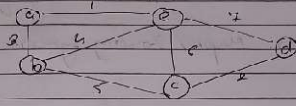




**2Bharatiya Vidya Bhavan's**  
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<b>Experiment</b>	2
<b>Aim</b>	To understand and implement greedy Approach
<b>Objective</b>	1) Learn GREEDY Approach 2) Implement Greedy approach problem 3) Solve Greedy approach problem
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<b>Date of Submission</b>	18/02/24

<b>Algorithm and explanation of the technique used</b>	<p>Sort all the edges in non-decreasing order of their weight. Pick the smallest edge. Check if it forms a cycle with the spanning tree formed so far. If the cycle is not formed, include this edge. Else, discard it. Repeat step#2 until there are (V-1) edges in the spanning tree</p> <p><b>Kruskal's Algorithm:</b> KRUSKAL(G): A = <math>\emptyset</math> For each vertex <math>v \in G</math>. V: MAKE-SET(v) For each edge <math>(u, v) \in G</math>.E ordered by increasing order by weight(u, v): if FIND-SET(u) <math>\neq</math> FIND-SET(v): A = A <math>\cup</math> {(u, v)} UNION(u, v) return A</p>
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	<p><u>Lab 2</u></p> <p>Kruskal Algorithm repeatedly selects the smallest edge that does not form a cycle, thus forming minimum spanning tree.</p>  <p>Step 1: Sort by weights</p> <p>Step 2: <math>a - 1 - e</math></p> <p>Step 3: <math>a - 1 - e</math> <math>c - 2 - d</math></p> <p>Step 4: <math>a - 1 - e</math> <math>b - 3 - a</math> (rejected, forms cycle) <math>c - 2 - d</math></p> <p>Step 5: <math>a - 1 - e</math> <math>b - 3 - a</math> (rejected, forms cycle) <math>c - 5 - b</math> (rejected, forms cycle) The final Minimum Spanning Tree consists of edges <math>(a,e)</math>, <math>(c,d)</math>, and <math>(c,b)</math>.</p> <p>Time complexity of Kruskal's Algorithm is typically <math>O(E \log E)</math> or <math>(E \log V)</math>, where <math>E</math> is the no. of edges &amp; <math>V</math> is no. of vertices, considering <math>E &lt; V^2</math> for sparse graph.</p>
Code	<pre> import java.util.*; class Edge implements Comparable&lt;Edge&gt; {     char src, dest;     int weight;      Edge(char src, char dest, int weight) {         this.src = src;         this.dest = dest;         this.weight = weight;     }      public int compareTo(Edge compareEdge) {         return this.weight - compareEdge.weight;     } }  class DisjointSet {     Map&lt;Character, Character&gt; parent;      DisjointSet() {         parent = new HashMap&lt;&gt;();     }      void makeSet(char vertex) {         parent.put(vertex, vertex);     } </pre>

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    }
    char find(char vertex) {
        if (parent.get(vertex) == vertex)
            return vertex;
        return find(parent.get(vertex));
    }
    void union(char vertex1, char vertex2) {
        char parent1 = find(vertex1);
        char parent2 = find(vertex2);
        parent.put(parent1, parent2);
    }
}

class Main {
    public static void main(String[] args) {
        Edge[] edges = {
            new Edge('a', 'b', 3),
            new Edge('a', 'e', 1),
            new Edge('b', 'c', 5),
            new Edge('b', 'e', 4),
            new Edge('c', 'd', 2),
            new Edge('e', 'd', 7),
            new Edge('e', 'c', 6)
        };

        Arrays.sort(edges);
        DisjointSet disjointSet = new DisjointSet();
        for (char c = 'a'; c <= 'h'; c++) {
            disjointSet.makeSet(c);
        }
        // Kruskal's algorithm
        List<Edge> minimumSpanningTree = new ArrayList<>();
        for (Edge edge : edges) {
            char srcParent = disjointSet.find(edge.src);
            char destParent = disjointSet.find(edge.dest);
            if (srcParent != destParent) {
                minimumSpanningTree.add(edge);
                disjointSet.union(edge.src, edge.dest);
            }
        }
        for (Edge edge : minimumSpanningTree) {
            System.out.println(edge.src + " - " + edge.dest + ": " +
edge.weight);
        }
    }
}

```

<b>Output</b>	<pre> "C:\Program Files\Java\jdk-21\bin\java.exe" a - e: 1 c - d: 2 a - b: 3 b - c: 5 </pre>
<b>Justification of the complexity calculated</b>	<p>The time complexity of Kruskal's algorithm is mainly influenced by the sorting of edges, which takes <math>O(E \log E)</math> time, where <math>E</math> represents the number of edges in the graph. Additionally, the union-find operations contribute a nearly constant factor per operation. Overall, the time complexity of Kruskal's algorithm is <math>O(E \log E)</math>, which can be simplified to <math>O(E \log V)</math> for sparse graphs, where <math>V</math> is the number of vertices in the graph.</p>
<b>Conclusion</b>	<p>Kruskal's Algorithm is one technique to find out minimum spanning tree from a graph, a tree containing all the vertices of the graph and <math>V-1</math> edges with minimum cost. The complexity of this graph is <math>(V \log E)</math> or <math>(E \log V)</math>.  With a time complexity of <math>O(E \log E)</math> or <math>O(E \log V)</math>, it offers a practical solution for a wide range of graph structures, making it a versatile and effective tool for network optimization problems.</p>