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CSC440

Assignment 4

1. First we split P into the left and right sides, L_0 and R_0 , respectively.

$$[L_0][R_0] \xrightarrow{-K} [R_0][L_0 \oplus f(R_0, K)]$$

$$L_1 = R_0, \text{ and } R_1 = L_0 \oplus f(R_0, K)$$

We also split P' into left and right sides, L_0' and R_0'

$$[L_0'][R_0'] \xrightarrow{-K'} [R_0'][L_0' \oplus f(R_0', K')]$$

$$R_0' = R_0 \oplus 111\dots, L_0' = L_0 \oplus 111\dots, \text{ and } K_0' = K_0 \oplus 111\dots,$$

$$L_0' \oplus f(R_0', K') = L_0' \oplus R_0 \oplus 111\dots \oplus K \oplus 111\dots = L_0' \oplus R_0 \oplus K = L_0' \oplus f(R_0, K)$$

And

$$L_0' \oplus f(R_0', K') = L_0 \oplus 111\dots \oplus R_0 \oplus K = L_0 \oplus R_0 \oplus K \oplus 111\dots$$

$$= L_0 \oplus f(R_0, K) \oplus 111\dots = R_1 \oplus 111\dots = R_1'$$

Therefore:

$$[L_0'][R_0'] \xrightarrow{-K'} [R_0'][L_0' \oplus f(R_0', K')] = [L_1'][R_1'] = C'$$

2. The message m is encrypted to c like this: $m \rightarrow EK_2 \rightarrow a \rightarrow EK_2 \rightarrow b \rightarrow EK_1 \rightarrow c$

We can use a brute force attack by encrypting m with all 2^{56} possible keys, one of which is K_2 and leads to a . We do the inverse for c and decrypt it with all possible keys, resulting in b and K_1 . We can now use our set of possible a 's and K_2 's to encrypt for b as we know $a \rightarrow EK_2 \rightarrow b$. We can now use this set of b 's and compare them to the ones we found in the earlier decryption step. Any pairs that match will give us a set of pairs of keys K_1 and K_2 . We can test these keys with other m and c pairs to find the true keys K_1 and K_2 .