 1:1 Relationship Types

- For each binary 1:1 relationship type *R* in the ER schema, identify the relations *S* and *T* that correspond to the entity types participating in *R*
- There are three possible approaches:
 - foreign key approach
 - merged relationship approach
 - crossreference or relationship relation approach

1. The foreign key approach

- Choose one of the relations—S, say—and include as a foreign key in S the primary key of T.
- It is better to choose an entity type with *total participation* in R in the role of S
- Include all the simple attributes (or simple components of composite attributes) of the 1:1 relationship type R as attributes of S.
- In our example, we map the 1:1 relationship type by choosing the participating entity type DEPARTMENT to serve in the role of *S* because its participation in the MANAGES relationship type is total
- We include the primary key of the EMPLOYEE relation as foreign key in the DEPARTMENT relation and rename it Mgr_ssn.
- We also include the simple attribute Start_date of the MANAGES relationship type in the DEPARTMENT relation and rename it Mgr_start_date

2. Merged relation approach:

- merge the two entity types and the relationship into a single relation
- This is possible when *both participations are total*, as this would indicate that the two tables will have the exact same number of tuples at all times.

3.Cross-reference or relationship relation approach:

- set up a third relation R for the purpose of cross-referencing the primary keys of the two relations S and T representing the entity types.
- required for binary M:N relationships
- The relation R is called a relationship relation (or sometimes a lookup table), because each tuple in R represents a relationship instance that relates one tuple from S with one tuple from T
- The relation R will include the primary key attributes of S and T as foreign keys to S and T.
- The primary key of R will be one of the two foreign keys, and the other foreign key will be a unique key of R.

• The drawback is having an extra relation, and requiring an extra join operation when combining related tuples from the tables.

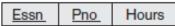
Step 4: Mapping of Binary 1:N Relationship Types

- For each regular binary 1:N relationship type *R*, identify the relation *S* that represents the participating entity type at the *N-side* of the relationship type.
- Include as foreign key in *S* the primary key of the relation *T* that represents the other entity type participating in *R*
- Include any simple attributes (or simple components of composite attributes) of the 1:N relationship type as attributes of *S*
- In our example, we now map the 1:N relationship types WORKS_FOR, CONTROLS, and SUPERVISION
- For WORKS_FOR we include the primary key Dnumber of the DEPARTMENT relation as foreign key in the EMPLOYEE relation and call it Dno.
- For SUPERVISION we include the primary key of the EMPLOYEE relation as foreign key in the EMPLOYEE relation itself—because the relationship is recursive—and call it Super_ssn.
- The CONTROLS relationship is mapped to the foreign key attribute Dnum of PROJECT, which references the primary key Dnumber of the DEPARTMENT relation.

Step 5: Mapping of Binary M:N Relationship Types

- For each binary M:N relationship type
 - Create a new relation S
 - Include primary key of participating entity types as foreign key attributes in S
 - Include any simple attributes of M:N relationship type
- In our example, we map the M:N relationship type WORKS_ON by creating the relation WORKS_ON.We include the primary keys of the PROJECT and EMPLOYEE relations as foreign keys in WORKS_ON and rename them Pno and Essn, respectively.
- We also include an attribute Hours in WORKS_ON to represent the Hours attribute of the relationship type.
- The primary key of the WORKS_ON relation is the combination of the foreign key attributes {Essn, Pno}.

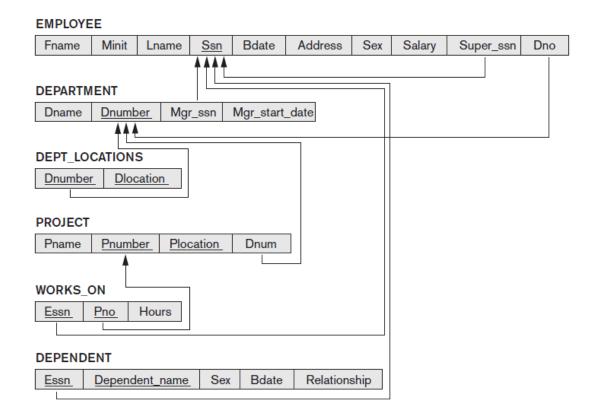
WORKS_ON



■ The propagate (CASCADE) option for the referential triggered action should be specified on the foreign keys in the relation corresponding to the relationship R, since each relationship instance has an existence dependency on each of the entities it relates. This can be used for both ON UPDATE and ON DELETE.

Step 6: Mapping of Multivalued Attributes

- For each multivalued attribute
 - Create a new relation
 - Primary key of *R* is the combination of *A* and *K*
 - If the multivalued attribute is composite, include its simple components
- In our example, we create a relation DEPT_LOCATIONS
- The attribute Dlocation represents the multivalued attribute LOCATIONS of DEPARTMENT, while Dnumber—as foreign key—represents the primary key of the DEPARTMENT relation.
- The primary key of DEPT_LOCATIONS is the combination of {Dnumber, Dlocation}
- A separate tuple will exist in DEPT_LOCATIONS for each location that a department has
- The propagate (CASCADE) option for the referential triggered action should be specified on the foreign key in the relation *R* corresponding to the multivalued attribute for both ON UPDATE and ON DELETE.



Step 7: Mapping of N-ary Relationship Types

- For each n-ary relationship type R
 - Create a new relation *S* to represent *R*
 - Include primary keys of participating entity types as foreign keys
 - Include any simple attributes as attributes
- The primary key of *S* is usually a combination of all the foreign keys that reference the relations representing the participating entity types.
- For example, consider the relationship type SUPPLY. This can be mapped to the relation SUPPLY whose primary key is the combination of the three foreign keys {Sname, Part_no, Proj_name}.

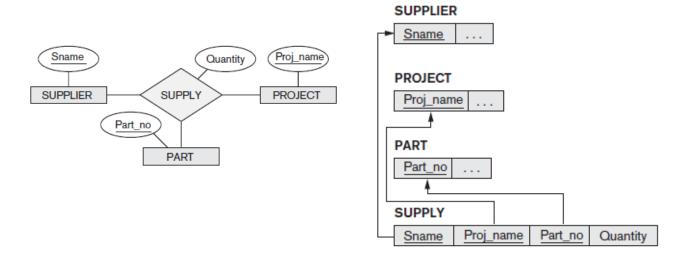


Figure 3.2: Mapping the *n*-ary relationship type SUPPLY

Chapter 4: SOL

4.1 Introduction

SQL was called SEQUEL (Structured English Query Language) and was designed and implemented at IBM Research. The SQL language may be considered one of the major reasons for the commercial success of relational databases. SQL is a comprehensive database language. It has statements for data definitions, queries, and updates. Hence, it is both a DDL *and* a DML. In addition, it has facilities for defining views on the database, for specifying security and authorization, for defining integrity constraints, and for specifying transaction controls. It also has rules for embedding SQL statements into a general-purpose programming language such as Java, COBOL, or C/C++.

4.2 SQL Data Definition and Data Types

SQL uses the terms table, row, and column for the formal relational model terms relation, tuple, and attribute, respectively. The main SQL command for data definition is the CREATE statement, which can be used to create schemas, tables (relations), domains, views, assertions and triggers.

4.2.1 Schema and Catalog Concepts in SQL

An SQL schema is identified by a schema name, and includes an authorization identifier to indicate the user or account who owns the schema, as well as descriptors for *each element* in the schema. Schema elements include tables, constraints, views, domains, and other constructs (such as authorization grants) that describe the schema. A schema is created via the CREATE SCHEMA statement.

For example, the following statement creates a schema called COMPANY, owned by the user with authorization identifier 'Jsmith'...

CREATE SCHEMA COMPANY **AUTHORIZATION** 'Jsmith';

In general, not all users are authorized to create schemas and schema elements. The privilege to create schemas, tables, and other constructs must be explicitly granted to the relevant user accounts by the system administrator or DBA.

SQL uses the concept of a **catalog**—a named collection of schemas in an SQL environment. A catalog always contains a special schema called INFORMATION_SCHEMA, which provides information on all the schemas in the catalog and all the element descriptors in these

schemas. Integrity constraints such as referential integrity can be defined between relations only if they exist in schemas within the same catalog. Schemas within the same catalog can also share certain elements, such as domain definitions.

4.2.2 The CREATE TABLE Command in SQL

The CREATE TABLE command is used to specify a new relation by giving it a name and specifying its attributes and initial constraints. The attributes are specified first, and each attribute is given a name, a data type to specify its domain of values, and any attribute constraints, such as NOT NULL. The key, entity integrity, and referential integrity constraints can be specified within the CREATE TABLE statement after the attributes are declared, or they can be added later using the ALTER TABLE command.

Typically, the SQL schema in which the relations are declared is implicitly specified in the environment in which the CREATE TABLE statements are executed. Alternatively, we can explicitly attach the schema name to the relation name, separated by a period. For example, by writing

CREATE TABLE COMPANY.EMPLOYEE ...

rather than

CREATE TABLE EMPLOYEE ...

The relations declared through CREATE TABLE statements are called base tables.

Examples:

CREATE TABLE EMPLOYEE

VARCHAR(15) NOT NULL, (Fname Minit CHAR, Lname VARCHAR(15) NOT NULL, Ssn NOT NULL, CHAR(9) Bdate DATE, Address VARCHAR(30), Sex CHAR, Salary DECIMAL(10,2), Super_ssn CHAR(9), Dno NOT NULL, PRIMARY KEY (Ssn), FOREIGN KEY (Super_ssn) REFERENCES EMPLOYEE(Ssn), FOREIGN KEY (Dno) REFERENCES DEPARTMENT(Dnumber));

```
CREATE TABLE DEPARTMENT
        ( Dname
                              VARCHAR(15)
                                                     NOT NULL,
          Dnumber
                              INT
                                                     NOT NULL,
          Mgr_ssn
                              CHAR(9)
                                                     NOT NULL,
          Mgr_start_date
                              DATE,
         PRIMARY KEY (Dnumber),
         UNIQUE (Dname),
         FOREIGN KEY (Mgr_ssn) REFERENCES EMPLOYEE(Ssn) );
 CREATE TABLE DEPT LOCATIONS
        ( Dnumber
                              INT
                                                     NOT NULL,
          Dlocation
                              VARCHAR(15)
                                                     NOT NULL,
         PRIMARY KEY (Dnumber, Dlocation),
         FOREIGN KEY (Dnumber) REFERENCES DEPARTMENT(Dnumber) );
 CREATE TABLE PROJECT
        (Pname
                                                     NOT NULL,
                              VARCHAR(15)
          Pnumber
                                                     NOT NULL,
                              INT
          Plocation
                              VARCHAR(15),
          Dnum
                              INT
                                                     NOT NULL,
         PRIMARY KEY (Pnumber),
         UNIQUE (Pname),
         FOREIGN KEY (Dnum) REFERENCES DEPARTMENT(Dnumber) );
CREATE TABLE WORKS_ON
       (Essn
                                                      NOT NULL,
                              CHAR(9)
        Pno
                              INT
                                                      NOT NULL,
        Hours
                              DECIMAL(3,1)
                                                      NOT NULL,
       PRIMARY KEY (Essn, Pno),
       FOREIGN KEY (Essn) REFERENCES EMPLOYEE(Ssn),
       FOREIGN KEY (Pno) REFERENCES PROJECT(Pnumber) );
CREATE TABLE DEPENDENT
       (Essn
                              CHAR(9)
                                                      NOT NULL,
        Dependent_name
                              VARCHAR(15)
                                                      NOT NULL,
        Sex
                              CHAR,
        Bdate
                              DATE,
        Relationship
                              VARCHAR(8),
       PRIMARY KEY (Essn, Dependent_name),
       FOREIGN KEY (Essn) REFERENCES EMPLOYEE(Ssn) );
```

4.2.3 Attribute Data Types and Domains in SQL

Basic data types

- 1. Numeric data types includes
 - integer numbers of various sizes (INTEGER or INT, and SMALLINT)
 - floating-point (real) numbers of various precision (FLOAT or REAL, and DOUBLE PRECISION).
 - Formatted numbers can be declared by using DECIMAL(i,j)—or

```
DEC(i,j) or NUMERIC(i,j)—where
```

- i precision, total number of decimal digits
- j scale, number of digits after the decimal point

2. Character-string data types

- fixed length—CHAR(n) or CHARACTER(n), where n is the number of characters
- varying length—VARCHAR(n) or CHAR VARYING(n) or CHARACTER VARYING(n), where n is the maximum number of characters
- When specifying a literal string value, it is placed between single quotation marks (apostrophes), and it is *case sensitive*
- For fixed length strings, a shorter string is padded with blank characters to the right
- For example, if the value 'Smith' is for an attribute of type CHAR(10), it is padded with five blank characters to become 'Smith' if needed
- Padded blanks are generally ignored when strings are compared
- Another variable-length string data type called CHARACTER LARGE OBJECT or CLOB is also available to specify columns that have large text values, such as documents
- The CLOB maximum length can be specified in kilobytes (K), megabytes (M), or gigabytes (G)
- For example, CLOB(20M) specifies a maximum length of 20 megabytes.

3. Bit-string data types are either of

- fixed length n—BIT(n)—or varying length—BIT VARYING(n), where n is the maximum number of bits.
- The default for *n*, the length of a character string or bit string, is 1.

- Literal bit strings are placed between single quotes but preceded by a B to distinguish them from character strings; for example, B'10101'
- Another variable-length bitstring data type called BINARY LARGE OBJECT or BLOB is also available to specify columns that have large binary values, such as images.
- The maximum length of a BLOB can be specified in kilobits (K), megabits (M), or gigabits (G)
- For example, BLOB(30G) specifies a maximum length of 30 gigabits.
- **4. A Boolean** data type has the traditional values of TRUE or FALSE.In SQL, because of the presence of NULL values, a three-valued logic is used, so a third possible value for a Boolean data type is UNKNOWN
- **5.** The **DATE** data type has ten positions, and its components are YEAR, MONTH, and DAY in the form YYYY-MM-DD
- **6.** The **TIME data** type has at least eight positions, with the components HOUR, MINUTE, and SECOND in the form HH:MM:SS.
 - Only valid dates and times should be allowed by the SQL implementation.
- 7. TIME WITH TIME ZONE data type includes an additional six positions for specifying the displacement from the standard universal time zone, which is in the range +13:00 to −12:59 in units of HOURS:MINUTES. If WITH TIME ZONE is not included, the default is the local time zone for the SQL session.

Additional data types

- Timestamp data type (TIMESTAMP) includes the DATE and TIME fields, plus a minimum
 of six positions for decimal fractions of seconds and an optional WITH TIME ZONE
 qualifier.
- 2. **INTERVA**L data type. This specifies an **interval**—a relative value that can be used to increment or decrement an absolute value of a date, time, or timestamp. Intervals are qualified to be either YEAR/MONTH intervals or DAY/TIME intervals.

It is possible to specify the data type of each attribute directly or a domain can be declared, and the domain name used with the attribute Specification. This makes it easier to change the data type for a domain that is used by numerous attributes in a schema, and improves schema readability. For example, we can create a domain SSN_TYPE by the following statement:

CREATE DOMAIN SSN_TYPE AS CHAR(9);

We can use SSN_TYPE in place of CHAR(9) for the attributes Ssn and Super_ssn of EMPLOYEE, Mgr_ssn of DEPARTMENT, Essn of WORKS_ON, and Essn of DEPENDENT

4.3 Specifying Constraints in SQL

Basic constraints that can be specified in SQL as part of table creation:

- key and referential integrity constraints
- Restrictions on attribute domains and NULLs
- constraints on individual tuples within a relation

4.3.1 Specifying Attribute Constraints and Attribute Defaults

Because SQL allows NULLs as attribute values, a constraint NOT NULL may be specified if NULL is not permitted for a particular attribute. This is always implicitly specified for the attributes that are part of the primary key of each relation, but it can be specified for any other attributes whose values are required not to be NULL.

It is also possible to define a default value for an attribute by appending the clause **DEFAULT** <value> to an attribute definition. The default value is included in any new tuple if an explicit value is not provided for that attribute.

Another type of constraint can restrict attribute or domain values using the **CHECK** clause following an attribute or domain definition . For example, suppose that department numbers are restricted to integer numbers between 1 and 20; then, we can change the attribute declaration of Dnumber in the DEPARTMENT table to the following:

Dnumber INT **NOT NULL CHECK** (Dnumber > 0 **AND** Dnumber < 21);

The CHECK clause can also be used in conjunction with the CREATE DOMAIN statement. For example, we can write the following statement:

CREATE DOMAIN D NUM AS INTEGER

CHECK (D_NUM > 0 AND D_NUM < 21);

We can then use the created domain D_NUM as the attribute type for all attributes that refer to department number such as Dnumber of DEPARTMENT, Dnum of PROJECT, Dno of EMPLOYEE, and so on.

4.3.2 Specifying Key and Referential Integrity Constraints

The **PRIMARY KEY** clause specifies one or more attributes that make up the primary key of a relation. If a primary key has a single attribute, the clause can follow the attribute directly. For example, the primary key of DEPARTMENT can be specified as:

Dnumber INT **PRIMARY KEY**;

The **UNIQUE** clause can also be specified directly for a secondary key if the secondary key is a single attribute, as in the following example:

Dname VARCHAR(15) UNIQUE;

Referential integrity is specified via the **FOREIGN KEY** clause

FOREIGN KEY (Super_ssn) REFERENCES EMPLOYEE(Ssn),
FOREIGN KEY (Dno) REFERENCES DEPARTMENT(Dnumber

A referential integrity constraint can be violated when tuples are inserted or deleted, or when a foreign key or primary key attribute value is modified. The default action that SQL takes for an integrity violation is to **reject** the update operation that will cause a violation, which is known as the RESTRICT option.

The schema designer can specify an alternative action to be taken by attaching a **referential triggered action** clause to any foreign key constraint. The options include SET NULL, CASCADE, and SET DEFAULT. An option must be qualified with either ON DELETE or ON UPDATE

- FOREIGN KEY(Dno) REFERENCES DEPARTMENT(Dnumber) ON DELETE SET DEFAULT ON UPDATE CASCADE
- FOREIGN KEY (Super_ssn) REFERENCES EMPLOYEE(Ssn) ON DELETE SET NULL ON UPDATE CASCADE
- FOREIGN KEY (Dnumber) REFERENCES DEPARTMENT(Dnumber) ON DELETE CASCADE ON UPDATE CASCADE

In general, the action taken by the DBMS for SET NULL or SET DEFAULT is the same for both ON DELETE and ON UPDATE: The value of the affected referencing attributes is changed to NULL for SET NULL and to the specified default value of the referencing attribute for SET DEFAULT.

The action for CASCADE ON DELETE is to delete all the referencing tuples whereas the action for CASCADE ON UPDATE is to change the value of the referencing foreign key attribute(s) to the updated (new) primary key value for all the referencing tuples. It is the responsibility of the database designer to choose the appropriate action and to specify it in the database schema. As a general rule, the CASCADE option is suitable for "relationship" relations such as WORKS_ON; for relations that represent multivalued attributes, such as DEPT_LOCATIONS; and for relations that represent weak entity types, such as DEPENDENT.

4.3.3 Giving Names to Constraints

The names of all constraints within a particular schema must be unique. A constraint name is used to identify a particular constraint in case the constraint must be dropped later and replaced with another constraint.

4.3.4 Specifying Constraints on Tuples Using CHECK

In addition to key and referential integrity constraints, which are specified by special keywords, other *table constraints* can be specified through additional CHECK clauses at the end of a CREATE TABLE statement. These can be called **tuple-based** constraints because they apply to each tuple individually and are checked whenever a tuple is inserted or modified

For example, suppose that the DEPARTMENT table had an additional attribute Dept_create_date, which stores the date when the department was created. Then we could add the following CHECK clause at the end of the CREATE TABLE statement for the DEPARTMENT table to make sure that a manager's start date is later than the department creation date

CHECK (Dept_create_date <= Mgr_start_date);</pre>

4.4 Basic Retrieval Queries in SQL

SQL has one basic statement for retrieving information from a database: the **SELECT** statement.

4.4.1 The SELECT-FROM-WHERE Structure of Basic SQL Queries

The basic form of the SELECT statement, sometimes called a **mapping** or a **select-from-where block**, is formed of the three clauses SELECT, FROM, and WHERE and has the following form:

SELECT <attribute list>

FROM

WHERE <condition>;

Where.

- <attribute list> is a list of attribute names whose values are to be retrieved by the query
- is a list of the relation names required to process the query
- <condition> is a conditional (Boolean) expression that identifies the tuples to be retrieved by the query.

Examples:

1. Retrieve the birth date and address of the employee(s) whose name is 'John B.

Smith'.

SELECT Bdate, Address

FROM EMPLOYEE

WHERE Fname='John' AND Minit='B' AND Lname='Smith';

The SELECT clause of SQL specifies the attributes whose values are to be retrieved, which are called the **projection attributes.** The WHERE clause specifies the Boolean condition that must be true for any retrieved tuple, which is known as the **selection condition.**

2. Retrieve the name and address of all employees who work for the 'Research' department.

SELECT Fname, Lname, Address

FROM EMPLOYEE, DEPARTMENT

WHERE Dname='Research' **AND** Dnumber=Dno;

In the WHERE clause, the condition Dname = 'Research' is a **selection condition** that chooses the particular tuple of interest in the DEPARTMENT table, because Dname is an attribute of DEPARTMENT. The condition Dnumber = Dno is called a **join condition**, because it combines two tuples: one from DEPARTMENT and one from EMPLOYEE, whenever the value of Dnumber in DEPARTMENT is equal to the value of Dno in EMPLOYEE. A query that involves only selection and join conditions plus projection attributes is known as a **select-project-join** query.

3. For every project located in 'Stafford', list the project number, the controlling department number, and the department manager's last name, address, and birth date.

SELECT Pnumber, Dnum, Lname, Address, Bdate

FROM PROJECT, DEPARTMENT, EMPLOYEE

WHERE Dnum=Dnumber AND Mgr_ssn=Ssn AND Plocation='Stafford';

The join condition Dnum = Dnumber relates a project tuple to its controlling department tuple, whereas the join condition Mgr_ssn = Ssn relates the controlling department tuple to the employee tuple who manages that department. Each tuple in the result will be a *combination* of one project, one department, and one employee that satisfies the join conditions. The projection attributes are used to choose the attributes to be displayed from each combined tuple.

4.4.2 Ambiguous Attribute Names, Aliasing, Renaming, and Tuple Variables

In SQL, the same name can be used for two or more attributes as long as the attributes are in different relations. If this is the case, and a multitable query refers to two or more attributes with the same name, we must **qualify** the attribute name with the relation name to prevent ambiguity. This is done by prefixing the relation name to the attribute name and separating the two by a period.

Example: Retrieve the name and address of all employees who work for the 'Research' department

SELECT Fname, EMPLOYEE.Name, Address

FROM EMPLOYEE, DEPARTMENT

WHERE DEPARTMENT.Name='Research' AND

DEPARTMENT.Dnumber=EMPLOYEE.Dnumber;

The ambiguity of attribute names also arises in the case of queries that refer to the same relation twice. For example consider the query: For each employee, retrieve the employee's first and last name and the first and last name of his or her immediate supervisor.

SELECT E.Fname, E.Lname, S.Fname, S.Lname

FROM EMPLOYEE AS E. EMPLOYEE AS S

WHERE E.Super_ssn=S.Ssn;

In this case, we are required to declare alternative relation names E and S, called **aliases** or **tuple variables**, for the EMPLOYEE relation. An alias can follow the keyword **AS**, or it can directly follow the relation name—for example, by writing EMPLOYEE E, EMPLOYEE S. It is also possible to **rename** the relation attributes within the query in SQL by giving them aliases. For example, if we write

EMPLOYEE AS E(Fn, Mi, Ln, Ssn, Bd, Addr, Sex, Sal, Sssn, Dno)

in the FROM clause, Fn becomes an alias for Fname, Mi for Minit, Ln for Lname, and so on

4.4.3 Unspecified WHERE Clause and Use of the Asterisk

A missing WHERE clause indicates no condition on tuple selection; hence, all tuples of the relation specified in the FROM clause qualify and are selected for the query result. If more than one relation is specified in the FROM clause and there is no WHERE clause, then the CROSS PRODUCT—all possible tuple combinations—of these relations is selected.

Example: Select all EMPLOYEE Ssns and all combinations of EMPLOYEE Ssn and DEPARTMENT Dname in the database.

SELECT Ssn

FROM EMPLOYEE;

SELECT Ssn, Dname

FROM EMPLOYEE, DEPARTMENT;

To retrieve all the attribute values of the selected tuples, we do not have to list the attribute names explicitly in SQL; we just specify an asterisk (*), which stands for all the attributes. For example, the following query retrieves all the attribute values of any EMPLOYEE who works in DEPARTMENT number 5

SELECT * **FROM** EMPLOYEE **WHERE** Dno=5;

SELECT * **FROM** EMPLOYEE, DEPARTMENT **WHERE** Dname='Research' **AND** Dno=Dnumber;

SELECT * **FROM** EMPLOYEE, DEPARTMENT;

4.4.4 Tables as Sets in SQL

SQL usually treats a table not as a set but rather as a multiset; duplicate tuples can appear more than once in a table, and in the result of a query. SQL does not automatically eliminate duplicate tuples in the results of queries, for the following reasons:

- Duplicate elimination is an expensive operation. One way to implement it is to sort the tuples first and then eliminate duplicates.
- The user may want to see duplicate tuples in the result of a query.
- When an aggregate function is applied to tuples, in most cases we do not want to eliminate duplicates.

If we do want to eliminate duplicate tuples from the result of an SQL query, we use the keyword **DISTINCT** in the SELECT clause, meaning that only distinct tuples should remain in the result.

Example: Retrieve the salary of every employee and all distinct salary values

- (a) **SELECT ALL** Salary **FROM** EMPLOYEE;
- (b) **SELECT DISTINCT** Salary **FROM** EMPLOYEE;

(a)		(b)	
	Salary		Salary
	30000		30000
	40000		40000
	25000		25000
	43000		43000
	38000		38000
	25000		55000
	25000		00000
	55000		

SQL has directly incorporated some of the set operations from mathematical *set theory*, which are also part of relational algebra. There are

- set union (UNION)
- set difference (EXCEPT) and
- set intersection (**INTERSECT**)

The relations resulting from these set operations are sets of tuples; that is, duplicate tuples are eliminated from the result. These set operations apply only to union-compatible relations, so we must make sure that the two relations on which we apply the operation have the same attributes and that the attributes appear in the same order in both relations.

Example: Make a list of all project numbers for projects that involve an employee whose last name is 'Smith', either as a worker or as a manager of the department that controls the project

```
(SELECT DISTINCT Pnumber FROM PROJECT, DEPARTMENT,

EMPLOYEE WHERE Dnum=Dnumber AND Mgr_ssn=Ssn AND Lname='Smith')

UNION

(SELECT DISTINCT Pnumber FROM PROJECT, WORKS_ON, EMPLOYEE

WHERE Pnumber=Pno AND Essn=Ssn AND Lname='Smith');
```

4.4.5 Substring Pattern Matching and Arithmetic Operators

Several more features of SQL

The first feature allows comparison conditions on only parts of a character string, using the **LIKE** comparison operator. This can be used for string **pattern matching**. Partial strings are specified using two reserved characters:

- % replaces an arbitrary number of zero or more characters
- _ (underscore) replaces a single character

For example, consider the following query: Retrieve all employees whose address is in Houston, Texas

SELECT Fname, Lname **FROM** EMPLOYEE **WHERE** Address **LIKE** '%Houston,TX%';

To retrieve all employees who were born during the 1950s, we can use Query

SELECT Fname, Lname **FROM** EMPLOYEE WHERE Bdate LIKE '__5___';

If an underscore or % is needed as a literal character in the string, the character should be preceded by an *escape character*, which is specified after the string using the keyword ESCAPE. For example, 'AB_CD\%EF' ESCAPE '\' represents the literal string 'AB_CD%EF' because \ is specified as the escape character. Also, we need a rule to specify apostrophes or single quotation marks (' ') if they are to be included in a string because they are used to begin and end strings. If an apostrophe (') is needed, it is represented as two consecutive apostrophes ('') so that it will not be interpreted as ending the string.

Another feature allows the use of arithmetic in queries. The standard arithmetic operators for addition (+), subtraction (-), multiplication (*), and division (/) can be applied to numeric values or attributes with numeric domains. For example, suppose that we want to see the effect of giving all employees who work on the 'ProductX' project a 10 percent raise; we can issue the following query:

SELECT E.Fname, E.Lname, 1.1 * E.Salary **AS** Increased_sal

FROM EMPLOYEE AS E, WORKS_ON AS W, PROJECT AS P

WHERE E.Ssn=W.Essn AND W.Pno=P.Pnumber AND P.Pname='ProductX';

Example: Retrieve all employees in department 5 whose salary is between \$30,000 and \$40,000.

SELECT * FROM EMPLOYEE **WHERE** (Salary **BETWEEN** 30000 **AND** 40000) **AND** Dno = 5;

The condition (Salary **BETWEEN** 30000 **AND** 40000) is equivalent to the condition((Salary >= 30000) **AND** (Salary <= 40000)).

4.4.6 Ordering of Query Results

SQL allows the user to order the tuples in the result of a query by the values of one or more of the attributes that appear in the query result, by using the **ORDER BY** clause.

Example:Retrieve a list of employees and the projects they are working on, ordered by department and, within each department, ordered alphabetically bylast name, then first name.

SELECT D.Dname, E.Lname, E.Fname, P.Pname

FROM DEPARTMENT D, EMPLOYEE E, WORKS_ON W, PROJECT P

WHERE D.Dnumber= E.Dno AND E.Ssn= W.Essn AND W.Pno= P.Pnumber

ORDER BY D.Dname, E.Lname, E.Fname;

The default order is in ascending order of values. We can specify the keyword **DESC** if we want to see the result in a descending order of values. The keyword ASC can be used to specify ascending order explicitly. For example, if we want descending alphabetical order on Dname and ascending order on Lname, Fname, the ORDER BY clause can be written as

ORDER BY D.Dname DESC, E.Lname ASC, E.Fname ASC

4.5 INSERT, DELETE, and UPDATE Statements in SQL

4.5.1The INSERT Command

INSERT is used to add a single tuple to a relation. We must specify the relation name and a list of values for the tuple. The values should be listed *in the same order* in which the corresponding attributes were specified in the CREATE TABLE command.

Example: INSERT INTO EMPLOYEE **VALUES** ('Richard', 'K', 'Marini', '653298653', '1962-12-30', '98 Oak Forest, Katy, TX', 'M', 37000, '653298653', 4);

INSERT INTO EMPLOYEE (Fname, Lname, Dno, Ssn)

VALUES ('Richard', 'Marini', 4, '653298653');

A second form of the INSERT statement allows the user to specify explicit attribute names that correspond to the values provided in the INSERT command. The values must include all attributes with NOT NULL specification and no default value. Attributes with NULL allowed or DEFAULT values are the ones that can be left out.

A variation of the INSERT command inserts multiple tuples into a relation in conjunction with creating the relation and loading it with the *result of a query*. For example, to create a temporary table that has the employee last name, project name, and hours per week for each employee working on a project, we can write the statements in U3A and U3B:

U3A: CREATE TABLE WORKS_ON_INFO(

Emp_name VARCHAR(15),

Proj_name VARCHAR(15),

Hours_per_week DECIMAL(3,1));

U3B: INSERT INTO WORKS ON INFO

(Emp name, Proj name, Hours per week)

SELECT E.Lname, P.Pname, W.Hours

FROM PROJECT P, WORKS_ON W, EMPLOYEE E

WHERE P.Pnumber=W.Pno AND W.Essn=E.Ssn;

A table WORKS_ON_INFO is created by U3A and is loaded with the joined information retrieved from the database by the query in U3B. We can now query WORKS_ON_INFO as we would any other relation:

4.5.2 The DELETE Command

The DELETE command removes tuples from a relation. It includes a WHERE clause, similar to that used in an SQL query, to select the tuples to be deleted. Tuples are explicitly deleted from only one table at a time. The deletion may propagate to tuples in other relations if *referential triggered actions* are specified in the referential integrity constraints of the DDL.

Example:

DELETE FROM EMPLOYEE **WHERE** Lname='Brown';

Depending on the number of tuples selected by the condition in the WHERE clause, zero, one, or several tuples can be deleted by a single DELETE command. A missing WHERE clause specifies that all tuples in the relation are to be deleted; however, the table remains in the database as an empty table.

4.5.3 The UPDATE Command

The UPDATE command is used to modify attribute values of one or more selected Tuples. An additional SET clause in the UPDATE command specifies the attributes to be modified and their new values. For example, to change the location and controlling department number of project number 10 to 'Bellaire' and 5, respectively, we use

UPDATE PROJECT **SET** Plocation = 'Bellaire', Dnum = 5 **WHERE** Pnumber=10;

As in the DELETE command, a WHERE clause in the UPDATE command selects the tuples to be modified from a single relation. However, updating a primary key value may propagate to the foreign key values of tuples in other relations if such a referential triggered action is specified in the referential integrity constraints of the DDL.

Several tuples can be modified with a single UPDATE command. An example is to give all employees in the 'Research' department a 10 percent raise in salary, as shown by the following query

UPDATE EMPLOYEE

SET Salary = Salary * 1.1

WHERE Dno = 5;

Each UPDATE command explicitly refers to a single relation only. To modify multiple relations, we must issue several UPDATE commands.

4.6 Additional Features of SQL

- SQL has various techniques for specifying complex retrieval queries, including nested queries, aggregate functions, grouping, joined tables, outer joins, and recursive queries; SQL views, triggers, and assertions; and commands for schema modification.
- SQL has various techniques for writing programs in various programming languages that include
 SQL statements to access one or more databases.
- SQL has transaction control commands. These are used to specify units of database processing for concurrency control and recovery purposes.
- SQL has language constructs for specifying the *granting and revoking of privileges* to users.
- SQL has language constructs for creating triggers. These are generally referred to as active
 database techniques, since they specify actions that are automatically triggered by events such as
 database updates.
- SQL has incorporated many features from object-oriented models to have more powerful
 capabilities, leading to enhanced relational systems known as object-relational.
- SQL and relational databases can interact with new technologies such as XML

Question Bank

- 1. Define the following terms as they apply to the relational model of data:
 - i) domain ii) attribute iii) n-tuple iv) relation schema v) relation state
 - vi) degree of a relation vii) relational database schema viii) relational database state.
- 2. What is the difference between a key and a superkey?
- 3. Discuss the various reasons that lead to the occurrence of NULL values in relations.
- 4. Discuss the characteristics of relations
- 5. Discuss the various restrictions on data that can be specified on a relational database in the form of constraints.
- 6. Suppose that each of the following Update operations is applied directly to the company database state. Discuss all integrity constraints violated by each operation, if any, and the different ways of enforcing these constraints.
 - a. Insert <'Robert', 'F', 'Scott', '943775543', '1972-06-21', '2365 Newcastle Rd,Bellaire, TX', M, 58000,
 - '888665555', 1> into EMPLOYEE.
 - b. Insert <'ProductA', 4, 'Bellaire', 2> into PROJECT.
 - c. Insert <'Production', 4, '943775543', '2007-10-01'> into DEPARTMENT.
 - d. Insert <'677678989', NULL, '40.0'> into WORKS_ON.
 - e. Insert <'453453453', 'John', 'M', '1990-12-12', 'spouse'> into DEPENDENT.
 - f. Delete the WORKS_ON tuples with Essn = '333445555'.
 - g. Delete the EMPLOYEE tuple with Ssn = '987654321'.
 - h. Delete the PROJECT tuple with Pname = 'ProductX'.
 - i. Modify the Mgr_ssn and Mgr_start_date of the DEPARTMENT tuple with Dnumber = 5 to '123456789' and '2007-10-01', respectively.
 - j. Modify the Super_ssn attribute of the EMPLOYEE tuple with Ssn = '999887777' to '943775543'.
 - k. Modify the Hours attribute of the WORKS_ON tuple with Essn = '999887777' and Pno = 10 to '5.0'.
 - 7. Expain the following unary operations with syntax and example
 - i) SELECT ii) PROJECT iii) RENAME

- 8. Explain the following binary operations with syntax and example
 - i) UNION ii) INTERSECTION iii) MINUS iv) CROSS PRODUCT V) DIVISION
- 9. What is union compatibility? Why do the UNION, INTERSECTION, and DIFFERENCE operations require that the relations on which they are applied be union compatible?
- 10.Discuss the various types of *join* operations.
- 11. Discuss the notation used in relational systems to represent queries internally.
- 12. Illustrate with an example, significance of generalized projection.
- 13. Illustrate with an example, Aggregate Functions and Grouping
- 14. Illustrate with an example, Recursive Closure Operations
- 15. How are the OUTER JOIN operations different from the INNER JOIN operations?
- 16. How is the OUTER UNION operation different from UNION?
- 17. Specify the following queries on the COMPANY relational database schema using the relational operators
 - a. Retrieve the names of all employees in department 5 who work more than 10 hours per week on the ProductX project.
 - b. List the names of all employees who have a dependent with the same first name as themselves.
 - c. Find the names of all employees who are directly supervised by 'Franklin Wong'.
 - d. For each project, list the project name and the total hours per week (by all employees) spent on that project.
 - e. Retrieve the names of all employees who do not work on any project.
 - f. Retrieve the average salary of all female employees.
- 18. Discuss the correspondences between the ER model constructs and the relational model constructs. Show how each ER model construct can be mapped to the relational model
- 19. Discuss the data types that are allowed for SQL attributes
- 20. Write SQL update statements to do the following on the database schema shown in Figure(1)
 - a. Insert a new student, <'Johnson', 25, 1, 'Math'>, in the database.
 - b. Change the class of student 'Smith' to 2.
 - c. Insert a new course, <'Knowledge Engineering', 'CS4390', 3, 'CS'>.
 - d. Delete the record for the student whose name is 'Smith' and whose student number is 17.

STUDENT

Name Student_number Class Major

COURSE

PREREQUISITE

Course_number	Prerequisite_number
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SECTION

Section_identifier	Course_number	Semester	Year	Instructor
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GRADE_REPORT

COUCETT TOTAL CONTRACT N	identifier	Grade
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COURSE

Course_name	Course_number	Credit_hours	Department
Intro to Computer Science	CS1310	4	CS
Data Structures	CS3320	4	CS
Discrete Mathematics	MATH2410	3	MATH
Database	CS3380	3	CS

PREREQUISITE

Course_number	Prerequisite_number
CS3380	CS3320
CS3380	MATH2410
CS3320	CS1310

STUDENT

Name	Student_number	Class	Major
Smith	17	1	CS
Brown	8	2	CS

GRADE_REPORT

Student_number	Section_identifier	Grade
17	112	В
17	119	С
8	85	Α
8	92	Α
8	102	В
8	135	Α

SECTION

Section_identifier	Course_number	Semester	Year	Instructor
85	MATH2410	Fall	07	King
92	CS1310	Fall	07	Anderson
102	CS3320	Spring	08	Knuth
112	MATH2410	Fall	08	Chang
119	CS1310	Fall	08	Anderson
135	CS3380	Fall	08	Stone

Fig (2):student scheme and database state

- 21. Briefly discuss how the different updata operations on a relation deal with constraint violations?
- 22. Consider the following schema for a COMPANY database:

EMPLOYEE (Fname, Lname, Ssn, Address, Super-ssn, Salary, Dno)

DEPARTMENT (Dname, Dnumber, Mgr-ssn, Mgr-start-date)

DEPT-LOCATIONS (Dnumber, Dlocation)

PROJECT (Pname, Pnumber, Plocation, Dnum)

WORKS-ON (Ess!!, Pno, Hours)

DEPENDENT (Essn, Dependent-name, Sex, Bdate, Relationship)

Write the queries in relational algebra.

- i) Retrieve the name and address of all emp loyees who work for Sales department.
- ii) Find the names of employees who work on all the projects controlled by the department number 3.
- iii) List the names of all employees with two or more dependents.
- iv) Retrieve the names of employees who have no dependents.