

# 13) Correlated Random Effects (CRE)

Vitor Kamada

August 2018

# Vella and Verbeek (1998)

$$\text{Log}(\text{wage})_{it} = \beta_0 + \beta_1 \text{Union}_{it} + X_{it} + u_{it}$$

use wagepan.dta

sum lwage educ black hisp exper married union

Variable	Obs	Mean	Std. Dev.	Min
lwage	4,360	1.649147	.5326094	-3.579079
educ	4,360	11.76697	1.746181	3
black	4,360	.1155963	.3197769	0
hisp	4,360	.1559633	.3628622	0
exper	4,360	6.514679	2.825873	0
married	4,360	.4389908	.4963208	0
union	4,360	.2440367	.4295639	0

# Compare OLS, RE, and FE

```
xtset nr year
```

```
reg lwage educ black hisp exper expersq married union i.year  
estimates store OLS
```

```
xtreg lwage educ black hisp exper expersq married union i.year, re  
estimates store RE
```

```
xtreg lwage educ black hisp exper expersq married union i.year, fe  
estimates store FE
```

# estimates table OLS RE FE, b(%7.4f) se

Variable	OLS	RE	FE
educ	0.0913 0.0052	0.0919 0.0107	(omitted)
black	-0.1392 0.0236	-0.1394 0.0477	(omitted)
hisp	0.0160 0.0208	0.0217 0.0426	(omitted)
exper	0.0672 0.0137	0.1058 0.0154	0.1321 0.0098
expersq	-0.0024 0.0008	-0.0047 0.0007	-0.0052 0.0007
married	0.1083 0.0157	0.0640 0.0168	0.0467 0.0183
union	0.1825 0.0172	0.1061 0.0179	0.0800 0.0193

# Hausman Test (1978)

$$H = (\hat{\delta}_{FE} - \hat{\delta}_{RE})' [Avar(\hat{\delta}_{FE}) - Avar(\hat{\delta}_{RE})]^{-1} (\hat{\delta}_{FE} - \hat{\delta}_{RE})$$

$H \sim \chi_M^2$ , where  $M$  is the vector of regressors varying across  $i$  and  $t$

Hausman Test has no power under violation of assumption RE.3

# hausman FE RE

	—— Coefficients ——			
	(b) FE	(B) RE	(b-B) Difference	sqrt(diag(V_b-V_B)) S.E.
exper	.1321464	.1057545	.0263919	.
expersq	-.0051855	-.0047239	-.0004616	.0001443
married	.0466804	.063986	-.0173057	.0073414
union	.0800019	.1061344	-.0261326	.0073572
year				
1981	.0190448	.040462	-.0214172	.
1982	-.011322	.0309212	-.0422431	.
1983	-.0419955	.0202806	-.0622762	.
1984	-.0384709	.0431187	-.0815896	.
1985	-.0432498	.0578155	-.1010653	.
1986	-.0273819	.0919476	-.1193295	.

b = consistent under  $H_0$  and  $H_a$ ; obtained from xtreg

B = inconsistent under  $H_a$ , efficient under  $H_0$ ; obtained from xtreg

Test:  $H_0$ : difference in coefficients not systematic

$\chi^2(10) = (b-B)' [(V_b - V_B)^{-1}] (b-B)$   
 $= 31.71$   
 Prob> $\chi^2 = 0.0004$

# hausman FE RE, sigmamore

	—— Coefficients ——			
	(b) FE	(B) RE	(b-B) Difference	sqrt(diag(V_b-V_B)) S.E.
exper	.1321464	.1057545	.0263919	.
expersq	-.0051855	-.0047239	-.0004616	.0001533
married	.0466804	.063986	-.0173057	.0074632
union	.0800019	.1061344	-.0261326	.0074922
year				
1981	.0190448	.040462	-.0214172	.
1982	-.011322	.0309212	-.0422431	.
1983	-.0419955	.0202806	-.0622762	.
1984	-.0384709	.0431187	-.0815896	.
1985	-.0432498	.0578155	-.1010653	.
1986	-.0273819	.0919476	-.1193295	.

b = consistent under  $H_0$  and  $H_a$ ; obtained from xtreg

B = inconsistent under  $H_a$ , efficient under  $H_0$ ; obtained from xtreg

Test:  $H_0$ : difference in coefficients not systematic

$$\begin{aligned}\chi^2(5) &= (b-B)' [(V_b - V_B)^{-1}] (b-B) \\ &= 26.22\end{aligned}$$

$$\text{Prob} > \chi^2 = 0.0001$$

## Correlated Random Effects - Mundlak (1978)

$$y_{it} = x_{it}\beta + c_i + u_{it}$$

$$x_{it}\beta = z_i\gamma + w_{it}\delta$$

$$c_i = \psi + \bar{w}_i\xi + \alpha_i$$

$$y_{it} = x_{it}\beta + \bar{w}_i\xi + \alpha_i + u_{it}$$

$$\hat{\beta}_{CRE} = \hat{\beta}_{FE}$$



# Create Variables for CRE

egen experbar = mean(exper), by(nr)

egen expersqbar = mean(expersq), by(nr)

egen marriedbar = mean(married), by(nr)

egen unionbar = mean(union), by(nr)

	nr	year	union	unionbar	exper	experbar
1.	13	1980	0	.125	1	4.5
2.	13	1981	1	.125	2	4.5
3.	13	1982	0	.125	3	4.5
4.	13	1983	0	.125	4	4.5
5.	13	1984	0	.125	5	4.5
6.	13	1985	0	.125	6	4.5
7.	13	1986	0	.125	7	4.5
8.	13	1987	0	.125	8	4.5
9.	17	1980	0	0	4	7.5
10.	17	1981	0	0	5	7.5

xtreg lwage educ black hisp exper expersq married  
union experbar expersqbar marriedbar unionbar  
i.year , re

lwage	Coef.	Std. Err.	z	P> z
educ	.0946036	.0109043	8.68	0.000
black	-.1388124	.0488709	-2.84	0.005
hisp	.0047758	.0426925	0.11	0.911
exper	.1321464	.0098247	13.45	0.000
expersq	-.0051855	.0007044	-7.36	0.000
married	.0466804	.0183104	2.55	0.011
union	.0800019	.0193103	4.14	0.000
experbar	-.1825835	.0512825	-3.56	0.000
expersqbar	.01031	.0032882	3.14	0.002
marriedbar	.0969833	.045084	2.15	0.031
unionbar	.1906747	.0504097	3.78	0.000

# Test for Endogeneity

test expersqbar marriedbar unionbar

```
( 1)  expersqbar = 0
( 2)  marriedbar = 0      chi2( 3) =    26.36
( 3)  unionbar = 0       Prob > chi2 =    0.0000
```

test unionbar

```
              chi2( 1) =    14.31
( 1)  unionbar = 0       Prob > chi2 =    0.0002
```

```
xtreg lwage educ black hisp exper expersq married
union experbar expersqbar marriedbar unionbar
i.year, re cluster(nr)
```

lwage	Coef.	Robust Std. Err.	z	P> z
educ	.0946036	.0112571	8.40	0.000
black	-.1388124	.0504943	-2.75	0.006
hisp	.0047758	.0386535	0.12	0.902
exper	.1321464	.0120177	11.00	0.000
expersq	-.0051855	.0008109	-6.39	0.000
married	.0466804	.0210207	2.22	0.026
union	.0800019	.0227614	3.51	0.000
experbar	-.1825835	.0467446	-3.91	0.000
expersqbar	.01031	.0028495	3.62	0.000
marriedbar	.0969833	.0448145	2.16	0.030
unionbar	.1906747	.0474693	4.02	0.000

# Fully Efficient Test

test expersqbar marriedbar unionbar

```
( 1)  expersqbar = 0
( 2)  marriedbar = 0      chi2( 3) =    29.87
( 3)  unionbar = 0       Prob > chi2 =    0.0000
```

test unionbar

```
              chi2( 1) =    16.13
( 1)  unionbar = 0       Prob > chi2 =    0.0001
```