



# EXPLOITING SHAPE PROPERTIES FOR IMPROVED RETRIEVAL, DISCRIMINATION AND RECOGNITION

Vittal Premachandran  
Thesis Defense Presentation  
February 2014

# Outline

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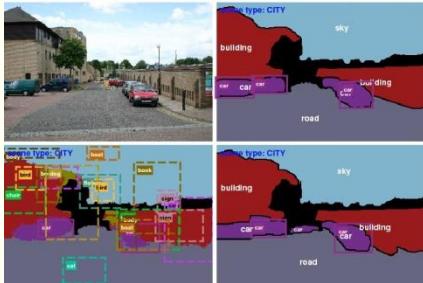
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- Introduction
- Background
- Perceptually Motivated Shape Context
- What parts of a shape are discriminative?
- Shape similarity propagation on manifolds
- Object detection in images using shapes
- Summary

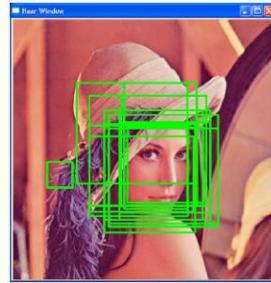
# Introduction

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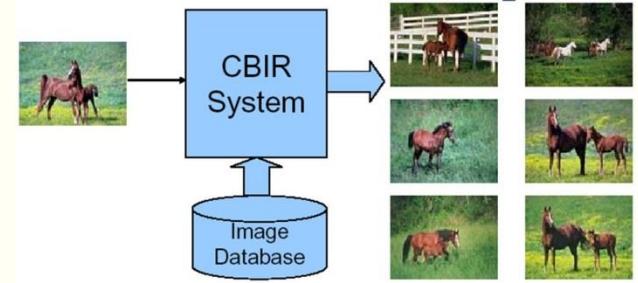
- Longstanding Goals of Computer Vision



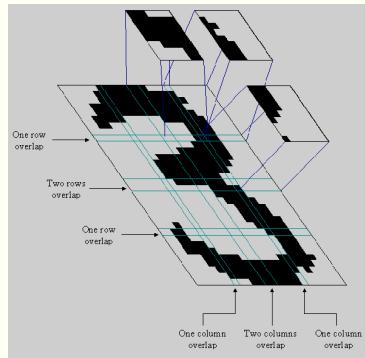
Scene Understanding



Face Recognition



Content-Based Image Retrieval



Optical Character Recognition

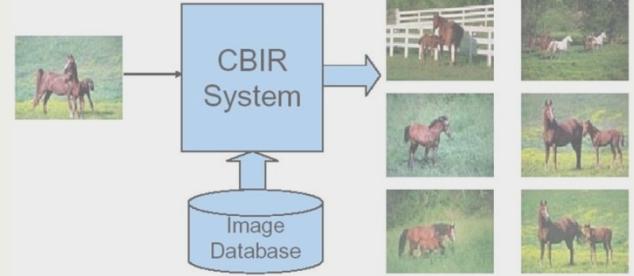
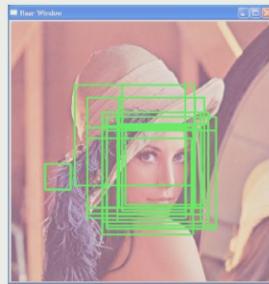


Tumor Detection

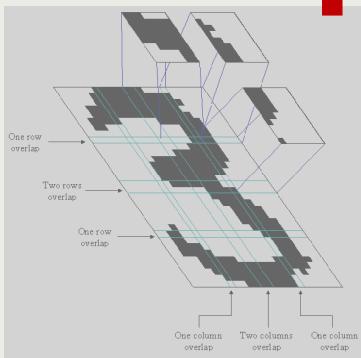
Common Task?

# Introduction

- Longstanding Goals of Computer Vision



Scene Understanding      Face Recognition      Content-Based Image Retrieval  
**Object Recognition!**



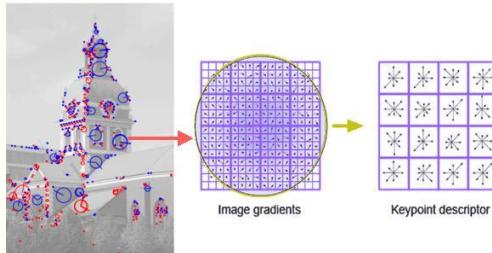
Common Task?

Optical Character Recognition

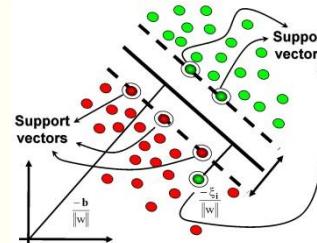
Tumor Detection

# Object Recognition

- How can we recognize objects?



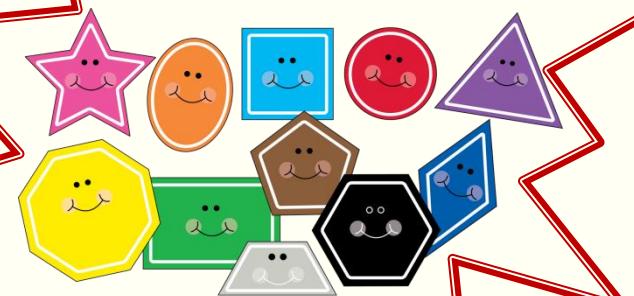
Extract Features



Train a classifier

+ve? Object ✓  
-ve? Object ✗

Make Decision



# What is Shape?

I'm in shape

A cartoon illustration of Peter Griffin, the main character from the TV show "Family Guy". He is a middle-aged man with a large, bulbous nose, wearing round-rimmed glasses, a white button-down shirt, and a dark green belt. He has a slightly grumpy or determined expression. The background behind him is a solid orange color.

Family Guy  
© FOX

Round is a shape

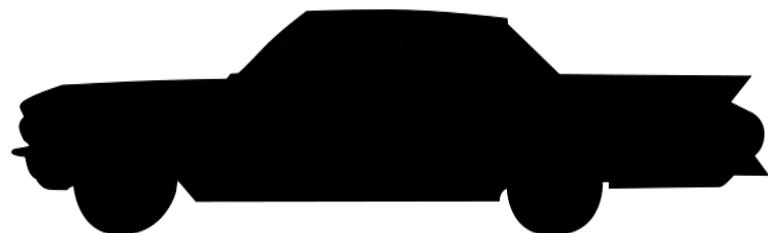
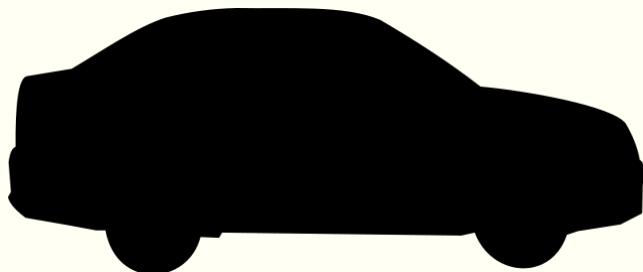
*“We here define ‘shape’ informally as ‘all the geometrical information that remains when location, scale and rotational effects are filtered out from an object.’”*

– David George Kendall (1918-2007)  
Statistician and Mathematician

## Why use shapes?

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- No colour, no texture; yet recognizable.
  - Shape enables class-level recognition
- 
- How to represent shapes?

# Outline

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# Modern Computer Vision

## Shape Matching and Object Recognition Using Shape Contexts

Serge Belongie, *Member, IEEE*, Jitendra Malik, *Member, IEEE*, and Jan Puzicha

**Abstract**—We present a novel approach to measuring similarity between shapes and exploit it for object recognition. In our framework, the measurement of similarity is preceded by 1) solving for correspondences between points on the two shapes, 2) using the correspondences to estimate an aligning transform. In order to solve the correspondence problem, we attach a descriptor, the *shape context*, to each point. The shape context at a reference point captures the distribution of the remaining points relative to it, thus offering a globally discriminative characterization. Corresponding points on two similar shapes will have similar shape contexts, enabling us to solve for correspondences as an optimal assignment problem. Given the point correspondences, we estimate the transformation that best aligns the two shapes; regularized thin-plate splines provide a flexible class of transformation maps for this purpose. The dissimilarity between the two shapes is computed as a sum of matching errors between corresponding points, together with a term measuring the magnitude of the aligning transform. We treat recognition in a nearest-neighbor classification framework as the problem of finding the stored prototype shape that is maximally similar to that in the image. Results are presented for silhouettes, trademarks, handwritten digits, and the COIL data set.

**Index Terms**—Shape, object recognition, digit recognition, correspondence problem, MPEG7, image registration, deformable templates.

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philtorr@microsoft.com

Serge Belongie,  
Jitendra Malik, S

**Abstract**—We demonstrate that shape contexts can be used for shape search for similar shapes. We present a new way to generate *representative shape contexts*, perform shape matching using *shape contexts*, and *shapemes*, using *shape contexts* to obtain prototypical shape prototypes.

**Index Terms**—Shape, object recognition

## Rigid Shapes with a Single Closed Contour

and Rolf Läkämper and Ulrich Eckhardt  
of Applied Mathematics  
University of Hamburg

## Deformable Scenes

R. Cipolla \*

Microsoft Research Ltd.  
Thompson Avenue  
Cambridge, CB3 0FB, UK

ed on  
arts

iper

ited and its  
ate in image

## Shape Classification Using the Inner-Distance

Haibin Ling

David W. Jacobs

Center for Automation Research and Computer Science Department

University of Maryland, College Park

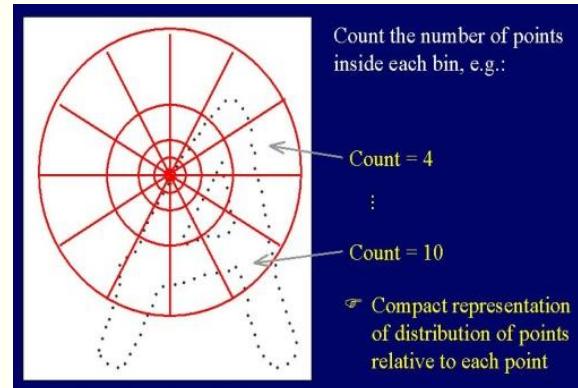
{hbling, djacobs}@umiacs.umd.edu

## Existing Methods

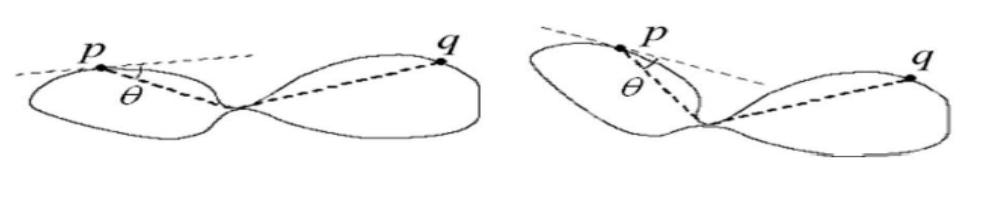
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- Belongie, S.; Malik, J.; Puzicha, J.; , "Shape matching and object recognition using shape contexts," *PAMI 2002*.

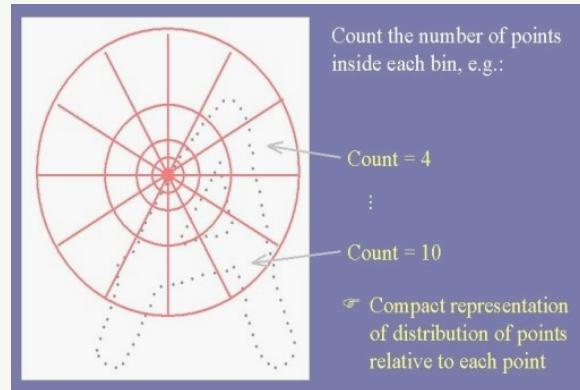


- Haibin Ling, David W. Jacobs, "Shape Classification Using the Inner-Distance", *PAMI, 2007*.
  - IDSC



## Existing Methods

- Belongie, S.; Malik, J.; Puzicha, J.; , "Shape matching and object recognition using shape contexts," *PAMI 2002*.



Belongie, S.; Malik, J.; Puzicha, J.; , "Shape Matching and Object Recognition Using Shape Context," *PAMI 2002*.

*PAMI, 2007.*

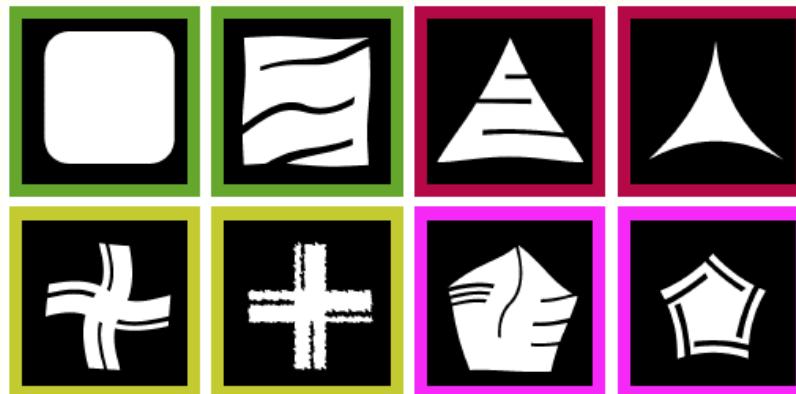
- IDSC



# Issues with Contour-Based Techniques

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- Two assumptions of contour-based techniques
  - Noise-free contours
  - Closed contours



Contours have indentations and noise



Contours have breaks

- Contours are important, but not always
- Need a way to capture entire shape; Gestalt Psychology
- Interior properties of a shape play an important role

# Outline

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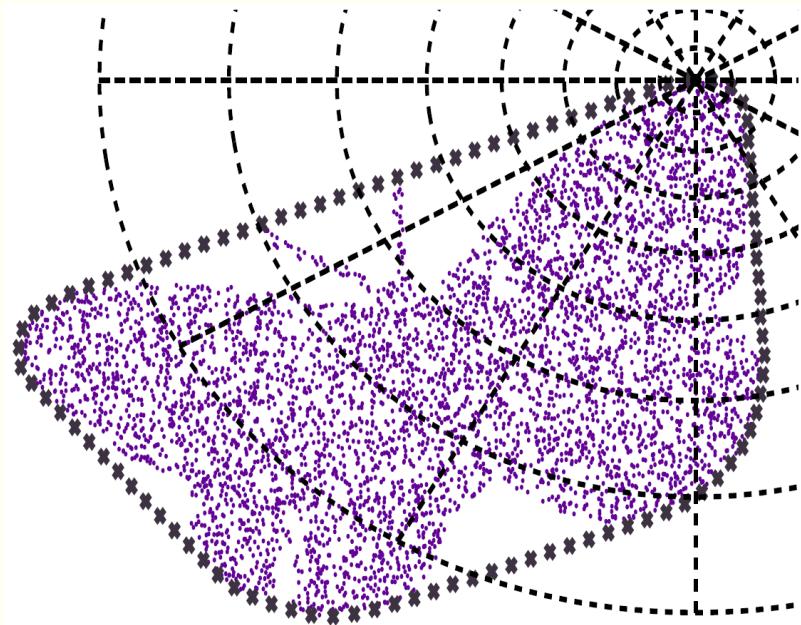
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# Solid Shape Context

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- Perceptually motivated variant of the Shape Context Descriptor
- Captures the interior properties of the shape (*Dense Points*)
- A sparse set of feature locations for easy shape-matching (*Sparse Points*)

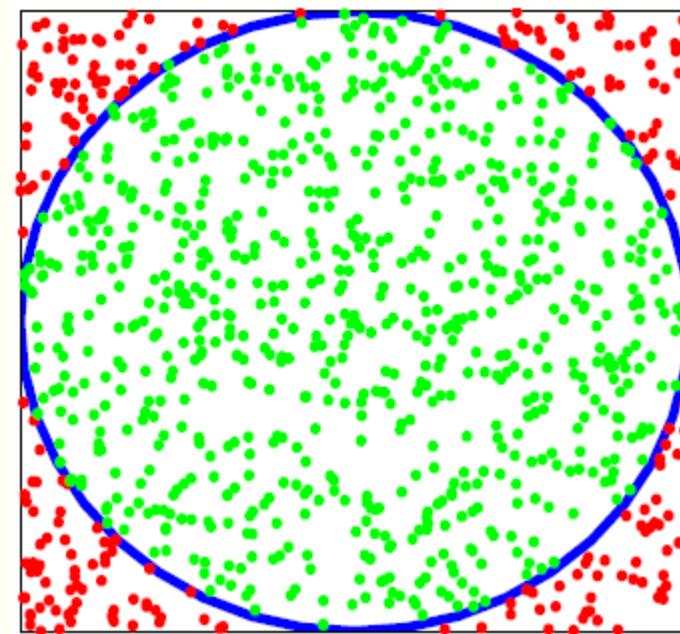
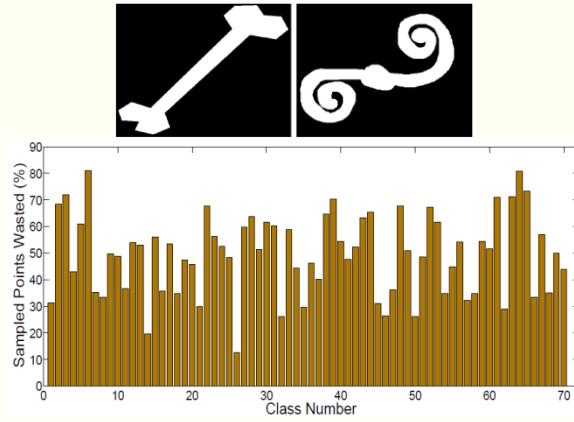


# Interior Properties

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- Contour Layout: Sample contour :: Interior Layout :: Sample from inside!
- How to sample points?
- A: Accept/Reject technique

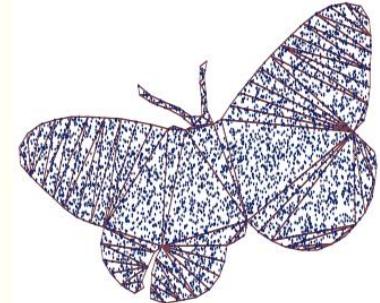
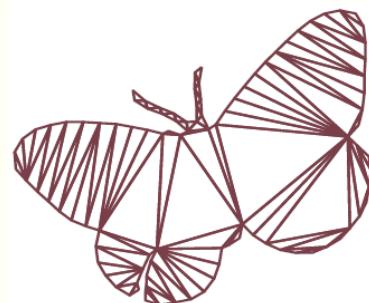
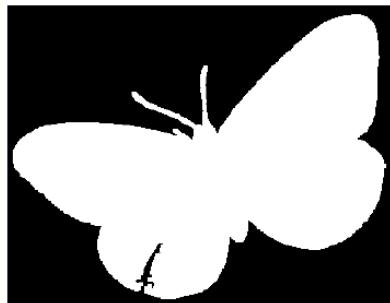


# Constrained Delaunay Triangulation - Sampling

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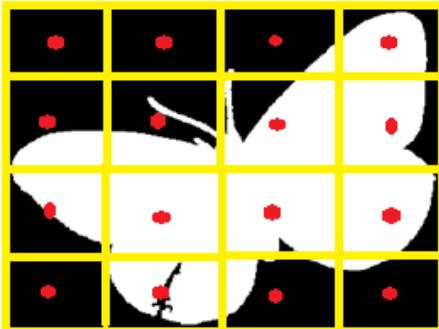
- Extract contour and sample a set of points
- Perform a Constrained Delaunay Triangulation  
on the sampled points
- Sample points from within each triangle



# Sparse Points

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- *Dense Points* ~ 2500
- Matching features are each *Dense Point* is computationally infeasible
  - (and unnecessary)
- So, need a sparser set of points to compute the descriptor
- What are a good set of sparse points?



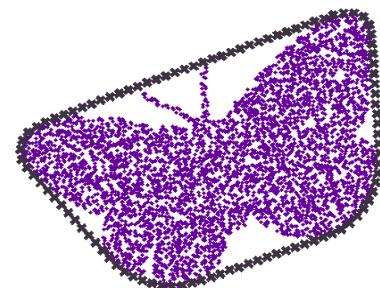
Centers of grids?

- We lose continuity constraints



Uniform points along contours?

- Susceptible to indentations in contour



Our method:

Sample points along the *convex hull* of the shape

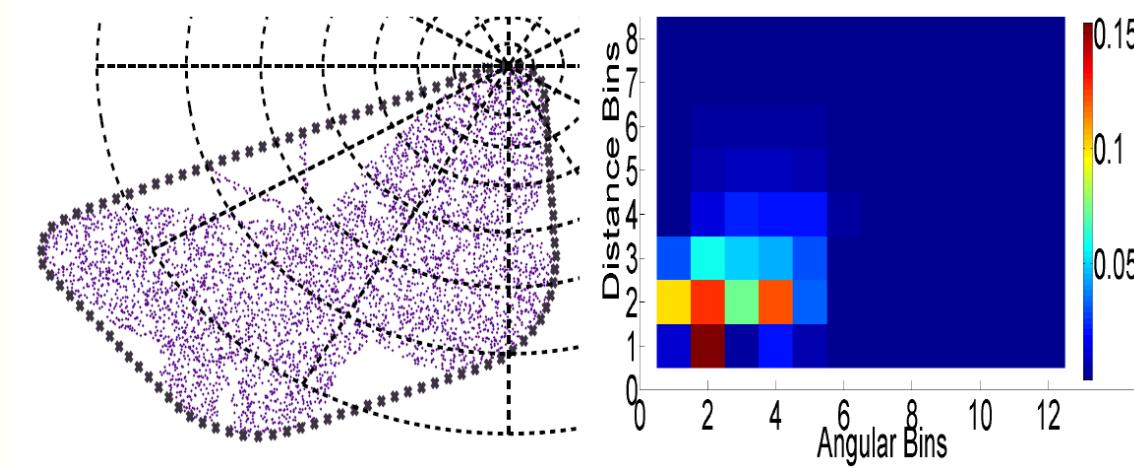
# Solid Shape Context Descriptor

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- SSC descriptor is a 2-D histogram of distances and angles
- The histogram is computed at each *Sparse Point*

$$\mathcal{H}_i^S(k) = \#\{\mathcal{DP}_j^S : \mathcal{DP}_j^S \in \text{bin}(k)\}$$



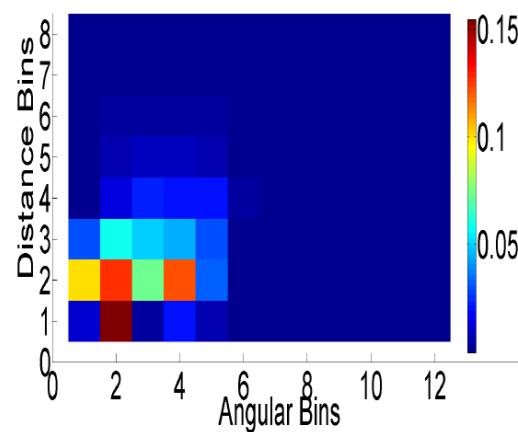
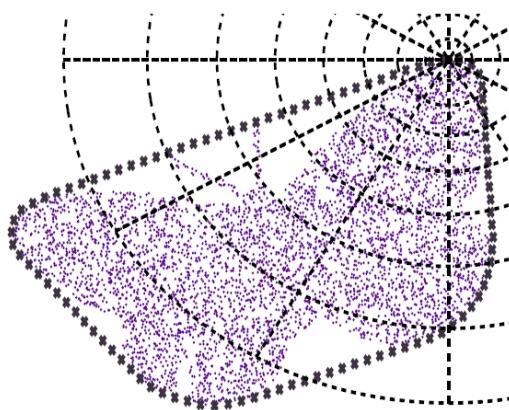
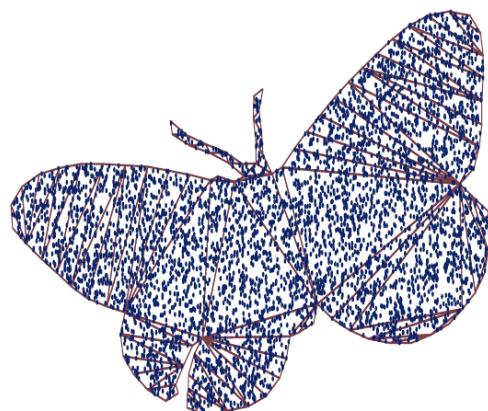
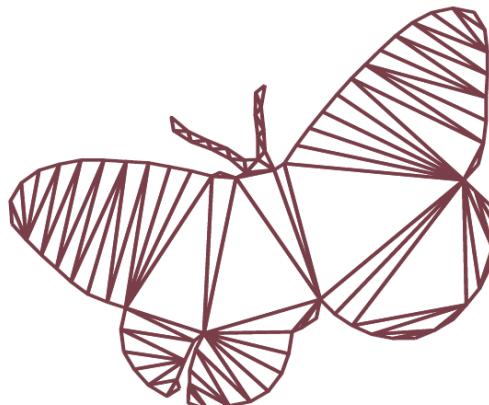
- A shape is now described by a set of histograms

$$SSC^S = \{\mathcal{H}_1^S, \mathcal{H}_2^S, \dots, \mathcal{H}_{N_{SP}}^S\}$$

# Putting it together

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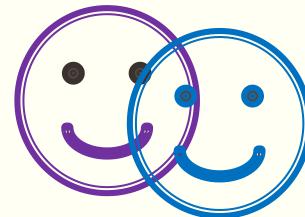


# Properties of SSC

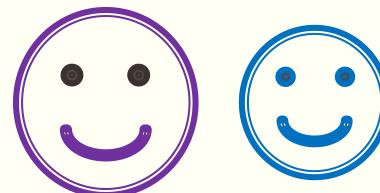
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- Robust to indentations and contour noise



- Invariant to translation



- Invariant to scale



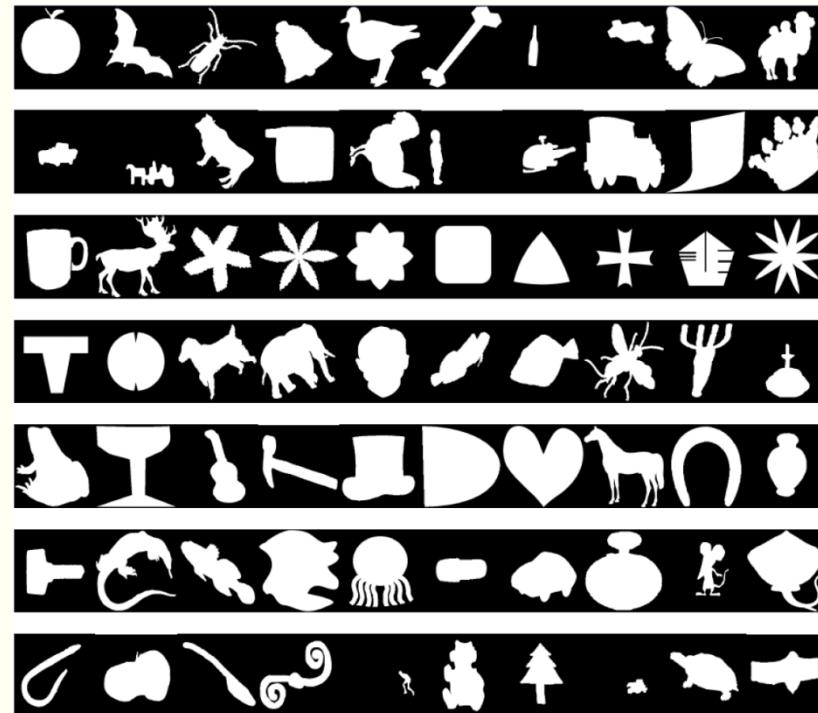
- Invariant to rotation

## Experiments and Results

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- MPEG-7 Database
- 1400 images, 70 classes, 20 objects per class
- Objects vary in scale, rotation, translation, articulation



# Experiments and Results

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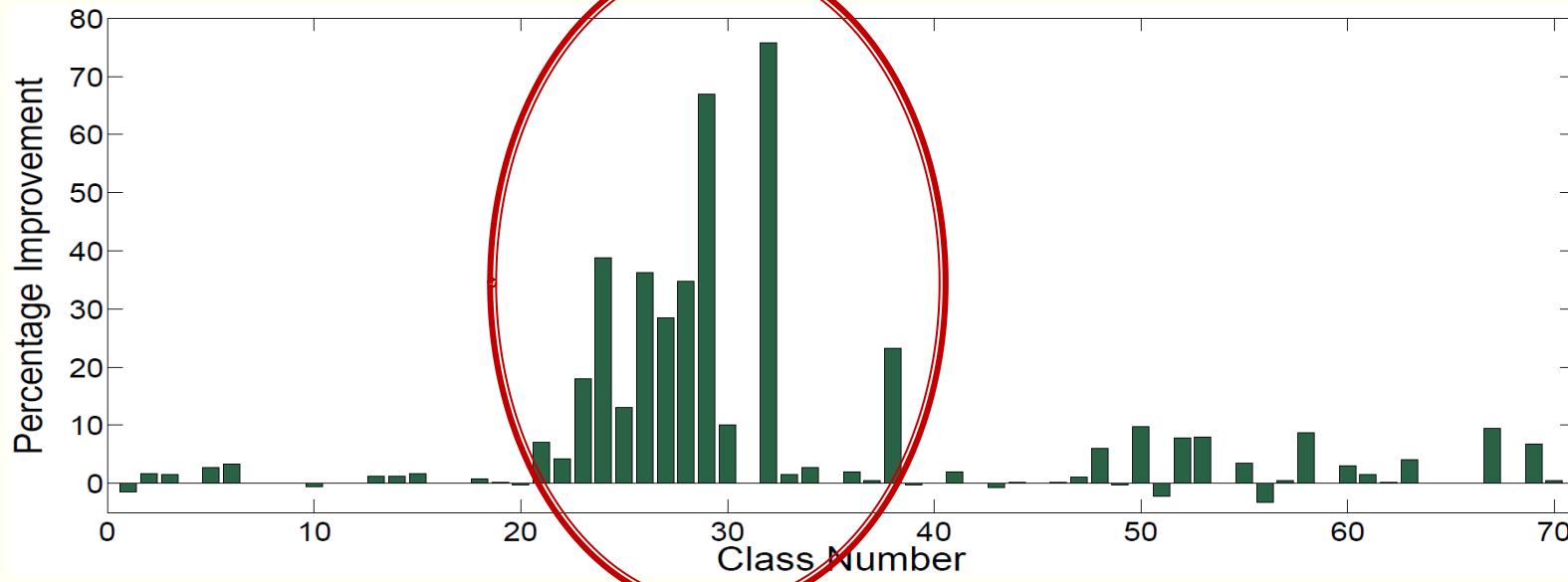
- Performance is measured using Bullseye score

Algorithm	Bullseye Score
Visual Parts [52]	76.45%
SC+TPS [13]	76.51%
Generative Model [96]	80.03%
Curvature Scale Space [65]	81.12%
SSC	82.39%
Polygonal Multiresolution [5]	84.33%
Multiscale Representation [1]	84.93%
IDSC [55]	85.40%
Symbolic Representation [26]	85.92%
Hierarchical Procrustes Matching [64]	86.35%
IDSC(EMD) [56]	86.53%
Triangle Area [2]	87.23%
Shape Tree [30]	87.70%
ASC [57]	88.30%
IDSC+AspectNorm.+StrandRemoval [92]	88.39%
Contour Flexibility [104]	89.31%
IDSC+PMMS [39]	90.18%
IDSC+LP [106]	91.00%
<b>IDSC+SSC</b>	<b>91.65%</b>
<b>IDSC+AspectNorm.+SSC</b>	<b>91.83%</b>
IDSC+LCDP [107]	92.36%
IDSC+Affine Normalization [37]	93.67%
IDSC+AspectNorm.+StrandRemoval+LCDP [92][107]	95.60%
ASC+LCDP [57][107]	95.96%
IDSC+PMMS+LCDP [39][107]	98.56%
<b>IDSC+SSC+LCDP</b>	<b>98.85%</b>
IDSC+Affine Normalization+TPG [108]	99.99%

# Improvement Over IDSC

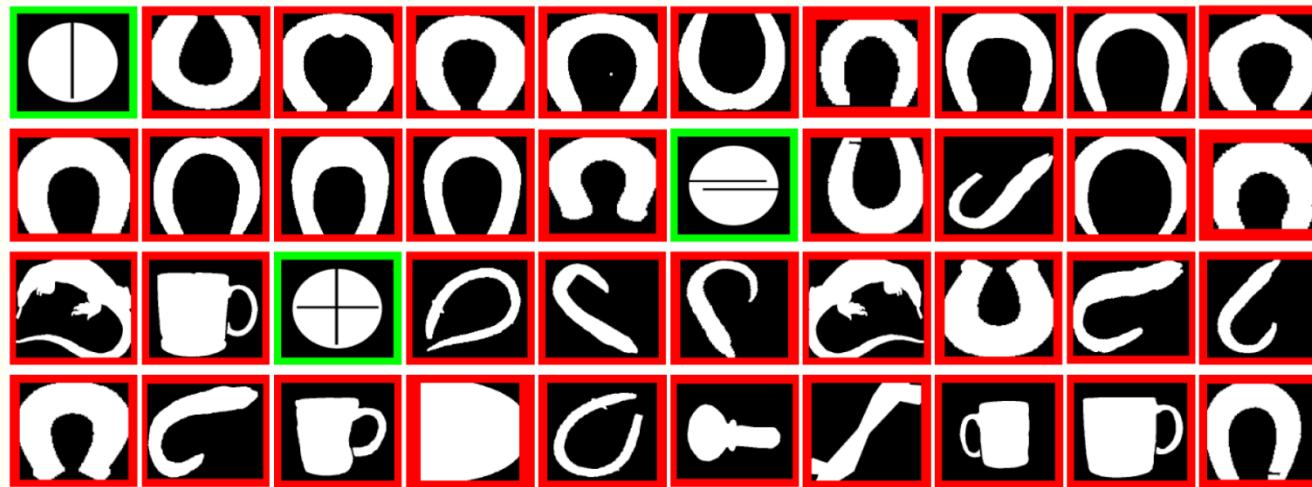
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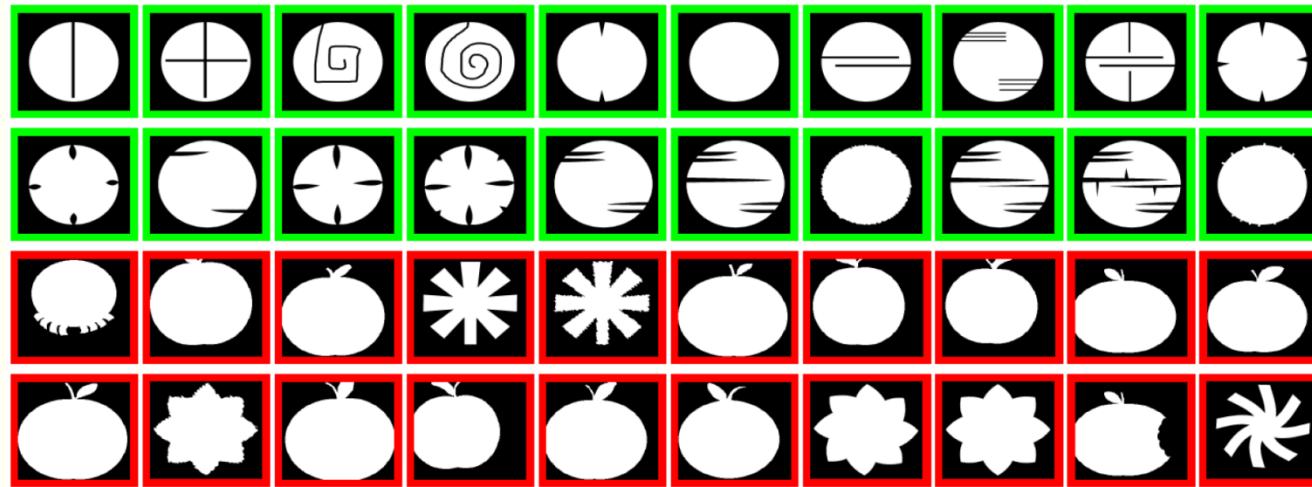


## Qualitative Results

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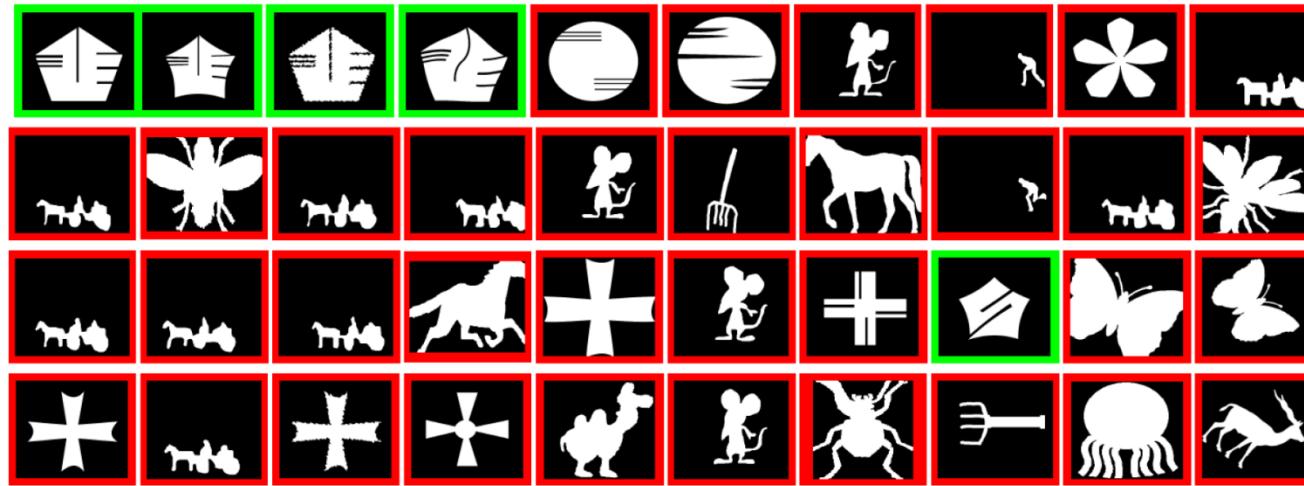
(A) IDSC



(B) SSC

## Qualitative Results - 2

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(c) IDSC



(d) SSC

## Perceptually Motivated Shape Context - Recap

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- Interior properties of the shape are important
  - Proposed the Solid Shape Context descriptor to capture interior properties.
- 
- Vittal Premachandran, and Ramakrishna Kakarala. "Perceptually motivated shape context which uses shape interiors." *Pattern Recognition* (2013).
  - Ramakrishna Kakarala, Prabhu Kaliamoorthi\*, and Vittal Premachandran\*. "Three-dimensional bilateral symmetry plane estimation in the phase domain." *Computer Vision and Pattern Recognition (CVPR)*, 2013 (\* indicates equal contribution)
- 
- We assume that all parts of the shape are equally important.
  - Is it so?

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Are all parts of the  
shape uniformly  
discriminative?

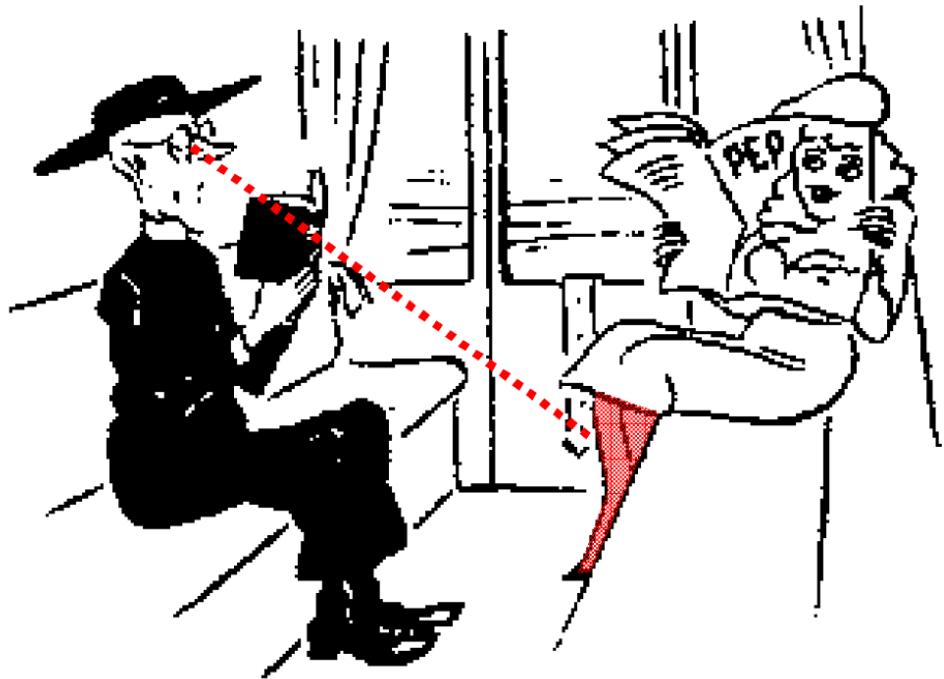


Illustration: Herluf Bidstrup

# Outline

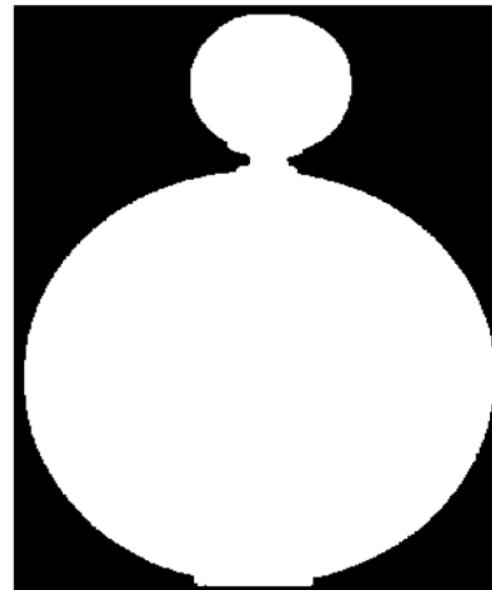
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## Motivation

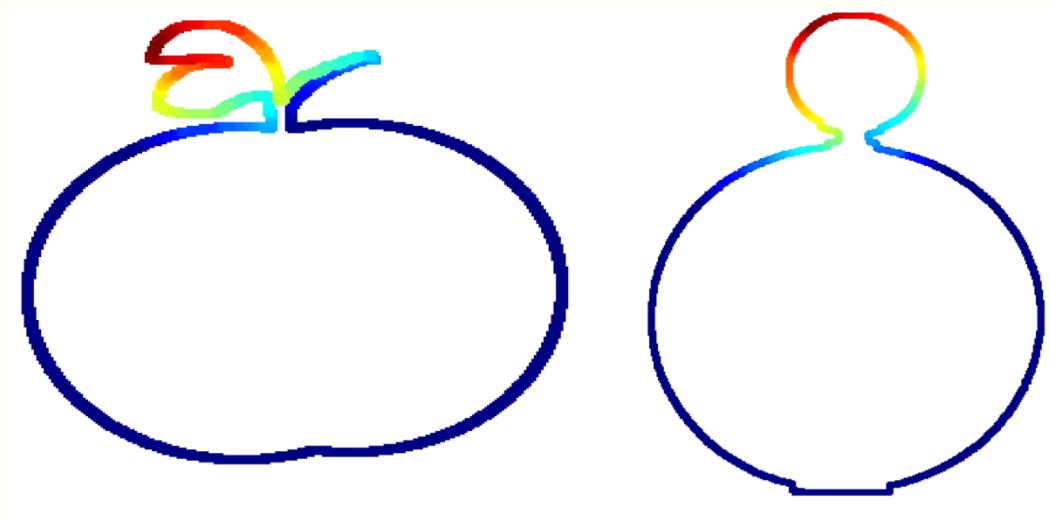
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# Motivation

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## Discriminative Parts

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- Definition: Parts of an object that are most different from parts of other objects belonging to similar-looking classes.
- Identifying discriminative parts:
  - Divide the shape into multiple parts
  - Find how unique each part is, compared to the negative examples
  - Assign an importance score to the part, which is proportional to its uniqueness

## Dividing the Shape

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- One way: Make cuts at points of extremum (i.e. corner points) on the contour
- But, identifying extrema points is difficult and subjective.
- Our approach:
  - *Randomly* split the contour into parts
  - Randomization does not introduce subjective bias
  - Bypass the use of not-so-perfect corner detectors

## Dividing the Shape - Detail

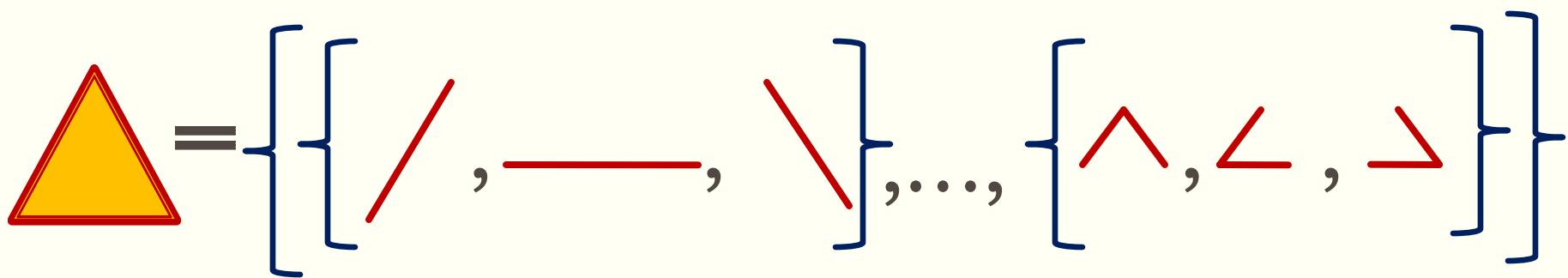
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- Given a shape  $S_i$ , extract its contour  $C_i$
- Randomly split the contour into  $p$  contour segments

$$C_i^{seg} = \{C_i^{seg_1}, C_i^{seg_2}, \dots, C_i^{seg_p}\}$$

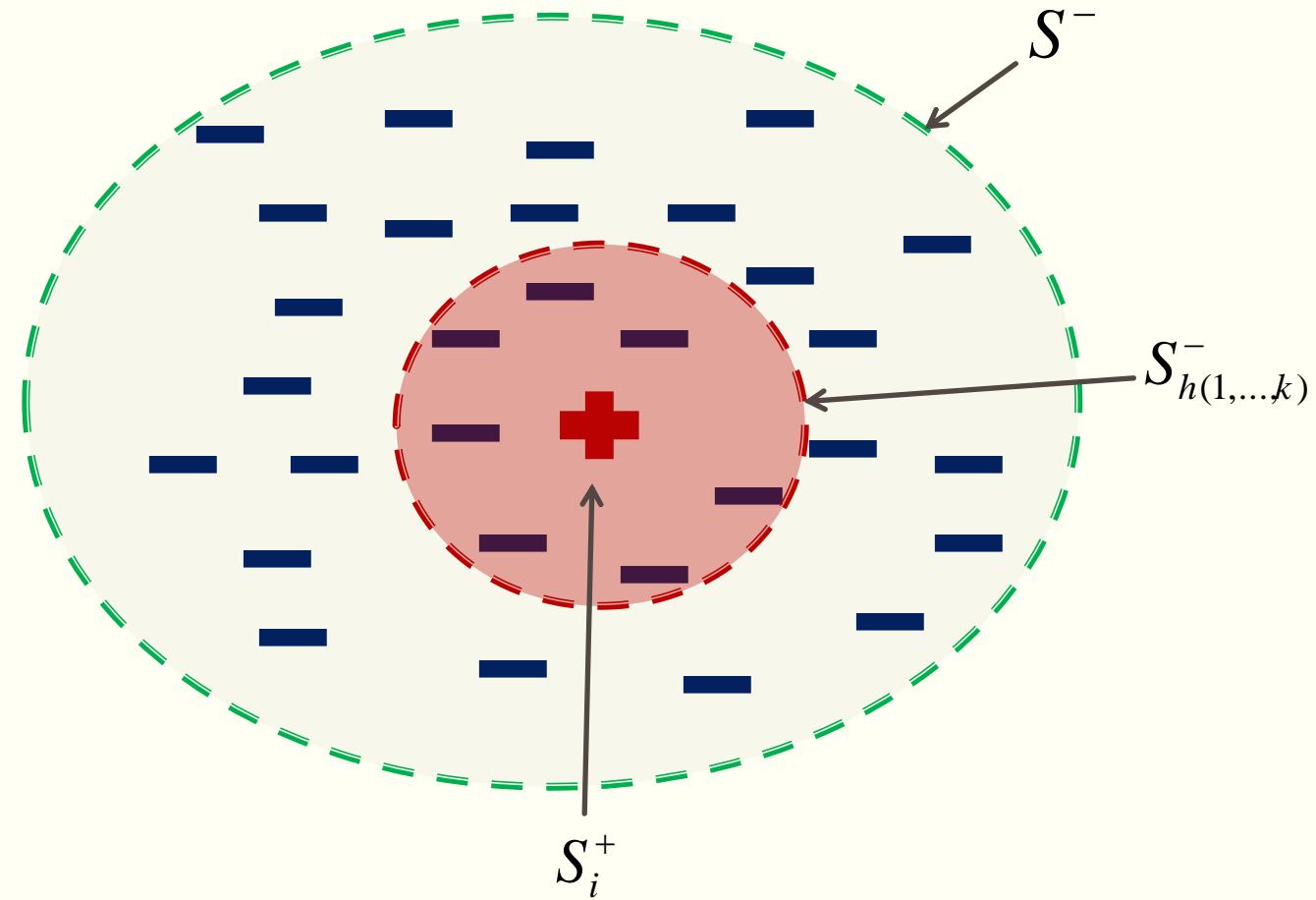
- Repeat the procedure  $T$  times to get  $T$  sets of  $p$  random parts



- Next step: Compute the uniqueness by comparing to parts from negative shapes

## Compare Parts to Negative Shapes

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$$S_h^- = \arg \min \Psi_{IDSC}(S_i^+, S_j^-)$$

# Shape Descriptor

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- Requirements:
  - Invariant to translations
  - Invariant to rotation
  - Invariant to scale
  - Should be a *partial* shape descriptor! (Most important requirement)
- SC, IDSC and SSC are all global shape descriptors

## Shape Descriptor - 2

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- Donoser et al. “Efficient partial shape matching of outer contours”, ACCV 2009.

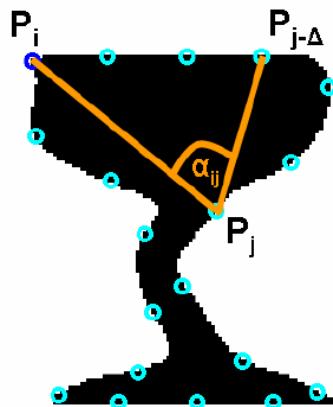


Figure from Donoser et al. ACCV '09

$$\alpha_{ij} = \angle(\overrightarrow{PP_j}, \overrightarrow{P_jP_{j-\Delta}})$$

$$A = \begin{pmatrix} \alpha_{11} & \cdot & \cdot & \cdot & \alpha_{1N} \\ \cdot & \cdot & & & \cdot \\ \cdot & & \cdot & & \cdot \\ \cdot & & & \cdot & \cdot \\ \alpha_{N1} & \cdot & \cdot & \cdot & \alpha_{NN} \end{pmatrix}$$

- Any sub matrix of the above matrix, is a partial shape descriptor.

■ **Distance: Distinctive**

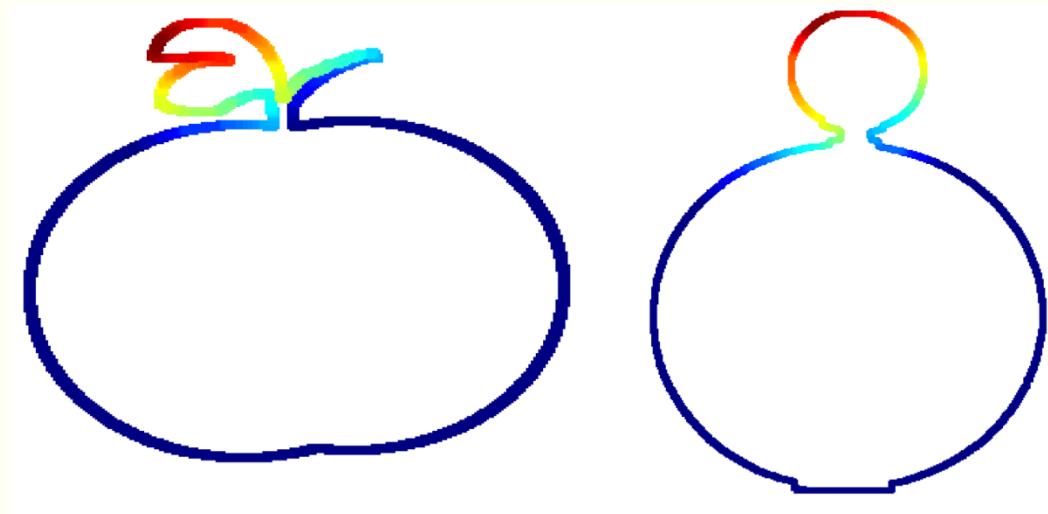
■ **Distance: Distinctive**

## Example

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- Learnt distinctiveness for two confusing classes

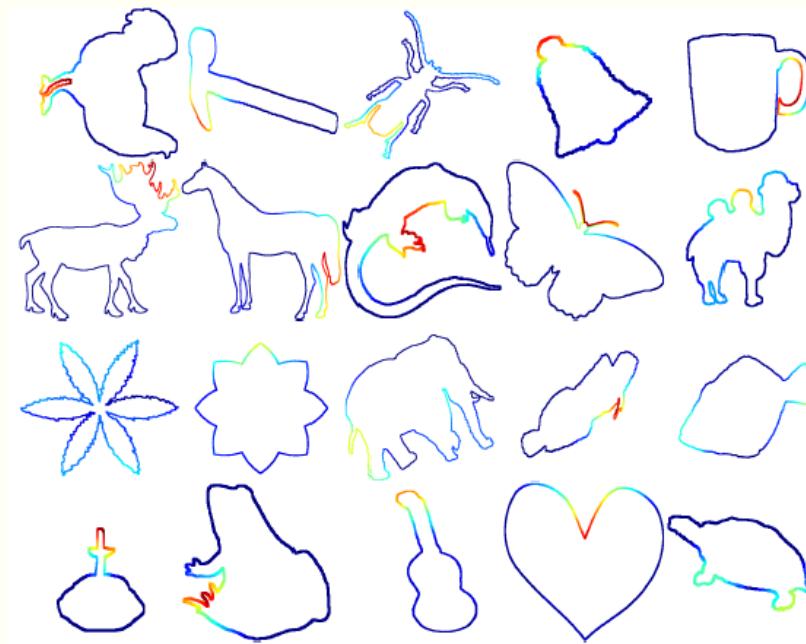


## More Examples

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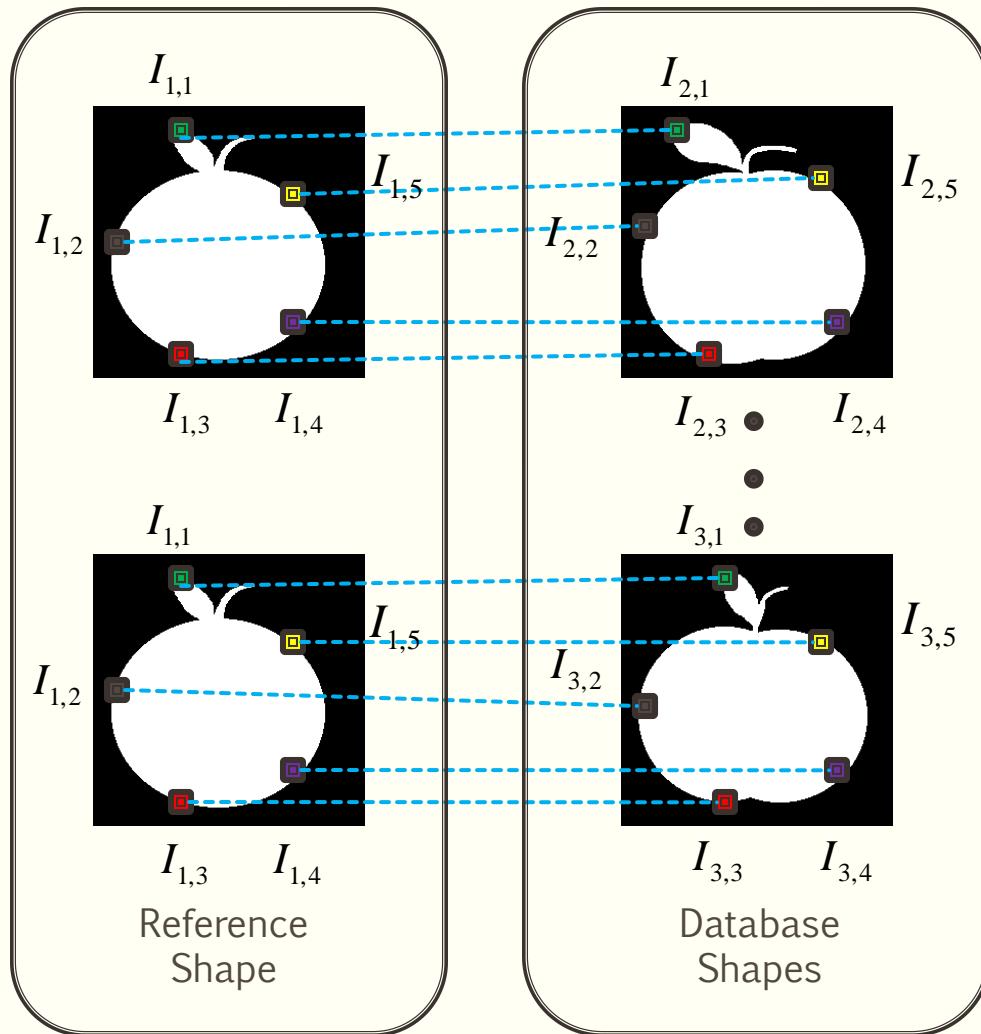
- Example heat maps from various classes.
- Semantically meaningful parts are identified as being distinctive.



# Part Consistency Matrix

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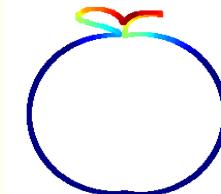
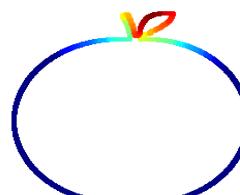
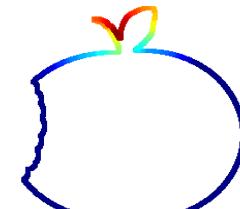
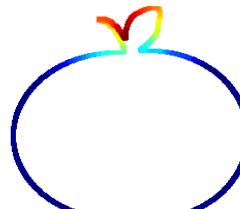
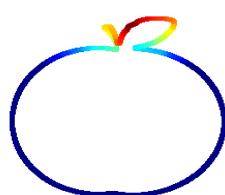
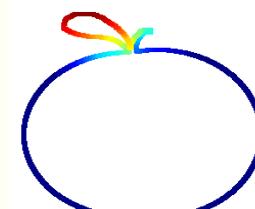
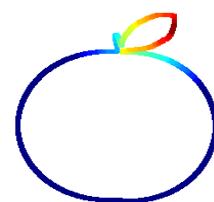
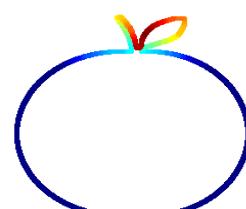
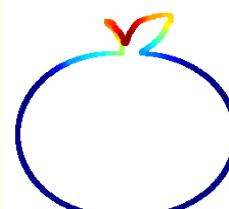
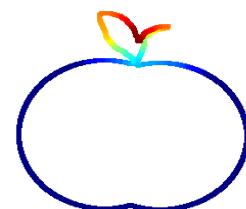
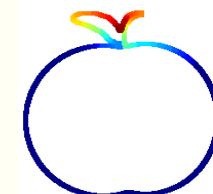
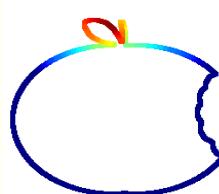
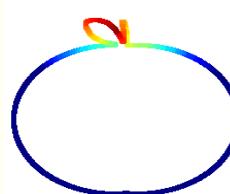
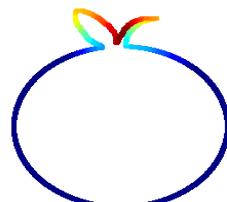
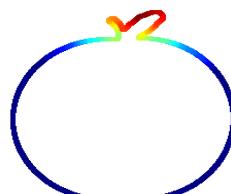
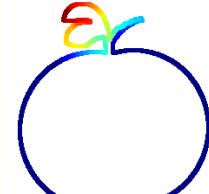
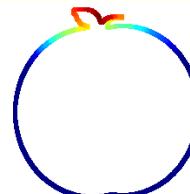
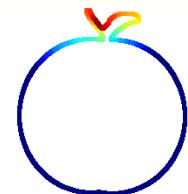


$$Q = \begin{bmatrix} I_{1,1} & I_{2,1} & I_{3,1} \\ I_{1,2} & I_{2,2} & I_{3,2} \\ I_{1,3} & I_{2,3} & I_{3,3} \\ I_{1,4} & I_{2,4} & I_{3,4} \\ I_{1,5} & I_{2,5} & I_{3,5} \end{bmatrix}$$

## Example Class with Low AUC - Apples

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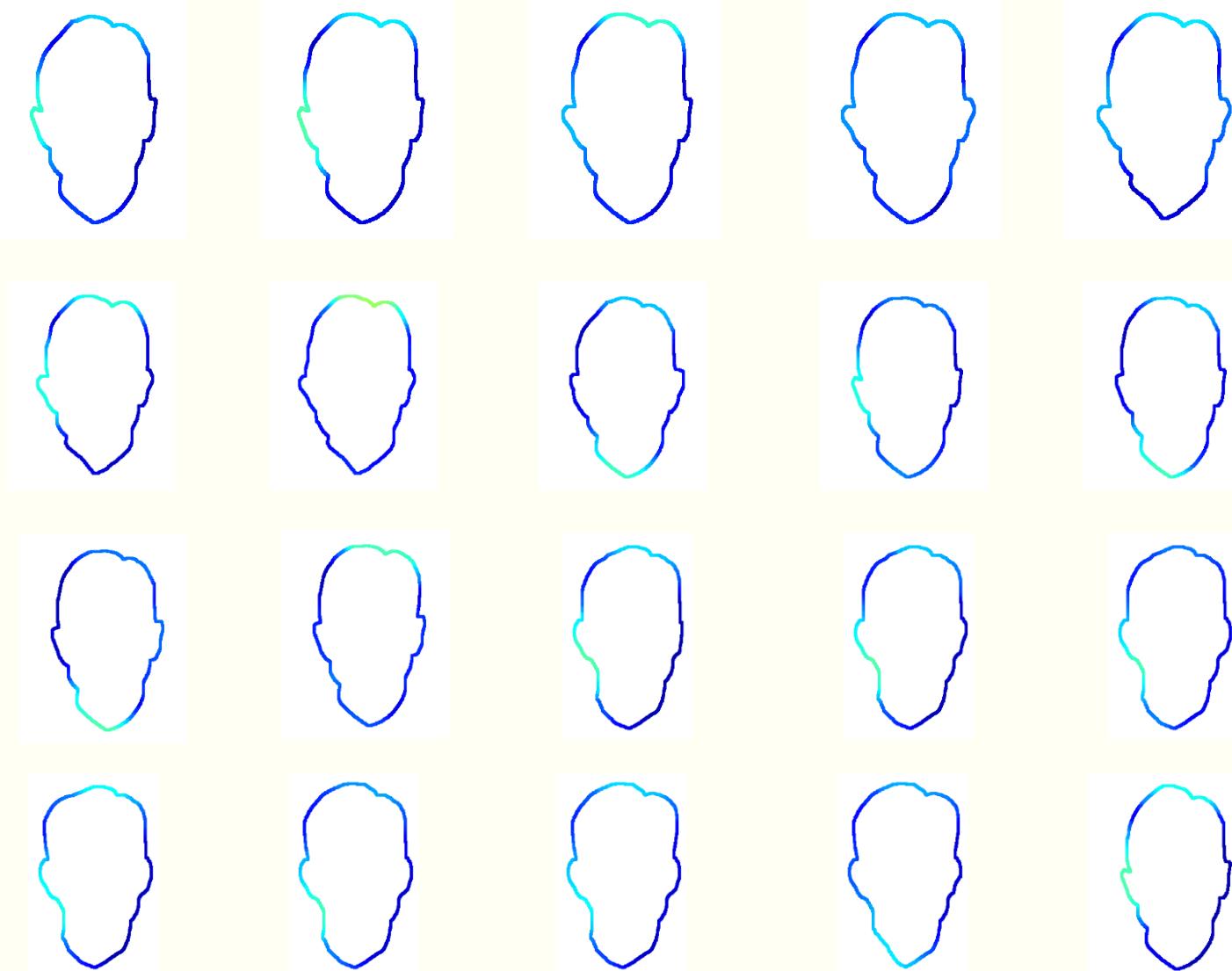
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## Example Class with High AUC – Face Silhouettes

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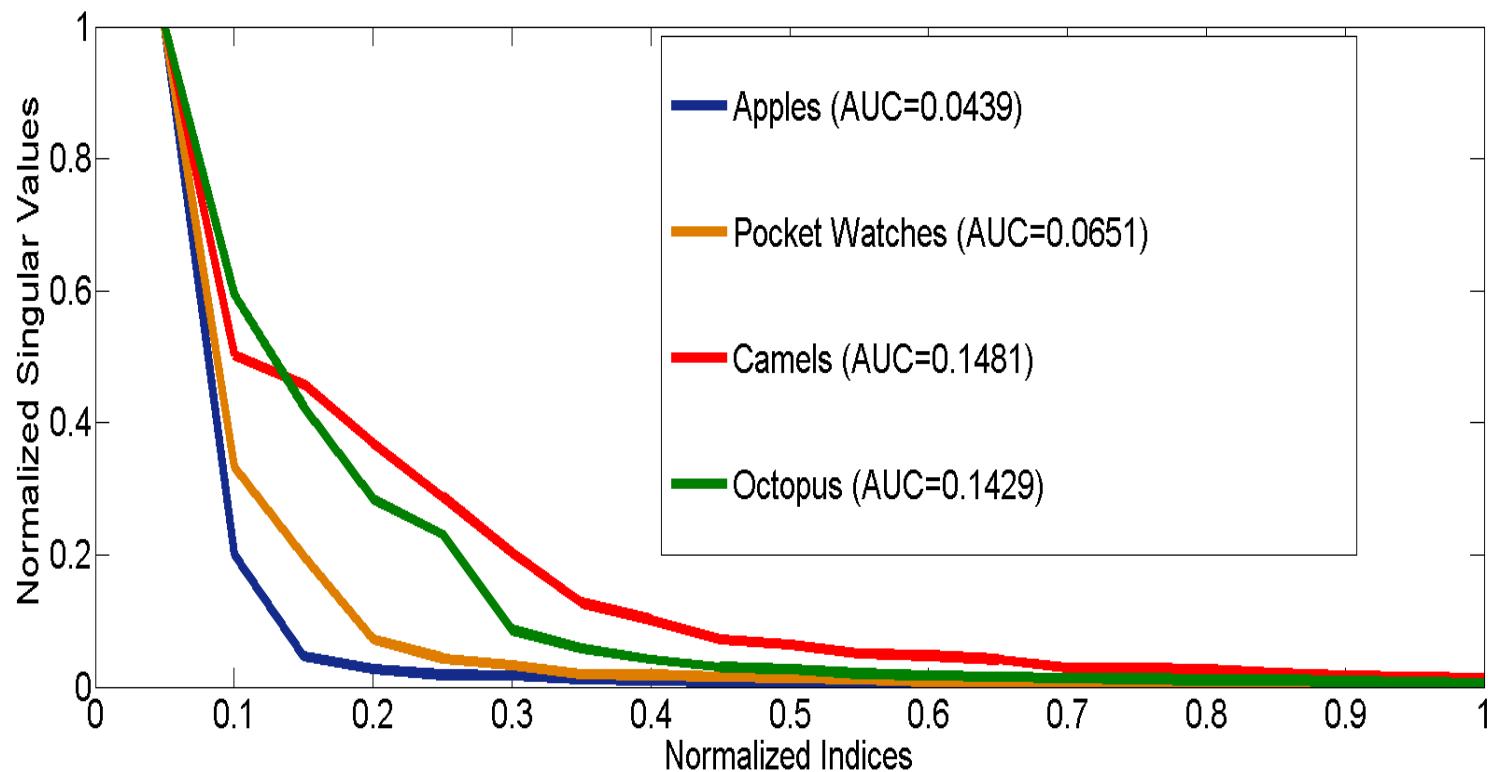
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# Singular Value Curves

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## Summary

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- Introduced the concept of distinctiveness with a strong motivating example and provided a simple way to extract discriminative parts.
- Vittal Premachandran, and Ramakrishna Kakarala. “What parts of a shape are discriminative?” *IEEE International Conference on Image Processing*, 2013. (**Best Student Paper Award!**)
- Pairwise comparison.
- Can we go Beyond Pairwise comparison of shapes?

# Outline

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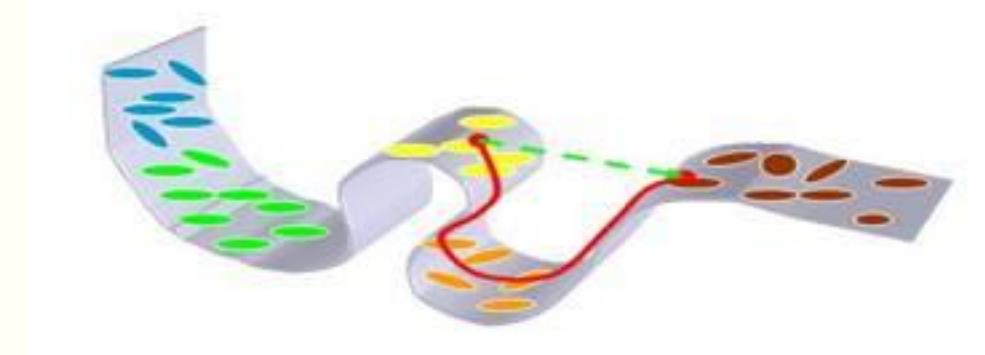
- Introduction
- Background
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- What parts of a shape are discriminative?
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# Shape Retrieval Using Shape Manifolds

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- Shapes lie in a high dimensional space
- However, the shape manifolds are usually of lower dimensionality
- Euclidean distance is a bad metric
- Need to learn the “true” geodesic distances



# Diffusion on Sparse Graphs

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- Diffusion is a process to learn the affinity between shapes
  - Sparse graphs are used for diffusion instead of fully-connected graphs
  - Fully connected graphs have lots of noisy edges;
- 
- Ways for graph sparsification:
    - K-NN graph neighborhood
    - Mutual K-NN graph neighborhood
    - Epsilon-NN graph neighborhood
    - Dominant neighborhood

## Related work

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- Yang, Xingwei, Suzan Koknar-Tezel, and Longin Jan Latecki. "Locally constrained diffusion process on locally densified distance spaces with applications to shape retrieval." *CVPR 2009*.
  - **LCDP** for short
    - Uses **k-NN** for graph sparsification
    - Improves retrieval performance by ~6%
- Xingwei Yang; Prasad, L.; Latecki, L.J., "Affinity Learning with Diffusion on Tensor Product Graph," *IEEE Trans. PAMI 2013*
  - **TPG** for short
    - Uses **Dominant Neighborhoods (DN)** for graph sparsification
    - Improves retrieval performance by ~6%
- However, graph sparsification is performed in a **supervised manner**
- For arbitrary neighborhood sizes, their performance drops (sometimes, drastically!)

## Consensus of k-NNs

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- Intuition behind Consensus of k-NNs
  - Nodes that appear consistently in neighborhoods of other nodes have a high chance of being similar to each other
  - So, edges in the sparse graph should be between nodes that appear consistently
  - Prune edges between inconsistent nodes
- Higher the value of ‘k’, higher the probability of adding noisy edges
- Our approach is more robust at higher values of ‘k’

## Consensus Information

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- Collecting consensus information is this simple!

```
C = 0;  
for i = 1 : N do  
    Si = k-NN(vi);  
    for p = 1 : N do  
        for q = p + 1 : N do  
            if p ∈ Si and q ∈ Si then  
                C(p, q) = C(p, q) + 1;  
                C(q, p) = C(q, p) + 1;  
            end  
        end  
    end  
end
```

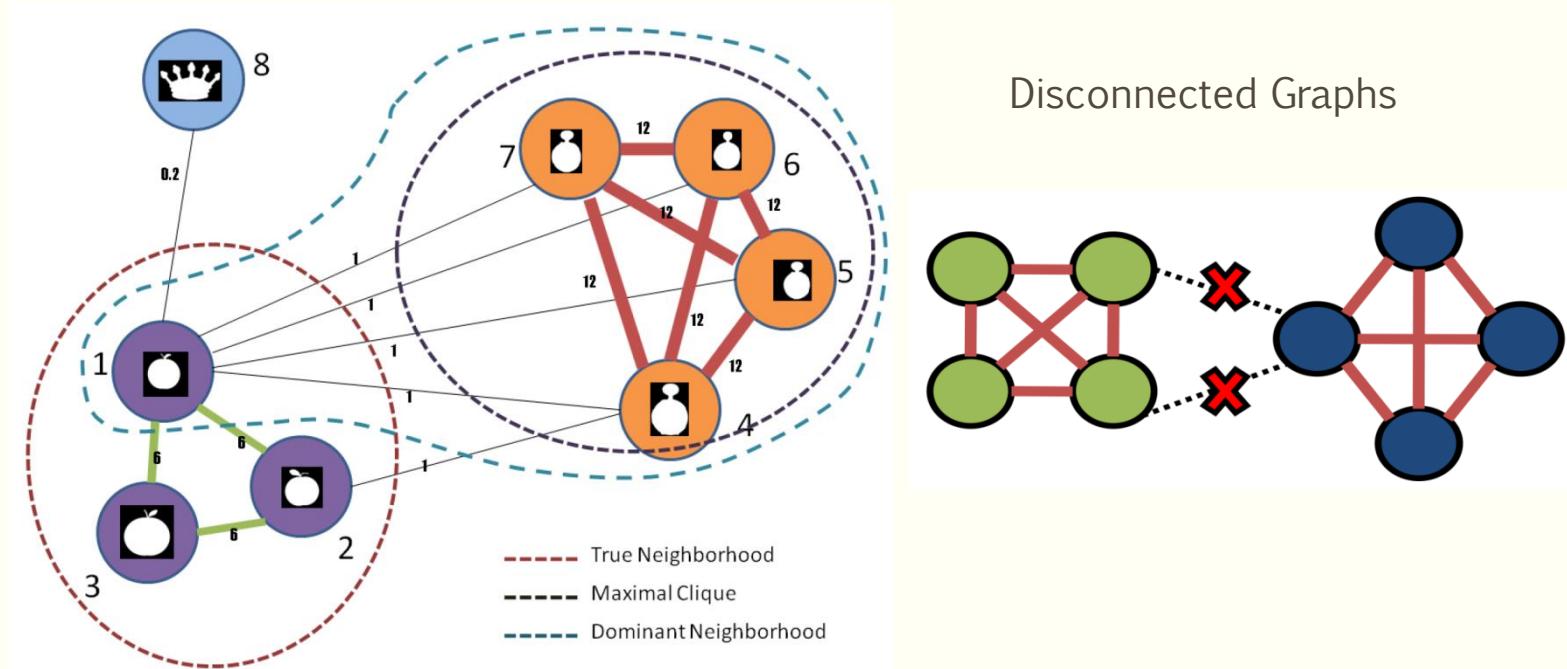
- Finally, retain the edge between  $p$  and  $q$  if  $C(p,q) > \tau$

# Dominant Neighborhoods

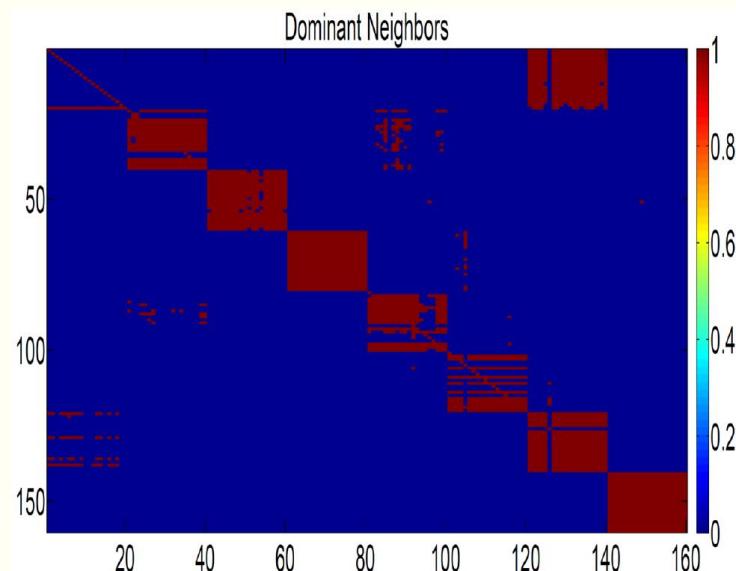
- Dominant neighbors are maximal cliques
- Issues with DN:
- False Neighborhoods

$$\begin{aligned} & \text{maximize} && f(\mathbf{x}) = \mathbf{x}^T A \mathbf{x} \\ & \text{subject to} && \mathbf{x} \in \Delta \end{aligned}$$

$$\Delta = \{\mathbf{x} \in \mathbb{R}^n | \mathbf{x} \geq 0 \text{ and } \mathbf{1}^T \mathbf{x} = 1\}$$

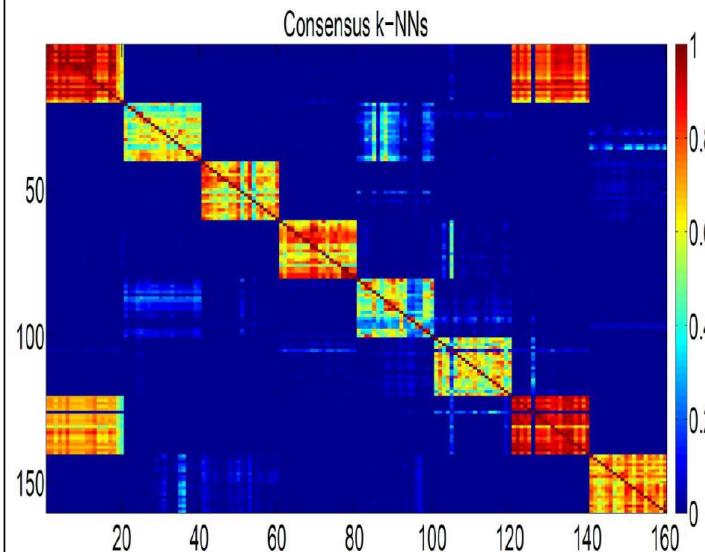


## Neighborhood Comparison



- Binary neighborhood
- Class #1 gets assigned instances from class #7 as its Dominant Neighbors.

- Soft, probabilistic measures for deciding on neighborhoods.
- Class #1's neighbors remain in class #1 with high probability.



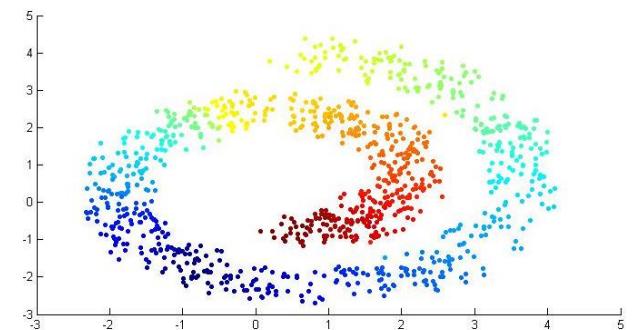
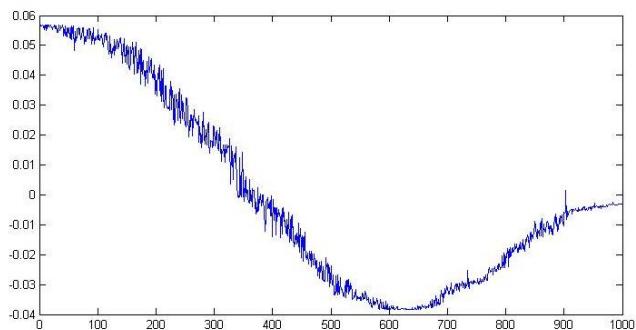
# Experiments

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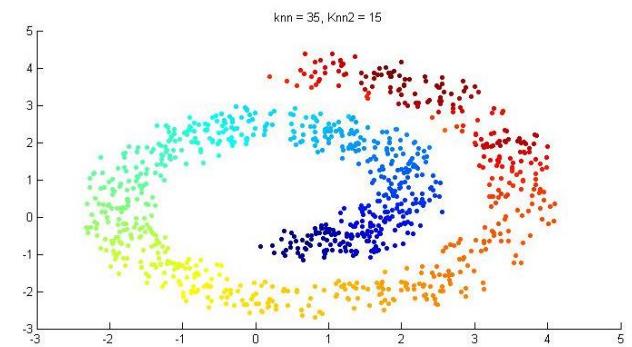
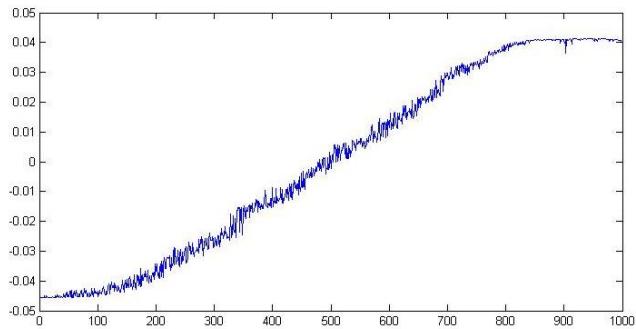
---

- Toy Dataset: Spiral

Simple k-NN



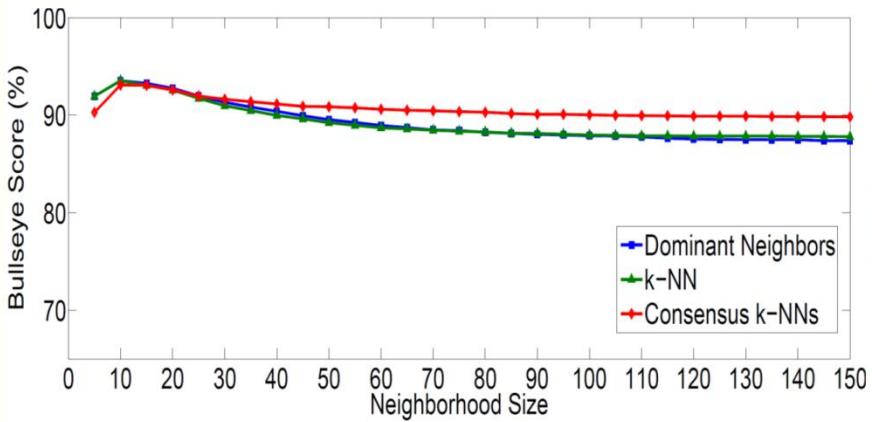
Consensus of k-NNs



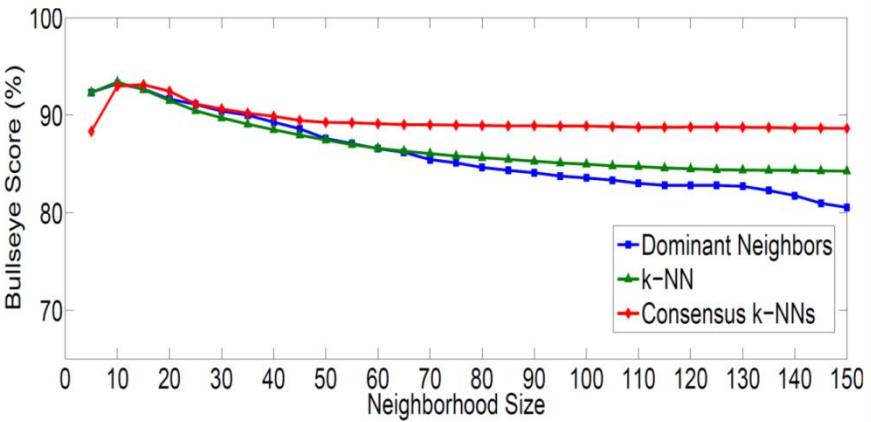
# Experiments on MPEG-7 Database

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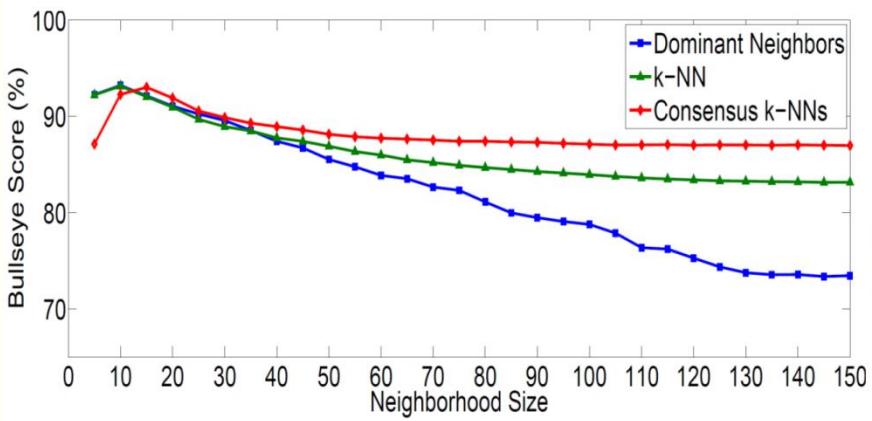
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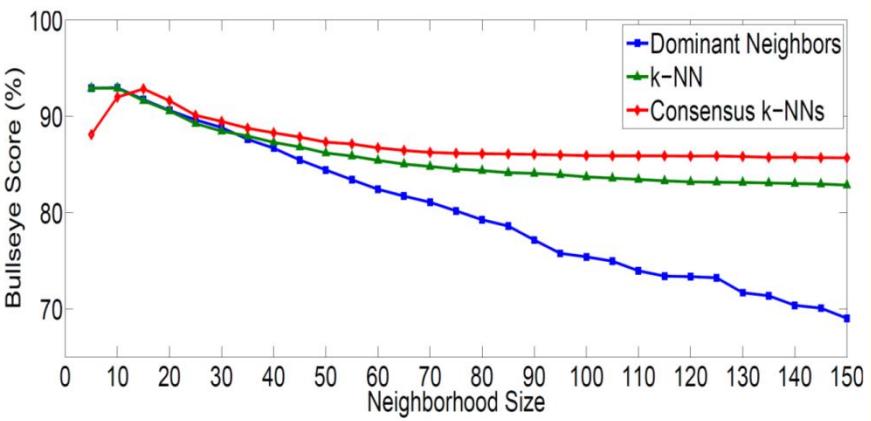
(a)  $K=25$



(b)  $K=50$



(c)  $K=75$



(d)  $K=100$

## Recap

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- Graph sparsification is important preprocessing step for diffusion
  - **Consensus of k-NNs** is a much more **robust** way of selecting neighborhoods
- 
- Vittal Premachandran, and Ramakrishna Kakarala. "Consensus of k-nns for robust neighborhood selection on graph-based manifolds." *Computer Vision and Pattern Recognition (CVPR)*, 2013

# Outline

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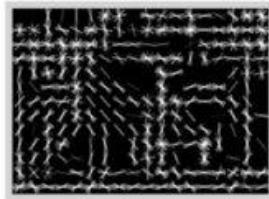
---

- Introduction
- Background
- Perceptually Motivated Shape Context
- What parts of a shape are discriminative?
- Shape similarity propagation on manifolds
- **Object detection in images using shapes**
- Summary

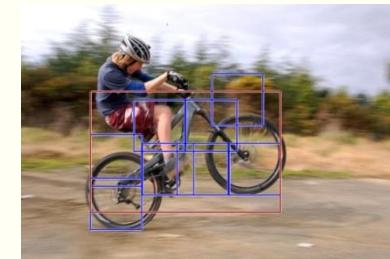
# Object Detection Using Shapes

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- Object detection is a highly challenging task
  - Detection = recognition + localization
- 
- Two main approaches for object detection:



HOG-based approach;  
strong discriminative capability



Contour-fragment based approach;  
strong localization ability

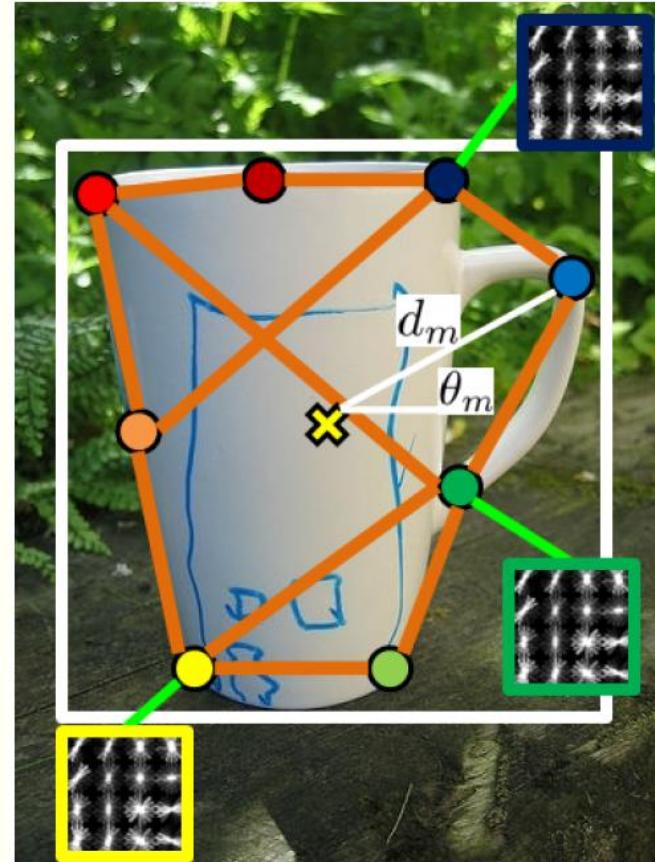
- We aim to bridge the gap between the two approaches

# Our Model

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- Parts-based model
- Each part denoted by two types of features:
  - Local features – HOG
  - Non-local features – Distance and Angle

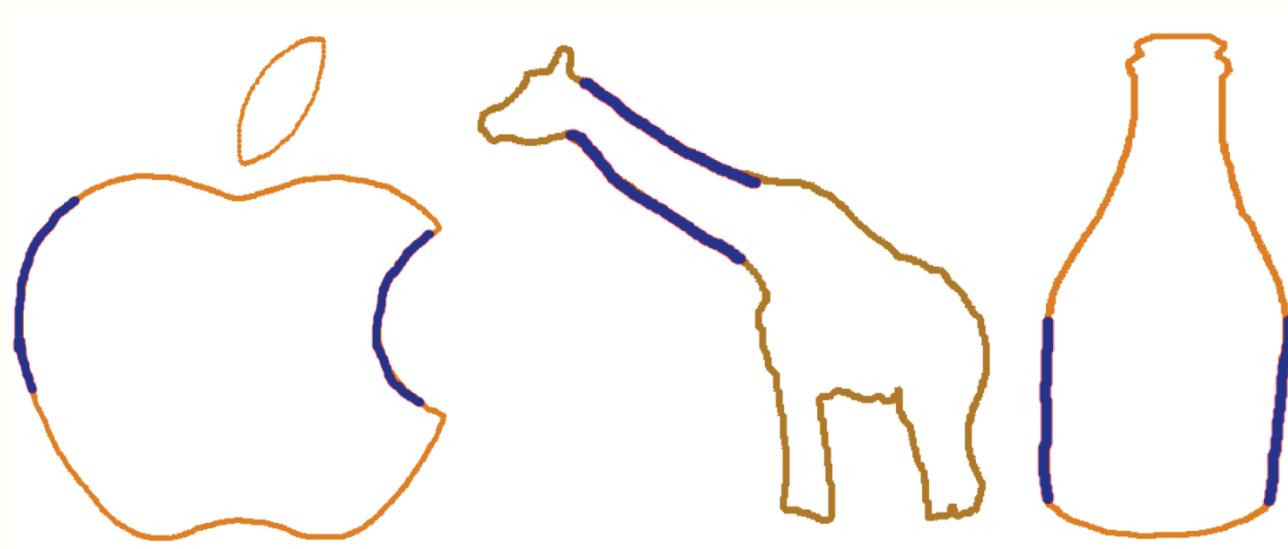


## Need For Non-Local Parts

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- Locally similar looking parts are highlighted in blue
- Without non-local features, they can generate false matches



## The Approach

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$$E(I, Y; \ell) = \sum_{p_i \in \mathcal{V}} \Phi(.) + \sum_{(p_i, p_j) \in \mathcal{E}} \Psi(.) + \sum_{(p_i, p_j) \in \mathcal{E}} \Omega(.)$$

Unary  
Potential

Pairwise  
Potential

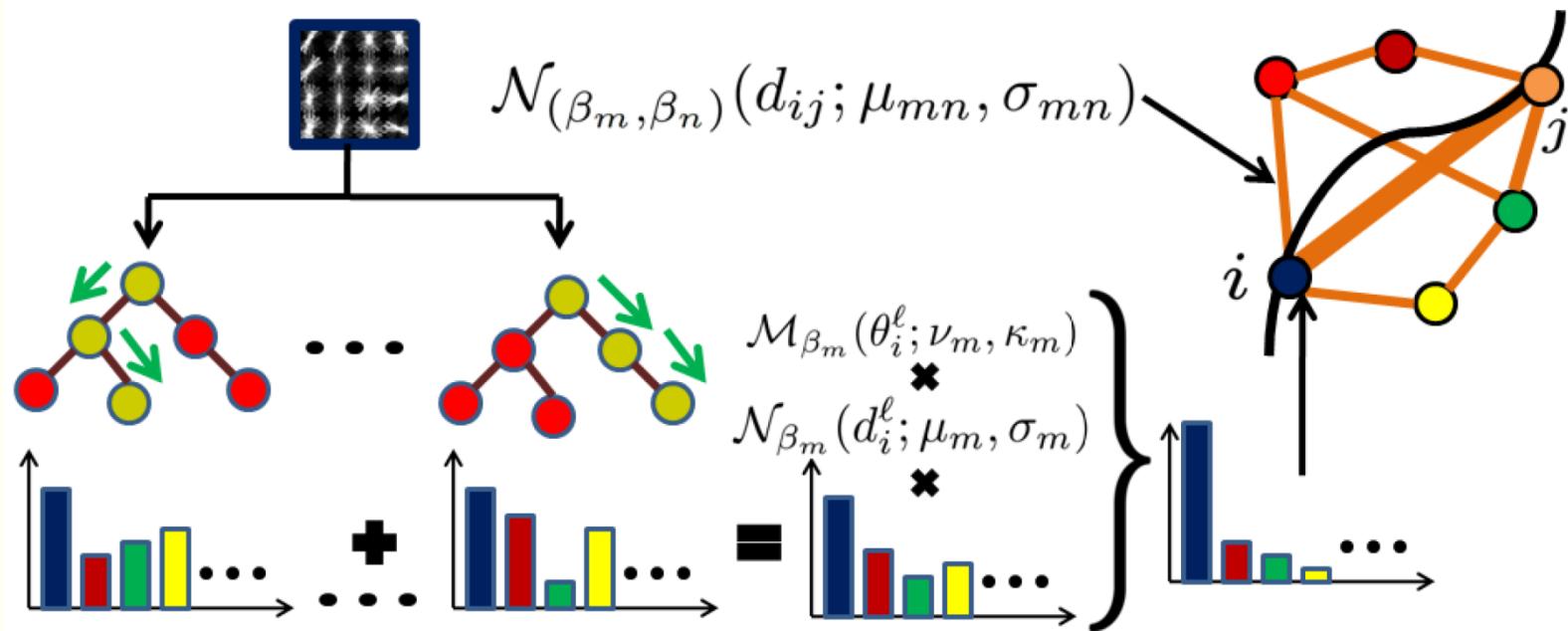
Potts  
Potential

- TRW-S for optimization

## Overall Procedure

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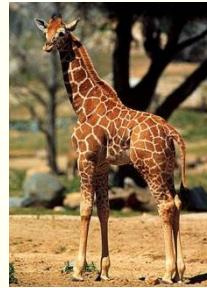


# Experiments and Results

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- ETH-Z Shape Database

- 5 classes

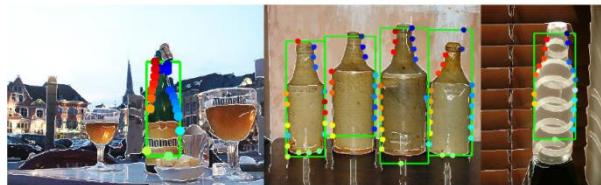
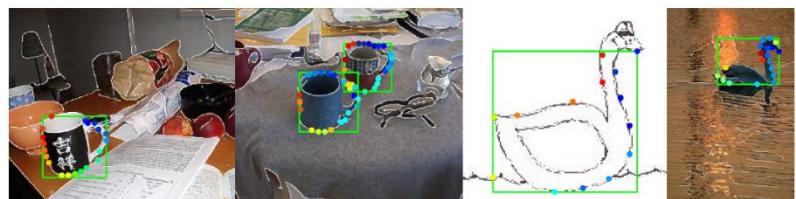
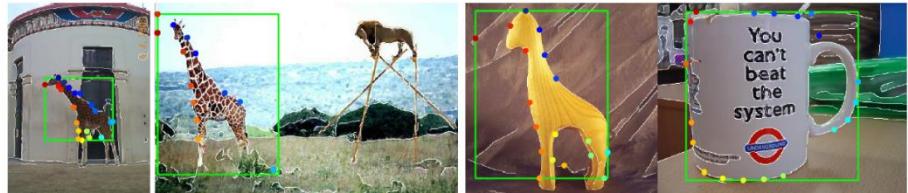
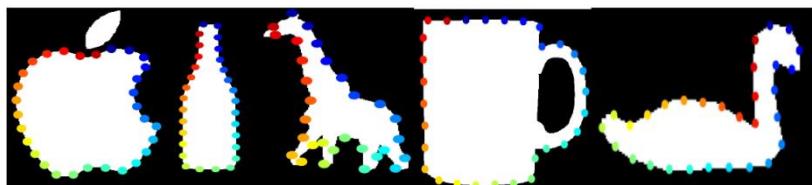


- 255 Images
  - PASCAL 50% overlap criteria
  - Performance measured by mean Average Precision and Detection Rate at 0.3/0.4 FPPI

# Detection Examples

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## Mean Average Precision

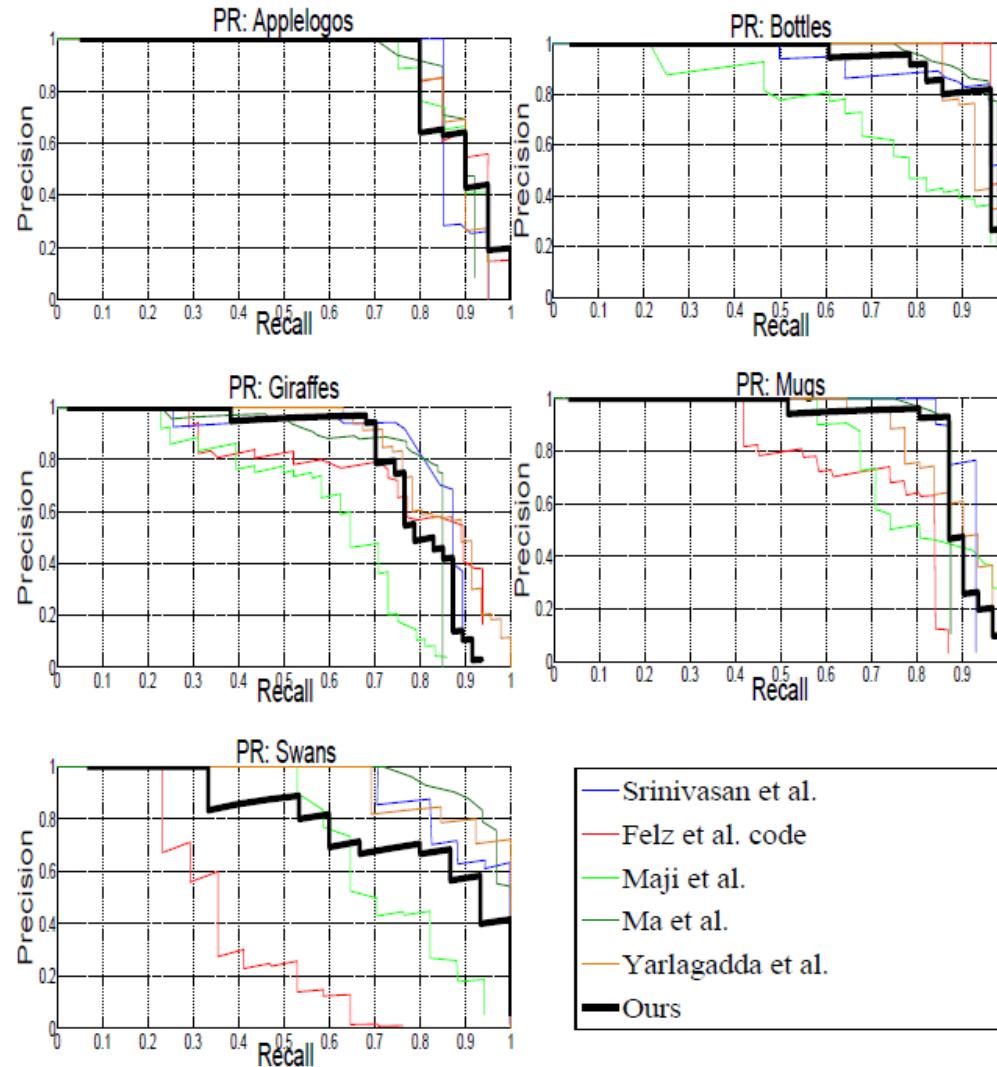
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	Applelogos	Bottles	Giraffes	Mugs	Swans	Mean
Ours	<b>0.897</b>	0.939	0.800	<b>0.889</b>	0.819	0.868
Srinivasan et al. [91]	0.845	0.916	0.787	0.888	0.922	0.872
Felzenswalb et al. [31]	0.891	0.950	0.608	0.721	0.391	0.712
Wang et al. [100]	0.866	<b>0.975</b>	<b>0.832</b>	0.843	0.828	0.869
Ma et al. [61]	0.881	0.920	0.756	0.868	<b>0.959</b>	<b>0.877</b>
Lin et al. [53]	<b>0.909</b>	0.898	0.811	0.893	<b>0.964</b>	<b>0.895</b>
Ours Random	0.908	<b>0.951</b>	<b>0.821</b>	<b>0.894</b>	0.847	0.884

# Precision Recall Curves

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# Outline

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# Summary

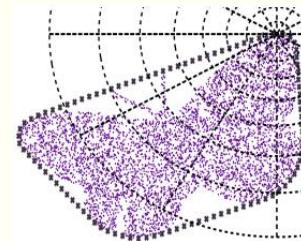
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- Presented a strong motivation to use shapes



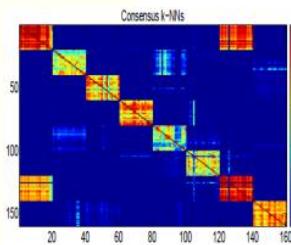
- Perceptually motivated technique to match shapes



- Presented a novel technique for identifying discriminative parts.



- Consensus of k-NNs for robust neighborhood selection



- Bridge the gap between HOG-based and contour-based object detection



## Future Work

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- Need other types of perceptually motivated techniques
- Use discriminativeness of parts for generating better shape descriptors
- Bigger shape databases are needed for object detection

Thank you!