## **CSE 2320 Notes 11: Rooted Trees**

(Last updated 10/21/18 10:41 AM)

CLRS 10.4, 12.1-12.3, 14.1, 13.2

#### 11.A. Trees

Representing Trees (main memory, disk devices in CSE 3330)

## Binary tree

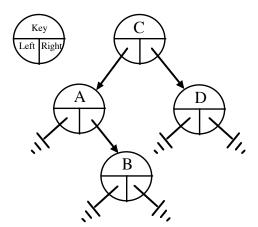
## Mandatory

Left Right

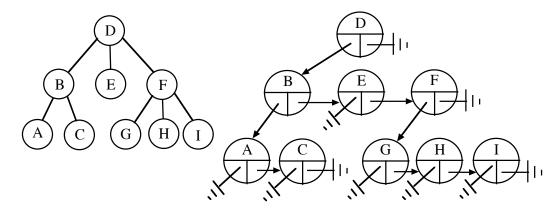
## Optional

Parent Key Data

Subtree Size



# Rooted tree with linked siblings



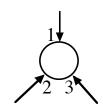
Mandatory

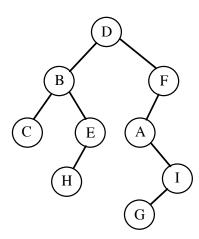
## Optional

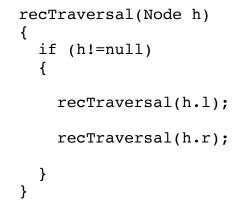
First Child
Right Sibling
Left Sibling
Parent
Key
Data
Subtree Size

#### 11.B. Binary Tree Traversals (review)

 $1^{st}$  Visit – Preorder  $2^{nd}$  Visit – Inorder  $3^{rd}$  Visit – Postorder







Preorder

DBCEHFAIG

Inorder

CBHEDAGIF

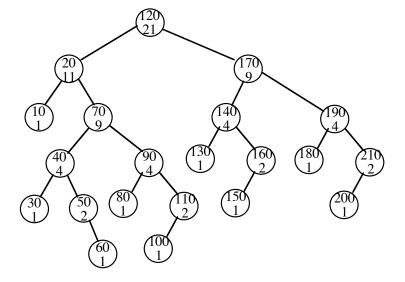
Postorder

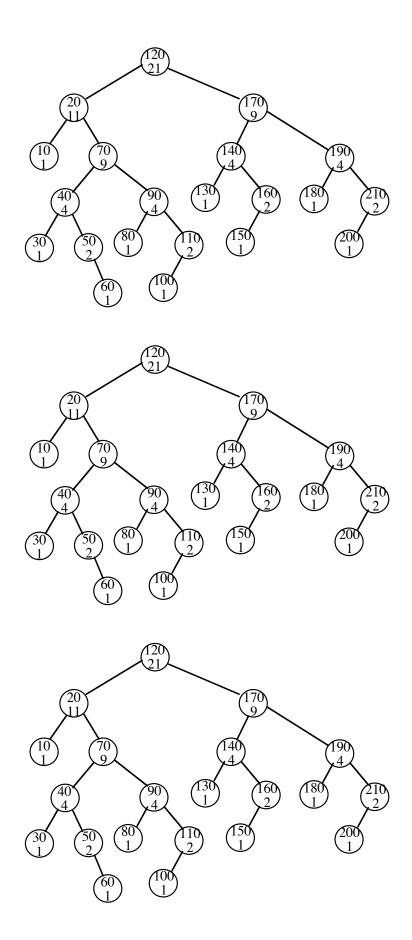
C H E B G I A F D

#### 11.C. BINARY SEARCH TREES

Basic property – Go left for smaller keys. Go right for larger keys. (Use of sentinel)

Which traversal lists the keys in ascending order?





Operations: (see http://ranger.uta.edu/~weems/NOTES2320/REDBLACKC/RB.c )

- 1. Search (searchR)
- 2. Minimum / maximum in tree
- 3. Successor/predecessor of a node
- 4. Insert (unbalanced in http://ranger.uta.edu/~weems/NOTES2320/REDBLACKC/RB.loadAndGo.c )
- 5. Deletion of key and associated data is contained in:
  - a. Leaf
  - b. Node with one child
  - c. Node with two children
    - 1. Find node's successor (convention)
    - 2. Move key and data (but not pointer values) from successor node to node of deletion.
    - 3. Successor has either
      - a. Zero children leaf is removed (5.a)
      - b. One child (right) point around successor node to remove (5.b)

May also use *tombstones* and periodically recycle garbage.

Implementing operations 6. and 7. efficiently requires maintaining subtree sizes "incrementally".

Rank of a key X that appears in tree = number of nodes with keys  $\leq X$ .

Number of nodes on search path to X with keys  $\leq$  key in given node

+

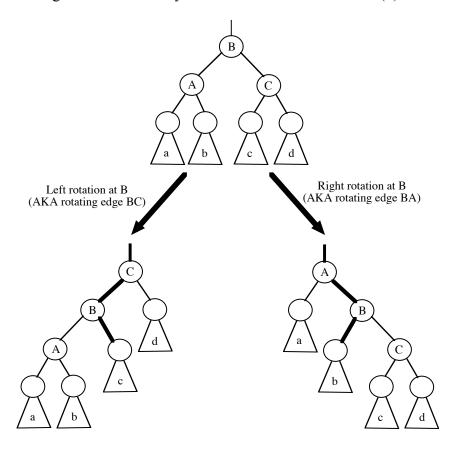
#### Sizes of their left subtrees

- 6. Rank of a key (invSelectR).
- 7. Finds key with a given rank (selectr) This is the same as flattening tree into an ordered array and then subscripting (or using inorder traversal).

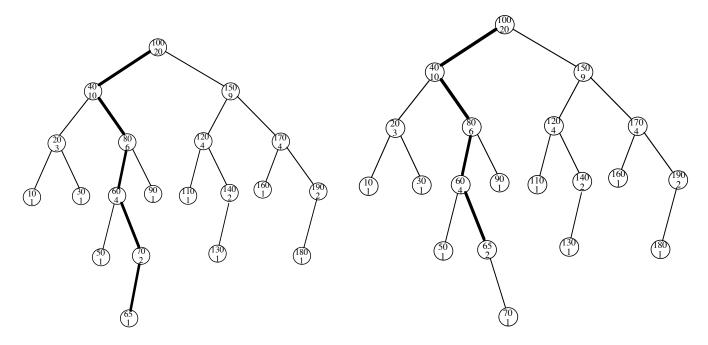
*Time for operations?* 

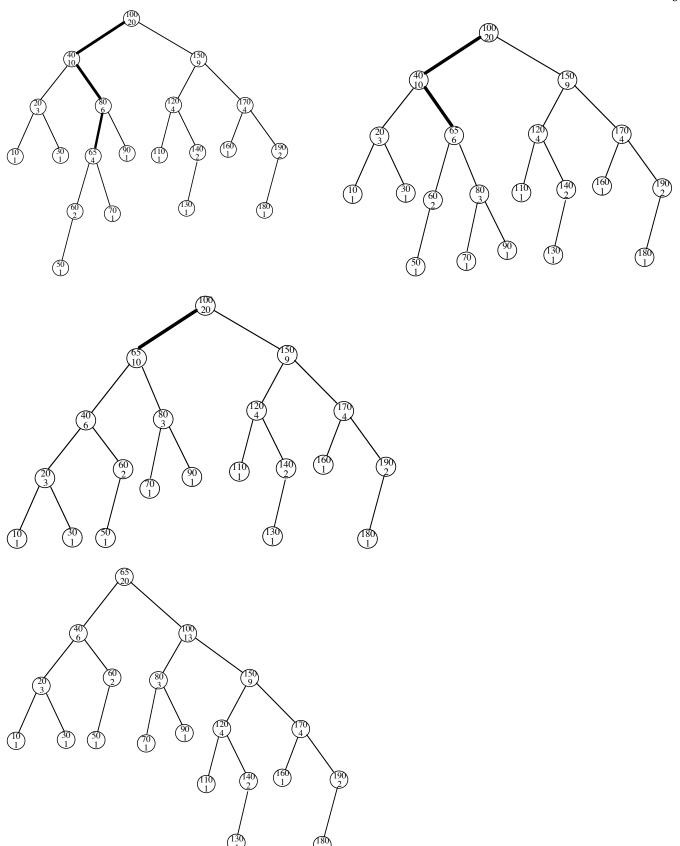
#### 11.D. ROTATIONS

Technique for rebalancing in balanced binary search tree schemes. Takes  $\Theta(1)$  time.



## 11.E. INSERTION AT ROOT: rotates all edges on the insertion path:





http://ranger.uta.edu/~weems/NOTES2320/bst.step.html