

## Okumara and Hata Model

Gain & weight

$$G = 20 \log \left( \frac{h_{te}}{200} \right)$$

$$100 \text{ m} > h > 30 \text{ m}$$

$$G(h_{re}) = 10 \log \left( \frac{h_{re}}{3} \right)$$

$$h_{te} \leq 3 \text{ m}$$

$$G(h_{re}) = 20 \log \left( \frac{h_{re}}{3} \right)$$

$$10 \text{ m} > h_{te} > 3 \text{ m}$$

Okumara model → path loss prediction model

$$L_{50}(\text{dB}) = L_F + A_m(f, d) - G(h_{te}) - G(h_{re}) - G_{area}$$

Hata and extended Hata model

$$L_{50}(\text{dB}) = 69.55 - 26.16 \log f_c (\text{MHz}) - 13.82 \log h_{te} - a(h_{re}) + (44.9 - 6.55 \log h_{te}) \log d$$

$h_{te}$  - BS height of antenna (30 to 200m)

$h_{re}$  - mobile antenna height (1m to 10m)

$a(h_{re})$  - is a correction factor for effective mobile

$$a(h_{re}) = \begin{cases} 8.29 (\log 15 - \log h_{re})^2 - 1.1 \text{ dB} & f_c \leq 300 \text{ MHz} \\ 3.2 (\log 11.75 h_{re})^2 - 4.97 \text{ dB} & f_c \geq 300 \text{ MHz} \end{cases}$$

(for large sized city)

$$L_{50}(\text{dB}) = L_{50}(\text{urban}) - 2 \log [f_c / 28]^2 - 5.4$$

⇒ extended Hata model

1) Employing the Okumura model compute the median loss at a distance of 10 km when the carrier frequency ( $f_c$ ) is 2.1 GHz. Assume  $h_{te} = 400\text{m}$ ,  $h_{re} = 2\text{m}$  for a large city. If EIRP is given by 1 kW at the carrier frequency. Find the received power for the same scenario.

Soln: -  $L_{50}(\text{dB}) = L_F + \underbrace{A_{m,u}(f, d)}_{\substack{\text{median} \\ \text{attenuation relative} \\ \text{free space to free space} \\ \text{propagation loss}}} - \underbrace{G(h_{te}) - G(h_{re}) - G_{area}}_{\text{gain}}$

50th percentile value (median) of the path loss

$\therefore f_c = 2.1\text{ GHz}, h_{te} = 400\text{m}, h_{re} = 2\text{m},$

$L_F = -10 \log \left( \frac{\lambda^2}{(4\pi)^2 d^2} \right) \approx 10 \log \left( \frac{d^2 (4\pi)^2}{\lambda^2} \right)$

$\therefore \lambda = \frac{c}{f} = \frac{1}{f} = 0.143\text{ m}$

$\therefore L_F = 10 \log \left( \frac{10^2 \times 10^6 \times 4\pi^2}{0.143^2} \right)$   
 $= 118\text{ dB}$

$\therefore G_{h_{te}} = 20 \log \left( \frac{h_{te}}{200} \right) = -13.97\text{ dB}$

$G_{re} = 10 \log \left( \frac{h_{re}}{3} \right) = -1.76\text{ dB} \quad \therefore h_{re} = 2\text{m} < 3\text{m}$

$A_{m,u}(2.1, 10\text{km}) = 34\text{ dB}$  (from graph.)

$G_{area}$ , area - large city

$\therefore G_{area} = 0$



$$L_{50dB} = 118 + 34 + 13.97 + 1.76$$

$$L_{50dB} = 167.73 \text{ dB} \rightarrow \text{okumara model}$$

Hata Model :-

$$L_{50dB} = 69.55 + 26.16 \log(f_c) - a(h_{re}) + (44.9 - 6.55 \log(h_{te}) \log(d))$$

$f_c = 2.16 \text{ MHz}$   
 $\uparrow$  in MHz

$$\therefore a(h_{re}) = ? = 3.2 (\log(11.75 \times h_{re}))^2 - 4.97$$

$$= 1.045 \text{ dB}$$

$$L_{50dB} = 69.55 + 26.16 \log(2100) - 1.045 + (44.9 - 6.55 \log(40) \log(2))$$

$$= 69.55 + 86.9 - 1.045 + 137.6$$

$$= 288 \text{ dB} \quad 271 \text{ dB}$$

power

$$P_R = P_T - L_{50}$$

$$P_T G_T = \text{EIRP} \quad \text{considering } G_T = 1$$

$$\therefore \text{EIRP} = P_T = 1 \text{ kW} = 10 \log\left(\frac{1 \times 10^6}{\text{mW}}\right) = 60 \text{ dBm}$$

$$P_R = 60 \text{ dBm} - 167 \text{ dB} = -107 \text{ dB} \quad \text{dBm} = \text{dBm} + 3.0$$

$$= 30 \text{ dB} - 167 \text{ dB}$$

$$= -137 \text{ dB}$$

1) determine the propagation path loss for a radio signal at 800 MHz with Tx antenna height of 30 m,  $h_r = 2$  m,  $d = 10$  km over a dense urban mobile environment; using Hata model propagation loss. If free space path loss is 110.5 dB, how is hata propagation path loss comparable with that of free space.

Soln:-  $\therefore h_{re} = 2$  m

$$L_{sdB} = 69.55 + 26.16 \log f_c \text{ (MHz)} - 13.82 \log h_t - a(h_{re}) + (44.9 - 6.55 \log h_t) \log d$$

$$\begin{aligned} a(h_{re}) &= 32(\log 11.75 h_{re})^2 - 4.97 \\ &= 3.2(\log 11.75 \times 2)^2 - 4.97 \\ &= 1.045 \end{aligned}$$

$$\begin{aligned} \therefore L_{sdB} &= 69.55 + 75.94 - 20.41 - 1.045 + \\ &= 140.89 \\ &= 264.425 \approx 265 \text{ dB} \end{aligned}$$

$$L_F = 110.5 \text{ dB (free space)}$$

$$L_{sdB} \gg L_F$$

$\therefore$  shadowing multipath effects.

The power received from an antenna radiating  $P_T$  watts in free space given by:

$$P_R = P_T G_T G_R \left( \frac{\lambda}{4\pi d} \right)^2, \quad P_R = \frac{P_0}{d^2}$$

$G_T$  - transmitting } antenna link gain  
 $G_R$  - receiving }

$\lambda$  - signal wavelength

$d$  - distance from tx antenna

Ex1:-  $P_T = 1 \text{ W}$ ,  
 $f_c = 1900 \text{ MHz} \therefore \lambda = \frac{c}{f} = \frac{3 \times 10^8}{19 \times 10^8} = 0.157 \text{ m}$

$$d = 1000 \text{ m}$$

$$G_T = G_R = 1.6, \text{ path loss} = ?$$

$$P_0 = 1 \times 1.6 \times 1.6 \times \frac{(0.157)^2}{(4\pi)^2} = 0.000399 \text{ W} = 0.399 \text{ mW}$$

$$10 \log \left( \frac{P_0}{1 \text{ m}} \right) = 4.08 \text{ dBm}$$

$$\text{Now, } d = 1000 \text{ m}$$

$$\therefore P_R = \frac{P_0}{d^2} = \frac{0.399 \text{ m}}{1000^2} = 0.399 \text{ nW} = -63.9 \text{ dBm}$$

Path loss in dB is

$$\begin{aligned} \text{Path loss} &= P_T - P_R \\ &= 30 \text{ dBm} - (-63.9 \text{ dBm}) \end{aligned}$$

$$\boxed{\text{Path loss} = 93.9 \text{ dBm}}$$



$$2) P_T = 120 \text{ watt} = 10 \log \left( \frac{120}{1 \text{ m}} \right) = 50.79 \text{ dBm}$$

$$G_T = 34 \text{ dB},$$

$$G_R = 33 \text{ dB},$$

$$f_c = 12.45 \text{ GHz} = 12450 \text{ MHz}$$

$$\lambda = \frac{c}{f} = \frac{3 \times 10^8}{12450 \times 10^6} = 0.024 \text{ m}$$

$$\therefore P_R = P_T + G_R + G_T - 20 \log \left( \frac{4\pi d}{\lambda} \right) \\ = 50.8 \text{ dBm} + 34 \text{ dB} + 33 \text{ dB} - 20 \log \left( \frac{4\pi \times 35786000}{0.024} \right)$$

$$P_R = -87.65 \text{ dBm}$$

$$3) f = 38 \text{ GHz} = 38000 \text{ MHz}, \quad P_T = 16 \text{ dBm},$$

$$G_T = G_R = 38.5 \text{ dB}, \quad d = ?$$

$$\text{receiver sensitivity} = -74 \text{ dBm}$$

$$P_R = P_T + G_T + G_R - 20 \log \left( \frac{4\pi d}{\lambda} \right) \\ = 16 + 38.5 + 38.5 - 20 \log \left( \frac{4\pi d}{\lambda} \right)$$

$$\text{link margin} = 15 \text{ dB},$$

$$\text{received signal power} = -74 \text{ dBm} + 15 \\ = -59 \text{ dBm} = P_R$$

$$-59 = 93 \text{ dBm} - 20 \log \left( \frac{4\pi d}{\lambda} \right)$$

$$\lambda = \frac{c}{f} = \frac{300}{38000} = 0.00789 \text{ m}$$

$$152 = 20 \log \left( \frac{4\pi d}{7.89 \times 10^{-3}} \right)$$

$$\Rightarrow 39.81 \times 10^6 = \frac{4\pi d}{7.89 \times 10^{-3}}$$

$$d = 24995 \text{ m} = 25 \text{ km}$$