



# DP Concepts

video  
33

&

## Questions

The future depends on  
what you do today.

Believe you can,  
and you're halfway  
there



MIK...



हाइव  
(Motivation)

cswithMIK → Twitter

Facebook

Instagram

→ code story with MIK

whatsapp → code story with MIK

Done

1-D based DP

Grid based DP

Done

String based DP

Digit DP

Game Strategy

We'll do:-

(i) RECURSION  
+  
MEMOIZATION  
(Top Down)

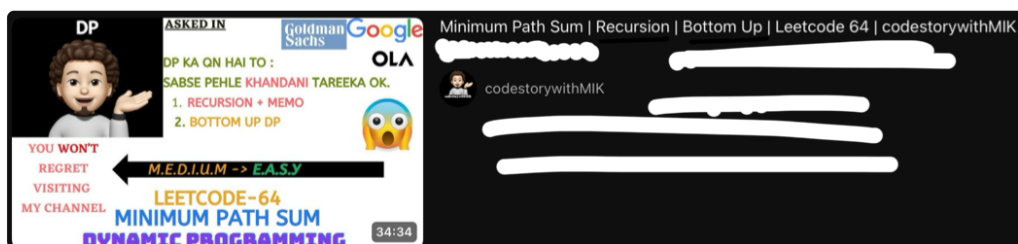
(ii) Bottom UP

(iii) Time & Space

# DP on Grids

Solve this on your own first :-

Leetcode-64 "Minimum Path Sum"



When you solve it, then  
only come to this video. 😊

## 1594. Maximum Non Negative Product in a Matrix

Medium

Topics

Companies

Hint

You are given a  $m \times n$  matrix `grid`. Initially, you are located at the top-left corner  $(0, 0)$ , and in each step, you can only move right or down in the matrix.

Among all possible paths starting from the top-left corner  $(0, 0)$  and ending in the bottom-right corner  $(m - 1, n - 1)$ , find the path with the maximum non-negative product. The product of a path is the product of all integers in the grid cells visited along the path.

Return the maximum non-negative product modulo  $10^9 + 7$ . If the maximum product is negative, return  $-1$ .

Notice that the modulo is performed after getting the maximum product.

$(0, 0)$  →

$(m-1, n-1)$

Example:-

1	-2	1
1	-2	1
3	-4	1

$$1 * 1 * (-2) * (-4) * 1 = 8$$

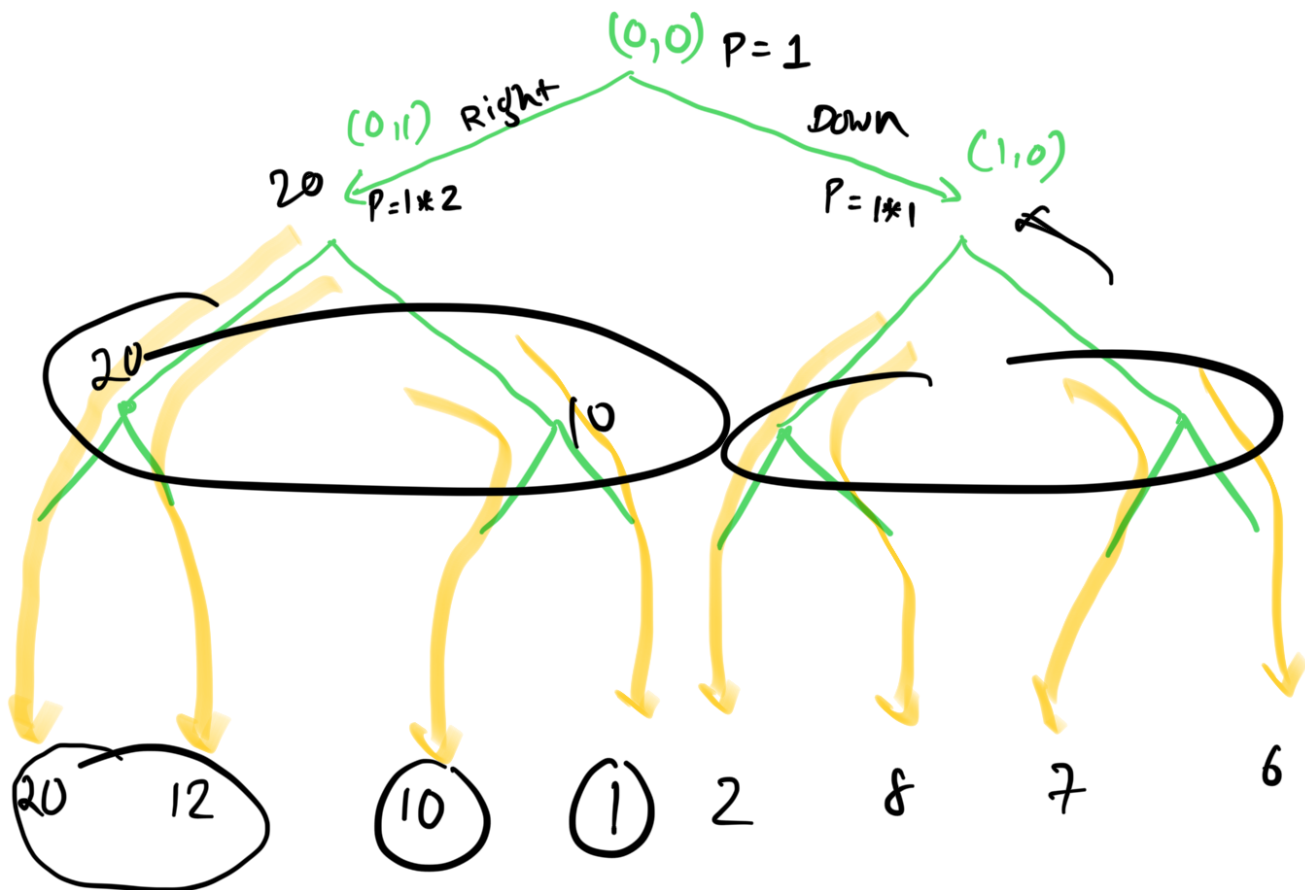
Output :- 8

# Thought Process

++ve numbers.

	0	1	2
0	1	2	1
1	1	2	1
2	3	4	1

(m-1, n-1)



if (m-1 & n-1) {  
return grid[i][j];

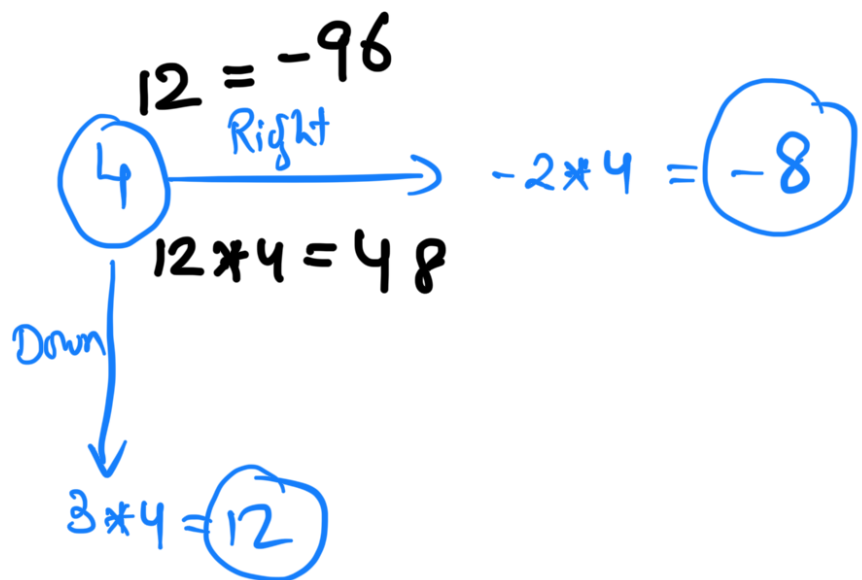
right = grid[i][j] \* solve(grid, i, j+1)

$down = grid[i][j] * solve(grid, i+1, j);$

return  $\max(right, down)$  ;

Grid contains -ve nos also :-

	0	1	2
0	1	-2	3
1	1	4	-2
2	2	3	4



1	-2	3
1	4	-2
2	3	4

$$-32 * -2 * 1$$

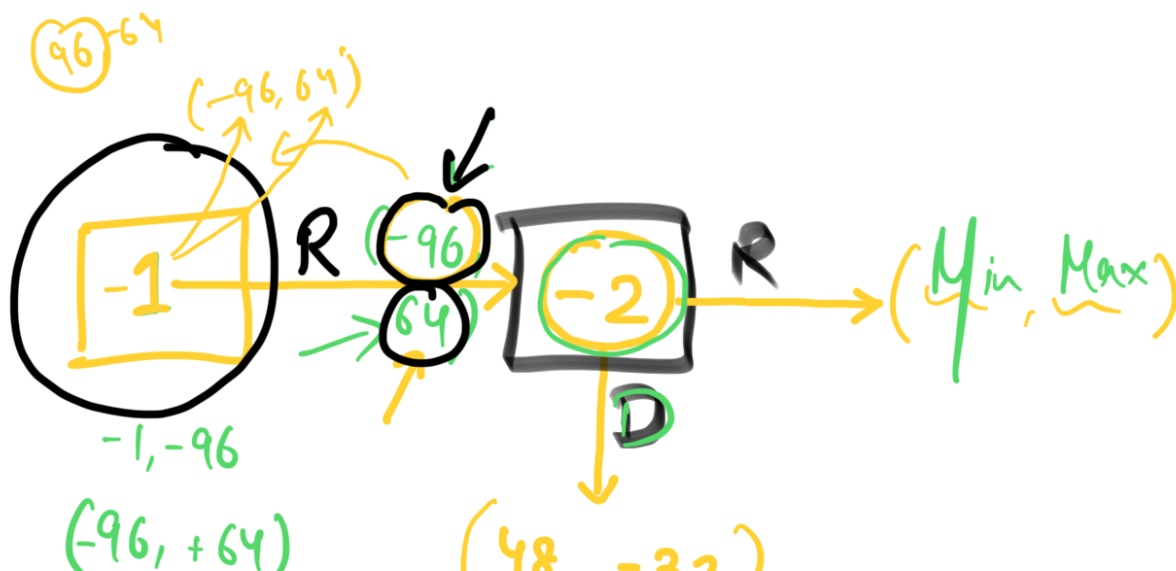
$$= \boxed{+64}$$

$$12 \leftarrow \max(-8, 12) \quad \text{R, D} \quad \times$$

	0	1	2
0	1 -96 64	-2 48	3 -32
1	1	4 12	-2
2	2	3	4

$$1 * -96 = -96$$

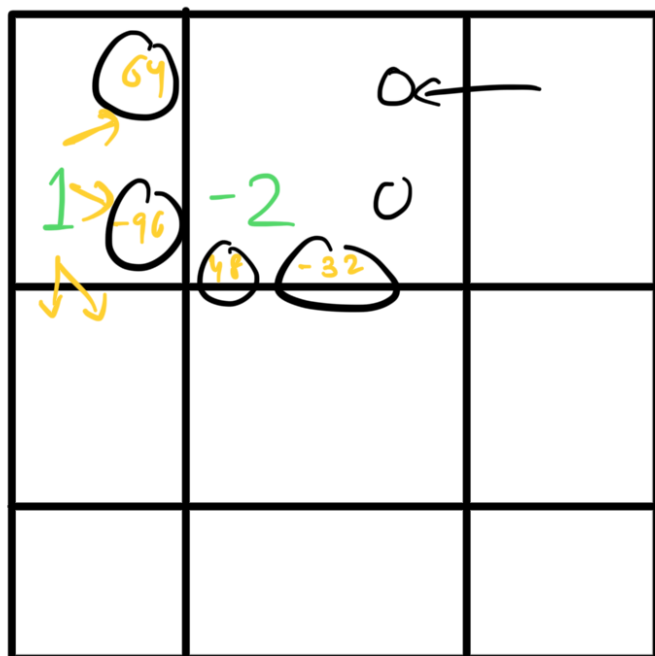
$$1 * 64 = 64$$



Every cell must have two  
information from

Right  $\rightarrow$  (rightMax,  
rightMin)

Down → (downmax, downmin)



-96, 64  
maxVal = 64  
minVal = -96

downMax = 48

downMin = -32



$\downarrow \text{grid}[i][j]$

$\text{maxVal} = \max(\text{maxVal}, \underline{-2 * \text{downMax}, -2 * \text{downMin}});$

$\text{minVal} = \min(\text{minVal}, \underline{-2 * \text{downMax}, -2 * \text{downMin}});$

$\text{rightMax} = x$

$\text{rightMin} = y$

$\text{maxVal} = \max(\text{maxVal}, \underline{-2 * \text{rightMax}, -2 * \text{rightMin}});$

$\text{minVal} = \min(\text{minVal}, \underline{-2 * \text{rightMax}, -2 * \text{rightMin}});$

return {maxVal, minVal};

if (maxVal < 0) -1

maxVal

1	2
3	1

-1	2
3	1

$-1 * 2 * 1 = -2$

$-1 * 3 * 1 = -3$

(\*)  $\text{vector} < \text{vector} < \text{pair} < \text{ll}, \text{ll} > > > \text{f}$

# Bottom Up

Solve  $(i, j)$  ;

$$t[i][j] = \text{pair} \langle ll, ll \rangle$$

### State Definition:-

$(0,0) \rightarrow (m-1, n-1)$

$$f[i][j] = \begin{cases} \text{max-product} & \text{from } (0,0) \text{ to } (i,j), \\ \text{min-product} & \text{" " " " " } \end{cases}$$

1	2	3
1	-4	-2
2	3	4

	0	1	2
0	$\{1, 1\}$	$\{2, 2\}$	$\{6, 6\}$
1	$\{1, 1\}$	?	
2	$\{2, 2\}$		

Base Case:- 0<sup>th</sup> row  
= 0<sup>th</sup> col ✓✓

$d[0][0] = ???$

$(i, j-1) \xrightarrow{R} \overset{(i-1, j)}{D \downarrow} [i][j]$