

STAT 440 Homework 10

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October 2022

```

16 bootstrap = function(samples, B, estimator) {
17   #' generic bootstrap function
18   #' @param samples vector of samples
19   #' @param B number of bootstrap estimates
20   #' @param estimator estimating function
21
22   # generate matrix of bootstrap resamples
23   n = dim(samples)[1]
24   # resamples = matrix(
25   #   sample(samples, size=n*B, replace=TRUE),
26   #   nrow=B
27   # )
28   bootstrap_ests = c()
29   for(i in 1:B){
30     index = sample(1:n, n, replace = TRUE)
31     sample_new = samples[index, ]
32     bootstrap_ests[i] = estimator(sample_new)
33   }
34
35   #d <- split(temp,rep(1:B,each=n/2))
36   #print(d)
37   #print(samples[resamples,])
38   # apply to each row
39   # bootstrap_ests = apply(resamples, 1, estimator)
40   # print(bootstrap_ests)
41   # return bootstrap mean and standard error estimates
42   c(
43     mean(bootstrap_ests),
44     sqrt(var(bootstrap_ests))
45   )
46 }
47
48 est_function = function(a){
49   x = a[,1]
50   y = a[,2]
51   return(cor(x,y))
52 }
53 set.seed(440)
54 bootstrap_corr = bootstrap(sample_set, 10000, est_function)
55 bootstrap_corr
56 c(lower=bootstrap_corr[1] - 2 * bootstrap_corr[2],
57   est=bootstrap_corr[1],
58   upper=bootstrap_corr[1] + 2 * bootstrap_corr[2])

```

47:1 (Top Level) ↕

Console	Terminal ×	Background Jobs ×
R 4.2.1 · C:/Users/Charlie Lu/Desktop/ ↗		
<pre> > bootstrap_corr [1] 0.7714517 0.1340042 > c(lower=bootstrap_corr[1] - 2 * bootstrap_corr[2], + est=bootstrap_corr[1], + upper=bootstrap_corr[1] + 2 * bootstrap_corr[2]) lower est upper 0.5034433 0.7714517 1.0394600 </pre>		

1 B

```
60 #Boot function
61 set.seed(440)
62 est_function1 = function(a,index){
63   x = a[index,1]
64   y = a[index,2]
65   return(cor(x,y))
66 }
67 set.seed(440)
68 non <- boot(sample_set, est_function1, R = 10000)
69 non
70 c(0.7763745 - 2*0.132994,0.7763745+ 2*0.132994)
71 c(lower=bootstrap_corr[1] - 2 * bootstrap_corr[2],
72   est=bootstrap_corr[1],
73   upper=bootstrap_corr[1] + 2 * bootstrap_corr[2])
74 }
```

75:1 (Top Level) ↕

Console	Terminal ×	Background Jobs ×
R 4.2.1 · C:/Users/Charlie Lu/Desktop/ ↗		

```
Bootstrap Statistics :
      original      bias    std. error
t1* 0.7763745 -0.004161978  0.132994
> c(0.7763745 - 2*0.132994,0.7763745+ 2*0.132994)
[1] 0.5103865 1.0423625
> c(lower=bootstrap_corr[1] - 2 * bootstrap_corr[2],
+   est=bootstrap_corr[1],
+   upper=bootstrap_corr[1] + 2 * bootstrap_corr[2])
      lower      est      upper
0.5034433 0.7714517 1.0394600
>
```

Comparing the 2 results we can see that they are very similar which makes sense because it's functionally similar as well.

2 C

```
75 #Parametric
76 mu <- c(mean(data$EntranceExam), mean(data$GPA))
77 mu
78 sigma <- cov(data.frame(sample_set))
79 sigma
80
81:1 (Top Level) ↕
```

Console	Terminal x	Background Jobs x
R 4.2.1 · C:/Users/Charlie Lu/Desktop/ ↗		
<pre>> #Parametric > mu <- c(mean(data\$EntranceExam), mean(data\$GPA)) > mu [1] 600.266667 3.094667 > sigma <- cov(data.frame(sample_set)) > sigma x1 x2 x1 0.0592981 7.901524 x2 7.9015238 1746.780952 > > .</pre>		

3 D

```
80  
81 set.seed(440)  
82 binorm <- mvrnorm(10000,mu,sigma)  
83 mv_mu <- c(mean(binorm[,1]),mean(binorm[,2]))  
84  
85 mv_mu  
86 mv_cov <- cov(data.frame(binorm))  
87 mv_cov  
88  
89:1 (Top Level) ⚡
```

Console	Terminal ×	Background Jobs ×
R 4.2.1 · C:/Users/Charlie Lu/Desktop/ ↗		
<pre>> binorm <- mvrnorm(10000,mu,sigma) > mv_mu <- c(mean(binorm[,1]),mean(binorm[,2])) > mv_mu [1] 600.268607 3.415991 > mv_cov <- cov(data.frame(binorm)) > mv_cov x1 x2 x1 0.0588713 7.981507 x2 7.9815073 1782.365149 ></pre>		

Compared the previous values we received, we can see that they are almost identical.

4 E

```

98
99 set.seed(440)
100 # aggregate our estimates using bootstrap rules
101 bootstrap_cov_est = mean(bootstrap_covs)
102 bootstrap_cov_se = sqrt(var(bootstrap_covs))
103 bootstrap_cov_est
104 bootstrap_cov_se
105
106 c(lower=bootstrap_cov_est - 2 * bootstrap_cov_se,
107   est=bootstrap_cov_est,
108   upper=bootstrap_cov_est + 2 * bootstrap_cov_se)
109
110 c(lower=(bootstrap_cov_est - 2 * bootstrap_cov_se) / sqrt(prod(diag(sigma))),
111   est=bootstrap_cov_est / sqrt(prod(diag(sigma))),
112   upper=(bootstrap_cov_est + 2 * bootstrap_cov_se) / sqrt(prod(diag(sigma))))
113
113:1 (Top Level) ⚡

```

Console	Terminal	Background Jobs
R 4.2.1 • C:/Users/Charlie Lu/Desktop/ ↗		
<pre> > c(lower=bootstrap_cov_est - 2 * bootstrap_cov_se, + est=bootstrap_cov_est, + upper=bootstrap_cov_est + 2 * bootstrap_cov_se) lower est upper 0.7811327 7.8704076 14.9596825 > c(lower=(bootstrap_cov_est - 2 * bootstrap_cov_se) / sqrt(prod(diag(sigma))), + est=bootstrap_cov_est / sqrt(prod(diag(sigma))), + upper=(bootstrap_cov_est + 2 * bootstrap_cov_se) / sqrt(prod(diag(sigma)))) lower est upper 0.07675121 0.77331713 1.46988305 </pre>		

Compared with the non-parametric version, the results are different by a significant margin. This makes sense because the parametric version only uses the sample data without any assumptions while the Non parametric assumes the distribution so naturally the results would differ as well.